Best practices for moving from correlation to causation in ecological research

1

25

2 Hannah E. Correia^{1,2*}, Laura E. Dee³, Jarrett E. K. Byrnes⁴, John R. Fieberg⁵, Marie-Josée 3 Fortin⁶, Clark Glymour⁷, Jakob Runge^{8,9}, Bill Shipley¹⁰, Ilya Shpitser¹¹, Katherine J. Siegel¹², 4 George Sugihara¹³, Betsy von Holle¹⁴, and Paul J. Ferraro^{1,15*} 5 6 ¹Department of Environmental Health and Engineering, Johns Hopkins University 7 ²Department of Biology, University of North Dakota 8 ³Department of Ecology and Evolutionary Biology, University of Colorado Boulder 9 ⁴Department of Biology, University of Massachusetts Boston 10 ⁵Department of Fisheries, Wildlife and Conservation Biology, University of Minnesota 11 ⁶Department of Ecology and Evolutionary Biology, University of Toronto 12 ⁷Department of Philosophy, Carnegie Mellon University 13 ⁸ Department of Computer Science, University of Potsdam 14 ⁹Faculty of Electrical Engineering and Computer Science, Technische Universität Berlin 15 ¹⁰Université de Sherbrooke 16 ¹¹Department of Computer Science, Johns Hopkins University 17 ¹²Department of Geography and Cooperative Institute for Research in Environmental Science, University of 18 Colorado-Boulder 19 ¹³Scripps Institution of Oceanography, University of California San Diego 20 ¹⁴Department of Biology, George Washington University 21 ¹⁵Carey Business School, Johns Hopkins University 22 23 *Correspondence to Hannah E. Correia (hec0003@auburn.edu) or Paul J. Ferraro (pferrar5@jhu.edu) 24

ABSTRACT

In ecology, causal questions are ubiquitous, yet the literature describing systematic approaches to answering these questions is vast and fragmented across different traditions (e.g., randomization, structural equation modeling, convergent cross mapping). In our Perspective, we connect the causal assumptions, tasks, frameworks, and methods across these traditions, thereby providing a synthesis of the concepts and methodological advances for detecting and quantifying causal relationships in ecological systems. Through a newly developed workflow, we emphasize how ecologists' choices among empirical approaches are guided by the pre-existing knowledge that ecologists have and the causal assumptions that ecologists are willing to make.

1 CAUSALITY IN ECOLOGICAL STUDIES

Ecology is centered around investigating causal relationships between living organisms and their environments. In ecology, as in many other scientific fields, causality is understood as a phenomenon where change in one variable (the "cause") induces change (the "effect") in another variable $^{1-4}$. Thus, a causal relationship between X and Y exists if a perturbation in the cause X produces a change in the responding variable $Y^{4,5}$, potentially through the perturbations of intermediary variables 6,7 . This "perturbation-based" definition of causality is the definition most familiar to scientists and philosophers 4,8 .

Because of a strong tradition of using manipulative experiments to establish causation, ecology has been shaped by two aphorisms: "correlation does not equal causation" and "causal claims can only be made from experiments." The first aphorism oversimplifies the complexity of causal relationships and has been critiqued in the literature^{5,9,10} – correlation does not *always*

equal causation, but correlation can suggest a causal relationship (see Section 2). More importantly, the first aphorism does not imply the second: imperfectly designed experimental studies can mistakenly suggest causal relationships where none exist, and causation can, in fact, be established through well-designed observational studies^{11–13}. Natural history approaches, for instance, have long been used to establish credible causal claims (e.g., sea otters driving trophic cascades in subtidal communities^{14,15}). Recently, interest in observational approaches has grown^{16,17} due to the economic, ethical, and logistical challenges of manipulating ecological variables¹⁸ and the limitations of experiments in capturing complex, large-scale causal relationships in nature¹⁹. Observational data, particularly from multiple locations and time points, are increasingly valued for complementing experiments and supporting more generalizable causal claims^{19–21}.

To formalize the requirements for making causal claims from experimental and observational data, scholars in various fields have made substantial advances in mathematical and statistical tools over the past 50 years ^{12,22–28}. Applications of these advances have changed how we think about scientific topics such as environmental and genetic causes of disease ^{29–31}, military veterans' health ³², criminology ^{33,34}, and education ^{35,36}, and have influenced policies on air pollution ^{37,38} and carcinogens ³⁹. These same advances are increasingly being proposed by ecologists to investigate causal questions using observational ^{9,27,40–49} and experimental data ^{50–52}.

Yet the way in which these advances relate to each other is not readily apparent from the published literature. For example, what are the conceptual connections between studies that use experimental designs and studies that use convergent cross mapping algorithms? Published reviews typically focus on one set of approaches at a time (e.g., quasi-experimental designs,

structural causal models, dynamical systems)^{27,41,44,53,54}, which makes it difficult for ecologists to understand how, or if, the seemingly disparate approaches are related.

70

71

72

73

74

75

76

77

78

79

80

81

82

83

84

85

86

87

88

89

90

91

92

In this Perspective, we connect the assumptions, tasks, frameworks, and methods across these approaches, thereby providing a synthesis of the concepts and methodological advances for detecting and quantifying causal relationships in ecological systems. When answering a causal question, we must first identify the appropriate causal task: either causal discovery, which focuses on detecting whether causal relationships are likely to exist between variables in a system, or causal inference, which focuses on quantifying the direction and magnitude of causal relationships without bias. To accomplish these tasks, we employ causal frameworks, such as the structural causal model framework¹², the potential outcomes framework²⁵, or the dynamical systems causality framework^{55,56}, which formally define causal relationships and specify the assumptions that must be satisfied to accurately detect or quantify causal relationships from data. These frameworks then guide the selection of causal methods, that is, study designs and algorithms, which are used to operationalize these assumptions and establish the conditions necessary to make causal claims. To outline the process of navigating tasks, frameworks, and methods, we created a workflow of best practices for answering causal questions in ecological research. To provide further readings and software to implement the ideas in the Perspective, we provide comprehensive Supplemental Information.

Throughout our Perspective, we highlight how well-articulated causal assumptions are the "glue" that unifies the myriad approaches to answering causal questions in ecology. These assumptions, together with the research question, shape every decision in the workflow – guiding which pre-existing knowledge is relevant, which causal task is pursued, and which study design or algorithm is implemented. Because understanding these assumptions is a prerequisite for

using the workflow, we provide a clear articulation of the fundamental causal assumptions required to move from correlation to causation. These assumptions also facilitate transparent discussions about the adequacy of the study designs and algorithms that help scholars move from observations of statistical dependence in data to claims about causal relationships in ecological systems.

2 <u>USING ASSUMPTIONS TO MOVE FROM CORRELATION TO CAUSATION</u>

Data never "speak" by themselves. To derive meaningful causal insights from data, we must rely on well-defined hypotheses, statistical models grounded in ecological theory, and both testable and untestable assumptions^{57–59}. The importance of hypotheses, appropriate statistical models, and statistical assumptions is well known in ecology.

Less well known is the importance of causal assumptions that allow researchers to go from making claims about correlations to making claims about causation. Unlike most statistical assumptions, causal assumptions are typically untestable; that is, causal assumptions cannot be verified from data, even unlimited data. For example, experimentalists assume that randomization of a treatment ensures that any differences in outcomes across the randomized groups can only be attributed to the treatment or sampling variability⁵⁰. Yet, this assumption cannot be verified. Causal assumptions, when combined with principles of probability theory and statistical dependence, allow us to make causal claims from data. The formalization of these assumptions is one of the most important scientific advances for answering causal questions^{26,28,58}. For more details on the contrast between statistical and causal assumptions, see Supplementary Note 1.

Causal assumptions, in tandem with statistical assumptions about the data structure, establish when statistical dependence can be interpreted as evidence for the perturbation-based notion of causality 12,25,27,60 . Consider a scenario in which we seek to determine whether, or by how much, variation in the abundance of aphid predators (e.g., ladybird beetles) (X) changes aphid abundance (Y). If our knowledge about the probability of aphid abundance changes after learning something about ladybird beetle abundance, then the two variables are statistically dependent. This dependence forms the starting point for using data to investigate potential causal relationships between two variables.

Statistical dependence is linked to causality through the Common Cause Principle⁶¹, which states that if a statistical dependence exists between two variables X and Y, then at least one of the following is true: X causes Y, Y causes X, or X and Y are both caused by a third variable C (Fig. 1). In ecology, a commonly used measure of statistical dependence is correlation, which describes the linear similarity between two sets of observations. The presence of correlation can therefore signal a causal relationship. The lack of correlation, however, does not necessarily rule out statistical dependence or causality, as correlation is just one possible measure of dependence between two variables.

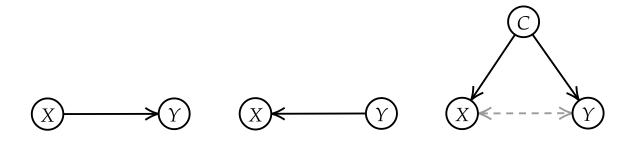


Fig. 1. Statistical dependence implies three possible causal relationships: X causes Y, Y causes X, or X and Y are caused by a common variable C. All three relationships can exist simultaneously

in many contexts (indicated by the dashed grey arrows). Causal assumptions aim to eliminate the third possibility because the presence of C introduces additional statistical dependence between X and Y that is not due to any direct causal relationship.

In causal analyses, we wish to distinguish variables with direct causal links from those that are not causally influencing each other. Thus, eliminating the possibility that a third variable C causes both X and Y is often a priority (i.e., we seek to eliminate non-causal, rival explanations for statistical dependencies). For example, in Fig. 2 broad-spectrum pesticide use affects ladybird beetle abundance and earthworm abundance. However, beetle abundance does not influence earthworm abundance, nor vice versa. In this case, any observed statistical dependence between beetle abundance (X) and earthworm abundance (Y) is entirely attributable to their common cause, pesticide use (C).

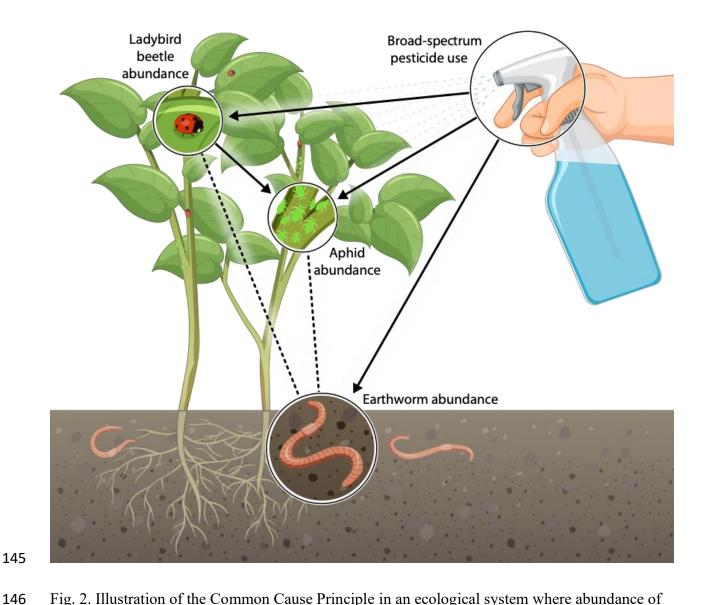


Fig. 2. Illustration of the Common Cause Principle in an ecological system where abundance of ladybird beetles, aphids, and earthworms are statistically dependent but not necessarily causally related. Solid arrows represent directional causal relationships, and dashed lines represent

To eliminate these "common causes" (a.k.a., "confounding variables" or "confounders"),
researchers make three assumptions: the Causal Sufficiency Assumption²⁸, the Causal Markov

statistical dependence but not causal relationships.

Condition^{61–63}, and the Causal Faithfulness Assumption²⁸ (Box 1). Together, these untestable assumptions allow us to distinguish direct causal relationships between variables from dependence between variables induced by a common cause. By including all common causes in a model of the relationship between X and Y (A1 in Box 1), we can eliminate the portion of dependence due to those common causes C (A2). Any remaining statistical independencies can be interpreted as evidence of no causal relationship between the variables (A3), while any remaining dependence implies the possibility of a direct causal relationship.

For example, if pesticide use is a common cause of both ladybird beetle abundance and aphid abundance, then we should include pesticide use in a model of the relationship between ladybird beetle abundance and aphid abundance (Fig. 2). If pesticide use is the only common cause and, after conditioning on it, beetle abundance is statistically independent of aphid abundance (i.e., they are conditionally independent), then, under the three causal assumptions, we can infer that no causal relationship exists between them. Conversely, if beetle abundance and aphid abundance are *not* independent conditional on pesticide use, then a causal relationship between beetle abundance and aphid abundance may exist (i.e., a lack of conditional independence means we cannot rule out a causal relationship, but it does not provide definitive evidence of causation).

The three causal assumptions required to connect statistical dependence to causal dependence – Causal Sufficiency, Causal Markov Condition, and Causal Faithfulness – are the foundation upon which causal claims are made from experimental and observational data. These causal assumptions allow us to differentiate the causal dependencies between two variables from the non-causal dependencies created by confounding variables.

Box 1. Three fundamental causal assumptions

For these assumptions, we define two variables X and Y as statistically dependent if the probability that Y takes a specific value given that X has taken a specific value is different from the probability that Y takes a specific value without any information about the value that X has taken (i.e., $P(Y|X) \neq P(Y)$). In other words, if X and Y are statistically dependent, knowing something about X changes what is known about the probability of Y.

- A1. Causal Sufficiency⁵² (a.k.a., the "no unmeasured confounding" assumption^{55–57}), requires that we observe all variables in a set C that causally influence any pairs of variables X and Y, and we include C in our model that describes the relationship between X and Y, thus ensuring that no confounding variables are unobserved.
- A2. The **Causal Markov Condition**^{54,58,59} states that if a pair of variables X and Y are statistically dependent solely because both are caused by a common variable C, and if we control for C by including it in our model, then X and Y become conditionally independent given C.
- A3. Causal Faithfulness⁵², stated very loosely, declares that statistical independence (conditional or unconditional) between a pair of variables *X* and *Y* indicates the absence of a causal relationship between those variables.

The combination of the Causal Markov Assumption (A2) and the Causal Faithfulness Assumption (A3) allows us to claim that if two variables, X and Y, are conditionally independent when C is included in the model, then X and Y are not causally related but instead are caused by a third common variable C. The Causal Sufficiency Assumption (A1) then ensures that we can distinguish causal relationships from dependence induced by a common cause if we include all possible confounders between variables in a model that describes the relationship between X and Y.

The Causal Markov and Causal Faithfulness assumptions have formal definitions requiring technical notation that are beyond the scope of this article. For a full discussion of these assumptions, we refer the reader to Pearl²³ and Spirtes and Zhang⁶⁰.

3 <u>SATISFYING CAUSAL ASSUMPTIONS WITH PRE-EXISTING KNOWLEDGE</u>,

STUDY DESIGNS, AND ALGORITHMS

Given the restrictive and untestable nature of the three causal assumptions introduced in Section 2, ecologists may wonder whether causal claims can realistically be made from ecological data, since satisfying these assumptions requires building models that account for all confounders. Unlike models built for prediction or description, models built to make causal claims cannot be validated using goodness-of-fit or predictive accuracy metrics, as these metrics assess how well a model describes the observed data but do not evaluate how well the model satisfies the untestable assumptions required for making causal claims^{64,65} (for more details, see Supplementary Note 2). In the following subsections, we describe how the foundations for satisfying causal assumptions are provided by pre-existing knowledge, study designs, and algorithms.

3.1 Pre-existing knowledge

To determine if the three causal assumptions can be satisfied in a specific study context, pre-existing knowledge is essential⁵⁹. Pre-existing knowledge guides us in our efforts to identify potential confounders and other potential factors that produce variation in the causal variable(s) (Section 5). It helps us determine which confounders can be measured^{43,66,67} and which are likely unobservable, a determination that guides the choice of study designs or algorithms (see Section 3.2). Pre-existing knowledge can also be used to detect or rule out the presence of uncontrolled confounders through, for example, falsification tests (see Section 8). The more pre-existing knowledge to which we have access, the stronger the causal claims that we can make from an

analysis of data (i.e., the more plausibly we can eliminate non-causal, rival explanations for statistical dependencies).

Pre-existing knowledge can include general and domain-specific ecological theory, subject matter expertise, field experience, and findings from other studies, including studies that use empirical approaches lacking causal interpretations (see Supplementary Note 2). Because pre-existing knowledge is often complex and wide-ranging, we need succinct and straightforward ways to summarize it. In Section 5, we describe two common tools for organizing our understanding of an ecological system (i.e., our 'mechanistic knowledge'⁶⁷).

3.2 Study designs and algorithms

Pre-existing knowledge is typically not sufficient to satisfy causal assumptions. For instance, even if we can identify all confounders with pre-existing knowledge, we are unlikely to be able to measure them all, which would be necessary to satisfy the Causal Sufficiency Assumption. However, study designs and algorithms provide us with the opportunity to address such challenges by relaxing one or more of the three causal assumptions in Section 2 in favor of equally untestable but (hopefully) more plausible causal assumptions.

Experimental designs, for example, substitute the Causal Sufficiency Assumption with the assumption that treatment randomization eliminates the effects of unmeasured confounding variables^{25,68}. Confounders are thus addressed through design rather than measurement. In non-experimental studies, observational designs often relax the Causal Sufficiency Assumption through statistical techniques that define the minimum set of confounding variables that need to be observed to accomplish the desired causal task^{57,58,69}, or through statistical techniques that

allow researchers to pursue alternative research goals that reduce the number of confounders that must be measured (e.g., by defining alternative causal effects^{70,71} or by detecting and accounting for possible unmeasured confounders⁵³). These statistical techniques and redefined research goals can also be used with experimental designs that face implementation challenges, such as when the experimental manipulation affects the outcome variable through other pathways (i.e., randomization is a confounder), or when post-randomization observations are missing (i.e., attrition). We provide more details on both experimental and observational study designs and algorithms in Section 8.

8:

4 A WORKFLOW FOR ANSWERING CAUSAL QUESTIONS IN ECOLOGY

We present a comprehensive workflow that summarizes the best practices for systematically addressing causal questions in ecology (Fig. 3). The workflow serves as a roadmap, beginning with the causal question and ending with the interpretation and validation of results. Each step in the workflow marks a decision point that reflects a best-practice principle that ensures our causal research is robust, transparent, and aligned with the assumptions necessary to make causal claims from statistical analyses of ecological data. The workflow is designed to be flexible, so ecologists can adapt it to their pre-existing knowledge, data, and preferred methods.

Here, we summarize the workflow steps, and we elaborate on them in Sections 5 through

1. **Define the Causal Question and Summarize Pre-Existing Knowledge** (Section 5):

Before any data are collected or examined, develop a clear, testable causal hypothesis

and describe all potential confounders.

We first define the causal research question with at least one outcome variable (Y) and one or more hypothesized causal variables (X) (see Supplementary Note 2 for differences between causal and non-causal questions in ecology). Then, to identify all confounding variables, we assess the corpus of pre-existing knowledge on the causes and outcomes of interest. We can summarize this knowledge using causal diagrams or thought experiments.

2. **Define the Causal Task** (Section 6): Choose a causal task that matches the study's causal question and the depth of available prior knowledge.

When answering causal questions, we use pre-existing knowledge to determine whether to pursue causal discovery or causal inference. Causal inference, which seeks to quantify the magnitudes of causal relationships, is feasible when we have sufficient pre-existing knowledge to be confident of the causal, outcome, and confounding variables and the directions of the causal relationships. If this knowledge is insufficient, we can instead pursue causal discovery, which aims to detect the existence and direction of causal relationships.

3. **Select Framework** (Section 7): Adopt a formal causal framework through which causal assumptions can be explicitly articulated, tested, and communicated.

To clearly articulate the causal and statistical assumptions that must be satisfied for valid claims in either causal task, we can use one or more causal frameworks. The potential outcomes framework and the structural causal model framework are two common frameworks used for causal inference. For causal discovery, the structural causal model and dynamical systems causality frameworks are frequently used.

4. Select Study Design or Algorithm, Collect Data and Apply Estimation Methods,

Obtain Results, and **Interpret Results** (Section 8): Select a study design or algorithm that aligns with the study's articulated causal assumptions, and then rigorously assess the plausibility of those assumptions and implications of violations to those assumptions when drawing conclusions.

For causal inference, study designs can be grouped into three categories: experimental designs, observational designs for measured confounders, and observational designs for unmeasured confounders. Within these categories, many approaches exist, (e.g., regression adjustment⁷², propensity score matching^{45,73}, and structural equation modeling⁹). For causal discovery, algorithms are used instead of study designs. These fall into four categories: constraint-based, score-based, functional model-based, and dynamical systems causality-based. Within these categories, many algorithms are available (e.g., convergent cross mapping²⁷, fast causal inference²⁸, and greedy equivalency search⁷⁴). Based on the requirements of the study design or algorithm, we then collect data and apply estimation methods to detect causal relationships or quantify causal effect(s). Afterwards, we interrogate the plausibility of the causal and statistical assumptions by identifying potential violations to the assumptions and exploring the implications of those violations for the conclusions.

To illustrate the workflow's application to real-word ecological research, we use two example ecologists, an intertidal ecologist and a tiger ecologist. In Box 2, we summarize how each ecologist navigates the workflow.

Although we present the workflow in a linear fashion, researchers can use it iteratively in two ways: (i) the results from one causal analysis will feed into future analyses in the form of pre-existing knowledge⁶⁷ (grey arrow in Fig. 3); and (ii) after taking actions at one step, researchers may need to return to previous steps before advancing in the workflow (e.g., refining the causal question if prior knowledge is insufficient; reassessing the study design if data collection did not go as planned).

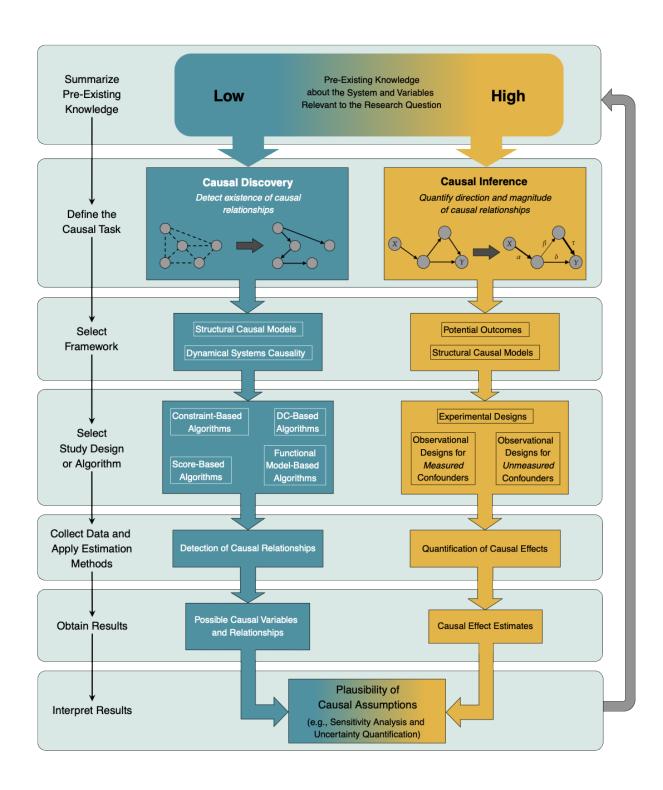


Fig. 3. A best-practice workflow that outlines the key steps and decisions for answering causal questions in ecological research.

Box 2. Ecologists conducting causal research using the best-practice workflow in Fig. 3.

"Define the Causal Question and Summarize Pre-Existing Knowledge"

An intertidal ecologist seeks to quantify the change in bivalve abundance (Y) caused by floods (X) through changes in nitrogen (M_1) and salinity (M_2) in intertidal zones at the mouth of an estuary. The ecologist summarizes knowledge about all confounders for each of the causal relationships of interest (i.e., floods on bivalves, floods on nitrogen, floods on salinity, nitrogen on bivalves, and salinity on bivalves).

A tiger ecologist seeks to determine the ecological factors (X) that encourage tigers to make more visits or spend more time (Y) in certain locations. The ecologist summarizes knowledge about confounders of the causal relationship between ecological factors and tiger occupancy (e.g., geographic and human factors).

"Define the Causal Task"

The intertidal ecologist has robust ecological theory and a large collection of prior studies to identify the full set of confounders that could bias estimation of any one of the causal relationships of interest. Thus, the ecologist decides to pursue causal inference.

The tiger ecologist has theory and field observations to identify some ecological factors that may influence tiger occupancy, but they do not have sufficient knowledge to identify all human and geographic confounders. Thus, the ecologist decides to pursue causal discovery.

"Select Framework"

The intertidal ecologist adopts the structural causal model framework, which they prefer for its structural approach to reasoning about multiple causes jointly.

The tiger ecologist adopts the dynamical systems causality (DC) framework to accommodate the complex and evolving dynamics of their study system.

"Select Study Design or Algorithm"

The intertidal ecologist selects an observational study design in which they measure and condition on all confounders. The tiger ecologist selects a DC-based algorithm appropriate for causal discovery when many confounders are unmeasured.

"Collect Data and Apply Estimation Methods"

The intertidal ecologist collects observational cross-sectional data on <u>all</u> causal, outcome, and confounding variables related to the causal relationships of interest and then fits a structural equation model to quantify the causal relationships of interest.

The tiger ecologist collects observational time series data for tiger occurrence, abundance of prey species, poaching activity, and weather conditions at a series of locations and uses convergent cross mapping (CCM) to detect causal relationships between pairs of variables.

"Obtain and Interpret Results"

The intertidal ecologist obtains estimates of the causal effects of floods on bivalve abundance that arise though the changes in nitrogen and salinity. They perform a causal sensitivity analysis that quantifies how much the estimates change in the presence of an unmeasured confounder.

The tiger ecologist obtains a network with detected causal relationships between pairs of variables. They perform a sensitivity analysis that shows how the detected causal relationships change when the CCM hyperparameter settings are changed.

5 <u>SUMMARIZE PRE-EXISTING KNOWLEDGE</u>

One common conceptual tool for summarizing pre-existing knowledge is a causal diagram. Causal diagrams help us organize our pre-existing knowledge by visually mapping the presumed causal relationships among causes (*X*), their outcomes (*Y*), and confounders (*C*). The most widely-used causal diagram is the causal directed acyclic graph (causal DAG), which follows a set of formal rules that define how causal relationships must be encoded⁷⁵. A causal DAG includes the focal variables of a study (i.e., the "cause" and the "outcome" variables), along with all suspected common causes (i.e., confounders) between the focal variables. Directed edges (arrows) between variables indicate that unidirectional causal relationships are presumed to exist, and the absence of an arrow between two variables reflects a strong assumption that a causal relationship does not exist¹². Causal DAGs, which must include all potential confounders of presumed causal relationships, enable us to identify the confounders we need to address with experimental or statistical techniques. Thus, causal DAGs should be constructed at the beginning of a study, before data are collected and the specific study design or algorithm is chosen.

Some ecologists will be familiar with the structural equation model (SEM) diagram⁹, which can be interpreted as a causal DAG when its structure represents only unidirectional relationships and explicitly encodes assumptions about causal relationships, including all relevant confounders^{76,77}. SEM diagrams also include additional parametric assumptions and are purpose-built for SEM analyses⁷⁶, whereas causal DAGs, which require no assumptions about the functional forms of causal relationships, can be used in any type of causal analysis.

Another conceptual tool for summarizing pre-existing knowledge is a thought experiment in which researchers consider how they would conduct a hypothetical ideal randomized controlled trial (RCT) – often termed a "target trial" ^{78,79} – to answer their causal research question²⁵. By comparing the ideal (target) trial with the actual data generating process, we can identify discrepancies that may lead to bias through confounding variables that distort the observed relationship between the causal variable and the outcome. Formulating such a target trial forces us to articulate all the key components of an ideal RCT and then systematically determine which of these components may be absent or imperfect in our study. In doing so, it becomes clearer which variables, including potential confounders, should be accounted for in the analysis to emulate the conditions of an ideal experiment. Just as drawing causal DAGs helps visualize the network of causal relationships and identify confounders, formulating these thought experiments provides a concrete tool for planning rigorous study designs (i.e., the thought experiment forces us to ask the question, "Where does the variation in the causal variable come from?" or, equivalently, "What is the treatment assignment mechanism?"). For resources that describe how to draw causal DAGs or develop RCT thought experiments for studies, see Supplementary Note 3.

334

335

336

337

338

339

318

319

320

321

322

323

324

325

326

327

328

329

330

331

332

333

6 DEFINE THE CAUSAL TASK – CAUSAL DISCOVERY OR CAUSAL INFERENCE

In choosing the most appropriate causal task for a research question, we must carefully consider the gap between available knowledge and the knowledge that would be required to plausibly satisfy causal assumptions. When pre-existing knowledge is extensive, we may pursue the task of causal inference. When pre-existing knowledge is limited, we may instead pursue

causal discovery. Although the dividing lines between these two tasks are not as clearcut as implied in our workflow (i.e., causal research lies on a continuum rather than in one of two camps), the contrast between their goals is illuminating for understanding how each task draws on pre-existing knowledge.

The goal of **causal inference** is to quantify the magnitudes of causal effects, such as the effect of a change in temperature of one degree on wildlife mortality or the effect of the introduction of a wildfire suppression program on tree species composition. Causal inference requires substantial pre-existing knowledge about which variables act as causes, outcomes, and confounders, as well as the directions of causal processes ("high" pre-existing knowledge in Fig. 3). Quantifying multiple causal effects within an ecological system is even more challenging because sufficient pre-existing knowledge must exist to satisfy the required causal assumptions for every pair of cause-outcome variables.

To quantify causal effects, all causal strategies begin by defining the specific effect(s) of interest that connects theoretical quantities to data. Different causal effects require different variations of the causal assumptions⁸⁰. Ecologists are often interested in the average effect of X on Y across all observations, that is, the average change in the outcome Y per unit change in X. However, other effects may also be relevant, such as average effects for subgroups⁸¹ and mediation effects⁸² (effects of intermediary variables between a cause and its outcome). Moreover, some causal effects may be preferred because the causal assumptions for these effects can be more plausibly satisfied for a study (e.g., complier average causal effects, local average treatment effects, etc.).

In contrast to causal inference, **causal discovery** aims to detect or "learn" causal relationships among measured variables, such as whether there is a causal relationship between

sardine and anchovy populations and in what direction(s). Although causal discovery requires causal assumptions, the assumptions are less restrictive than they are in causal inference, and thus, less pre-existing knowledge is required ("low" pre-existing knowledge in Fig. 3). While causal discovery methods offer flexibility in investigating causal questions with limited pre-existing knowledge, this advantage comes with the trade-off of potentially less precise or less certain conclusions about causal relationships. Causal discovery is therefore primarily valuable for generating more knowledge to guide subsequent studies.

To detect causal relationships, all causal discovery strategies begin by defining an initial causal diagram (see Section 5) and then refining it with statistical evidence from data. One strategy begins with a causal diagram that assumes causal relationships exist among all variables. Statistical independence tests are then systematically applied to eliminate connections between variables where evidence of a causal relationship is not supported by the data⁵³. Another strategy starts with a causal diagram that assumes no causal connections among variables and iteratively adds them where statistical evidence suggests a potential causal relationship⁸³. Both strategies rely on variations of the three causal assumptions introduced in Section 2 and aim to produce a refined causal diagram that reflects only the causal relationships consistent with the observed data and the underlying assumptions.

7 SELECT A CAUSAL FRAMEWORK

Both causal inference and causal discovery rely on untestable causal assumptions (Section 2) that allow researchers to interpret statistical patterns as evidence of causation. Causal frameworks structure how these causal assumptions are represented for a given task, ensuring consistency among study design/algorithm, data collection, and estimation procedures.

7.1 Causal frameworks for causal inference

For causal inference, assumptions and estimation procedures are expressed using one of three causal frameworks: the Neyman-Rubin causal model, also commonly known as the potential outcomes (PO) framework; the structural causal model (SCM) framework; and the decision-theoretic framework²². We focus on the PO and SCM frameworks, but readers interested in the decision-theoretic framework can refer to Dawid (2000)²² and Dawid (2012)⁸⁴.

The choice of framework is primarily based on researcher preferences, as the PO and SCM frameworks have been shown to be logically and mathematically equivalent^{85–87}. The PO framework may appeal to experimentalists because it expresses causal assumptions by approximating the conditions that most accurately represent an idealized "gold standard" randomized controlled experiment. Alternatively, researchers who primarily model ecological systems as collections of simultaneously interacting variables may prefer the SCM framework, which represents systems as causal DAGs. Structural equation modeling, when used to make causal claims under causal assumptions^{9,46}, is a subset of the SCM framework^{77,88}.

The ways in which the PO and SCM frameworks express causal assumptions for causal inference are described in Supplementary Note 4 and Box S1. Resources for learning more about the core concepts of the PO and SCM frameworks can be found in Supplementary Note 5.

404

405

406

407

408

409

410

411

412

413

414

415

416

417

418

419

420

421

401

402

403

7.2 Causal frameworks for causal discovery

For causal discovery, the assumptions and estimation procedures are expressed using either the SCM framework or the dynamical systems causality (DC) framework^{55,56}. Causal discovery using the SCM framework is well-suited for ecological systems with multiple interacting variables, where causal relationships are expected to be stable across observations. SCM-based causal discovery algorithms also allow researchers to incorporate pre-existing knowledge by specifying constraints on potential causal relationships, making them particularly useful for exploratory studies where some causal relationships are known or hypothesized. In contrast, the DC framework may be more suitable for complex dynamic systems where causal effects unfold over time and cannot be represented as static combinations of causes. DC-based algorithms typically use time series data to infer causal relationships by testing whether knowledge of one variable's past improves the ability to anticipate changes in another variable. Measures of improvement are typically comprised of changes in predictability or statistical dependence, including those estimated by information-theoretic measures^{83,89}. In both the SCM and DC frameworks, multiple causal diagrams can be consistent with the same structure of statistical dependencies in data, but pre-existing knowledge can refine the causal diagrams by constraining what relationships are possible.

The ways in which the SCM and DC frameworks express causal assumptions for causal discovery are described in Supplementary Note 4 and Box S2. Resources for learning more about the core concepts of the SCM and DC frameworks can be found in Supplementary Note 5.

8 <u>SELECT A STUDY DESIGN OR ALGORITHM, APPLY ESTIMATION METHODS,</u> OBTAIN RESULTS, AND INTERPRET RESULTS

Study designs for causal inference and algorithms for causal discovery provide structured approaches for satisfying or relaxing the untestable causal assumptions through decisions about the data and analysis (i.e., designs and algorithms operationalize causal frameworks). Designs and algorithms also lead us to appropriate methods for estimation and interpretation of the results.

This section provides an overview of key study designs and algorithms. Their details and applications are beyond the scope of this Perspective, but in Supplementary Note 6 we provide resources, including guidance on implementation and relevant software packages. While we focus on foundational study designs and algorithms, we summarize in Supplementary Note 7 some advanced approaches, including those that integrate machine learning techniques, which are rapidly emerging and may offer new opportunities for causal research in ecology.

8.1 Study designs for causal inference

Study designs for causal inference fall into three categories: (1) experimental designs that aim to minimize confounding from both measured and unmeasured variables through

manipulation of the causal variable, (2) observational designs that explicitly identify and control for measured confounders, and (3) observational designs that eliminate unmeasured, and potentially unknown, confounding by leveraging external sources of variation. Representative approaches from these three categories are listed in Table 1 (references, applications, and available software implementations are provided in Table S6).

Table 1. Descriptions of study designs for causal inference.

Category	Representative Approaches ^a	Description
Experimental designs	Randomized Controlled Trials	Randomly assign units, or clusters of units, to treatment or control groups, which can address all confounders across groups ("all" = both measurable and unmeasurable confounders).
	Factorial Designs	Randomly assign units to combinations of treatments, which can address all confounders across all treatment combinations (interactions).
	Crossover Trials	Assign units to treatment and control conditions in a random sequence, which can address all confounders by allowing each unit to serve as its own control.
Observational Designs: Controlling measured	Regression Adjustment	Reweight observations using regression models, which can address measured confounders across groups exposed to different values of a cause ("cause" = a causal variable).
confounders	Multi-level Modeling with Mixed Effects	Reweight observations using regression models, which can address measured confounders ("fixed effects") across groups exposed to different values of a cause.
	Structural Equation Modeling	Reweight observations using systems of regression models, which can address measured confounders across groups exposed to different values of a cause. ^b
	Marginal Structural Modeling ^c	Reweight observations over time using regression models, which can address measured confounders across groups exposed to different values of a cause when those values vary over

		time and confounders may be affected by past values of the cause.
	Subgroup (Stratified) Analysis	Reweight observations by grouping units into subgroups made during study design (e.g., stratified sampling) or analysis (e.g., subgroup comparisons), which can address measured confounders across groups exposed to different values of a cause.
	Covariate and Propensity Score Matching	Reweight observations by matching units on their probability of being exposed to a specific value of the cause (propensity score matching) or on a metric of similarity in the values of confounders (e.g., Mahalanobis distance metric), which can address measured confounders across groups exposed to different values of a cause. Inverse propensity scores (i.e., Inverse Probability Weighting, IPW) can also be used as alternative weights in other approaches, like regression models.
Observational Designs: Controlling unmeasured	Instrumental Variables	Use a variable that affects the cause but has no direct effect on the outcome, which can address all unmeasured confounders for a subset of the units (units called "compliers").
confounders	Regressions Discontinuity Design	Use a variable that, at specific values, creates discontinuous change in the value of a cause but has no effect on the outcome, which can address all unmeasured confounders for a subset of the units (units "near" the discontinuity value).
	Front-door Criterion	Use measured variables that comprise all intermediate variables on the causal path between a cause and an outcome, which can address all unmeasured confounders across groups exposed to different values of a cause.
	Before-After-Control-Impact ^c	Use within-unit, temporal variation in the cause within a subset of units, which can address unmeasured confounders that are constant across time or are varying at scales larger than the unit. The BACI approach is also known as Difference-in-Differences. Extensions exist, such as two-way fixed-effects and matrix completion methods.
	Multi-level Modeling with Fixed Effects ^c	Use within-unit, temporal variation in the cause within a subset of units, which can address

		unmeasured confounders that are constant across time or are varying at scales larger than the unit.
	Synthetic Control Methods ^c	Construct synthetic control groups from a weighted combination of unexposed units, which can address unmeasured confounders across groups exposed to different values of a cause.
	Interrupted Time Series Analysis ^d	Use a sudden change in a cause from a known source, which can address unmeasured confounders from pre-existing trends in the outcome.
	Principal Stratification	Reweight observations by grouping units based on their potential values of a post-treatment variable (e.g., attrition), which addresses unmeasured confounders that operate through the post-treatment variable.

^a In practice, multiple approaches can be combined to more credibly satisfy causal assumptions.

Experimental designs are often well-suited for causal inference because they provide a structured approach for directly manipulating the causal variable and defining the temporal order of cause and effect^{50,90}. Through strategies like randomization, we aim to control or eliminate the effects of confounding variables, which provide justification for causal claims. However, suboptimal decisions in the design and analysis of experiments can produce invalid causal conclusions⁹¹, and even well-designed experiments may face challenges⁹², such as non-compliance or non-random dropout. Moreover, in ecology, experiments may be prohibitively expensive at the scales needed to detect causal effects, or they may distort natural ecological conditions⁸², making them impractical or unrepresentative.

^b With additional assumptions, SEMs can incorporate unobserved constructs (i.e., "latent variables") which are inferred from measured variables.

^c Requires longitudinal data for which the value of the causal variable varies within and across units.

^d Requires longitudinal data for which the value of the causal variable varies within units.

When experiments are infeasible, impractical, or unethical, observational designs for measured and unmeasured confounders are available. Advances in causal approaches for observational studies provide statistical techniques to satisfy causal assumptions without experimental manipulation^{12,22,25,75,93}. Observational designs for measured confounders rely on measuring all confounding variables^{9,72,73}. When measuring, or even knowing, all relevant confounders is not feasible, we can use observational designs for unmeasured confounders. These designs relax the causal sufficiency assumption of no unmeasured confounders by replacing it with assumptions about the structure of unmeasured confounders, typically informed by pre-existing knowledge. These designs then use statistical techniques to represent the influence of confounders based on their assumed structure^{94,95}, without needing to directly measure the confounders.

Experimental and observational designs can be implemented using either cross-sectional or longitudinal data. However, strong assumptions about temporal ordering (cause must precede its outcome) and stable effects over time are required to quantify causal effects using cross-sectional data.

Once data are collected, we can quantify the causal effect of interest using a range of estimation methods ("Collect Data and Apply Estimation Methods" and "Obtain Results" in Fig. 3). Many estimation methods are available to implement a chosen study design, each providing a different statistical approach for estimating the causal effect of interest^{96,97}. After estimating a causal effect, we must then interrogate the plausibility of the causal assumptions underlying the study design and explore the implications of violations to these assumptions ("Interpret Results" in Fig. 3). One common approach for assessing the implications of violations is to perform causal sensitivity analyses, which quantify how an estimated effect would change in the presence

of unaddressed confounding. Many sensitivity analysis techniques are available for a variety of causal inference methods^{98–102}, including SEM¹⁰³. An alternative approach to interrogating the plausibility of causal assumptions involves detecting under-adjustment of confounding variables by drawing on pre-existing knowledge to formulate tests of known effects^{11,104,105} (e.g., falsification or placebo tests). We must also consider how other forms of bias^{106,107}, such as selection bias^{108,109} and measurement bias^{110–112}, may influence the estimated effects and the robustness of our conclusions.

8.2 Algorithms for causal discovery

Algorithms for causal discovery fall into four categories: DC-based algorithms and three types of SCM-based algorithms, which are called constraint-based, score-based, and functional model-based algorithms. Representative algorithms from these four categories are listed in Table 2 (references, applications, and available software implementations are provided in Table S7). DC-based methods are suited for dynamic systems and assess causal relationships based on predictability and information flow over time. Constraint-based methods use conditional independence tests to eliminate implausible causal relationships. Score-based methods evaluate possible graph configurations that represent causal interrelationships using a scoring criterion that captures how well the graph fits patterns of conditional independencies in the data. Functional model-based methods assume specific functional relationships between variables (e.g., linear or non-linear equations with noise) and infer causal direction by identifying which graph configuration satisfies those assumptions.

Category	Representative Algorithms	Description
Constraint-based methods	PC (Peter and Clark) FCI (Fast Causal Inference)	Uses repeated conditional independence tests to infer causal relationships from observed independencies in data, producing a set of causal graphs that represent possible causal relationships consistent with the data. Extends the PC algorithm to detect possible
	PCMCI (Peter and Clark Momentary Conditional Independence)	unmeasured confounders, producing a causal graph that reflects uncertainty about edges. A time-series adaptation of PC that improves detection of causal effects in autocorrelated data by iteratively testing for conditional independencies among variables and their lags.
Score-based methods	GES (Greedy Equivalence Search)	Searches for the best causal graph by iteratively adding or removing edges based on a scoring criterion, such as the Bayesian Information Criterion (BIC), balancing data fit and simplicity.
	GIES (Greedy Interventional Equivalence Search)	An extension of GES that incorporates interventional data or assumptions to distinguish between equivalent causal graphs.
	FGES (Fast Greedy Equivalence Search)	A variant of GES that uses a parallelized greedy approach to rapidly search for the optimal causal graph, making it suitable for high-dimensional datasets.
Functional model-based methods	LiNGAM (Linear Non- Gaussian Acyclic Model)	Identifies causal direction among variables by assuming linear relationships and non-Gaussian noise.
	ANM (Additive Noise Model)	Assumes the outcome variable is an unknown function of the causal variable plus independent additive noise, which enables identification of causal direction in both linear and nonlinear settings.
	IGCI (Information Geometric Causal Inference)	Determines causal direction by analyzing asymmetries in the joint distributions of cause-effect pairs, without inherently controlling for or detecting unmeasured confounders or indirect causal effects.
Dynamical systems	Granger Causality (GC)	Tests whether past values of one time series can predict future values of another, assuming linear relationships in time-series data.

causality (DC)-	Information Theoretic (IT)	A class of nonparametric and model-based
based methods	Causality	methods that infer direct causal relationships by
		quantifying how knowledge of one variable
		reduces uncertainty about the future states of
		another variable. Includes Transfer Entropy
		(TE) approaches.
	Convergent Cross Mapping	Uses state-space reconstruction to infer causal
	(CCM)	relationships in nonlinear systems by testing
		whether past states of the causal variable can
		reliably predict current states of another
		variable.
	Partial Cross Mapping	An extension of CCM that adjusts for potential
	(PCM)	unmeasured confounders to isolate direct causal
		relationships more accurately.

Causal discovery algorithms have been developed to accommodate different data structures, with approaches often tailored to either longitudinal data or cross-sectional data. DC-based methods require bivariate or multivariate time-series data (i.e., regularly spaced longitudinal data) to infer causal relationships through changes over time^{27,60}. In contrast, SCM-based algorithms can be applied to both cross-sectional and longitudinal data, but additional assumptions about temporal ordering (i.e., causes precede their outcomes) must be satisfied when using cross-sectional data^{28,74,113}. As with causal inference, pre-existing knowledge can enhance results from SCM-based discovery methods by explicitly specifying certain relationships that should or should not be included in the causal diagram.

Once candidate causal diagrams have been obtained ("Collect Data and Apply Estimation Methods" and "Obtain Results" in Fig. 3), we must assess whether the causal assumptions of the chosen discovery algorithm are plausible for the ecological system under study and explore the implications of violations to these assumptions ("Interpret Results" in Fig. 3). To assess the reliability of conclusions drawn from the causal discovery process and to evaluate the robustness

of the inferred causal relationships, sensitivity analyses that explore the stability of results across different parameter settings should be undertaken¹¹⁴.

9 CHALLENGES AND OPPORTUNITIES

Making valid causal claims from ecological data requires moving beyond analyses that use prediction- and association-focused models, which typically fail to represent the true underlying causal structures of ecological systems^{64,115,116}. It instead requires satisfying or carefully relaxing the causal assumptions that allow observed statistical dependencies to be interpreted as evidence of causal relationships.

The cornerstone of high-quality causal research is to deliberately and critically assess whether the requisite causal assumptions can be plausibly satisfied or relaxed given the available pre-existing knowledge, the selected causal task, and the chosen study design or algorithm.

While this assessment may seem daunting, especially given the complexity of ecological systems, advances in causal methodologies have demonstrated how the strength of causal claims can be more transparently communicated (see Box 3).

Box 3. Best practices for transparently communicating results from causal analyses in ecology.

- Clearly state and justify all the causal assumptions required by the study design or algorithm.
 - Studies that explicitly state and justify the assumptions underlying their causal claims allow subject matter experts to more effectively evaluate the credibility of these assumptions and use that evaluation to refine subsequent research.
- Frankly discuss the most likely sources of violations in causal assumptions that could invalidate the conclusions.
 - Transparency about potential unmeasured confounding variables or other violations to causal assumptions should be the norm in causal research.
- Report how detected or quantified causal relationships change under the most plausible potential violations of causal and statistical assumptions.
 - Perfectly satisfying causal assumptions is unlikely in any study, and thus an assessment of the robustness of conclusions to violations is an essential component of all high-quality studies (for examples, see Section 8).

537

538

539

540

541

542

543

544

545

546

As causal methods evolve, new advances help us relax or probe untestable assumptions in challenging real-world settings, which expands the relevance and applicability of causal methods to the complexities of ecological systems. Ecologists are uniquely positioned not only to benefit from these advances, but also to contribute meaningfully to their development. Ecologists' experiences with experimental study designs, multiscale complex systems, and the integration of biotic and abiotic processes offer valuable insights into widespread challenges in causal research, such as spatial interactions, downscaling, and unit-to-unit causation.

By connecting the causal assumptions, tasks, frameworks, and methods that play essential roles in causal research, our workflow (Fig. 3) provides a set of best practices for investigating

causal questions in ecology. The workflow emphasizes the role of causal assumptions, which help us to formalize pre-existing knowledge, align the causal task with the research objective, and select a study design or algorithm that satisfies those assumptions and guides data collection and analysis. Thus, our workflow not only supports ecologists in conducting rigorous and transparent causal research, but it also facilitates cogent discussions about the potential for unresolved weaknesses in prior studies, which can motivate new studies. Through an iterative application of the workflow, we can enhance the accumulation and synthesis of ecological knowledge.

As causal approaches become more accessible and adaptable, ecologists have an opportunity to refine long-standing questions, generate new theory, and develop credible causal explanations of the natural world.

Acknowledgements

This work emerged partly from discussions at the workshop "Causality in Ecology" in August 21–23, 2023 in Baltimore, MD, USA. We thank Johns Hopkins University for funding and Rachel Pickett, Carter Polston, Kip Hinton, and Shang Jones for assistance in hosting the workshop. We thank Ashley E. Larsen for insightful discussions during the workshop and feedback on drafts of the paper. H.E.C and P.J.F. acknowledge funding support from USDANIFA award 2023-67023-39033.

Author Contributions Statement

568

H.E.C. led the paper. H.E.C, L.E.D and P.J.F co-organized, and P.J.F. funded, the workshop in
which J.E.K.B., H.E.C., L.E.D., J.R.F., P.J.F., M-J.F., C.G., J.R. B.S., I.S., K.J.S., G.S., and
B.vH. contributed to establishing the goals and emphases of the paper. H.E.C., L.E.D and P.J.F
initiated the paper concept and framing. H.E.C. and P.J.F. wrote the main text. J.E.K.B., L.E.D.,
J.R.F., M-J.F., J.R. B.S., I.S., K.J.S., G.S., and B.vH. suggested edits to the drafts of the paper.
H.E.C. conceived and wrote the Supplemental Information.

REFERENCES

- Laland, K. N., Sterelny, K., Odling-Smee, J., Hoppitt, W. & Uller, T. Cause and Effect in Biology Revisited: Is Mayr's Proximate-Ultimate Dichotomy Still Useful? *Science* 334, 1512–1516 (2011).
- 2. Mayr, E. Cause and Effect in Biology. Science 134, 1501–1506 (1961).
- 3. Woodward, J. Causation in biology: stability, specificity, and the choice of levels of explanation. *Biol. Philos.* **25**, 287–318 (2010).
- 4. Ben-Menahem, Y. Causation in Science. (Princeton University Press, 2018).
- 5. Wagner, A. Causality in Complex Systems. *Biol. Philos.* **14**, 83–101 (1999).
- 6. Poliseli, L., Coutinho, J. G. E., Viana, B., Russo, F. & El-Hani, C. N. Philosophy of science in practice in ecological model building. *Biol. Philos.* **37**, 21 (2022).
- 7. Raerinne, J. Causal and Mechanistic Explanations in Ecology. *Acta Biotheor.* **59**, 251–271 (2011).
- 8. Woodward, J. *Making Things Happen: A Theory of Causal Explanation*. (Oxford University Press, 2004). doi:10.1093/0195155270.001.0001.
- 9. Shipley, B. Cause and Correlation in Biology: A User's Guide to Path Analysis, Structural Equations and Causal Inference with R. (Cambridge university press, Cambridge (GB), 2016).
- 10. Ross, L. N. Causes with material continuity. Biol. Philos. 36, 52 (2021).
- Rosenbaum, P. R. Known Effects. in *Observational Studies* 136–153 (Springer New York, New York, NY, 1995). doi:10.1007/978-1-4757-2443-1_5.
- 12. Pearl, J. *Causality: Models, Reasoning, and Inference*. (Cambridge University Press, Cambridge, U.K.; New York, 2009).

- 13. Dominici, F., Bargagli-Stoffi, F. J. & Mealli, F. From Controlled to Undisciplined Data: Estimating Causal Effects in the Era of Data Science Using a Potential Outcome Framework. Harv. Data Sci. Rev. (2021) doi:10.1162/99608f92.8102afed.
- 14. Estes, J. A. & Palmisano, J. F. Sea Otters: Their Role in Structuring Nearshore Communities. *Science* **185**, 1058–1060 (1974).
- 15. Estes, J. E., Smith, N. S. & Palmisano, J. F. Sea Otter Predation and Community Organization in the Western Aleutian Islands, Alaska. *Ecology* **59**, 822–833 (1978).
- 16. Sagarin, R. & Pauchard, A. Observational approaches in ecology open new ground in a changing world. *Front. Ecol. Environ.* **8**, 379–386 (2010).
- 17. Sagarin, R. & Pauchard, A. Observation and Ecology: Broadening the Scope of Science to Understand a Complex World. (Island Press/Center for Resource Economics, Washington, DC, 2012).
- 18. Benedetti-Cecchi, L. *et al.* Hybrid datasets: integrating observations with experiments in the era of macroecology and big data. *Ecology* **99**, 2654–2666 (2018).
- 19. De Boeck, H. J. *et al.* Global Change Experiments: Challenges and Opportunities. *BioScience* **65**, 922–931 (2015).
- 20. McCleery, R. *et al.* Uniting Experiments and Big Data to advance ecology and conservation. *Trends Ecol. Evol.* **38**, 970–979 (2023).
- 21. Wootten, T. & Pfister, C. The Motivation for and Context of Experiments in Ecology. in *Experimental ecology: issues and perspectives* (Oxford University Press, 1998).
- 22. Dawid, P. Causal Inference without Counterfactuals. J. Am. Stat. Assoc. 95, 407–424 (2000).
- 23. Holland, P. W. Statistics and Causal Inference. J. Am. Stat. Assoc. 81, 945–960 (1986).

- 24. Imbens, G. W. & Rubin, D. B. Causal Inference for Statistics, Social, and Biomedical Sciences: An Introduction. (Cambridge University Press, 2015).
 doi:10.1017/CBO9781139025751.
- 25. Rubin, D. B. Estimating causal effects of treatments in randomized and nonrandomized studies. *J. Educ. Psychol.* **66**, 688–701 (1974).
- 26. Rubin, D. B. Causal Inference Using Potential Outcomes: Design, Modeling, Decisions. *J. Am. Stat. Assoc.* **100**, 322–331 (2005).
- 27. Sugihara, G. *et al.* Detecting Causality in Complex Ecosystems. *Science* **338**, 496–500 (2012).
- 28. Spirtes, P., Glymour, C. N. & Scheines, R. *Causation, Prediction, and Search*. (MIT Press, Cambridge, Mass, 2000).
- 29. D'Onofrio, B. M. *et al.* Causal Inferences Regarding Prenatal Alcohol Exposure and Childhood Externalizing Problems. *Arch. Gen. Psychiatry* **64**, 1296–1304 (2007).
- 30. Pearce, N., Vandenbroucke, J. P. & Lawlor, D. A. Causal Inference in Environmental Epidemiology: Old and New Approaches. *Epidemiology* **30**, 311–316 (2019).
- 31. Pingault, J.-B. *et al.* Using genetic data to strengthen causal inference in observational research. *Nat. Rev. Genet.* **19**, 566–580 (2018).
- 32. White, R. F. *et al.* Recent research on Gulf War illness and other health problems in veterans of the 1991 Gulf War: Effects of toxicant exposures during deployment. *Cortex J. Devoted Study Nerv. Syst. Behav.* **74**, 449–475 (2016).
- 33. Beck, B., Antonelli, J. & Piñeros, G. Effects of New York City's Neighborhood Policing Policy. *Police Q.* **25**, 470–496 (2022).

- 34. Wikström, P.-O. H. & Kroneberg, C. Analytic Criminology: Mechanisms and Methods in the Explanation of Crime and its Causes. *Annu. Rev. Criminol.* **5**, 179–203 (2022).
- 35. Jacob, B. A. & Lefgren, L. Remedial Education and Student Achievement: A Regression-Discontinuity Analysis. *Rev. Econ. Stat.* **86**, 226–244 (2004).
- 36. Long, B. T. & Kurlaender, M. Do Community Colleges Provide a Viable Pathway to a Baccalaureate Degree? *Educ. Eval. Policy Anal.* **31**, 30–53 (2009).
- 37. Brewer, D., Dench, D. & Taylor, L. O. Advances in Causal Inference at the Intersection of Air Pollution and Health Outcomes. *Annu. Rev. Resour. Econ.* **15**, 455–469 (2023).
- 38. National Academies of Sciences, Engineering, and Medicine *et al.* Definition of Causality. in *Advancing the Framework for Assessing Causality of Health and Welfare Effects to Inform National Ambient Air Quality Standard Reviews* (National Academies Press (US), Washington (DC), 2022).
- 39. International Agency for Research on Cancer. Non-ionizing Radiation, Part 2: Radiofrequency Electromagnetic Fields. in *IARC monographs on the evaluation of carcinogenic risks to humans* vol. 102 (IARC, Lyon, France, 2013).
- 40. Yuan, A. E. & Shou, W. Data-driven causal analysis of observational biological time series. *eLife* **11**, e72518 (2022).
- 41. Arif, S. & MacNeil, M. A. Applying the structural causal model framework for observational causal inference in ecology. *Ecol. Monogr.* **93**, e1554 (2022).
- 42. Butsic, V., Lewis, D. J., Radeloff, V. C., Baumann, M. & Kuemmerle, T. Quasi-experimental methods enable stronger inferences from observational data in ecology. *Basic Appl. Ecol.* **19**, 1–10 (2017).

- 43. Grace, J. B. & Irvine, K. M. Scientist's guide to developing explanatory statistical models using causal analysis principles. *Ecology* **101**, e02962 (2020).
- 44. Larsen, A. E., Meng, K. & Kendall, B. E. Causal analysis in control–impact ecological studies with observational data. *Methods Ecol. Evol.* **10**, 924–934 (2019).
- 45. Ramsey, D. S. L., Forsyth, David. M., Wright, E., McKay, M. & Westbrooke, I. Using propensity scores for causal inference in ecology: Options, considerations, and a case study. *Methods Ecol. Evol.* **10**, 320–331 (2019).
- 46. Grace, J. B., Scheiner, S. M. & Schoolmaster, Jr., D. R. Structural equation modeling: building and evaluating causal models. in *Ecological Statistics* (eds Fox, G. A., Negrete-Yankelevich, S. & Sosa, V. J.) 168–199 (Oxford University PressOxford, 2015). doi:10.1093/acprof:oso/9780199672547.003.0009.
- 47. Paul, W. L. A causal modelling approach to spatial and temporal confounding in environmental impact studies. *Environmetrics* **22**, 626–638 (2011).
- 48. Dee, L. E. *et al.* Clarifying the effect of biodiversity on productivity in natural ecosystems with longitudinal data and methods for causal inference. *Nat. Commun.* **14**, 2607 (2023).
- 49. Siegel, K. J., Larsen, L., Stephens, C., Stewart, W. & Butsic, V. Quantifying drivers of change in social-ecological systems: land management impacts wildfire probability in forests of the western US. *Reg. Environ. Change* 22, 98 (2022).
- 50. Kimmel, K., Dee, L. E., Avolio, M. L. & Ferraro, P. J. Causal assumptions and causal inference in ecological experiments. *Trends Ecol. Evol.* **36**, 1141–1152 (2021).
- 51. Rubin, D. B. For objective causal inference, design trumps analysis. *Ann. Appl. Stat.* **2**, (2008).

- 52. Shadish, W. R., Cook, T. D. & Campbell, D. T. *Experimental and Quasi-Experimental Designs for Generalized Causal Inference*. (Houghton Mifflin, Boston, 2001).
- 53. Glymour, C., Zhang, K. & Spirtes, P. Review of Causal Discovery Methods Based on Graphical Models. *Front. Genet.* **10**, 524 (2019).
- 54. Runge, J. *et al.* Inferring causation from time series in Earth system sciences. *Nat. Commun.* **10**, 2553 (2019).
- 55. Harnack, D., Laminski, E., Schünemann, M. & Pawelzik, K. R. Topological Causality in Dynamical Systems. *Phys. Rev. Lett.* **119**, 098301 (2017).
- 56. Shi, J., Chen, L. & Aihara, K. Embedding entropy: a nonlinear measure of dynamical causality. *J. R. Soc. Interface* **19**, 20210766 (2022).
- 57. Hernán, M. A. & Robins, J. M. Causal Inference: What If. (CRC Press, Boca Raton, 2025).
- 58. Pearl, J. Causal inference in statistics: An overview. Stat. Surv. 3, (2009).
- Robins, J. M. & Wasserman, L. On the Impossibility of Inferring Causation from Association without Background Knowledge. in *Computation, Causation, and Discovery* (eds Cooper, G. F. & Glymour, C.) (The MIT Press, 1999). doi:10.7551/mitpress/2006.001.0001.
- 60. Granger, C. W. J. Investigating Causal Relations by Econometric Models and Cross-spectral Methods. *Econometrica* **37**, 424 (1969).
- 61. Reichenbach, H. The Direction of Time. (University of California Press, Berkeley, 1956).
- 62. Kiiveri, H. T., Speed, T. P. & Carlin, J. B. Recursive causal models. *J. Aust. Math. Soc. Ser. Pure Math. Stat.* **36**, 30–52 (1984).
- 63. Scheines, R. An Introduction to Causal Inference. (1997).

- 64. Addicott, E. T., Fenichel, E. P., Bradford, M. A., Pinsky, M. L. & Wood, S. A. Toward an improved understanding of causation in the ecological sciences. *Front. Ecol. Environ.* **20**, 474–480 (2022).
- 65. Arif, S. & MacNeil, M. A. Predictive models aren't for causal inference. *Ecol. Lett.* **25**, 1741–1745 (2022).
- 66. Burnham, K. P. & Anderson, D. R. Model Selection and Multimodel Inference: A Practical Information-Theoretic Approach. (Springer, New York, NY, 2010).
- 67. Grace, J. B. An integrative paradigm for building causal knowledge. *Ecol. Monogr.* **94**, e1628 (2024).
- 68. Greenland, S., Pearl, J. & Robins, J. M. Confounding and Collapsibility in Causal Inference. *Stat. Sci.* **14**, (1999).
- 69. Shpitser, I., VanderWeele, T. & Robins, J. M. On the validity of covariate adjustment for estimating causal effects. in *Proceedings of the Twenty-Sixth Conference on Uncertainty in Artificial Intelligence* 527–536 (AUAI Press, Arlington, Virginia, USA, 2010). doi:10.48550/arXiv.1203.3515.
- 70. Imbens, G. W. & Angrist, J. D. Identification and Estimation of Local Average Treatment Effects. *Econometrica* **62**, 467 (1994).
- 71. Rosenbaum, P. R. Choice as an Alternative to Control in Observational Studies. *Stat. Sci.* **14**, (1999).
- 72. Causal inference using regression on the treatment variable. in *Regression and Other Stories* (eds Gelman, A., Hill, J. & Vehtari, A.) 363–382 (Cambridge University Press, Cambridge, 2020). doi:10.1017/9781139161879.020.

- 73. Wiik, E. *et al.* Mechanisms and impacts of an incentive-based conservation program with evidence from a randomized control trial. *Conserv. Biol.* **34**, 1076–1088 (2020).
- 74. Chickering, D. M. Optimal structure identification with greedy search. *J Mach Learn Res* **3**, 507–554 (2003).
- 75. Pearl, J. Causal diagrams for empirical research. *Biometrika* 82, 669–688 (1995).
- 76. Kunicki, Z. J., Smith, M. L. & Murray, E. J. A Primer on Structural Equation Model
 Diagrams and Directed Acyclic Graphs: When and How to Use Each in Psychological and
 Epidemiological Research. *Adv. Methods Pract. Psychol. Sci.* **6**, 251524592311560 (2023).
- 77. Pearl, J. The causal foundations of structural equation modeling. in *Handbook of structural Equation Modeling* 68–91 (The Guilford Press, New York, NY, US, 2012).
- 78. Hernán, M. A., Wang, W. & Leaf, D. E. Target Trial Emulation: A Framework for Causal Inference From Observational Data. *JAMA* **328**, 2446 (2022).
- 79. Hernán, M. A., Dahabreh, I. J., Dickerman, B. A. & Swanson, S. A. The Target Trial Framework for Causal Inference From Observational Data: Why and When Is It Helpful? *Ann. Intern. Med.* (2025) doi:10.7326/ANNALS-24-01871.
- 80. Lundberg, I., Johnson, R. & Stewart, B. M. What Is Your Estimand? Defining the Target Quantity Connects Statistical Evidence to Theory. *Am. Sociol. Rev.* **86**, 532–565 (2021).
- 81. Spake, R. *et al.* Understanding 'it depends' in ecology: a guide to hypothesising, visualising and interpreting statistical interactions. *Biol. Rev.* **98**, 983–1002 (2023).
- 82. Correia, H. E., Dee, L. E. & Ferraro, P. J. Designing causal mediation analyses to quantify intermediary processes in ecology. *Biol. Rev.* brv.70011 (2025) doi:10.1111/brv.70011.
- 83. Paluš, M. From nonlinearity to causality: statistical testing and inference of physical mechanisms underlying complex dynamics. *Contemp. Phys.* **48**, 307–348 (2007).

- 84. Dawid, P. The Decision-Theoretic Approach to Causal Inference. in *Wiley Series in Probability and Statistics* (eds Berzuini, C., Dawid, P. & Bernardinelli, L.) 25–42 (Wiley, 2012). doi:10.1002/9781119945710.ch4.
- 85. Ibeling, D. & Icard, T. Comparing Causal Frameworks: Potential Outcomes, Structural Models, Graphs, and Abstractions. in *Advances in Neural Information Processing Systems* (eds Oh, A. et al.) vol. 36 80130–80141 (Curran Associates, Inc., 2023).
- 86. Pearl, J. Graphical models, potential outcomes and causal inference: Comment on Linquist and Sobel. *NeuroImage* **58**, 770–771 (2011).
- 87. Weinberger, N. Comparing Rubin and Pearl's causal modelling frameworks: a commentary on Markus (2021). *Econ. Philos.* **39**, 485–493 (2023).
- 88. Bollen, K. A. & Pearl, J. Eight Myths About Causality and Structural Equation Models. in Handbook of Causal Analysis for Social Research (ed. Morgan, S. L.) 301–328 (Springer Netherlands, Dordrecht, 2013). doi:10.1007/978-94-007-6094-3 15.
- 89. Wiener, N. Modern Mathematics for Engineers. (McGraw-Hill, New York, 1956).
- 90. Zhao, A. & Ding, P. Regression-based causal inference with factorial experiments: estimands, model specifications and design-based properties. *Biometrika* **109**, 799–815 (2022).
- 91. Imai, K., King, G. & Stuart, E. A. Misunderstandings Between Experimentalists and Observationalists about Causal Inference. *J. R. Stat. Soc. Ser. A Stat. Soc.* **171**, 481–502 (2008).
- 92. Bulbulia, J. A. Methods in causal inference. Part 4: confounding in experiments. *Evol. Hum. Sci.* **6**, e43 (2024).

- 93. Rubin, D. B. Bayesian Inference for Causal Effects: The Role of Randomization. *Ann. Stat.*6, 34–58 (1978).
- 94. Smokorowski, K. E. & Randall, R. G. Cautions on using the Before-After-Control-Impact design in environmental effects monitoring programs. *FACETS* **2**, 212–232 (2017).
- 95. Gelman, A. & Hill, J. Causal inference using multilevel models. in *Data Analysis Using Regression and Multilevel/Hierarchical Models* 503–512 (Cambridge University Press, 2006). doi:10.1017/CBO9780511790942.
- 96. Cousineau, M., Verter, V., Murphy, S. A. & Pineau, J. Estimating causal effects with optimization-based methods: A review and empirical comparison. *Eur. J. Oper. Res.* **304**, 367–380 (2023).
- 97. Igelström, E. *et al.* Causal inference and effect estimation using observational data. *J. Epidemiol. Community Health* **76**, 960 (2022).
- 98. Huang, M. Y. Sensitivity analysis for the generalization of experimental results. *J. R. Stat. Soc. Ser. A Stat. Soc.* qnae012 (2024) doi:10.1093/jrsssa/qnae012.
- 99. Rosenbaum, P. R. Sensitivity to Hidden Bias. in *Observational Studies* 105–170 (Springer New York, New York, NY, 1995). doi:10.1007/978-1-4757-2443-1 5.
- 100. Shen, C., Li, X., Li, L. & Were, M. C. Sensitivity analysis for causal inference using inverse probability weighting. *Biom. J.* **53**, 822–837 (2011).
- 101. VanderWeele, T. J. & Arah, O. A. Bias Formulas for Sensitivity Analysis of Unmeasured Confounding for General Outcomes, Treatments, and Confounders. *Epidemiology* **22**, 42–52 (2011).
- 102. Yadlowsky, S., Namkoong, H., Basu, S., Duchi, J. & Tian, L. Bounds on the conditional and average treatment effect with unobserved confounding factors. *Ann. Stat.* **50**, (2022).

- 103. Sullivan, A. J. & VanderWeele, T. J. Bias and sensitivity analysis for unmeasured confounders in linear structural equation models. Preprint at https://doi.org/10.48550/ARXIV.2103.05775 (2021).
- 104. Rosenbaum, P. R. The Role of Known Effects in Observational Studies. *Biometrics* **45**, 557 (1989).
- 105. Rosenbaum, P. R. Sensitivity analyses informed by tests for bias in observational studies.

 *Biometrics 79, 475–487 (2023).
- 106. Rothman, K. J., Greenland, S. & Lash, T. L. Validity in Epidemiologic Studies. in *Modern epidemiology* 128–147 (Wolters Kluwer Health/Lippincott Williams & Wilkins, Philadelphia, 2008).
- 107. Greenland, S. & Lash, T. L. Bias Analysis. in *Modern epidemiology* 128–147 (Wolters Kluwer Health/Lippincott Williams & Wilkins, Philadelphia, 2008).
- 108. Bareinboim, E., Tian, J. & Pearl, J. Recovering from Selection Bias in Causal and Statistical Inference. in *Probabilistic and Causal Inference* (eds Geffner, H., Dechter, R. & Halpern, J. Y.) 433–450 (ACM, New York, NY, USA, 2022). doi:10.1145/3501714.3501740.
- 109. Hernán, M. A., Hernández-Díaz, S. & Robins, J. M. A Structural Approach to Selection Bias: *Epidemiology* **15**, 615–625 (2004).
- 110. Imai, K. & Yamamoto, T. Causal Inference with Differential Measurement Error:

 Nonparametric Identification and Sensitivity Analysis. *Am. J. Polit. Sci.* **54**, 543–560 (2010).
- 111. Pearl, J. On measurement bias in causal inference. in *Proceedings of the Twenty-Sixth Conference on Uncertainty in Artificial Intelligence* 425–432 (AUAI Press, Arlington, Virginia, USA, 2010). doi:10.48550/arXiv.1203.3504.

- 112. Valeri, L. Measurement Error in Causal Inference. in *Handbook of measurement error* (eds Yi, G. Y., Delaigle, A. & Gustafson, P.) (CRC Press, Boca Raton, 2022).
- 113. Runge, J., Nowack, P., Kretschmer, M., Flaxman, S. & Sejdinovic, D. Detecting and quantifying causal associations in large nonlinear time series datasets. *Sci. Adv.* **5**, eaau4996 (2019).
- 114. Kummerfeld, E., Williams, L. & Ma, S. Power analysis for causal discovery. *Int. J. Data Sci. Anal.* 17, 289–304 (2024).
- 115. Li, J., Liu, L., Le, T. D. & Liu, J. Accurate data-driven prediction does not mean high reproducibility. *Nat. Mach. Intell.* **2**, 13–15 (2020).
- 116. Tredennick, A. T., Hooker, G., Ellner, S. P. & Adler, P. B. A practical guide to selecting models for exploration, inference, and prediction in ecology. *Ecology* **102**, e03336 (2021).

Supplementary Information

Supplementary Note 1: Causal versus statistical assumptions

As noted in the main text, causal and statistical assumptions are both necessary components of deriving valid causal interpretations from observed relationships in data (Stone, 1993). Although the distinctions between these two types of assumptions are not always clear cut in casual research, we find it useful to distinguish them in the following way. Statistical assumptions are formal conditions about the data and model structure that must be satisfied for valid characterizations of relationships between variables from statistical analyses. These assumptions are often testable from data. Causal assumptions are additional conditions that are required to infer causation from statistically dependent relationships and are typically untestable (Hernán et al., 2019). By "untestable", we mean that these assumptions cannot be verified through statistical checks of data, even unlimited data, but instead must be justified using pre-existing knowledge.

Statistical assumptions commonly include assumptions about the probability distribution of random variables or observations, the specifications of relationships between variables, and conditions about data gathering or sampling (see Table S1). For example, they include assumptions about the functional relationships among variables (e.g., linearity, additivity) and about the probability distribution of random errors or observations (e.g., normality, independent and identically distributed random variables, constant variance). Statistical assumptions are encoded in the model structure; thus, they are often not described in applied data analyses.

Unlike causal assumptions (see Section 2 of the main text and Table S1 below), many of the statistical assumptions underlying empirical analyses in ecology are testable – that is, the assumptions can be verified from available data – even if they are often untested by researchers conducting the analyses. There are, however, untestable statistical assumptions that are also necessary for model-based inference, and these assumptions overlap with the causal assumptions described in Section 2 and in Table S1. For example, the basis of the Causal Sufficiency Assumption is a ubiquitous statistical assumption that requires correct specification of the explanatory variables in a model, specifically the inclusion of all confounding variables and the omission of all irrelevant variables. This assumption cannot be directly verified from data (i.e., the assumption is untestable) and must be supported by background knowledge about the system being modeled. Violations to the assumption that explanatory variables have been correctly specified can result in omitted variable bias, overfitting, and simultaneity bias that negatively impact interpretability and generalizability of results.

Other statistical considerations are also important for accurate conclusions from modeled data. These can include: ensuring sufficient statistical power to detect relationships between variables (Kimmel et al., 2023), decreasing measurement error or observational noise to better detect dependent relationships (Brown et al., 1990; Hyslop & Imbens, 2001), appropriately identifying and handling patterns of missingness (Little, 2021), and using robust statistics to accommodate a wider array of probability distributions and modest departures from model assumptions. While these considerations may not be viewed as statistical assumptions *per se*,

they play an important role in determining the credibility of quantitative evidence about ecological phenomena.

The statistical and causal assumptions that are fundamental for making causal claims from ecological data are not tied to specific estimation approaches (e.g., frequentist versus Bayesian estimation). Many ecological studies emphasize the mode of estimation (mode of statistical inference) and overlook potential violations to causal and statistical assumptions that must be satisfied for valid inferences, but even minor violations can impair interpretability. Thus, extracting meaningful causal inferences from data in ecology requires both thoughtful construction of models and the scrutiny of the assumptions underlying these models (Burnham & Anderson, 2010).

Table S1. Common statistical and causal assumptions used for valid causal inference from data.

Statistical Assumptions	Causal Assumptions	
Correct model specification		
 Model(s) include all relevant variables and no irrelevant variables. Functional forms of the relationships among variables are correctly specified (e.g., linearity, additivity). 	 Confounding variables are neither unmeasured or omitted (Causal Sufficiency Assumption). Causal relationships follow the Causal Markov Assumption and Causal Faithfulness Assumption. 	
Random (unit-level) error conditions		
 Observations are independent and identically distributed (i.i.d.). Random errors follow a specific probability distribution (e.g., Gaussian). Random errors have constant variance (homoskedasticity). Explanatory variables not correlated with random error. Measurement error in explanatory variables is independent of the true values. 	- A unit's treatment does not affect another unit's outcome (i.e., "no interference"). Related to the statistical i.i.d. assumption: i.i.d. can be violated by the presence of interference, which implies a lack of independence across units (see Zhang et al., 2023).	
Data-specific criteria		
- For time-series: Stationarity (constant mean and variance over time).	- No instantaneous causal effects ("no simultaneity").	
 No perfect multicollinearity among explanatory variables. 	- Every unit has a non-zero probability of receiving any level of treatment, conditional on covariates (i.e., "positivity" or "overlap").	

Supplementary Note 2: Defining causal and non-causal research questions

Describing and quantifying ecological phenomena often requires a model, which is a mathematical description of how ecologists presume that variables of interest interact with each other. The form of the model is typically determined by the objective of the research question, which we divide into five categories: making causal claims, making associational claims, making predictions, summarizing data through descriptive statistics, and testing logical reasoning of hypotheses via simulations ("Define Research Question" in Figure S1).

Answering the first three types of questions requires statistical inference, which allows ecologists to learn information from observations using probability theory and use that information to make claims about relationships between variables, predict new information, and describe patterns in data (darker-shaded portion of the top box, to the left of the vertical dashed line in Figure S1). When sufficient data are not available or statistical inference is not suitable, mathematical modeling can be used to simulate hypothesized ecological interactions and check for logical fallacies (lighter-shaded portion of the top box, to the right of the vertical dashed line in Figure S1). Associational analyses, predictive models, or simulation-based approaches can also be useful for deriving knowledge that can contribute to future causal research questions (Figure S1 and Figure 3 in main text).

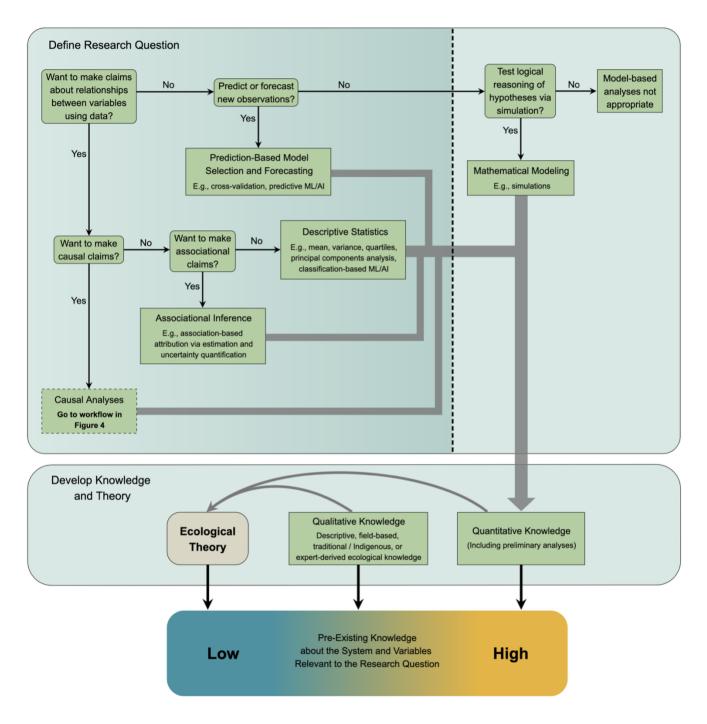


Figure S1. Decision tree for determining the type of analysis most appropriate for the research goal. Prediction-based model selection and forecasting, descriptive statistics, associational inference, and causal analyses use statistical inference, which separates them from approaches like simulation-based mathematical modeling. That separation is represented by the vertical dashed line that separates lighter and darker shaded regions of the top box. The bottom gradient box is also represented in the first box in the workflow of Fig. 3.

A. <u>Using data to derive claims about relationships between variables</u>

When causal interpretations of statistical models are desired, causal methodologies, a subset of statistical inference, allow ecologists to make causal claims about relationships between variables from data. However, as we make clear in Section S4, using statistical inference to make causal claims requires that the experimental or nonexperimental data collection and analyses satisfy many conditions (i.e., assumptions). We provide more details on the tasks that can be accomplished through causal studies and specific methods in Section 6.

If causal claims are not desired, ecologists can draw on classical tools from statistical inference (Efron & Hastie, 2016; Holland, 1986; Nakagawa & Cuthill, 2007). These associational studies can also shape the formulation of causal research questions for subsequent studies. Many research questions have causal goals, but researchers will usually cast these questions as associational due to perceived limitations of statistical methodologies or concerns about misuse of their findings (Hernán, 2018; Jones & Schooling, 2018; Kezios & Hayes-Larson, 2018). Researchers also commonly draw causal-sounding conclusions (e.g., using terms like "drives" or "leads to") from predictive or associational analyses (Haber et al., 2022; Han & Guyatt, 2020; Sargeant et al., 2022; Singer, 2022), thus overstating the evidence of causality by implying that the underlying causes have been properly isolated from unrelated or spurious associations (i.e., that alternative explanations for the observed associations have been ruled out). This tendency is now heavily ingrained in the scientific culture of many fields, but we strongly encourage ecologists to principally consider the goals behind their research questions before considering the methods that may be taken to achieve those goals.

Alternatively, ecologists may instead wish to probe data for general patterns among variables by using statistical inference to explore or summarize the data ("Descriptive Statistics" in Figure S1). Approaches used to describe data are often included in studies aiming to make causal or associational claims, but descriptive statistics are not the primary source of evidence for making such claims.

B. Not deriving claims about relationships among variables from data

At times, ecologists may want to predict unobserved outcomes from new input data by using training data to optimize parameter estimation such that a set of input features predict output values that most closely match observed data output values in verification data ("Prediction-Based Model Selection and Forecasting" in Figure S1). Predictive studies rely on procedures that emphasize model evaluation and selection through predictive performance, including model averaging that derives inferences from several plausible models (i.e., multi-model inference; Burnham & Anderson, 2010). Results from models selected for high prediction accuracy are often believed to produce more meaningful parameter estimates for inference than models with low prediction accuracy (Harrison et al., 2018), which has spurred the popularity of machine learning approaches touted to provide "data-driven" understandings of complex ecological processes (Christin et al., 2019; Olden et al., 2008). However, prediction models merely need to capture the rudimentary patterns and relationships in the data to produce highly accurate

predictions. Thus, models with high prediction accuracy often do not accurately represent the true underlying causal processes of the ecological system from which the data were generated, and thus they are usually not appropriate for making associational or causal claims (Addicott et al., 2022; J. Li et al., 2020; Tredennick et al., 2021).

In other studies, ecologists may wish to simulate hypothesized relationships between variables using mathematical "proof-of-concept" models (sometimes called "mechanistic models"), which play an integral role in translating ecological theories and hypotheses into mathematical language (e.g., the Lokta-Volterra model; Baker et al., 2018; Marquet et al., 2014; Servedio et al., 2014). Numerical analysis of mathematical models allows ecologists to explore and refine hypotheses, examine a model's internal consistency, and assess how well the model represents theoretical or empirical relationships. Additionally, data collected from experiments and field observations can be used to constrain model parameter values or to compare model output to naturally occurring patterns (Caldararu et al., 2023; Evans et al., 2013; Levins, 1966; Luo et al., 2011; Tredennick et al., 2021), but statistical inference is not the goal of such models.

Although mathematical models, predictive models, associational studies, and descriptive statistics can all contribute to quantitative ecological knowledge and pre-existing knowledge for developing causal research questions ("Develop Knowledge and Theory" in Figure S1), current methodologies for making causal claims from data require principles of probability theory and statistical inference to be combined with the rigorous conditions for experimental and observational data collection and analysis defined by causal assumptions. Some researchers have argued that, under certain conditions, predictive models may also contribute to refining or corroborating causal hypotheses when results from predictive studies align with theoretical expectations (Nichols & Cooch, 2025). While consistent findings from predictive models may contribute to pre-existing or "mechanistic" ecological knowledge (Grace, 2024), particularly when supported by ecological theory and expert understanding, predictive performance alone is insufficient to justify causal claims.

Supplementary Note 3: Formally summarizing pre-existing knowledge

Establishing the conditions for making valid causal claims from data is achieved by satisfying the causal assumptions that permit us to detect and quantify causal relationships using statistical dependence. A central task for ecologists interested in causal relationships is to carefully consider the study design, the potential variables to be included or not included in the model, and the data collection procedures. One of the fundamental conditions for valid statistical inference and interpretability of results is that the model correctly specifies the true underlying process from which the data were generated. Developing such a correctly specified model requires preexisting knowledge to identify potentially causative factors and potential pathways of influence through other interacting variables.

The assumptions required for causal analyses highlight how causal tasks (i.e., causal discovery and causal inference) differ from non-causal tasks (e.g., prediction or association). Unlike non-causal analyses, causal tasks depend on pre-existing knowledge to construct and justify models for causal tasks (particularly for causal inference) that satisfy these untestable causal assumptions, rather than selecting the "best" model among several plausible models based on fit metrics that evaluate prediction performance. Even causal discovery is fine-tuned with pre-existing knowledge, guiding algorithms to retain specific plausible relationships specified by the user's pre-existing knowledge, and its results must be validated through further research.

Proper model specification is crucial for valid causal conclusions (Burnham & Anderson, 2010), thus more attention must be invested in the process of designing studies and building models using pre-existing knowledge to make causal claims from experimental and observational ecological studies. To formalize pre-existing knowledge in causal analysis, researchers may use two widely used tools: directed acyclic graphs (DAGs) and thought experiments based on ideal randomized controlled trials (RCTs). These tools help define causal relationships and identify confounders that must be addressed to satisfy causal assumptions before any data are analyzed. Table S2 provides a guide to accessible and foundational references for learning how to apply these tools.

Table S2. Key concepts and accessible references for creating and applying causal DAGs and thought experiments of hypothetical ideal RCTs for summarizing pre-existing knowledge.

Concept	Suggested Readings
Basics of causal DAGs – What they are, variables to include, why they help in confounder identification	Bulbulia, 2024a; Greenland et al., 1999a; Laubach et al., 2021; Shrier & Platt, 2008
Drawing DAGs in practice – User-friendly guidelines for causal DAGs in experimental and observational settings	Arif & MacNeil, 2022; Textor et al., 2011
Using thought experiments of hypothetical ideal RCTs (i.e., "target trials") – How to use thought experiments to simulate an ideal experiment to find confounders	Greenland, 2003; Hernán et al., 2022, 2025; Hernán & Robins, 2025, pp. 37–40; Morgan & Winship, 2015 (Ch. 1); Rubin, 1974
Distinguishing confounders vs. colliders – Ensuring we do not control for the wrong variables	Arif & Massey, 2023; Bulbulia, 2024a; Greenland, 2003

<u>Supplementary Note 4: Causal assumptions translated through causal</u> frameworks

Causal inference and causal discovery both rely on the three fundamental assumptions (Section 2) that allow researchers to interpret statistical patterns as evidence of causation: Causal Sufficiency, Causal Markov, and Causal Faithfulness. However, the way these assumptions are expressed, along with the specific terminology and extensions they involve, varies across causal frameworks. In this section, we show how different frameworks formalize these assumptions and illustrate the conceptual bridges between them.

We focus on three widely used causal frameworks: the structural causal model (SCM) framework (Pearl, 2009), the potential outcomes (PO) framework (Rubin, 1974), and the dynamical systems causality (DC) framework (Harnack et al., 2017; J. Shi et al., 2022). A fourth not covered here – the decision-theoretic framework (Dawid, 2000, 2012) – also shares overlapping assumptions. Each framework uses its own notation and formalism to express the causal assumptions and structure causal reasoning. The PO and SCM frameworks are most common for causal inference, while the SCM and DC frameworks are commonly used for causal discovery.

Theoretical work has established formal correspondences among several major causal frameworks. The PO and SCM frameworks have been shown to be theoretically equivalent (Imbens, 2020; Pearl, 2009), with modern formalizations demonstrating that every Rubin Causal Model from the PO framework can be represented as an abstraction of an SCM (Ibeling & Icard, 2023). A measure-theoretic approach has also been proposed to generalize aspects of SCM and PO frameworks and address challenges like cycles, latent variables, and stochastic processes (Park et al., 2023). Causal properties of the decision-theoretic framework can be expressed through extended conditional independence assertions, aligning with the PO and SCM frameworks under specific conditions (Dawid, 2021, 2024; Pearl, 2022). Connections between the SCM and DC frameworks have also been developed, including approaches that extend SCMs to time-dependent settings and systems with feedback loops (Bongers et al., 2018, 2021) and approaches that link Granger causality (a DC-based approach) to SCMs by representing interventions and dynamic feedback processes (White et al., 2011; White & Chalak, 2009). Methods like transfer entropy, which is used in DC-based analyses, have similarly been related back to conditional independence structures central to SCMs (Runge et al., 2012). Commentaries have also highlighted key conceptual differences and areas of overlap between the PO, SCM, and DC frameworks (Lechner, 2010; Markus, 2021). While recent reviews (e.g., Vonk et al., 2023; Yuan & Shou, 2022) have discussed assumptions in causal discovery and causal inference broadly, here we systematically map how core causal assumptions translate across SCM, PO, and DC frameworks for causal inference and causal discovery.

In Box S1, we map the assumptions used for quantifying the average causal effect of *X* on *Y* in causal inference via the PO and SCM frameworks onto the three basic causal

assumptions. We also summarize two additional assumptions widely used in practice for causal inference. Together, these assumptions allow us to quantify causal effects without bias. For full details of PO assumptions for causal inference, see Hernán & Robins, 2025; for full details of SCM assumptions for causal inference, see Pearl, 2009 or Pearl, 2010.

For causal inference, the inclusion of all relevant confounding variables is necessary to satisfy the causal sufficiency assumption. However, this does not always require directly measuring every confounder. In both frameworks, design-based approaches and statistical techniques can be used to account for unmeasured confounding under certain conditions. Some frameworks, such as SCM, allow for adjustment using variables that are not direct confounders (e.g., descendants of common causes), provided that colliders and other bias-inducing paths are avoided that would otherwise introduce non-causal statistical dependencies (Pearl, 1995; Rohrer, 2018).

In Box S2, we map the assumptions used for causal discovery via the SCM and DC frameworks onto the three basic causal assumptions. We also summarize three additional assumptions commonly required in practice for causal discovery. For full details of SCM assumptions for causal discovery, see Glymour et al., 2019; for full details of DC assumptions for causal discovery, see J. Shi et al., 2022. For relationships between SCM and DC assumptions in causal discovery, see Runge, 2018.

For causal discovery, causal assumptions are used to ensure the reliability of the causal structure inferred from data. SCM-based algorithms primarily rely on the Causal Markov and Causal Faithfulness assumptions, often alongside Causal Sufficiency and additional assumptions like acyclicity and i.i.d. sampling (Glymour et al., 2019). These assumptions can often be relaxed in more advanced approaches. DC-based algorithms often implicitly rely on the causal sufficiency assumption (Paluš, 2007; Runge, 2018), where all common causes are assumed to be measured or contained within the information of the measured variables (i.e., there are no unmeasured confounders, a.k.a., "hidden common causes"), and usually require separability, which is a consequence of the causal faithfulness assumption (Eichler, 2013; Peters et al., 2017; Runge, Nowack, et al., 2019; Spirtes et al., 2000). However, some DC-based causal discovery methods have been developed for non-separable systems (e.g., J. Shi et al., 2022) and for detecting and handling the presence of unmeasured confounders (e.g., Cai et al., 2023).

Together, Boxes S1 and S2 provide a unique synthesis of how the three foundational causal assumptions are formalized and applied across diverse causal frameworks. By explicitly mapping the assumptions of each framework to these shared foundations, the Boxes serve as practical tools for clarifying how these assumptions support valid causal claims across different, and sometimes seemingly disparate, frameworks and causal tasks, thereby clarifying both their common foundations and distinct assumptions.

Box S1. Assumptions for causal inference

Choice of framework

Potential Outcomes (PO) Framework	Structural Causal Models (SCM) Framework
Useful for those familiar with randomized experimental designs. Emphasizes addressing non-causal dependencies (confounding) by leveraging specific experimental designs or imitating such scenarios via statistical techniques.	Useful for those who think about multiple causes jointly ("all-cause models"). Emphasizes defining the minimal set of conditions under which causal effects can be identified and estimated.

Causal assumptions

A1. Causal Sufficiency: All relevant confounders are measured (i.e., no unmeasured common causes).

Potential Outcomes (PO) Framework	Structural Causal Models (SCM) Framework
Terminology: "No unmeasured confounders", "ignorability", or "exchangeability"†. Key Idea: Once we adjust for all relevant confounders, the probability of receiving any given exposure level does not depend on any common causes. Therefore, we must measure and adjust for (i.e., include in the model) all variables that influence both the exposure and the outcome (and any intermediary variables; see Correia et al., 2025). Also requires positivity – individual units are equally likely to be exposed to a specific value of a causal factor (see below). References: Hernán & Robins, 2025; Morgan & Winship, 2015; Rosenbaum & Rubin, 1983	Terminology: "All front-door and back-door paths blocked", or "no omitted common causes in the causal DAG". Key Idea: All confounders identified by the front-door and back-door criteria (or additional criteria; see Maathuis & Colombo, 2015 and Shpitser & Pearl, 2008) are measured and adjusted for (e.g., included in the model). Also requires consistency (the statistical property) – with infinite data, the estimated graph will converge to the true causal graph (see Pearl, 2009; Spirtes et al., 2000). References: Greenland et al., 1999b; Pearl, 2009
Terminology: "No interference", "no spillover", "no unit-to-unit causation", or "no interactions between units" (see Cox, 1958); part of Stable Unit Treatment Value Assumption (SUTVA) (see Rubin, 1980). Key Idea: One unit's exposure does not affect another unit's outcome. Real-world systems often violate this assumption, requiring more complex methods (see Hudgens & Halloran 2008). References: Hudgens & Halloran, 2008; Rubin, 1978, 1980	Terminology: No spillover is implicitly assumed by SCM notation and causal DAGs. Key Idea: In a causal DAG, there are no edges from one unit's exposure to another unit's outcome, i.e., each unit's outcome depends only on its own exposure. Systems that violate this assumption require multi-unit DAGs or specialized methods (see Pearl, 2009). Part of assumption that units are independent and identically distributed (i.i.d.) assumption; see Zhang et al., 2023. References: Pearl, 2009; Spirtes et al., 2000

A2. Causal Markov Condition: In a system with no cycles or feedback loops, any dependence between two variables that do not directly affect each other must come from a common cause influencing both. Once that common cause is accounted for, the two variables should no longer be dependent.

Potential Outcomes (PO) Framework Structural Causal Models (SCM) Framework **Terminology**: "No feedback" or "no cyclic causation" (i.e., **Terminology**: By definition, causal DAGs are acyclic; simultaneous causation) are implied by the potential therefore, feedback loops or bidirectional arrows outcome notation: the outcome Y(a) is measured after an (simultaneous causation) are disallowed. Sometimes exposure A = a. The exposure and outcome are referred to as *factorization* or the *local Markov property* conditionally independent once we account for all - each node is conditionally independent of its nonconfounding variables. descendants, given its parents. **Key Idea**: Once we measure and adjust for any shared **Key Idea**: Once we condition on the parents (common causes, any dependence between two variables that do not causes), the dependence between two variables that do share a direct causal relationship should no longer remain. not directly affect each other is "blocked". Since arrows This also requires that the cause precede the effect, ruling in causal DAGs flow in one direction, it is assumed there out simultaneity. is no cyclic causation. **References**: Hernán & Robins, 2025; Morgan & Winship, References: Pearl, 2009; Spirtes et al., 2000 2015; Rubin, 1978

A3. Causal Faithfulness: If two variables are statistically independent even after adjusting for confounders, then there is no causal relationship between those variables.

Potential Outcomes (PO) Framework	Structural Causal Models (SCM) Framework
Terminology: Implicitly assumed that any true causal effect would manifest as a dependence after all confounders are adjusted for. Key Idea: If two variables remain independent after controlling for all relevant confounders, we assume it's not due to a coincidence but instead conclude there is no causal relationship. References: Hernán & Robins, 2025; Morgan & Winship, 2015	Terminology: Explicitly called <i>faithfulness</i> or <i>stability</i> , in which the causal DAG encodes all conditional independences. If two variables are independent, there exists no causal path (i.e., no causal relationship) between those variables in the causal DAG. Key Idea: If two variables remain independent after conditioning on the variables that block any back-door paths in a causal DAG, we assume this reflects a genuine absence of a causal relationship. References: Pearl, 2009; Spirtes et al., 2000; Wermuth & Lauritzen, 1990

B1. The exposure is well-defined (i.e., no multiple versions of the treatment, such as different strains of a disease being categorized as a single exposure). That is, there must be no ambiguity about what the cause or exposure is.

Potential Outcomes (PO) Framework	Structural Causal Models (SCM) Framework
Terminology : "Causal consistency" (not the same as the statistical property of consistency) or "well-defined treatment"; part of SUTVA (Rubin 1978, 1980).	Terminology : A well-defined or unambiguous exposure is implied by the causal DAGs – the exposure must be unambiguous when declared as node in the causal DAG.
Key Idea: No ambiguous exposure or no multiple versions of a single cause. A cause or exposure must be identically represented across all units. References: Hernán & Robins, 2025; Rubin, 1978, 1980	Key Idea: The causal DAG must represent exactly one well-specified cause or exposure. If we can declare the cause or exposure as one node, we are assuming that it is well-defined. References: Pearl, 2009; Spirtes et al., 2000

B2. Among units that share the same values for the confounders, there must be some that are exposed and some that are not. In other words, the confounders must not perfectly predict the probability of exposure.*

Potential Outcomes (PO) Framework	Structural Causal Models (SCM) Framework
Terminology: "Positivity", "overlap", or "common support"† Key Idea: For any given combination of confounder	Terminology : All exposure levels are sufficiently represented in the data is implied by representing the exposure as a node in the causal DAG.
values, there must be a nonzero chance of receiving each exposure level.	Key Idea : Even if the causal DAG is correctly specified, the data must exhibit variation in exposure for every
References : Hernán & Robins, 2025; Morgan & Winship, 2015; Rosenbaum & Rubin, 1983	configuration of confounders. References : Pearl, 2009; Spirtes et al., 2000

†Causal consistency, positivity, and exchangeability make up the 'identifiability conditions' for causal effects. These conditions hold under idealized randomized experiments (see Kimmel et al., 2021).

*Positivity is a statistical assumption rather than a purely causal assumption. It requires that our data exhibit variation in exposures across all relevant confounders. See Hernán & Robins, 2025; Morgan & Winship, 2015; Rosenbaum & Rubin, 1983.

Box S2. Assumptions for causal discovery

Choice of framework

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Useful for those who think about evolving states of systems over time; focuses on identifying causal relationships for dynamic or complex systems where long time series of observations are available, often under challenging scenarios (e.g., non-separability, high-dimensional nonlinearity).	Useful for those who think about multiple causes jointly ("all-cause models"). Emphasizes defining the minimal set of conditions under which causal effects can be identified and estimated.

Causal assumptions

A1. Causal Sufficiency: All relevant confounders are measured (i.e., no unmeasured common causes).

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology: "All variables that drive the system are embedded in the reconstructed state space", "no missing drivers", or "intrinsic noise is not attributable to external disturbances or measurement errors". Key Idea: Implicitly assumes the measured variables capture the main dynamic influences. If crucial state variables are omitted, apparent causal links can be spurious. References: Ding & Toulis, 2018; Harnack et al., 2017; Orava, 1973; Sun et al., 2015	Terminology: "All relevant variables included", or "no omitted common causes". Key Idea: Discovery algorithms (e.g., PC, FCI) typically assume all major confounders are measured or the algorithm is adjusted to detect them. Also required consistency (the statistical property) – with infinite data, the estimated graph will converge to the true causal graph. References: Glymour et al., 2019; Peters et al., 2017; Spirtes et al., 2000
Terminology: The observed time series fully capture the dynamics of the unit, with no external influences (i.e., no inter-unit interference). Key Idea: The dynamics of each unit are self-contained; the time series used for discovery must reflect the complete internal state of the system. If significant spillover exists, the predictive relationships used to infer causality may be confounded by external influences.	Terminology: "No cross-unit edges" or "independence of units" in causal DAGs. Key Idea: Each unit is independent – one unit's exposure does not affect another unit's outcome. Part of the i.i.d. assumption – units are independent and identically distributed (see Zhang et al. 2023). References: Glymour et al., 2019; Spirtes et al., 2000
References: Harnack et al., 2017; Orava, 1973	

A2. Causal Markov Condition: In a system with no cycles or feedback loops, any dependence between two variables that do not directly affect each other must come from a common cause influencing both. Once that common cause is accounted for, the two variables should no longer be dependent.

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology : If two system components do not interact (directly or indirectly), their time series become conditionally independent (or uncorrelated) after controlling for the relevant state variables.	Terminology : Sometimes referred to as <i>factorization</i> or the <i>local Markov property</i> – each variable is conditionally independent of its confounders given its direct causes.
Key Idea : In time-lagged embedding, if variable <i>A</i> does not help predict <i>B</i> once the relevant lags of <i>B</i> (and possibly other variables) are included, we treat them as causally disconnected. This also requires that the cause precede the outcome, ruling out simultaneity and cyclic causation (see below). References : Runge, Bathiany, et al., 2019; Sun et al., 2015	Key Idea: If two variables are conditionally independent given some conditioning set in the data, they are not connected by any path in the DAG (or are d-separated). Implicitly assumes there is no simultaneity or cyclic causation (see below). References: Glymour et al., 2019; Peters et al., 2017; Spirtes et al., 2000

A3. Causal Faithfulness: If two variables are statistically independent even after adjusting for confounders, then there is no causal relationship between those variables.

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology : Referred to as <i>separability</i> – the influence of measured confounding variables can be eliminated from the information contained in the effect variable's temporal trajectory without changing the direct relationship between the cause and effect; thus, an observed temporal dependence implies the presence of a causal relationship.	Terminology : Explicitly called <i>faithfulness</i> or <i>stability</i> , in which the causal DAG encodes all conditional independences. If two variables are statistically independent, there exists no causal path (i.e., no causal relationship) between those variables in the causal DAG.
Key Idea : If two variables remain independent after controlling for all relevant confounders, we assume it's not due to a coincidence but instead conclude there is no causal relationship.	Key Idea : If two variables remain independent after conditioning on the confounders, we assume this reflects a genuine absence of a causal relationship. References : Glymour et al., 2019; Peters et al., 2017;
References : Paluš et al., 2018; Runge, Bathiany, et al., 2019; Schreiber, 2000; Sun et al., 2015	Spirtes et al., 2000

Additional assumptions

B1. Cause precedes effect; no simultaneity and no feedback loops.

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology : "Temporal ordering", or "one variable's state at the current time t influences the other's state at future time $t + \ell$ ". Key Idea : The future state of a system is conditionally independent of its past states, given its present state (i.e., cause precede effects in time). References : Ding & Toulis, 2018; Paluš et al., 2018	Terminology: "Acyclic", "no bidirectional edges", or "no feedback loops" implied in the causal DAG. Key Idea: Assumes no feedback loops or simultaneous causation exists in the data, since resultant causal DAGs are acyclic. References: Peters et al., 2017; Spirtes et al., 2000

B2. Stationarity – the system's behavior doesn't change dramatically over time (i.e., overall distributional patterns such as mean and variance of causes and outcomes remain relatively constant over time).

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology : The system's behavior does not change over time.	Terminology : The conditional independencies among variables are consistent over time.
Key Idea : Causal relationships remain consistent over time (dependencies should not fundamentally change or vanish). Also requires <i>ergodicity</i> – statistical properties (e.g., mean and variance) calculated from time series samples through the ergodic theorem do not change substantially over time. References : Harnack et al., 2017; McGoff et al., 2012; J. Shi et al., 2022	Key Idea : The influence of a variable's state at a previous time $t-\ell$ on its state at the current time t remains consistent throughout the time series when controlling for the rest of the system's state at the present time t . References : McGoff et al., 2012; Peters et al., 2017; Runge, Bathiany, et al., 2019

B3. Sufficient variability within variables in the system so that differences in exposure and outcome can be reliably detected.

Dynamical Systems Causality (DC) Framework	Structural Causal Models (SCM) Framework
Terminology: Time series provide a faithful representation of the system's dynamics. Additionally, many approaches require that states of the system (e.g., from time series data) can be represented as a low-dimensional attractive manifold. Key Idea: There must be enough dynamic variation in the observed data to reveal causal influences, and the measured variables must adequately reflect the system's underlying states.	Terminology: "Positivity" and "consistency". Key Idea: Each variable (cause or outcome) exhibits enough variation to detect dependence (akin to positivity in causal inference). Also, each variable must be well-defined, so that distinct real-world processes aren't lumped under one label (consistency). References: Glymour et al., 2019; Peters et al., 2017
References: Barański et al., 2020; Deyle & Sugihara, 2011; J. Shi et al., 2022; Takens, 1981	

Supplementary Note 5: Core concepts for each causal framework

While assumptions define the foundation for making valid causal claims, each causal framework also introduces a range of concepts and tools that shape how researchers think about variables, causal relationships, and estimation. To help readers navigate these differences, we provide three tables (Tables S3–S5), one for each framework (PO, SCM, and DC, respectively), that highlight foundational concepts across the frameworks, along with seminal and accessible sources for further reading. These tables are designed as navigational tools for readers seeking intuitive or technical entry points into each framework, such as ignorability and causal estimands in the PO framework, d-separation and *do*-calculus in the SCM framework, and state space reconstruction and separability in the DC framework. Familiarity with these concepts is important for understanding how causal inference and causal discovery are framed and implemented within each framework's structure. These frameworks are not mutually exclusive and can be complementary depending on the causal task and data characteristics. Researchers should familiarize themselves with each to determine which assumptions and tools best align with their research goals.

Table S3. Key concepts and recommended references for understanding the potential outcomes (PO) framework.

Concept	Suggested Readings	
Fundamentals of the PO framework	Holland, 1986; Rubin, 2005; Sobel, 2009	
Stable Unit Treatment Value Assumption (SUTVA)	Sobel, 2006; VanderWeele & Hernán, 2013	
Ignorability Assumption (Unconfoundedness)	Imbens, 2004; Rosenbaum & Rubin, 1983	
Positivity Assumption (Overlap Condition)	Petersen et al., 2012; Westreich & Cole, 2010	
Confounding variables to control for in analyses	Gelman et al., 2020; VanderWeele, 2019; VanderWeele & Shpitser, 2011	
Causal estimands: average treatment effect (ATE) and others	Heiss, 2024; Imbens, 2004; Imbens & Angrist, 1994; Lipkovich et al., 2020; Wooldridge, 2010 (Ch. 21)	
Multiple versions of treatment and interference	Hudgens & Halloran, 2008; Tchetgen Tchetgen & VanderWeele, 2012; VanderWeele & Hernán, 2013	

Table S4. Key concepts and recommended references for understanding the structural causal models (SCM) framework.

Concept	Suggested Readings
Fundamentals of the SCM framework	Burnett & Blackwell, 2024; Cheng et al., 2024; Petersen & van der Laan, 2014; Scheines, 1997
Confounding variables to control for in analyses (d-separation; Back-door and Front-door Criteria)	Arif & Massey, 2023; Bulbulia, 2024a; Elwert, 2013; Greenland, 2003; Morgan & Winship, 2015 (Ch. 4 & 10); Pearl, 2010
Graphical rules for causal identification in graphs (do-calculus)	Hayduk et al., 2003; Pearl, 2009 (Ch. 1 & 11); Shpitser & Pearl, 2008; Tian & Pearl, 2002
Total and path-specific causal effects	Bulbulia, 2024b; Pearl, 2009 (Ch. 3, 4, 7); VanderWeele, 2015d
Model equivalence and Markov equivalence classes	Andersson et al., 1997; Pearl, 2009 (Ch. 5)
Causal graphs with unmeasured/latent variables	Pearl, 2009 (Ch. 12); Richardson & Spirtes, 2002

Table S5. Key concepts and recommended references for understanding the dynamical systems causality (DC) framework.

Concept	Suggested Readings
Fundamentals of the DC framework	Deyle & Sugihara, 2011; Harnack et al., 2017; Runge, 2018; J. Shi et al., 2022; Yuan & Shou, 2022
State space reconstruction (SSR) and attractor manifolds	Cummins et al., 2015; Sauer et al., 1991; Takens, 1981
Causality via predictability	Paluš, 2007; Runge, 2018; Sugihara et al., 2012
Transfer entropy and information-theoretic causality	Schreiber, 2000; Sun et al., 2015; Sun & Bollt, 2014
Separability and causal faithfulness	Eichler, 2013; Peters et al., 2017; Runge, Nowack, et al., 2019
Confounding and hidden variables in time series	De Brouwer et al., 2021; Eichler, 2013; Sun & Bollt, 2014
Limitations in stochastic or weakly coupled systems	Cobey & Baskerville, 2016; McCracken & Weigel, 2014

Supplementary Note 6: Study designs and algorithms for causal analyses

Selecting a study design or algorithm is a critical step in implementing a causal analysis. Different designs and algorithms offer structured ways to satisfy or relax the untestable causal assumptions and must be chosen in light of the causal task, available data, and pre-existing knowledge. Some approaches are grounded in experimental control, while others rely on statistical adjustments or algorithmic structure learning to address confounding and identify causal relationships.

To help readers explore available options, we provide a series of tables that group study designs and algorithms according to the type of causal task (inference or discovery) and whether they address measured or unmeasured confounding. Table S6 summarizes study designs for causal inference, including experimental designs, observational designs for measured confounders, and observational designs for unmeasured confounders. Table S7 summarizes algorithms for causal discovery, grouped by the causal framework and assumptions each algorithm relies on. These tables provide references for the method and its application, as well as software libraries available to implement the methods. Tables S6 and S7 are intended to serve as a reference for researchers selecting and comparing appropriate strategies for their study goals, system knowledge, and data constraints. For additional guidance on the selection of specific causal inference study designs and causal discovery algorithms for time-series data, see the flow chart in Figure 2 in Runge et al., 2023.

Causal inference requires that all confounders be addressed (see Box S1), but this does not necessarily mean every confounder must be explicitly included in a model. Instead, confounding is typically handled using a combination of design-based approaches: directly controlling for measured confounders and employing statistical designs that reduce bias from unmeasured confounders (e.g., experimental randomization or statistical approaches that mimic randomization).

If significant pre-existing knowledge is available and the goal is to obtain system-level understanding (i.e., to model the effects of all causes of an outcome), then SCM-based adjustment methods (e.g., Front-door and Back-door Criteria; see Pearl, 2009 and Arif & MacNeil, 2022) or structural equation modeling (SEM) may be appropriate approaches. While SCM-based adjustment methods typically target specific causal effects, SEM is often used to model entire systems of causal relationships simultaneously. However, this comes with tradeoffs: SEM requires more restrictive assumptions to support system-level causal interpretations (see Bollen & Pearl, 2013; Pearl, 2012). These tradeoffs underscore the need to carefully align the use of SEM with the level of pre-existing knowledge and assumptions that can be plausibly justified for the ecological system under study (Grace, 2024; Pearl, 2012; Shipley, 2016). In cases where unobserved variables are present, acyclic directed mixed graphs (ADMGs) can represent the same set of conditional independencies as a DAG. ADMGs also allow for bidirectional (i.e., double-headed) arrows, enabling representation of latent confounding. These graphs rely on an

extension of Pearl's *d*-separation criterion, called *m*-separation (for details, see Richardson, 2003 and Drton & Richardson, 2004).

While both SEM and SCM approaches rely on a causal graph to represent assumptions, they differ in how those assumptions are used. SCMs (Pearl, 2009) use the graph to derive conditions under which causal effects can be identified from data, often targeting specific effects of interest via tools such as the Back-door or Front-door criteria. In an SCM approach, the causal graph is used to ask, "Given this DAG, can I even estimate the causal effect of X on Y from observed data, and if so, how?" In contrast, SEMs as used in ecology (Grace et al., 2015; Shipley, 2016) typically assume the full system of causal relationships is known, and use the graph to specify a system of structural equations whose fit can be statistically tested (Kunicki et al., 2023). That is, for SEMs, the causal graph is used to ask, "Assuming this DAG is correct, do the observed data support it, and can I fit a model to estimate the effects I care about?" SEMbased causal inference does not provide formal identification criteria to assess whether these effects can be uniquely determined from the data (Wang & Sobel, 2013), and estimation is typically linear, even when nonlinear terms are used. While some software implementations of SEM allow some nonlinear specifications (e.g., via generalized additive models), they estimate causal effects using path coefficients or smooth terms derived from model components (Lefcheck, 2016). Thus, SEMs rely more heavily on model specification and goodness-of-fit, whereas SCMs prioritize identifiability of causal effects under minimal assumptions (Pearl, 1998). SEMs can yield unbiased causal effect estimates if the model includes all relevant confounders and is correctly specified; however, unlike SCM-based methods, they do not provide formal identification criteria to assess whether these conditions are met (Bollen & Pearl, 2013; Markus, 2010; Wang & Sobel, 2013). This distinction highlights that while both approaches can be used for causal modeling, they support different inferential goals and require different standards of justification.

Causal discovery approaches rely on algorithms, rather than study designs, to provide structured approaches for satisfying or relaxing untestable causal assumptions. SCM-based causal discovery algorithms generally begin with a causal diagram that assumes relationships among all variables in the data, and then they iteratively test for statistical independence between pairs of variables. Edges are removed where statistical independence is found, refining the causal diagram to represent only causal relationships consistent with the statistical independencies reflected in the data (Glymour et al., 2019). In contrast, DC-based algorithms typically start with no assumed causal relationships among variables, and test whether statistical dependence between each pair of variables in each direction ($X \rightarrow Y$ and $Y \rightarrow X$) is significantly different from white noise or null hypothesis models (Paluš, 2007; Theiler et al., 1992). If the dependence meets the threshold for significance (typically, $\alpha = 0.05$) in only one of the directions, say $X \rightarrow Y$, then asymmetric coupling is detected, indicating a causal information flow from X (the driving system) to Y (the response system). The strength of the causal relationship is then estimated using a distance metric (Paluš, 2007; J. Shi et al., 2022).

Table S6. Study designs for causal inference, grouped by category. Each study design includes key references (including applications in ecology, where available), and links to available software and code. The resources and applications listed are not exhaustive – we prioritized accessible sources and informative, causally focused applications.

Category	Representative Approachesa	Resources and Applications	Software and packages ¹
Experimental	Randomized Controlled	RCTs:	RCTs:
designs ²	Trials	Kim & DeVries, 2001; Kimmel et al.,	experiment (R package; see https://cran.r-
		2021; Pynegar et al., 2021;	project.org/package=experiment)
		Tilman et al., 2006; Weigel et al.,	RCT (R package; see https://cran.r-
		2021; Wiik et al., 2020	project.org/package=RCT)
		Cluster RCTs:	ExpAn (Python library; see
		Benitez et al., 2023; Branas et al.,	https://github.com/zalando/expan)
		2018; Hemming & Taljaard, 2023;	Cluster RCTs:
		Schochet, 2013	cvcrand (R package; see https://cran.r-
			<pre>project.org/package=cvcrand)</pre>
			experiment (R package; see https://cran.r-
			<pre>project.org/package=experiment)</pre>
			cluster_experiments (Python library; see
			https://github.com/david26694/cluster-
			<u>experiments</u>)
	Factorial Designs	Dasgupta et al., 2015; Jayewardene,	GFD (R package; see https://cran.r-
		2009; Kaspari et al., 2012; King &	<pre>project.org/package=GFD)</pre>
		Tschinkel, 2008; Laube & Zotz,	fullfact (R package; see https://cran.r-
		2003; Nicolaisen et al., 2014;	<pre>project.org/package=fullfact)</pre>
		Zhao & Ding, 2022	DoE.base (R package; see https://cran.r-
			<pre>project.org/package=DoE.base)</pre>
			pyDOE2 (Python library; see
			https://github.com/clicumu/pyDOE2)
			dexpy (Python library; see
			https://github.com/statease/dexpy)
	Crossover Trials	Díaz-Uriarte, 2002; Feinsinger et al.,	crossdes (R package; see https://cran.r-
		1991; Fergus et al., 2023;	project.org/package=crossdes)

¹ See also https://cran.r-project.org/view=CausalInference
² See also https://cran.r-project.org/view=ExperimentalDesign

Observational designs - controlling measured confounders	Regression Adjustment	Jaakkola, 2003; Montesanto & Cividini, 2017; Ohrens et al., 2019; Shahn et al., 2023; Treves et al., 2024 Fieberg & Ditmer, 2012; Gelman et al., 2020; Moss et al., 2025; Nogueira et al., 2022; Simler-Williamson & Germino, 2022	CrossCarry (R package; https://cran.r-project.org/package=Crossover) R packages: Base R functions – lm(), glm(), etc. – or dedicated regression packages Python libraries: statsmodels, linearmodels, etc. Note: No dedicated packages or libraries – standard regression functions are used when confounders are explicitly specified in models used for causal interpretation.
	Multi-level Modeling with Mixed Effects	Bingenheimer & Raudenbush, 2004; Clough, 2012; Gelman, 2006; Gelman & Hill, 2006	lme4 (R package; see https://cran.r-project.org/package=lme4) brms (R package; see https://package=brms) statsmodels (Python library; see https://www.statsmodels.org/) Bambi (Python library; see https://bambinos.github.io/bambi)
	Structural Equation Modeling (SEM) ^{b,c}	Bollen & Pearl, 2013; Cronin & Schoolmaster, 2018; Grace et al., 2015; Hatami, 2019; Pearl, 1998, 2012; Saavedra et al., 2022	pwSEMd (R package; see https://github.com/BillShipley/pwSEM) piecewiseSEMd (R package; see https://cran.r- project.org/package=piecewiseSEM) lavaan (R package; see https://cran.r- project.org/package=lavaan) semopy (Python library; see https://semopy.com)
	Marginal Structural Modeling (MSM)†	Cole & Hernán, 2008; Hernán & Robins, 2025 (Ch. 12); Lei et al., 2019; Mandujano Reyes et al., 2025; Nandi et al., 2012; VanderWeele et al., 2011	bayesmsm (R package; see https://github.com/Kuan-Liu- Lab/bayesmsm) trajmsm (R package; see https://cran.r- project.org/package=trajmsm)

	Subgroup (Stratified)	Morgan & Winship, 2014; Oehri et	stdReg2 (R package; see https://cran.r-
	Analysis	al., 2020; Rosenbaum, 2002	project.org/package=stdReg2)
	Midiy3i3	an, 2020, Rosenbaum, 2002	stratamatch (R package; see https://cran.r-
			project.org/package=stratamatch)
	Covariate and Propensity	Inverse Probability Weighting	IPW:
	Score Matching	(IPW):	ipw (R package; see https://cran.r-
	Score matching	Hernán & Robins, 2025 (Ch. 12);	project.org/package=ipw)
			twang (R package; see https://cran.r-
		Nogueira et al., 2022; West et al., 2022	
			project.org/package=twang)
		Propensity Score Matching	WeightIt (R package; see https://cran.r-
		(PSM):	project.org/package=WeightIt)
		Butsic et al., 2017; Emmons et al.,	CausalPy (Python library; see
		2024; Nogueira et al., 2022;	https://github.com/pymc-labs/CausalPy)
		Pearson et al., 2016; Siegel,	PSM:
		Larsen, et al., 2022; Siegel,	Matching (R package; see https://cran.r-
		Macaulay, et al., 2022; Simler-	<pre>project.org/package=Matching)</pre>
		Williamson & Germino, 2022;	MatchIt (R package; see https://cran.r-
		West et al., 2022; Wiik et al., 2020	<pre>project.org/package=MatchIt)</pre>
			CausalGPS (R package; see https://cran.r-
			<pre>project.org/package=CausalGPS) and</pre>
			pycausalgps (Python library; see
			https://github.com/NSAPH-
			Software/pycausalgps)
			psmpy (Python library; see
			https://pypi.org/project/psmpy)
	Back-door Criterion	Arif et al., 2022; Arif & MacNeil,	causaleffect (R package; see https://cran.r-
		2022; Paul, 2011; Pearl, 2009;	<pre>project.org/package=causaleffect)</pre>
		Schoolmaster et al., 2020; Stewart	daggity (R package and Web interface; see
		et al., 2023	https://dagitty.net)
			DoWhy (Python library; see https://py-
			why.github.io/dowhy)
Observational designs	Instrumental Variables (IV)	Butsic et al., 2017; Kendall, 2015;	ivreg (R package; see https://cran.r-
controlling		Larsen et al., 2019; MacDonald et	project.org/package=ivreg)
unmeasured		al., 2019; MacDonald & Mordecai,	AER (R package; see https://cran.r-
confounders		2019	project.org/package=AER)

		FaceML (Dath and Planters
		EconML (Python library; see
		https://github.com/py-why/econml)
		CausalPy (Python library; see
		https://github.com/pymc-labs/CausalPy)
Regressions Discontinuity	Butsic et al., 2017; Cook et al., 2008;	rdrobust (R package; see https://cran.r-
Design (RDD)	Imbens & Lemieux, 2008; Larsen	<pre>project.org/package=rdrobust)</pre>
	et al., 2019; Noack et al., 2022	rddensity (R package; see https://cran.r-
		<pre>project.org/package=rddensity)</pre>
		CausalPy (Python library; see
		https://github.com/pymc-labs/CausalPy)
Front-door Criterion	Arif et al., 2022; Arif & MacNeil,	causaleffect (R package; see https://cran.r-
	2022; Paul, 2011; Pearl, 2009;	<pre>project.org/package=causaleffect)</pre>
	Stewart et al., 2023	daggity (R package and Web interface; see
		https://dagitty.net)
		fdtlme (R package; see
		https://github.com/annaguo-bios/fdtmle)
		DoWhy (Python library; see https://py-
		why.github.io/dowhy)
Before-After-Control-Impact	BACI:	BACI:
(BACI) ^c	Chevalier et al., 2019; Christie et al.,	Note: No dedicated packages for BACI designs –
	2019; Comte et al., 2023; Ferraro	analyses typically use mixed-effects models
	et al., 2019; Kerr et al., 2019; Paul,	with an interaction term between Time
	2011; Pitcher et al., 2009;	(Before vs. After) and Treatment (Control vs.
	Smokorowski & Randall, 2017;	Impact) to estimate causal effects.
	Wauchope et al., 2021	DiD:
	Difference-in-Differences (DiD):	did (R package; see https://cran.r-
	Butsic et al., 2017; Larsen et al.,	project.org/package=did)
	Butsic et al., 2017; Larsen et al.,	project.org/package=did)
	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson &	<pre>project.org/package=did) fixest (R package; see https://cran.r-</pre>
	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson &	<pre>project.org/package=did) fixest (R package; see https://cran.r- project.org/package=fixest)</pre>
Multi-level Modeling with	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson &	project.org/package=did) fixest (R package; see https://cran.r- project.org/package=fixest) CausalPy (Python library; see
Multi-level Modeling with Fixed Effects ^c	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson & Germino, 2022	project.org/package=did) fixest (R package; see https://cran.r- project.org/package=fixest) CausalPy (Python library; see https://github.com/pymc-labs/CausalPy)
	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson & Germino, 2022 Byrnes & Dee, 2025; Gelman & Hill,	project.org/package=did) fixest (R package; see https://cran.r- project.org/package=fixest) CausalPy (Python library; see https://github.com/pymc-labs/CausalPy) fixest (R package; see https://cran.r-
	Butsic et al., 2017; Larsen et al., 2019; Simler-Williamson & Germino, 2022 Byrnes & Dee, 2025; Gelman & Hill, 2006; Simler-Williamson &	project.org/package=did) fixest (R package; see https://cran.r- project.org/package=fixest) CausalPy (Python library; see https://github.com/pymc-labs/CausalPy) fixest (R package; see https://cran.r- project.org/package=fixest)

T		1 (D 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
		plm (R package; see https://cran.r-
		project.org/package=plm)
		PyFixest (Python library; see
		https://github.com/py-
		econometrics/pyfixest)
Synthetic Control Methods ^c	Abadie et al., 2010; Fick et al., 2021;	Synth (R package; see https://cran.r-
	West et al., 2022; X. Wu et al.,	project.org/package=Synth)
	2023	tidysynth (R package; see https://cran.r-
		<pre>project.org/package=tidysynth)</pre>
		CausalPy (Python library; see
		https://github.com/pymc-labs/CausalPy)
Interrupted Time Series	Gilmour et al., 2006; Kontopantelis	CausalImpact (R package; see
Analysis ^d	et al., 2015; Lopez Bernal et al.,	https://github.com/google/CausalImpact)
	2016; Wauchope et al., 2021	and CausalImpact (Python library; see
		https://pypi.org/project/causalimpact)
		segmented (R package; see https://cran.r-
		project.org/package=segmented)
		CausalPy (Python library; see
		https://github.com/pymc-labs/CausalPy)

^a In practice, multiple approaches can be combined to more credibly satisfy causal assumptions.

^b With additional assumptions, SEMs can incorporate unobserved constructs (i.e., "latent variables") which are inferred from measured variables.

^c Requires longitudinal data for which the value of the causal variable varies within and across units.

^d Requires longitudinal data for which the value of the causal variable varies within units.

Table S7. Algorithms for causal discovery, grouped by category. Each algorithm includes key references (including applications in ecology, where available), and links to available software and code.

Category	Representative Algorithms	Resources and Applications	Software and packages
Constraint-based	PC (Peter and Clark)	Bystrova et al., 2024; Chu et al.,	pcalg (R package; see https://cran.r-
methods		2018; Ebert-Uphoff & Deng, 2012;	project.org/package=pcalg)
		Glymour et al., 2019; Kalisch et	bnlearn (R package; see https://cran.r-
		al., 2012; J. Li et al., 2015, pp. 9–	project.org/package=bnlearn and
		20; Spirtes et al., 2000	https://www.bnlearn.com)
			Tetrad (GUI, Python library, R package; see
			https://www.cmu.edu/dietrich/philosophy/
			tetrad/use-tetrad)
			causal-learn (Python library; see
			https://causal-learn.readthedocs.io)
			pgmpy (Python library; see
			https://pgmpy.org)
	FCI (Fast Causal Inference)	Bystrova et al., 2024; Glymour et al.,	pcalg (R package; see https://cran.r-
		2019; Kalisch et al., 2012; La	project.org/package=pcalg)
		Bastide-van Gemert et al., 2014;	Tetrad (GUI, Python library, R package; see
		Mielke et al., 2022; Nogueira et	https://www.cmu.edu/dietrich/philosophy/
		al., 2022; Shen et al., 2020	tetrad/use-tetrad)
			causal-learn (Python library; see
			https://causal-learn.readthedocs.io)
	PCMCI (Peter and Clark	Docquier et al., 2024; Krich et al.,	Tigramite (Python library; see
	Momentary Conditional	2020; Nogueira et al., 2022;	https://github.com/jakobrunge/tigramite)
	Independence)	Runge, Nowack, et al., 2019;	CausalFlow (Python library; see
		Tárraga et al., 2024	https://github.com/lcastri/causalflow)
Score-based	GES (Greedy Equivalence	Gong et al., 2025; La Bastide-van	pcalg (R package; see https://cran.r-
methods	Search)	Gemert et al., 2014	project.org/package=pcalg)
			Tetrad (GUI, Python library, R package; see
			https://www.cmu.edu/dietrich/philosophy/
			tetrad/use-tetrad)
			pgmpy (Python package; see
			https://pgmpy.org/)

			causal-learn (Python library; see https://causal-learn.readthedocs.io)
	GIES (Greedy Interventional	Hauser & Bühlmann, 2012; Shah et	pcalg (R package; see https://cran.r-
	Equivalence Search)	al., 2023	project.org/package=pcalg)
			Causal Discovery Toolbox (Python library; see
			https://github.com/FenTechSolutions/Caus
			alDiscoveryToolbox)
			gies (Python library; see
			https://github.com/juangamella/gies)
	FGES (Fast Greedy	Kitson & Constantinou, 2021;	Tetrad (GUI, Python library, R package; see
	Equivalence Search)	Ramsey et al., 2017; Shen et al.,	https://www.cmu.edu/dietrich/philosophy/
		2020	tetrad/use-tetrad)
Functional model-	LiNGAM (Linear Non-	Ikeuchi et al., 2023; Kotoku et al.,	Tetrad (GUI, Python library, R package; see
based methods	Gaussian Acyclic Model)	2020; Kurotani et al., 2024;	https://www.cmu.edu/dietrich/philosophy/
		Shimizu, 2014; Shimizu et al.,	tetrad/use-tetrad)
		2006, 2011	causal-learn (Python library; see
			https://causal-learn.readthedocs.io)
			lingam (Python library; see
			https://github.com/cdt15/lingam)
	ANM (Additive Noise Model)	Bühlmann et al., 2014; Mooij et al.,	CANM (R package; see https://github.com/Jie-
		2016; Peters et al., 2014; Song et	Qiao/CANM)
		al., 2022	causal-learn (Python library; see
			https://causal-learn.readthedocs.io)
			Causal Discovery Toolbox (Python library; see
			https://github.com/FenTechSolutions/Caus
			<u>alDiscoveryToolbox</u>)
			lingam (Python library; see
			https://github.com/cdt15/lingam)
	IGCI (Information Geometric	Janzing et al., 2012; Mooij et al.,	CANM (R package; see https://github.com/Jie-
	Causal Inference)	2016; Song et al., 2022	Qiao/CANM)
			Causal Discovery Toolbox (Python library; see
			https://github.com/FenTechSolutions/Caus
			alDiscoveryToolbox)
			IGCI (Python library; see
			https://github.com/amber0309/IGCI)

Dynamical systems	Granger Causality (GC)	Detto et al., 2012; Granger, 1969;	NlinTS (R package; see https://cran.r-
causality (DC)-		Nogueira et al., 2022; Reygadas et	project.org/package=NlinTS)
based methods		al., 2020; Singh & Borrok, 2019;	causal-learn (Python library; see
		Yuan & Shou, 2022	https://causal-learn.readthedocs.io)
	Information Theoretic (IT)	Benocci et al., 2025; Docquier et al.,	NlinTS (R package; see https://cran.r-
	Causality	2024; Hmamouche, 2020;	project.org/package=NlinTS)
		Schreiber, 2000; Sun et al., 2015;	copent (R package; see
		Sun & Bollt, 2014; Yang et al.,	https://github.com/majianthu/copent)
		2018	crossmapy (Python library; see
			https://github.com/PengTao-
			HUST/crossmapy)
			IDTxl (Python library; see
			https://github.com/pwollstadt/IDTxl)
	Convergent Cross Mapping	Chang et al., 2017; Karakoç et al.,	rEDM (R package) and pyEDM (Python
	(CCM)	2020; Kitayama et al., 2021;	library); see
		Matsuzaki et al., 2018; Nova et al.,	https://sugiharalab.github.io/EDM Docume
		2021; Sugihara et al., 2012; Ushio	<u>ntation</u>
		et al., 2018; J. Wu et al., 2023; Ye	
		et al., 2015; Yuan & Shou, 2022	
	Partial Cross Mapping (PCM)	Leng et al., 2020; Yongmei & Yulian,	MATLAB code (see https://github.com/Partial-
		2024	Cross-Mapping)
			crossmapy (Python library; see
			https://github.com/PengTao-
			HUST/crossmapy)

Supplementary Note 7: Advanced methods for causal inference and causal discovery

While many of the fundamental methods for causal discovery and causal inference have existed for several decades, the field of causal inference is continually evolving to incorporate novel statistical techniques and address increasingly complex data scenarios. For example, machine learning (ML) techniques are being integrated into methods for causal discovery and causal inference (Leist et al., 2022). Causal discovery with ML approaches, such as deep causal learning algorithms, use neural approaches to learn causal networks from a combination of empirical data and prior causal knowledge (C. Li et al., 2024; Scherrer et al., 2021; Yu et al., 2019). ML models can also be used in causal inference, provided the model and covariates are specified to accurately represent the underlying causal process (Brand et al., 2023; Hernán & Robins, 2024; Huber, 2023). For example, causal forests estimate causal effects using random forests (Wager & Athey, 2018), while double/debiased ML methods, such as targeted maximum likelihood estimation (TLME) (van der Laan & Rubin, 2006), control for measured confounders using ML models that can capture complex nonlinear and high-dimensional patterns of confounding (Chernozhukov et al., 2018). We summarize some of these advanced methods for both causal discovery and causal inference in Table S8.

It should be noted that not all ML approaches are appropriate for causal analyses (Pichler & Hartig, 2023). ML approaches are merely a class of models that, without pre-existing knowledge and assumptions, are purely intended for predictive tasks and are not appropriate for obtaining causal interpretations (Section S2). Thus, causal ML approaches still require the principles and assumptions linking statistical dependence to causal dependence (Section S4), and careful model building using pre-existing knowledge about all relevant confounding variables is essential for these methods to detect and estimate causal effects without bias (Section S3).

Table S8. Advanced methods for causal discovery and causal inference, grouped by causal task. Each method includes a brief description, key references and links to relevant software and code.

Causal Task	Representative Methods	Resources and Applications	Software and packages ³
Causal	Deep causal learning: Uses deep	C. Li et al., 2024; Luo et al., 2020; Yu	DAG-GNN (Python code; see
discovery	learning models (e.g., neural	et al., 2019; K. Zheng et al., 2024	https://github.com/fishmoon1234/DAG-
	networks) to detect causal		<u>GNN</u>)
	relationships in complex, high-		DeFuSE (Python code; see
	dimensional data, often		https://github.com/chunlinli/defuse)
	incorporating pre-existing		Dagma (Python library; see
	knowledge to improve accuracy.		https://github.com/kevinsbello/dagma)
	Causal representation learning:	Ahuja et al., 2023; Brehmer et al.,	Emei (Python library; see
	Learning disentangled latent	2022; Scholkopf et al., 2021	https://github.com/FrankTianTT/emei)
	representations that correspond to		DRL (Python code; see
	underlying causal variables and		https://github.com/CausalRL/DRL)
	capture the structure of the data-		gCastle (Python library; see
	generating process.		https://pypi.org/project/gcastle)
	Causal reinforcement learning:	Buesing et al., 2019; Wang et al.,	CARL (Python code; see
	Incorporates causal assumptions	2021; Zeng et al., 2025; Zhu et al.,	https://github.com/arquimides/carl)
	or causal models into	2020	Note: No dedicated packages or libraries –
	reinforcement learning (a machine		most implementations of causal
	learning approach where models		reinforcement learning are ad hoc in
	learn by trying actions and		published papers or preprints.
	observing which ones produce the		
	best outcomes).		
	Invariant causal prediction:	Peters et al., 2016; Pfister et al.,	InvariantCausalPrediction (R package; see
	Identifies causal variables by	2019	https://cran.r-
	selecting predictors whose		<pre>project.org/package=InvariantCausalPre</pre>
	statistical relationships with the		diction)
	outcome remain invariant across		causalicp (Python library; see
	environments or experimental		https://github.com/juangamella/icp)
	settings.		

³See also https://github.com/rguo12/awesome-causality-algorithms

Causal	Targeted Maximum Likelihood	Luque-Fernandez et al., 2018;	tmle3 (R package; see
inference	Estimation (TMLE): Semi-	Schuler & Rose, 2017; van der	https://tlverse.org/tmle3)
	parametric method that uses	Laan & Rubin, 2006	causal-curve (Python library; see
	machine learning models for		https://github.com/ronikobrosly/causal-
	flexible outcome and treatment		<u>curve</u>)
	modeling, with a targeted		
	correction step to ensure valid		
	inference.		
	Double/debiased machine	Chernozhukov et al., 2018; Fink et	DoubleML (R package; see https://cran.r-
	learning: Uses machine learning to	al., 2023; B. Shi et al., 2024	project.org/package=DoubleML)
	model outcomes and treatments		EconML (Python library; see
	separately, then combines them to		https://github.com/py-why/econml)
	estimate treatment effects while		
	controlling for confounding in		
	high-dimensional settings.		
	Causal forests: Uses ensembles of	Athey et al., 2019; Athey & Wager,	grf (R package; see https://cran.r-
	decision trees to estimate	2019; Fink et al., 2023; Wager &	project.org/package=grf)
	heterogeneous treatment effects	Athey, 2018; Xie et al., 2012; L.	EconML (Python library; see
	while accounting for confounding.	Zheng & Yin, 2023	https://github.com/py-why/econml)
	Meta-learners for heterogeneous	Jiang et al., 2021; Künzel et al., 2019;	rlearner (R package; see
	treatment effects (e.g., S-learner,	Nie & Wager, 2021; Salditt et al.,	https://github.com/xnie/rlearner)
	T-learner, X-learner, and R-	2024	EconML (Python library; see
	learner): Use machine learning		https://github.com/py-why/econml)
	models to estimate heterogeneous		CausalML (Python library; see
	treatment effects by modeling		https://github.com/uber/causalml)
	outcomes separately for different		metalearners (Python library; see
	treatment levels, with a tradeoff		https://github.com/quantco/metalearne
	between simple implementation		<u>rs</u>)
	and reduced reliability in inference.		
	Causal inference using Bayesian	Green & Kern, 2012; Hahn et al.,	bartCause (R package; see
	machine learning: Estimate	2020; J. Hill et al., 2020; J. L. Hill,	https://github.com/vdorie/bartCause)
	treatment effects using Bayesian	2011; Zeldow et al., 2019	BCI Toolbox (Python library; see
	machine learning models (e.g.,		https://github.com/evans1112/bcitoolb
	Bayesian Additive Regression		<u>ox</u>)
	Trees [BART]) to capture nonlinear		

relationships and quantify		
uncertainty via posterior		
distributions.		
Counterfactual fairness: Defines	Chiappa, 2019; Nabi & Shpitser,	EXOC (Python code; see
fairness based on counterfactual	2018; Y. Wu et al., 2019	https://github.com/CASE-Lab-
comparisons across protected		UMD/counterfactual fairness 2025)
attributes using structural causal		Note: No dedicated packages or libraries –
models, ensuring outcomes would		most implementations of counterfactual
remain the same in a hypothetical		fairness are ad hoc in published papers or
world where protected group		preprints.
membership had been different.		
Causal data fusion: Combines data	Bareinboim & Pearl, 2016; Chau et	Note: Data fusion methods remain in
from different sources (e.g.,	al., 2021; Josey et al., 2022; Pearl	development, thus general-purpose
observational and experimental) to	& Bareinboim, 2014	implementations are not currently widely
estimate causal effects when no		available. Implementations of some data
single dataset is sufficient, using		fusion concepts are available via a GUI at
assumptions encoded in		https://causalfusion.net. A Python library
transportability diagrams (causal		called Y ₀ (see <u>https://github.com/y0-</u>
diagrams that represent		causal-inference/y0) also implements
differences between data sources).		some data fusion concepts (e.g., parsing
		transportability graphs).

References

- Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic Control Methods for Comparative Case Studies: Estimating the Effect of California's Tobacco Control Program. *Journal of the American Statistical Association*, 105(490), 493–505. https://doi.org/10.1198/jasa.2009.ap08746
- Addicott, E. T., Fenichel, E. P., Bradford, M. A., Pinsky, M. L., & Wood, S. A. (2022). Toward an improved understanding of causation in the ecological sciences. *Frontiers in Ecology and the Environment*, 20(8), 474–480. https://doi.org/10.1002/fee.2530
- Ahuja, K., Mahajan, D., Wang, Y., & Bengio, Y. (2023). Interventional Causal Representation Learning. In A. Krause, E. Brunskill, K. Cho, B. Engelhardt, S. Sabato, & J. Scarlett (Eds.), *Proceedings of the 40th International Conference on Machine Learning* (Vol. 202, pp. 372–407). PMLR. https://proceedings.mlr.press/v202/ahuja23a.html
- Andersson, S. A., Madigan, D., & Perlman, M. D. (1997). A characterization of Markov equivalence classes for acyclic digraphs. *The Annals of Statistics*, 25(2). https://doi.org/10.1214/aos/1031833662
- Arif, S., Graham, N. A. J., Wilson, S., & MacNeil, M. A. (2022). Causal drivers of climate-mediated coral reef regime shifts. *Ecosphere*, *13*(3), e3956. https://doi.org/10.1002/ecs2.3956
- Arif, S., & MacNeil, M. A. (2022). Applying the structural causal model framework for observational causal inference in ecology. *Ecological Monographs*, *93*(1), e1554. https://doi.org/10.1002/ecm.1554
- Arif, S., & Massey, M. D. B. (2023). Reducing bias in experimental ecology through directed acyclic graphs. *Ecology and Evolution*, *13*(3), e9947. https://doi.org/10.1002/ece3.9947
- Athey, S., Tibshirani, J., & Wager, S. (2019). Generalized random forests. *The Annals of Statistics*, 47(2). https://doi.org/10.1214/18-AOS1709

- Athey, S., & Wager, S. (2019). Estimating Treatment Effects with Causal Forests: An Application. *Observational Studies*, 5(2), 37–51. https://doi.org/10.1353/obs.2019.0001
- Baker, R. E., Peña, J.-M., Jayamohan, J., & Jérusalem, A. (2018). Mechanistic models versus machine learning, a fight worth fighting for the biological community? *Biology Letters*, 14(5), 20170660. https://doi.org/10.1098/rsbl.2017.0660
- Barański, K., Gutman, Y., & Śpiewak, A. (2020). A probabilistic Takens theorem. *Nonlinearity*, 33(9), 4940–4966. https://doi.org/10.1088/1361-6544/ab8fb8
- Bareinboim, E., & Pearl, J. (2016). Causal inference and the data-fusion problem. *Proceedings of the National Academy of Sciences*, 113(27), 7345–7352. https://doi.org/10.1073/pnas.1510507113
- Benitez, A., Petersen, M. L., Van Der Laan, M. J., Santos, N., Butrick, E., Walker, D., Ghosh, R., Otieno, P., Waiswa, P., & Balzer, L. B. (2023). Defining and estimating effects in cluster randomized trials: A methods comparison. *Statistics in Medicine*, *42*(19), 3443–3466. https://doi.org/10.1002/sim.9813
- Benocci, R., Guagliumi, G., Potenza, A., Zaffaroni-Caorsi, V., Roman, H. E., & Zambon, G. (2025). Application of Transfer Entropy Measure to Characterize Environmental Sounds in Urban and Wild Parks. *Sensors (Basel, Switzerland)*, 25(4), 1046. https://doi.org/10.3390/s25041046
- Bingenheimer, J. B., & Raudenbush, S. W. (2004). Statistical and Substantive Inferences in Public Health: Issues in the Application of Multilevel Models. *Annual Review of Public Health*, 25(1), 53–77. https://doi.org/10.1146/annurev.publhealth.25.050503.153925
- Bollen, K. A., & Pearl, J. (2013). Eight Myths About Causality and Structural Equation Models.

 In S. L. Morgan (Ed.), *Handbook of Causal Analysis for Social Research* (pp. 301–328).

 Springer Netherlands. https://doi.org/10.1007/978-94-007-6094-3_15

- Bongers, S., Blom, T., & Mooij, J. M. (2018). *Causal Modeling of Dynamical Systems* (Version 4). arXiv. https://doi.org/10.48550/ARXIV.1803.08784
- Bongers, S., Forré, P., Peters, J., & Mooij, J. M. (2021). Foundations of structural causal models with cycles and latent variables. *The Annals of Statistics*, 49(5). https://doi.org/10.1214/21-AOS2064
- Branas, C. C., South, E., Kondo, M. C., Hohl, B. C., Bourgois, P., Wiebe, D. J., & MacDonald, J. M. (2018). Citywide cluster randomized trial to restore blighted vacant land and its effects on violence, crime, and fear. *Proceedings of the National Academy of Sciences*, 115(12), 2946–2951. https://doi.org/10.1073/pnas.1718503115
- Brand, J. E., Zhou, X., & Xie, Y. (2023). Recent Developments in Causal Inference and Machine Learning. *Annual Review of Sociology*, 49(1), 81–110. https://doi.org/10.1146/annurev-soc-030420-015345
- Brehmer, J., de Haan, P., Lippe, P., & Cohen, T. S. (2022). Weakly supervised causal representation learning. In S. Koyejo, S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, & A. Oh (Eds.), *Advances in Neural Information Processing Systems* (Vol. 35, pp. 38319–38331). Curran Associates, Inc. https://proceedings.neurips.cc/paper_files/paper/2022/file/fa567e2b2c870f8f09a87b6e73 370869-Paper-Conference.pdf
- Brown, P. J., Fuller, W. A., American Mathematical Society, Institute of Mathematical Statistics, & Society for Industrial and Applied Mathematics (Eds.). (1990). Statistical analysis of measurement error models and applications: proceedings of the AMS-IMS-SIAM joint summer research conference held June 10-16, 1989. American Mathematical Society.
- Buesing, L., Weber, T., Zwols, Y., Heess, N., Racaniere, S., Guez, A., & Lespiau, J.-B. (2019). Woulda, Coulda, Shoulda: Counterfactually-Guided Policy Search. *International*

- Conference on Learning Representations.

 https://openreview.net/forum?id=BJG0voC9YQ
- Bühlmann, P., Peters, J., & Ernest, J. (2014). CAM: Causal additive models, high-dimensional order search and penalized regression. *The Annals of Statistics*, 42(6). https://doi.org/10.1214/14-AOS1260
- Bulbulia, J. A. (2024a). Methods in causal inference. Part 1: causal diagrams and confounding. *Evolutionary Human Sciences*, 6, e40. https://doi.org/10.1017/ehs.2024.35
- Bulbulia, J. A. (2024b). Methods in causal inference. Part 2: Interaction, mediation, and time-varying treatments. *Evolutionary Human Sciences*, 6, e41. https://doi.org/10.1017/ehs.2024.32
- Burnett, J. W., & Blackwell, C. (2024). Graphical causal modelling: an application to identify and estimate cause-and-effect relationships. *Applied Economics*, *56*(33), 3986–4000. https://doi.org/10.1080/00036846.2023.2208856
- Burnham, K. P., & Anderson, D. R. (2010). *Model selection and multimodel inference: a practical information-theoretic approach* (2. ed., [4. printing]). Springer.
- Butsic, V., Lewis, D. J., Radeloff, V. C., Baumann, M., & Kuemmerle, T. (2017). Quasi-experimental methods enable stronger inferences from observational data in ecology.

 *Basic and Applied Ecology, 19, 1–10. https://doi.org/10.1016/j.baae.2017.01.005
- Byrnes, J. E. K., & Dee, L. E. (2025). Causal Inference With Observational Data and Unobserved Confounding Variables. *Ecology Letters*, 28(1), e70023. https://doi.org/10.1111/ele.70023
- Bystrova, D., Assaad, C. K., Si-moussi, S., & Thuiller, W. (2024). Causal discovery from ecological time-series with one timestamp and multiple observations. https://doi.org/10.1101/2024.10.10.608447

- Cai, M., Wang, Z., Xiao, J., Hu, X., Chen, G., & Yang, C. (2023). XMAP: Cross-population fine-mapping by leveraging genetic diversity and accounting for confounding bias.

 Nature Communications, 14(1), 6870. https://doi.org/10.1038/s41467-023-42614-7
- Caldararu, S., Rolo, V., Stocker, B. D., Gimeno, T. E., & Nair, R. (2023). Ideas and perspectives:

 Beyond model evaluation combining experiments and models to advance terrestrial ecosystem science. *Biogeosciences*, 20(17), 3637–3649. https://doi.org/10.5194/bg-20-3637-2023
- Chang, C., Ushio, M., & Hsieh, C. (2017). Empirical dynamic modeling for beginners. *Ecological Research*, 32(6), 785–796. https://doi.org/10.1007/s11284-017-1469-9
- Chau, S. L., Ton, J.-F., González, J., Teh, Y., & Sejdinovic, D. (2021). BayesIMP: Uncertainty Quantification for Causal Data Fusion. In M. Ranzato, A. Beygelzimer, Y. Dauphin, P. S. Liang, & J. W. Vaughan (Eds.), *Advances in Neural Information Processing Systems*(Vol. 34, pp. 3466–3477). Curran Associates, Inc.

 https://proceedings.neurips.cc/paper_files/paper/2021/file/1ca5c750a30312d1919ae6a4d6
 36dcc4-Paper.pdf
- Cheng, D., Li, J., Liu, L., Liu, J., & Le, T. D. (2024). Data-Driven Causal Effect Estimation

 Based on Graphical Causal Modelling: A Survey. *ACM Computing Surveys*, *56*(5), 1–37. https://doi.org/10.1145/3636423
- Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., & Robins, J. (2018). Double/debiased machine learning for treatment and structural parameters. *The Econometrics Journal*, *21*(1), C1–C68. https://doi.org/10.1111/ectj.12097
- Chevalier, M., Russell, J. C., & Knape, J. (2019). New measures for evaluation of environmental perturbations using Before-After-Control-Impact analyses. *Ecological Applications*, 29(2), e01838. https://doi.org/10.1002/eap.1838

- Chiappa, S. (2019). Path-Specific Counterfactual Fairness. *Proceedings of the AAAI Conference on Artificial Intelligence*, 33(01), 7801–7808. https://doi.org/10.1609/aaai.v33i01.33017801
- Christie, A. P., Amano, T., Martin, P. A., Shackelford, G. E., Simmons, B. I., & Sutherland, W. J. (2019). Simple study designs in ecology produce inaccurate estimates of biodiversity responses. *Journal of Applied Ecology*, *56*(12), 2742–2754. https://doi.org/10.1111/1365-2664.13499
- Christin, S., Hervet, É., & Lecomte, N. (2019). Applications for deep learning in ecology.

 Methods in Ecology and Evolution, 10(10), 1632–1644. https://doi.org/10.1111/2041-210X.13256
- Chu, T., Danks, D., & Glymour, C. (2018). Data Driven Methods for Nonlinear Granger

 Causality: Climate Teleconnection Mechanisms. https://doi.org/10.1184/R1/6491327.v1
- Clough, Y. (2012). A generalized approach to modeling and estimating indirect effects in ecology. *Ecology*, *93*(8), 1809–1815. https://doi.org/10.1890/11-1899.1
- Cobey, S., & Baskerville, E. B. (2016). Limits to Causal Inference with State-Space

 Reconstruction for Infectious Disease. *PLOS ONE*, *11*(12), e0169050.

 https://doi.org/10.1371/journal.pone.0169050
- Cole, S. R., & Hernán, M. A. (2008). Constructing inverse probability weights for marginal structural models. *American Journal of Epidemiology*, *168*(6), 656–664. https://doi.org/10.1093/aje/kwn164
- Comte, S., Bengsen, A. J., Thomas, E., Bennett, A., Davis, N. E., Brown, D., & Forsyth, D. M. (2023). A Before-After Control-Impact experiment reveals that culling reduces the impacts of invasive deer on endangered peatlands. *Journal of Applied Ecology*, 60(11), 2340–2350. https://doi.org/10.1111/1365-2664.14498

- Cook, T. D., Shadish, W. R., & Wong, V. C. (2008). Three conditions under which experiments and observational studies produce comparable causal estimates: New findings from within-study comparisons. *Journal of Policy Analysis and Management*, 27(4), 724–750. https://doi.org/10.1002/pam.20375
- Correia, H. E., Dee, L. E., & Ferraro, P. J. (2025). Designing causal mediation analyses to quantify intermediary processes in ecology. *Biological Reviews*, brv.70011. https://doi.org/10.1111/brv.70011
- Cox, D. R. (1958). Planning of experiments (p. 308). Wiley.
- Cronin, J. P., & Schoolmaster, D. R. (2018). A causal partition of trait correlations: using graphical models to derive statistical models from theoretical language. *Ecosphere*, 9(9), e02422. https://doi.org/10.1002/ecs2.2422
- Cummins, B., Gedeon, T., & Spendlove, K. (2015). On the Efficacy of State Space

 Reconstruction Methods in Determining Causality. *SIAM Journal on Applied Dynamical Systems*, *14*(1), 335–381. https://doi.org/10.1137/130946344
- Dasgupta, T., Pillai, N. S., & Rubin, D. B. (2015). Causal Inference from 2K Factorial Designs by Using Potential Outcomes. *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 77(4), 727–753. https://doi.org/10.1111/rssb.12085
- Dawid, P. (2000). Causal Inference without Counterfactuals. *Journal of the American Statistical Association*, 95(450), 407–424. https://doi.org/10.1080/01621459.2000.10474210
- Dawid, P. (2012). The Decision-Theoretic Approach to Causal Inference. In C. Berzuini, P.
 Dawid, & L. Bernardinelli (Eds.), Wiley Series in Probability and Statistics (1st ed., pp. 25–42). Wiley. https://doi.org/10.1002/9781119945710.ch4
- Dawid, P. (2021). Decision-theoretic foundations for statistical causality. *Journal of Causal Inference*, 9(1), 39–77. https://doi.org/10.1515/jci-2020-0008

- Dawid, P. (2024). Potential outcomes and decision-theoretic foundations for statistical causality:

 Response to Richardson and Robins. *Journal of Causal Inference*, *12*(1), 20230058.

 https://doi.org/10.1515/jci-2023-0058
- De Brouwer, E., Arany, A., Simm, J., & Moreau, Y. (2021). Latent Convergent Cross Mapping.

 International Conference on Learning Representations.

 https://openreview.net/forum?id=4TSiOTkKe5P
- Detto, M., Molini, A., Katul, G., Stoy, P., Palmroth, S., & Baldocchi, D. (2012). Causality and Persistence in Ecological Systems: A Nonparametric Spectral Granger Causality

 Approach. *The American Naturalist*, 179(4), 524–535. https://doi.org/10.1086/664628
- Deyle, E. R., & Sugihara, G. (2011). Generalized Theorems for Nonlinear State Space

 Reconstruction. *PLoS ONE*, 6(3), e18295. https://doi.org/10.1371/journal.pone.0018295
- Ding, Y., & Toulis, P. (2018). Dynamical systems theory for causal inference with application to synthetic control methods (Version 3). arXiv. https://doi.org/10.48550/ARXIV.1808.08778
- Díaz-Uriarte, R. (2002). Incorrect analysis of crossover trials in animal behaviour research.

 Animal Behaviour, 63(4), 815–822. https://doi.org/10.1006/anbe.2001.1950
- Docquier, D., Di Capua, G., Donner, R. V., Pires, C. A. L., Simon, A., & Vannitsem, S. (2024).

 A comparison of two causal methods in the context of climate analyses. *Nonlinear Processes in Geophysics*, 31(1), 115–136. https://doi.org/10.5194/npg-31-115-2024
- Drton, M., & Richardson, T. S. (2004). Iterative conditional fitting for Gaussian ancestral graph models. *Proceedings of the 20th Conference on Uncertainty in Artificial Intelligence*, 130–137. https://doi.org/10.48550/arXiv.1207.4118
- Ebert-Uphoff, I., & Deng, Y. (2012). Causal Discovery for Climate Research Using Graphical Models. *Journal of Climate*, 25(17), 5648–5665. https://doi.org/10.1175/JCLI-D-11-00387.1

- Efron, B., & Hastie, T. (2016). Computer age statistical inference: algorithms, evidence, and data science. Cambridge University Press.
- Eichler, M. (2013). Causal inference with multiple time series: principles and problems.

 Philosophical Transactions. Series A, Mathematical, Physical, and Engineering Sciences,
 371(1997), 20110613. https://doi.org/10.1098/rsta.2011.0613
- Elwert, F. (2013). Graphical Causal Models. In S. L. Morgan (Ed.), *Handbook of Causal Analysis for Social Research* (pp. 245–273). Springer Netherlands. https://doi.org/10.1007/978-94-007-6094-3 13
- Emmons, S., Woods, T., Cashman, M., Devereux, O., Noe, G., Young, J., Stranko, S., Kilian, J., Hanna, K., & Maloney, K. (2024). Causal inference approaches reveal both positive and negative unintended effects of agricultural and urban management practices on instream biological condition. *Journal of Environmental Management*, 361, 121234. https://doi.org/10.1016/j.jenvman.2024.121234
- Evans, M. R., Grimm, V., Johst, K., Knuuttila, T., De Langhe, R., Lessells, C. M., Merz, M., O'Malley, M. A., Orzack, S. H., Weisberg, M., Wilkinson, D. J., Wolkenhauer, O., & Benton, T. G. (2013). Do simple models lead to generality in ecology? *Trends in Ecology & Evolution*, 28(10), 578–583. https://doi.org/10.1016/j.tree.2013.05.022
- Feinsinger, P., Tiebout, H. M., & Young, B. E. (1991). Do Tropical Bird-Pollinated Plants

 Exhibit Density-Dependent Interactions? Field Experiments. *Ecology*, 72(6), 1953–1963.

 https://doi.org/10.2307/1941550
- Fergus, A. R., Hermanstorfer, S. J., & Treves, A. (2023). *Combining two non-lethal methods in crossover design randomized experiments*. https://doi.org/10.31220/agriRxiv.2023.00203
- Ferraro, P. J., Sanchirico, J. N., & Smith, M. D. (2019). Causal inference in coupled human and natural systems. *Proceedings of the National Academy of Sciences*, *116*(12), 5311–5318. https://doi.org/10.1073/pnas.1805563115

- Fick, S. E., Nauman, T. W., Brungard, C. C., & Duniway, M. C. (2021). Evaluating natural experiments in ecology: using synthetic controls in assessments of remotely sensed land treatments. *Ecological Applications*, *31*(3), e02264. https://doi.org/10.1002/eap.2264
- Fieberg, J., & Ditmer, M. (2012). Understanding the causes and consequences of animal movement: a cautionary note on fitting and interpreting regression models with time-dependent covariates. *Methods in Ecology and Evolution*, *3*(6), 983–991. https://doi.org/10.1111/j.2041-210X.2012.00239.x
- Fink, D., Johnston, A., Strimas-Mackey, M., Auer, T., Hochachka, W. M., Ligocki, S.,
 Oldham Jaromczyk, L., Robinson, O., Wood, C., Kelling, S., & Rodewald, A. D. (2023).
 A Double machine learning trend model for citizen science data. *Methods in Ecology and Evolution*, 14(9), 2435–2448. https://doi.org/10.1111/2041-210X.14186
- Gelman, A. (2006). Multilevel (Hierarchical) Modeling: What It Can and Cannot Do. *Technometrics*, 48(3), 432–435. https://doi.org/10.1198/004017005000000661
- Gelman, A., & Hill, J. (2006). Causal inference using multilevel models. In *Data Analysis Using Regression and Multilevel/Hierarchical Models* (1st ed., pp. 503–512). Cambridge University Press. https://doi.org/10.1017/CBO9780511790942
- Gelman, A., Hill, J., & Vehtari, A. (Eds.). (2020). Causal inference using regression on the treatment variable. In *Regression and Other Stories* (pp. 363–382). Cambridge University Press; Cambridge Core. https://doi.org/10.1017/9781139161879.020
- Gilmour, S., Degenhardt, L., Hall, W., & Day, C. (2006). Using intervention time series analyses to assess the effects of imperfectly identifiable natural events: a general method and example. *BMC Medical Research Methodology*, 6, 16. https://doi.org/10.1186/1471-2288-6-16

- Glymour, C., Zhang, K., & Spirtes, P. (2019). Review of Causal Discovery Methods Based on Graphical Models. *Frontiers in Genetics*, 10, 524. https://doi.org/10.3389/fgene.2019.00524
- Gong, K., Chen, Y., Song, X., Fu, Z., & Ding, X. (2025). Causal Inference for Hypertension Prediction With Wearable E lectrocardiogram and P hotoplethysmogram Signals:

 Feasibility Study. *JMIR Cardio*, 9, e60238–e60238. https://doi.org/10.2196/60238
- Grace, J. B. (2024). An integrative paradigm for building causal knowledge. *Ecological Monographs*, 94(4), e1628. https://doi.org/10.1002/ecm.1628
- Grace, J. B., Scheiner, S. M., & Schoolmaster, Jr., D. R. (2015). Structural equation modeling: building and evaluating causal models. In G. A. Fox, S. Negrete-Yankelevich, & V. J. Sosa (Eds.), *Ecological Statistics* (1st ed., pp. 168–199). Oxford University PressOxford. https://doi.org/10.1093/acprof:oso/9780199672547.003.0009
- Granger, C. W. J. (1969). Investigating Causal Relations by Econometric Models and Cross-spectral Methods. *Econometrica*, *37*(3), 424. https://doi.org/10.2307/1912791
- Green, D. P., & Kern, H. L. (2012). Modeling Heterogeneous Treatment Effects in Survey

 Experiments with Bayesian Additive Regression Trees. *Public Opinion Quarterly*, 76(3),
 491–511. https://doi.org/10.1093/poq/nfs036
- Greenland, S. (2003). Quantifying biases in causal models: classical confounding vs collider-stratification bias. *Epidemiology (Cambridge, Mass.)*, *14*(3), 300–306.
- Greenland, S., Pearl, J., & Robins, J. M. (1999a). Causal diagrams for epidemiologic research. *Epidemiology (Cambridge, Mass.)*, 10(1), 37–48.
- Greenland, S., Pearl, J., & Robins, J. M. (1999b). Confounding and Collapsibility in Causal Inference. *Statistical Science*, *14*(1). https://doi.org/10.1214/ss/1009211805
- Haber, N. A., Wieten, S. E., Rohrer, J. M., Arah, O. A., Tennant, P. W. G., Stuart, E. A., Murray, E. J., Pilleron, S., Lam, S. T., Riederer, E., Howcutt, S. J., Simmons, A. E., Leyrat, C.,

- Schoenegger, P., Booman, A., Dufour, M.-S. K., O'Donoghue, A. L., Baglini, R., Do, S., ... Fox, M. P. (2022). Causal and Associational Language in Observational Health

 Research: A Systematic Evaluation. *American Journal of Epidemiology*, 191(12), 2084–2097. https://doi.org/10.1093/aje/kwac137
- Hahn, P. R., Murray, J. S., & Carvalho, C. M. (2020). Bayesian Regression Tree Models for Causal Inference: Regularization, Confounding, and Heterogeneous Effects (with Discussion). *Bayesian Analysis*, 15(3). https://doi.org/10.1214/19-BA1195
- Han, M. A., & Guyatt, G. (2020). Systematic survey of the causal language use in systematic reviews of observational studies: a study protocol. *BMJ Open*, *10*(7), e038571. https://doi.org/10.1136/bmjopen-2020-038571
- Harnack, D., Laminski, E., Schünemann, M., & Pawelzik, K. R. (2017). Topological Causality in Dynamical Systems. *Physical Review Letters*, *119*(9), 098301. https://doi.org/10.1103/PhysRevLett.119.098301
- Harrison, X. A., Donaldson, L., Correa-Cano, M. E., Evans, J., Fisher, D. N., Goodwin, C. E. D.,
 Robinson, B. S., Hodgson, D. J., & Inger, R. (2018). A brief introduction to mixed effects
 modelling and multi-model inference in ecology. *PeerJ*, 6, e4794.
 https://doi.org/10.7717/peerj.4794
- Hatami, R. (2019). A Review of the Techniques Used to Control Confounding Bias and How Spatiotemporal Variation Can Be Controlled in Environmental Impact Studies. *Water, Air, & Soil Pollution*, 230(6), 132. https://doi.org/10.1007/s11270-019-4150-9
- Hauser, A., & Bühlmann, P. (2012). Characterization and Greedy Learning of Interventional Markov Equivalence Classes of Directed Acyclic Graphs. *Journal of Machine Learning Research*, 13(79), 2409–2464.
- Hayduk, L., Cummings, G., Stratkotter, R., Nimmo, M., Grygoryev, K., Dosman, D., Gillespie,M., Pazderka-Robinson, H., & Boadu, K. (2003). Pearl's D-Separation: One More Step

- Into Causal Thinking. *Structural Equation Modeling: A Multidisciplinary Journal*, 10(2), 289–311. https://doi.org/10.1207/S15328007SEM1002 8
- Heiss, A. (2024, March 21). Demystifying causal inference estimands: ATE, ATT, and ATU. *Andrew Heiss's Blog.* https://doi.org/10.59350/c9z3a-rcq16
- Hemming, K., & Taljaard, M. (2023). Key considerations for designing, conducting and analysing a cluster randomized trial. *International Journal of Epidemiology*, *52*(5), 1648–1658. https://doi.org/10.1093/ije/dyad064
- Hernán, M. A. (2018). The C-Word: Scientific Euphemisms Do Not Improve Causal Inference From Observational Data. *American Journal of Public Health*, *108*(5), 616–619. https://doi.org/10.2105/AJPH.2018.304337
- Hernán, M. A., Dahabreh, I. J., Dickerman, B. A., & Swanson, S. A. (2025). The Target Trial Framework for Causal Inference From Observational Data: Why and When Is It Helpful?

 Annals of Internal Medicine. https://doi.org/10.7326/ANNALS-24-01871
- Hernán, M. A., Hsu, J., & Healy, B. (2019). A Second Chance to Get Causal Inference Right: A Classification of Data Science Tasks. *CHANCE*, *32*(1), 42–49. https://doi.org/10.1080/09332480.2019.1579578
- Hernán, M. A., & Robins, J. M. (2024). Variable selection and high-dimensional data. In *Causal inference: What if* (First edition, pp. 235–246). Taylor and Francis.
- Hernán, M. A., & Robins, J. M. (2025). Causal inference: What if (First edition). CRC Press.
- Hernán, M. A., Wang, W., & Leaf, D. E. (2022). Target Trial Emulation: A Framework for Causal Inference From Observational Data. *JAMA*, 328(24), 2446. https://doi.org/10.1001/jama.2022.21383
- Hill, J. L. (2011). Bayesian Nonparametric Modeling for Causal Inference. *Journal of Computational and Graphical Statistics*, 20(1), 217–240.
 https://doi.org/10.1198/jcgs.2010.08162

- Hill, J., Linero, A., & Murray, J. (2020). Bayesian Additive Regression Trees: A Review and Look Forward. *Annual Review of Statistics and Its Application*, 7(1), 251–278. https://doi.org/10.1146/annurev-statistics-031219-041110
- Hmamouche, Y. (2020). NlinTS: An R Package For Causality Detection in Time Series. *The R Journal*, 12(1), 21. https://doi.org/10.32614/RJ-2020-016
- Holland, P. W. (1986). Statistics and Causal Inference. *Journal of the American Statistical Association*, 81(396), 945–960. https://doi.org/10.1080/01621459.1986.10478354
- Huber, M. (2023). *Causal analysis: impact evaluation and causal machine learning with applications in R.* The MIT Press.
- Hudgens, M. G., & Halloran, M. E. (2008). Toward Causal Inference With Interference. *Journal of the American Statistical Association*, 103(482), 832–842. https://doi.org/10.1198/016214508000000292
- Hyslop, D. R., & Imbens, G. W. (2001). Bias From Classical and Other Forms of Measurement Error. *Journal of Business & Economic Statistics*, 19(4), 475–481. https://doi.org/10.1198/07350010152596727
- Ibeling, D., & Icard, T. (2023). Comparing Causal Frameworks: Potential Outcomes, Structural Models, Graphs, and Abstractions. In A. Oh, T. Naumann, A. Globerson, K. Saenko, M. Hardt, & S. Levine (Eds.), Advances in Neural Information Processing Systems (Vol. 36, pp. 80130–80141). Curran Associates, Inc. https://proceedings.neurips.cc/paper_files/paper/2023/file/fd83f4e0dcaf1c64ea15bbb1695 bb40f-Paper-Conference.pdf
- Ikeuchi, T., Ide, M., Zeng, Y., Maeda, T. N., & Shimizu, S. (2023). Python package for causal discovery based on LiNGAM. *Journal of Machine Learning Research*, 24(14), 1–8.

- Imbens, G. W. (2004). Nonparametric Estimation of Average Treatment Effects Under Exogeneity: A Review. *Review of Economics and Statistics*, 86(1), 4–29. https://doi.org/10.1162/003465304323023651
- Imbens, G. W. (2020). Potential Outcome and Directed Acyclic Graph Approaches to Causality:

 Relevance for Empirical Practice in Economics. *Journal of Economic Literature*, *58*(4),

 1129–1179. https://doi.org/10.1257/jel.20191597
- Imbens, G. W., & Angrist, J. D. (1994). Identification and Estimation of Local Average

 Treatment Effects. *Econometrica*, 62(2), 467. https://doi.org/10.2307/2951620
- Imbens, G. W., & Lemieux, T. (2008). Regression discontinuity designs: A guide to practice.

 Journal of Econometrics, 142(2), 615–635.

 https://doi.org/10.1016/j.jeconom.2007.05.001
- Jaakkola, J. J. K. (2003). Case-crossover design in air pollution epidemiology. *European Respiratory Journal*, 21(40 suppl), 81s–85s. https://doi.org/10.1183/09031936.03.00402703
- Janzing, D., Mooij, J., Zhang, K., Lemeire, J., Zscheischler, J., Daniušis, P., Steudel, B., & Schölkopf, B. (2012). Information-geometric approach to inferring causal directions.

 *Artificial Intelligence, 182–183, 1–31. https://doi.org/10.1016/j.artint.2012.01.002
- Jayewardene, D. (2009). A factorial experiment quantifying the influence of parrotfish density and size on algal reduction on Hawaiian coral reefs. *Journal of Experimental Marine Biology and Ecology*, 375(1–2), 64–69. https://doi.org/10.1016/j.jembe.2009.05.006
- Jiang, H., Qi, P., Zhou, J., Zhou, J., & Rao, S. (2021). A Short Survey on Forest Based
 Heterogeneous Treatment Effect Estimation Methods: Meta-learners and Specific
 Models. 2021 IEEE International Conference on Big Data (Big Data), 3006–3012.
 https://doi.org/10.1109/BigData52589.2021.9671439

- Jones, H. E., & Schooling, C. M. (2018). Let's Require the "T-Word." *American Journal of Public Health*, 108(5), 624–624. https://doi.org/10.2105/AJPH.2018.304365
- Josey, K. P., Yang, F., Ghosh, D., & Raghavan, S. (2022). A calibration approach to transportability and data-fusion with observational data. *Statistics in Medicine*, 41(23), 4511–4531. https://doi.org/10.1002/sim.9523
- Kalisch, M., Mächler, M., Colombo, D., Maathuis, M. H., & Bühlmann, P. (2012). Causal Inference Using Graphical Models with the *R* Package **pcalg**. *Journal of Statistical Software*, 47(11). https://doi.org/10.18637/jss.v047.i11
- Karakoç, C., Clark, A. T., & Chatzinotas, A. (2020). Diversity and coexistence are influenced by time-dependent species interactions in a predator–prey system. *Ecology Letters*, *23*(6), 983–993. https://doi.org/10.1111/ele.13500
- Kaspari, M., Donoso, D., Lucas, J. A., Zumbusch, T., & Kay, A. D. (2012). Using nutritional ecology to predict community structure: a field test in Neotropical ants. *Ecosphere*, *3*(11), 1–15. https://doi.org/10.1890/ES12-00136.1
- Kendall, B. E. (2015). A statistical symphony: instrumental variables reveal causality and control measurement error. In G. A. Fox, S. Negrete-Yankelevich, & V. J. Sosa (Eds.), *Ecological Statistics* (1st ed., pp. 149–167). Oxford University PressOxford. https://doi.org/10.1093/acprof:oso/9780199672547.003.0008
- Kerr, L. A., Kritzer, J. P., & Cadrin, S. X. (2019). Strengths and limitations of before–after–control–impact analysis for testing the effects of marine protected areas on managed populations. *ICES Journal of Marine Science*, 76(4), 1039–1051.
 https://doi.org/10.1093/icesjms/fsz014
- Kezios, K. L., & Hayes-Larson, E. (2018). A Clarification on Causal Questions: We Ask Them More Often Than We Realize. *American Journal of Public Health*, 108(8), e4–e4. https://doi.org/10.2105/AJPH.2018.304547

- Kim, G. W., & DeVries, D. R. (2001). Adult Fish Predation on Freshwater Limnetic Fish Larvae: A Mesocosm Experiment. *Transactions of the American Fisheries Society*, 130(2), 189–203. https://doi.org/10.1577/1548-8659(2001)130%253C0189:AFPOFL%253E2.0.CO;2
- Kimmel, K., Avolio, M. L., & Ferraro, P. J. (2023). Empirical evidence of widespread exaggeration bias and selective reporting in ecology. *Nature Ecology & Evolution*, 7(9), 1525–1536. https://doi.org/10.1038/s41559-023-02144-3
- Kimmel, K., Dee, L. E., Avolio, M. L., & Ferraro, P. J. (2021). Causal assumptions and causal inference in ecological experiments. *Trends in Ecology & Evolution*, *36*(12), 1141–1152. https://doi.org/10.1016/j.tree.2021.08.008
- King, J. R., & Tschinkel, W. R. (2008). Experimental evidence that human impacts drive fire ant invasions and ecological change. *Proceedings of the National Academy of Sciences*, 105(51), 20339–20343. https://doi.org/10.1073/pnas.0809423105
- Kitayama, K., Ushio, M., & Aiba, S. (2021). Temperature is a dominant driver of distinct annual seasonality of leaf litter production of equatorial tropical rain forests. *Journal of Ecology*, 109(2), 727–736. https://doi.org/10.1111/1365-2745.13500
- Kitson, N. K., & Constantinou, A. C. (2021). Learning Bayesian networks from demographic and health survey data. *Journal of Biomedical Informatics*, *113*, 103588. https://doi.org/10.1016/j.jbi.2020.103588
- Kontopantelis, E., Doran, T., Springate, D. A., Buchan, I., & Reeves, D. (2015). Regression based quasi-experimental approach when randomisation is not an option: interrupted time series analysis. *BMJ*, *350*(jun09 5), h2750–h2750. https://doi.org/10.1136/bmj.h2750
- Kotoku, J., Oyama, A., Kitazumi, K., Toki, H., Haga, A., Yamamoto, R., Shinzawa, M., Yamakawa, M., Fukui, S., Yamamoto, K., & Moriyama, T. (2020). Causal relations of health indices inferred statistically using the DirectLiNGAM algorithm from big data of

- Osaka prefecture health checkups. *PloS One*, *15*(12), e0243229. https://doi.org/10.1371/journal.pone.0243229
- Krich, C., Runge, J., Miralles, D. G., Migliavacca, M., Perez-Priego, O., El-Madany, T., Carrara,
 A., & Mahecha, M. D. (2020). Estimating causal networks in biosphere–atmosphere
 interaction with the PCMCI approach. *Biogeosciences*, 17(4), 1033–1061.
 https://doi.org/10.5194/bg-17-1033-2020
- Kunicki, Z. J., Smith, M. L., & Murray, E. J. (2023). A Primer on Structural Equation Model Diagrams and Directed Acyclic Graphs: When and How to Use Each in Psychological and Epidemiological Research. *Advances in Methods and Practices in Psychological Science*, 6(2), 251524592311560. https://doi.org/10.1177/25152459231156085
- Künzel, S. R., Sekhon, J. S., Bickel, P. J., & Yu, B. (2019). Metalearners for estimating heterogeneous treatment effects using machine learning. *Proceedings of the National Academy of Sciences of the United States of America*, 116(10), 4156–4165. https://doi.org/10.1073/pnas.1804597116
- Kurotani, A., Miyamoto, H., & Kikuchi, J. (2024). Validation of causal inference data using DirectLiNGAM in an environmental small-scale model and calculation settings.

 MethodsX, 12, 102528. https://doi.org/10.1016/j.mex.2023.102528
- La Bastide-van Gemert, S., Stolk, R. P., Van Den Heuvel, E. R., & Fidler, V. (2014). Causal inference algorithms can be useful in life course epidemiology. *Journal of Clinical Epidemiology*, 67(2), 190–198. https://doi.org/10.1016/j.jclinepi.2013.07.019
- Larsen, A. E., Meng, K., & Kendall, B. E. (2019). Causal analysis in control–impact ecological studies with observational data. *Methods in Ecology and Evolution*, 10(7), 924–934. https://doi.org/10.1111/2041-210X.13190

- Laubach, Z. M., Murray, E. J., Hoke, K. L., Safran, R. J., & Perng, W. (2021). A biologist's guide to model selection and causal inference. *Proceedings of the Royal Society B: Biological Sciences*, 288(1943), 20202815. https://doi.org/10.1098/rspb.2020.2815
- Laube, S., & Zotz, G. (2003). Which abiotic factors limit vegetative growth in a vascular epiphyte? *Functional Ecology*, 17(5), 598–604. https://doi.org/10.1046/j.1365-2435.2003.00760.x
- Lechner, M. (2010). The Relation of Different Concepts of Causality Used in Time Series and Microeconometrics. *Econometric Reviews*, 30(1), 109–127. https://doi.org/10.1080/07474938.2011.520571
- Lefcheck, J. S. (2016). piecewiseSEM: Piecewise structural equation modelling in R for ecology, evolution, and systematics. *Methods in Ecology and Evolution*, 7(5), 573–579. https://doi.org/10.1111/2041-210X.12512
- Lei, M.-K., Simons, R. L., Beach, S. R. H., & Philibert, R. A. (2019). Neighborhood

 Disadvantage and Biological Aging: Using Marginal Structural Models to Assess the

 Link Between Neighborhood Census Variables and Epigenetic Aging. *The Journals of Gerontology: Series B*, 74(7), e50–e59. https://doi.org/10.1093/geronb/gbx015
- Leist, A. K., Klee, M., Kim, J. H., Rehkopf, D. H., Bordas, S. P. A., Muniz-Terrera, G., & Wade, S. (2022). Mapping of machine learning approaches for description, prediction, and causal inference in the social and health sciences. *Science Advances*, 8(42), eabk1942. https://doi.org/10.1126/sciadv.abk1942
- Leng, S., Ma, H., Kurths, J., Lai, Y.-C., Lin, W., Aihara, K., & Chen, L. (2020). Partial cross mapping eliminates indirect causal influences. *Nature Communications*, *11*(1), 2632. https://doi.org/10.1038/s41467-020-16238-0
- Levins, R. (1966). The strategy of model building in population biology. *American Scientist*, 54(4), 421–431. JSTOR.

- Li, C., Shen, X., & Pan, W. (2024). Nonlinear Causal Discovery with Confounders. *Journal of the American Statistical Association*, 119(546), 1205–1214. https://doi.org/10.1080/01621459.2023.2179490
- Li, J., Liu, L., & Le, T. D. (2015). *Practical Approaches to Causal Relationship Exploration*. Springer International Publishing. https://doi.org/10.1007/978-3-319-14433-7
- Li, J., Liu, L., Le, T. D., & Liu, J. (2020). Accurate data-driven prediction does not mean high reproducibility. *Nature Machine Intelligence*, *2*(1), 13–15. https://doi.org/10.1038/s42256-019-0140-2
- Lipkovich, I., Ratitch, B., & Mallinckrodt, C. H. (2020). Causal Inference and Estimands in Clinical Trials. *Statistics in Biopharmaceutical Research*, *12*(1), 54–67. https://doi.org/10.1080/19466315.2019.1697739
- Little, R. J. (2021). Missing Data Assumptions. *Annual Review of Statistics and Its Application*, 8(1), 89–107. https://doi.org/10.1146/annurev-statistics-040720-031104
- Lopez Bernal, J., Cummins, S., & Gasparrini, A. (2016). Interrupted time series regression for the evaluation of public health interventions: a tutorial. *International Journal of Epidemiology*, dyw098. https://doi.org/10.1093/ije/dyw098
- Luo, Y., Ogle, K., Tucker, C., Fei, S., Gao, C., LaDeau, S., Clark, J. S., & Schimel, D. S. (2011). Ecological forecasting and data assimilation in a data-rich era. *Ecological Applications*, 21(5), 1429–1442. https://doi.org/10.1890/09-1275.1
- Luo, Y., Peng, J., & Ma, J. (2020). When causal inference meets deep learning. *Nature Machine Intelligence*, 2(8), 426–427. https://doi.org/10.1038/s42256-020-0218-x
- Luque-Fernandez, M. A., Schomaker, M., Rachet, B., & Schnitzer, M. E. (2018). Targeted maximum likelihood estimation for a binary treatment: A tutorial. *Statistics in Medicine*, 37(16), 2530–2546. https://doi.org/10.1002/sim.7628

- Maathuis, M. H., & Colombo, D. (2015). A generalized back-door criterion. *The Annals of Statistics*, 43(3). https://doi.org/10.1214/14-AOS1295
- MacDonald, A. J., Larsen, A. E., & Plantinga, A. J. (2019). Missing the people for the trees: Identifying coupled natural–human system feedbacks driving the ecology of Lyme disease. *Journal of Applied Ecology*, *56*(2), 354–364. https://doi.org/10.1111/1365-2664.13289
- MacDonald, A. J., & Mordecai, E. A. (2019). Amazon deforestation drives malaria transmission, and malaria burden reduces forest clearing. *Proceedings of the National Academy of Sciences*, *116*(44), 22212–22218. https://doi.org/10.1073/pnas.1905315116
- Mandujano Reyes, J. F., Ma, T. F., McGahan, I. P., Storm, D. J., Walsh, D. P., & Zhu, J. (2025).

 Spatiotemporal Causal Inference With Mechanistic Ecological Models: Evaluating

 Targeted Culling on Chronic Wasting Disease Dynamics in Cervids. *Environmetrics*,

 36(2), e2901. https://doi.org/10.1002/env.2901
- Markus, K. A. (2010). Structural Equations and Causal Explanations: Some Challenges for Causal SEM. *Structural Equation Modeling: A Multidisciplinary Journal*, *17*(4), 654–676. https://doi.org/10.1080/10705511.2010.510068
- Markus, K. A. (2021). Causal effects and counterfactual conditionals: contrasting Rubin, Lewis and Pearl. *Economics and Philosophy*, *37*(3), 441–461. https://doi.org/10.1017/S0266267120000437
- Marquet, P. A., Allen, A. P., Brown, J. H., Dunne, J. A., Enquist, B. J., Gillooly, J. F., Gowaty,
 P. A., Green, J. L., Harte, J., Hubbell, S. P., O'Dwyer, J., Okie, J. G., Ostling, A., Ritchie,
 M., Storch, D., & West, G. B. (2014). On Theory in Ecology. *BioScience*, 64(8), 701–710. https://doi.org/10.1093/biosci/biu098

- Matsuzaki, S. S., Suzuki, K., Kadoya, T., Nakagawa, M., & Takamura, N. (2018). Bottom-up linkages between primary production, zooplankton, and fish in a shallow, hypereutrophic lake. *Ecology*, *99*(9), 2025–2036. https://doi.org/10.1002/ecy.2414
- McCracken, J. M., & Weigel, R. S. (2014). Convergent cross-mapping and pairwise asymmetric inference. *Physical Review. E, Statistical, Nonlinear, and Soft Matter Physics*, 90(6), 062903. https://doi.org/10.1103/PhysRevE.90.062903
- McGoff, K., Mukherjee, S., & Pillai, N. S. (2012). *Statistical inference for dynamical systems: a review* (Version 3). arXiv. https://doi.org/10.48550/ARXIV.1204.6265
- Mielke, K. P., Schipper, A. M., Heskes, T., Zijp, M. C., Posthuma, L., Huijbregts, M. A. J., & Claassen, T. (2022). Discovering Ecological Relationships in Flowing Freshwater
 Ecosystems. Frontiers in Ecology and Evolution, 9, 782554.
 https://doi.org/10.3389/fevo.2021.782554
- Montesanto, G., & Cividini, S. (2017). A crossover design to assess feeding preferences in terrestrial isopods: A case study in a Mediterranean species. *Biologia*, 72(2), 194–203. https://doi.org/10.1515/biolog-2017-0020
- Mooij, J. M., Peters, J., Janzing, D., Zscheischler, J., & Schölkopf, B. (2016). Distinguishing Cause from Effect Using Observational Data: Methods and Benchmarks. *Journal of Machine Learning Research*, 17(32), 1–102.
- Morgan, S. L., & Winship, C. (2014). Matching Estimators of Causal Effects. In *Counterfactuals* and Causal Inference: Methods and Principles for Social Research (2nd ed., pp. 140–187). Cambridge University Press. https://doi.org/10.1017/CBO9781107587991
- Morgan, S. L., & Winship, C. (2015). Counterfactuals and Causal Inference: Methods and Principles for Social Research (Second edition). Cambridge University press.
- Moss, W. E., Binfet, J., Hall, L. E., Allen, S. E., Edwards, W. H., Jennings-Gaines, J. E., & Cross, P. C. (2025). The effectiveness of harvest for limiting wildlife disease: Insights

- from 20 years of chronic wasting disease in Wyoming. *Ecological Applications*, *35*(1), e3089. https://doi.org/10.1002/eap.3089
- Nabi, R., & Shpitser, I. (2018). Fair Inference on Outcomes. *Proceedings of the ... AAAI*Conference on Artificial Intelligence. AAAI Conference on Artificial Intelligence, 2018, 1931–1940.
- Nakagawa, S., & Cuthill, I. C. (2007). Effect size, confidence interval and statistical significance: a practical guide for biologists. *Biological Reviews*, 82(4), 591–605. https://doi.org/10.1111/j.1469-185X.2007.00027.x
- Nandi, A., Glymour, M. M., Kawachi, I., & VanderWeele, T. J. (2012). Using Marginal Structural Models to Estimate the Direct Effect of Adverse Childhood Social Conditions on Onset of Heart Disease, Diabetes, and Stroke. *Epidemiology*, 23(2), 223–232. https://doi.org/10.1097/EDE.0b013e31824570bd
- Nichols, J. D., & Cooch, E. G. (2025). Predictive models are indeed useful for causal inference. *Ecology*, 106(1), e4517. https://doi.org/10.1002/ecy.4517
- Nicolaisen, O., Cuny, M., & Bolla, S. (2014). Factorial experimental designs as tools to optimize rearing conditions of fish larvae. *Aquaculture*, 422–423, 253–260. https://doi.org/10.1016/j.aquaculture.2013.12.018
- Nie, X., & Wager, S. (2021). Quasi-oracle estimation of heterogeneous treatment effects.

 *Biometrika, 108(2), 299–319. https://doi.org/10.1093/biomet/asaa076
- Noack, F., Larsen, A., Kamp, J., & Levers, C. (2022). A bird's eye view of farm size and biodiversity: The ecological legacy of the iron curtain. *American Journal of Agricultural Economics*, 104(4), 1460–1484. https://doi.org/10.1111/ajae.12274
- Nogueira, A. R., Pugnana, A., Ruggieri, S., Pedreschi, D., & Gama, J. (2022). Methods and tools for causal discovery and causal inference. *WIREs Data Mining and Knowledge Discovery*, 12(2), e1449. https://doi.org/10.1002/widm.1449

- Nova, N., Deyle, E. R., Shocket, M. S., MacDonald, A. J., Childs, M. L., Rypdal, M., Sugihara, G., & Mordecai, E. A. (2021). Susceptible host availability modulates climate effects on dengue dynamics. *Ecology Letters*, *24*(3), 415–425. https://doi.org/10.1111/ele.13652
- Oehri, J., Schmid, B., Schaepman-Strub, G., & Niklaus, P. A. (2020). Terrestrial land-cover type richness is positively linked to landscape-level functioning. *Nature Communications*, 11(1), 154. https://doi.org/10.1038/s41467-019-14002-7
- Ohrens, O., Bonacic, C., & Treves, A. (2019). Non-lethal defense of livestock against predators: flashing lights deter puma attacks in Chile. *Frontiers in Ecology and the Environment*, 17(1), 32–38. https://doi.org/10.1002/fee.1952
- Olden, J. D., Lawler, J. J., & Poff, N. L. (2008). Machine Learning Methods Without Tears: A Primer for Ecologists. *The Quarterly Review of Biology*, 83(2), 171–193. https://doi.org/10.1086/587826
- Orava, P. J. (1973). Causality and state concepts in dynamical systems theory. *International Journal of Systems Science*, 4(4), 679–690. https://doi.org/10.1080/00207727308920048
- Paluš, M. (2007). From nonlinearity to causality: statistical testing and inference of physical mechanisms underlying complex dynamics. *Contemporary Physics*, 48(6), 307–348. https://doi.org/10.1080/00107510801959206
- Paluš, M., Krakovská, A., Jakubík, J., & Chvosteková, M. (2018). Causality, dynamical systems and the arrow of time. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 28(7), 075307. https://doi.org/10.1063/1.5019944
- Park, J., Buchholz, S., Schölkopf, B., & Muandet, K. (2023). A Measure-Theoretic Axiomatisation of Causality. *Thirty-Seventh Conference on Neural Information Processing Systems*. https://openreview.net/forum?id=sPLTQSf6GI

- Paul, W. L. (2011). A causal modelling approach to spatial and temporal confounding in environmental impact studies. *Environmetrics*, 22(5), 626–638. https://doi.org/10.1002/env.1111
- Pearl, J. (1995). Causal diagrams for empirical research. *Biometrika*, 82(4), 669–688. https://doi.org/10.1093/biomet/82.4.669
- Pearl, J. (1998). Graphs, Causality, and Structural Equation Models. *Sociological Methods & Research*, 27(2), 226–284. https://doi.org/10.1177/0049124198027002004
- Pearl, J. (2009). *Causality: Models, Reasoning, and Inference* (2nd ed). Cambridge University Press. https://doi.org/10.1017/CBO9780511803161
- Pearl, J. (2010). An Introduction to Causal Inference. *The International Journal of Biostatistics*, 6(2). https://doi.org/10.2202/1557-4679.1203
- Pearl, J. (2012). The causal foundations of structural equation modeling. In *Handbook of structural Equation Modeling* (pp. 68–91). The Guilford Press.
- Pearl, J. (2022). Causation and decision: On Dawid's "Decision theoretic foundation of statistical causality." *Journal of Causal Inference*, 10(1), 221–226. https://doi.org/10.1515/jci-2022-0046
- Pearl, J., & Bareinboim, E. (2014). External Validity: From Do-Calculus to Transportability Across Populations. *Statistical Science*, *29*(4). https://doi.org/10.1214/14-STS486
- Pearson, C. E., Ormerod, S. J., Symondson, W. O. C., & Vaughan, I. P. (2016). Resolving large-scale pressures on species and ecosystems: propensity modelling identifies agricultural effects on streams. *Journal of Applied Ecology*, *53*(2), 408–417. https://doi.org/10.1111/1365-2664.12586
- Peters, J., Bühlmann, P., & Meinshausen, N. (2016). Causal Inference by using Invariant Prediction: Identification and Confidence Intervals. *Journal of the Royal Statistical*

- Society Series B: Statistical Methodology, 78(5), 947–1012. https://doi.org/10.1111/rssb.12167
- Peters, J., Janzing, D., & Schölkopf, B. (2017). Elements of Causal Inference: Foundations and Learning Algorithms. The MIT Press.
- Peters, J., Mooij, J. M., Janzing, D., & Schölkopf, B. (2014). Causal Discovery with Continuous Additive Noise Models. *Journal of Machine Learning Research*, 15(58), 2009–2053.
- Petersen, M. L., Porter, K. E., Gruber, S., Wang, Y., & van der Laan, M. J. (2012). Diagnosing and responding to violations in the positivity assumption. *Statistical Methods in Medical Research*, 21(1), 31–54. https://doi.org/10.1177/0962280210386207
- Petersen, M. L., & van der Laan, M. J. (2014). Causal models and learning from data: integrating causal modeling and statistical estimation. *Epidemiology (Cambridge, Mass.)*, 25(3), 418–426. https://doi.org/10.1097/EDE.000000000000000000
- Pfister, N., Bühlmann, P., & Peters, J. (2019). Invariant Causal Prediction for Sequential Data.

 Journal of the American Statistical Association, 114(527), 1264–1276.

 https://doi.org/10.1080/01621459.2018.1491403
- Pichler, M., & Hartig, F. (2023). Machine learning and deep learning—A review for ecologists.

 Methods in Ecology and Evolution, 14(4), 994–1016. https://doi.org/10.1111/2041-210X.14061
- Pitcher, C. R., Burridge, C. Y., Wassenberg, T. J., Hill, B. J., & Poiner, I. R. (2009). A large scale BACI experiment to test the effects of prawn trawling on seabed biota in a closed area of the Great Barrier Reef Marine Park, Australia. *Fisheries Research*, 99(3), 168–183. https://doi.org/10.1016/j.fishres.2009.05.017
- Pynegar, E. L., Gibbons, J. M., Asquith, N. M., & Jones, J. P. G. (2021). What role should randomized control trials play in providing the evidence base for conservation? *Oryx*, 55(2), 235–244. https://doi.org/10.1017/S0030605319000188

- Ramsey, J., Glymour, M., Sanchez-Romero, R., & Glymour, C. (2017). A million variables and more: the Fast Greedy Equivalence Search algorithm for learning high-dimensional graphical causal models, with an application to functional magnetic resonance images.

 *International Journal of Data Science and Analytics, 3(2), 121–129.

 https://doi.org/10.1007/s41060-016-0032-z
- Reygadas, Y., Jensen, J. L. R., Moisen, G. G., Currit, N., & Chow, E. T. (2020). Assessing the relationship between vegetation greenness and surface temperature through Granger causality and Impulse-Response coefficients: a case study in Mexico. *International Journal of Remote Sensing*, 41(10), 3761–3783.

 https://doi.org/10.1080/01431161.2019.1711241
- Richardson, T. (2003). Markov Properties for Acyclic Directed Mixed Graphs. *Scandinavian Journal of Statistics*, 30(1), 145–157. https://doi.org/10.1111/1467-9469.00323
- Richardson, T., & Spirtes, P. (2002). Ancestral graph Markov models. *The Annals of Statistics*, 30(4). https://doi.org/10.1214/aos/1031689015
- Rohrer, J. M. (2018). Thinking Clearly About Correlations and Causation: Graphical Causal Models for Observational Data. *Advances in Methods and Practices in Psychological Science*, *1*(1), 27–42. https://doi.org/10.1177/2515245917745629
- Rosenbaum, P. R. (2002). Constructing Matched Sets and Strata. In P. R. Rosenbaum,

 Observational Studies (pp. 295–331). Springer New York. https://doi.org/10.1007/978-1-4757-3692-2_10
- Rosenbaum, P. R., & Rubin, D. B. (1983). The central role of the propensity score in observational studies for causal effects. *Biometrika*, 70(1), 41–55. https://doi.org/10.1093/biomet/70.1.41

- Rubin, D. B. (1974). Estimating causal effects of treatments in randomized and nonrandomized studies. *Journal of Educational Psychology*, 66(5), 688–701. https://doi.org/10.1037/h0037350
- Rubin, D. B. (1978). Bayesian Inference for Causal Effects: The Role of Randomization. *The Annals of Statistics*, 6(1), 34–58. JSTOR.
- Rubin, D. B. (1980). Randomization Analysis of Experimental Data: The Fisher Randomization

 Test Comment. *Journal of the American Statistical Association*, 75(371), 591.

 https://doi.org/10.2307/2287653
- Rubin, D. B. (2005). Causal Inference Using Potential Outcomes: Design, Modeling, Decisions.

 *Journal of the American Statistical Association, 100(469), 322–331.

 https://doi.org/10.1198/016214504000001880
- Runge, J. (2018). Causal network reconstruction from time series: From theoretical assumptions to practical estimation. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 28(7), 075310. https://doi.org/10.1063/1.5025050
- Runge, J., Bathiany, S., Bollt, E., Camps-Valls, G., Coumou, D., Deyle, E., Glymour, C.,
 Kretschmer, M., Mahecha, M. D., Muñoz-Marí, J., Van Nes, E. H., Peters, J., Quax, R.,
 Reichstein, M., Scheffer, M., Schölkopf, B., Spirtes, P., Sugihara, G., Sun, J., ...
 Zscheischler, J. (2019). Inferring causation from time series in Earth system sciences.
 Nature Communications, 10(1), 2553. https://doi.org/10.1038/s41467-019-10105-3
- Runge, J., Gerhardus, A., Varando, G., Eyring, V., & Camps-Valls, G. (2023). Causal inference for time series. *Nature Reviews Earth & Environment*, 4(7), 487–505. https://doi.org/10.1038/s43017-023-00431-y
- Runge, J., Heitzig, J., Petoukhov, V., & Kurths, J. (2012). Escaping the Curse of Dimensionality in Estimating Multivariate Transfer Entropy. *Physical Review Letters*, *108*(25), 258701. https://doi.org/10.1103/PhysRevLett.108.258701

- Runge, J., Nowack, P., Kretschmer, M., Flaxman, S., & Sejdinovic, D. (2019). Detecting and quantifying causal associations in large nonlinear time series datasets. *Science Advances*, 5(11), eaau4996. https://doi.org/10.1126/sciadv.aau4996
- Saavedra, S., Bartomeus, I., Godoy, O., Rohr, R. P., & Zu, P. (2022). Towards a system-level causative knowledge of pollinator communities. *Philosophical Transactions of the Royal Society B: Biological Sciences*, *377*(1853), 20210159.

 https://doi.org/10.1098/rstb.2021.0159
- Salditt, M., Eckes, T., & Nestler, S. (2024). A Tutorial Introduction to Heterogeneous Treatment

 Effect Estimation with Meta-learners. *Administration and Policy in Mental Health and*Mental Health Services Research, 51(5), 650–673. https://doi.org/10.1007/s10488-023-01303-9
- Sargeant, J. M., O'Connor, A. M., Totton, S. C., & Vriezen, E. R. (2022). Watch your language:

 An exploration of the use of causal wording in veterinary observational research.

 Frontiers in Veterinary Science, 9. https://www.frontiersin.org/journals/veterinary-science/articles/10.3389/fvets.2022.1004801
- Sauer, T., Yorke, J. A., & Casdagli, M. (1991). Embedology. *Journal of Statistical Physics*, 65(3–4), 579–616. https://doi.org/10.1007/BF01053745
- Scheines, R. (1997). *An Introduction to Causal Inference*. Carnegie Mellon University. https://doi.org/10.1184/R1/6490904.V1
- Scherrer, N., Bilaniuk, O., Annadani, Y., Goyal, A., Schwab, P., Schölkopf, B., Mozer, M. C., Bengio, Y., Bauer, S., & Ke, N. R. (2021). *Learning Neural Causal Models with Active Interventions* (Version 2). arXiv. https://doi.org/10.48550/ARXIV.2109.02429
- Schochet, P. Z. (2013). Estimators for Clustered Education RCTs Using the Neyman Model for Causal Inference. *Journal of Educational and Behavioral Statistics*, *38*(3), 219–238. https://doi.org/10.3102/1076998611432176

- Scholkopf, B., Locatello, F., Bauer, S., Ke, N. R., Kalchbrenner, N., Goyal, A., & Bengio, Y. (2021). Toward Causal Representation Learning. *Proceedings of the IEEE*, *109*(5), 612–634. https://doi.org/10.1109/JPROC.2021.3058954
- Schoolmaster, D. R., Zirbel, C. R., & Cronin, J. P. (2020). A graphical causal model for resolving species identity effects and biodiversity–ecosystem function correlations. *Ecology*, 101(8), e03070. https://doi.org/10.1002/ecy.3070
- Schreiber, T. (2000). Measuring Information Transfer. *Physical Review Letters*, 85(2), 461–464. https://doi.org/10.1103/PhysRevLett.85.461
- Schuler, M. S., & Rose, S. (2017). Targeted Maximum Likelihood Estimation for Causal Inference in Observational Studies. *American Journal of Epidemiology*, 185(1), 65–73. https://doi.org/10.1093/aje/kww165
- Servedio, M. R., Brandvain, Y., Dhole, S., Fitzpatrick, C. L., Goldberg, E. E., Stern, C. A., Van Cleve, J., & Yeh, D. J. (2014). Not Just a Theory—The Utility of Mathematical Models in Evolutionary Biology. *PLoS Biology*, *12*(12), e1002017. https://doi.org/10.1371/journal.pbio.1002017
- Shah, A., Ramanathan, A., Hayot-Sasson, V., & Stevens, R. (2023). Causal Discovery and Optimal Experimental Design for Genome-Scale Biological Network Recovery. *ArXiv*, arXiv:2304.03210v1.
- Shahn, Z., Hernán, M. A., & Robins, J. M. (2023). A Formal Causal Interpretation of the Case-Crossover Design. *Biometrics*, 79(2), 1330–1343. https://doi.org/10.1111/biom.13749
- Shen, X., Ma, S., Vemuri, P., Simon, G., the Alzheimer's Disease Neuroimaging Initiative,
 Weiner, M. W., Aisen, P., Petersen, R., Jack, C. R., Saykin, A. J., Jagust, W.,
 Trojanowki, J. Q., Toga, A. W., Beckett, L., Green, R. C., Morris, J., Shaw, L. M.,
 Khachaturian, Z., Sorensen, G., ... Fargher, K. (2020). Challenges and Opportunities

- with Causal Discovery Algorithms: Application to Alzheimer's Pathophysiology. *Scientific Reports*, 10(1), 2975. https://doi.org/10.1038/s41598-020-59669-x
- Shi, B., Mao, X., Yang, M., & Li, B. (2024). What, Why, and How: An Empiricist's Guide to Double/Debiased Machine Learning. SSRN Electronic Journal. https://doi.org/10.2139/ssrn.4677153
- Shi, J., Chen, L., & Aihara, K. (2022). Embedding entropy: a nonlinear measure of dynamical causality. *Journal of The Royal Society Interface*, 19(188), 20210766. https://doi.org/10.1098/rsif.2021.0766
- Shimizu, S. (2014). Lingam: Non-Gaussian Methods for Estimating Causal Structures. *Behaviormetrika*, 41(1), 65–98. https://doi.org/10.2333/bhmk.41.65
- Shimizu, S., Hoyer, P. O., Hyvärinen, A., & Kerminen, A. (2006). A Linear Non-Gaussian Acyclic Model for Causal Discovery. *Journal of Machine Learning Research*, 7(72), 2003–2030.
- Shimizu, S., Inazumi, T., Sogawa, Y., Hyvärinen, A., Kawahara, Y., Washio, T., Hoyer, P. O., & Bollen, K. (2011). DirectLiNGAM: A Direct Method for Learning a Linear Non-Gaussian Structural Equation Model. *Journal of Machine Learning Research*, *12*(33), 1225–1248.
- Shipley, B. (2016). Cause and correlation in biology: a user's guide to path analysis, structural equations and causal inference with R. Cambridge university press.
- Shpitser, I., & Pearl, J. (2008). Complete Identification Methods for the Causal Hierarchy. *Journal of Machine Learning Research*, 9(64), 1941–1979.
- Shrier, I., & Platt, R. W. (2008). Reducing bias through directed acyclic graphs. *BMC Medical Research Methodology*, 8, 70. https://doi.org/10.1186/1471-2288-8-70
- Siegel, K. J., Larsen, L., Stephens, C., Stewart, W., & Butsic, V. (2022). Quantifying drivers of change in social-ecological systems: land management impacts wildfire probability in

- forests of the western US. *Regional Environmental Change*, 22(3), 98. https://doi.org/10.1007/s10113-022-01950-y
- Siegel, K. J., Macaulay, L., Shapero, M., Becchetti, T., Larson, S., Mashiri, F. E., Waks, L., Larsen, L., & Butsic, V. (2022). Impacts of livestock grazing on the probability of burning in wildfires vary by region and vegetation type in California. *Journal of Environmental Management*, 322, 116092.
 https://doi.org/10.1016/j.jenvman.2022.116092
- Simler-Williamson, A. B., & Germino, M. J. (2022). Statistical considerations of nonrandom treatment applications reveal region-wide benefits of widespread post-fire restoration action. *Nature Communications*, *13*(1), 3472. https://doi.org/10.1038/s41467-022-31102-z
- Singer, R. S. (2022). Continued abuse of causal inference in studies of antimicrobial resistance: revisiting the confusion between ecological correlation and causation. *Journal of Global Antimicrobial Resistance*, *30*, 485–486. https://doi.org/10.1016/j.jgar.2022.05.007
- Singh, N. K., & Borrok, D. M. (2019). A Granger causality analysis of groundwater patterns over a half-century. *Scientific Reports*, 9(1), 12828. https://doi.org/10.1038/s41598-019-49278-8
- Smokorowski, K. E., & Randall, R. G. (2017). Cautions on using the Before-After-Control-Impact design in environmental effects monitoring programs. *FACETS*, 2(1), 212–232. https://doi.org/10.1139/facets-2016-0058
- Sobel, M. E. (2006). What Do Randomized Studies of Housing Mobility Demonstrate?: Causal Inference in the Face of Interference. *Journal of the American Statistical Association*, 101(476), 1398–1407. https://doi.org/10.1198/016214506000000636
- Sobel, M. E. (2009). Causal Inference in Randomized and Non-Randomized Studies: The Definition, Identification, and Estimation of Causal Parameters. In R. Millsap & A.

- Maydeu-Olivares, *The SAGE Handbook of Quantitative Methods in Psychology* (pp. 3–22). SAGE Publications Ltd. https://doi.org/10.4135/9780857020994.n1
- Song, C., Simmons, B. I., Fortin, M.-J., & Gonzalez, A. (2022). Generalism drives abundance: A computational causal discovery approach. *PLOS Computational Biology*, *18*(9), e1010302. https://doi.org/10.1371/journal.pcbi.1010302
- Spirtes, P., Glymour, C. N., & Scheines, R. (2000). *Causation, prediction, and search* (2nd ed).

 MIT Press.
- Stewart, P. S., Stephens, P. A., Hill, R. A., Whittingham, M. J., & Dawson, W. (2023). Model selection in occupancy models: Inference versus prediction. *Ecology*, *104*(3), e3942. https://doi.org/10.1002/ecy.3942
- Stone, R. (1993). The Assumptions on Which Causal Inferences Rest. *Journal of the Royal Statistical Society. Series B, Methodological*, *55*(2), 455–466.
- Sugihara, G., May, R., Ye, H., Hsieh, C., Deyle, E., Fogarty, M., & Munch, S. (2012). Detecting Causality in Complex Ecosystems. *Science*, *338*(6106), 496–500. https://doi.org/10.1126/science.1227079
- Sun, J., & Bollt, E. M. (2014). Causation entropy identifies indirect influences, dominance of neighbors and anticipatory couplings. *Physica D: Nonlinear Phenomena*, 267, 49–57. https://doi.org/10.1016/j.physd.2013.07.001
- Sun, J., Taylor, D., & Bollt, E. M. (2015). Causal Network Inference by Optimal Causation Entropy. SIAM Journal on Applied Dynamical Systems, 14(1), 73–106. https://doi.org/10.1137/140956166
- Takens, F. (1981). Detecting strange attractors in turbulence. In D. Rand & L.-S. Young (Eds.),

 *Dynamical Systems and Turbulence, Warwick 1980 (Vol. 898, pp. 366–381). Springer

 Berlin Heidelberg. https://doi.org/10.1007/BFb0091924

- Tárraga, J. M., Sevillano-Marco, E., Muñoz-Marí, J., Piles, M., Sitokonstantinou, V., Ronco, M., Miranda, M. T., Cerdà, J., & Camps-Valls, G. (2024). Causal discovery reveals complex patterns of drought-induced displacement. iScience, 27(9), 110628.
 https://doi.org/10.1016/j.isci.2024.110628
- Tchetgen Tchetgen, E. J., & VanderWeele, T. J. (2012). On causal inference in the presence of interference. *Statistical Methods in Medical Research*, *21*(1), 55–75. https://doi.org/10.1177/0962280210386779
- Textor, J., Hardt, J., & Knüppel, S. (2011). DAGitty: a graphical tool for analyzing causal diagrams. *Epidemiology (Cambridge, Mass.)*, 22(5), 745. https://doi.org/10.1097/EDE.0b013e318225c2be
- Theiler, J., Eubank, S., Longtin, A., Galdrikian, B., & Doyne Farmer, J. (1992). Testing for nonlinearity in time series: the method of surrogate data. *Physica D: Nonlinear Phenomena*, 58(1), 77–94. https://doi.org/10.1016/0167-2789(92)90102-S
- Tian, J., & Pearl, J. (2002). A general identification condition for causal effects. *Eighteenth National Conference on Artificial Intelligence*, 567–573. https://doi.org/10.5555/777092
- Tilman, D., Reich, P. B., & Knops, J. M. H. (2006). Biodiversity and ecosystem stability in a decade-long grassland experiment. *Nature*, *441*(7093), 629–632. https://doi.org/10.1038/nature04742
- Tredennick, A. T., Hooker, G., Ellner, S. P., & Adler, P. B. (2021). A practical guide to selecting models for exploration, inference, and prediction in ecology. *Ecology*, *102*(6), e03336. https://doi.org/10.1002/ecy.3336
- Treves, A., Fergus, A. R., Hermanstorfer, S. J., Louchouarn, N. X., Ohrens, O., & Pineda-Guerrero, A. (2024). Gold-standard experiments to deter predators from attacking farm animals. *Animal Frontiers*, 14(1), 40–52. https://doi.org/10.1093/af/vfad072

- Ushio, M., Hsieh, C., Masuda, R., Deyle, E. R., Ye, H., Chang, C.-W., Sugihara, G., & Kondoh, M. (2018). Fluctuating interaction network and time-varying stability of a natural fish community. *Nature*, *554*(7692), 360–363. https://doi.org/10.1038/nature25504
- van der Laan, M. J., & Rubin, D. (2006). Targeted Maximum Likelihood Learning. *The International Journal of Biostatistics*, 2(1). https://doi.org/10.2202/1557-4679.1043
- VanderWeele, T. J. (2015). Explanation in causal inference: methods for mediation and interaction.
- VanderWeele, T. J. (2019). Principles of confounder selection. *European Journal of Epidemiology*, 34(3), 211–219. https://doi.org/10.1007/s10654-019-00494-6
- VanderWeele, T. J., Hawkley, L. C., Thisted, R. A., & Cacioppo, J. T. (2011). A marginal structural model analysis for loneliness: Implications for intervention trials and clinical practice. *Journal of Consulting and Clinical Psychology*, 79(2), 225–235. https://doi.org/10.1037/a0022610
- VanderWeele, T. J., & Hernán, M. A. (2013). Causal Inference Under Multiple Versions of Treatment. *Journal of Causal Inference*, *I*(1), 1–20. https://doi.org/10.1515/jci-2012-0002
- VanderWeele, T. J., & Shpitser, I. (2011). A New Criterion for Confounder Selection. *Biometrics*, 67(4), 1406–1413. https://doi.org/10.1111/j.1541-0420.2011.01619.x
- Vonk, M. C., Malekovic, N., Bäck, T., & Kononova, A. V. (2023). Disentangling causality: assumptions in causal discovery and inference. *Artificial Intelligence Review*, *56*(9), 10613–10649. https://doi.org/10.1007/s10462-023-10411-9
- Wager, S., & Athey, S. (2018). Estimation and Inference of Heterogeneous Treatment Effects using Random Forests. *Journal of the American Statistical Association*, *113*(523), 1228–1242. https://doi.org/10.1080/01621459.2017.1319839

- Wang, X., Du, Y., Zhu, S., Ke, L., Chen, Z., Hao, J., & Wang, J. (2021). Ordering-Based Causal Discovery with Reinforcement Learning. *Proceedings of the Thirtieth International Joint Conference on Artificial Intelligence*, 3566–3573. https://doi.org/10.24963/ijcai.2021/491
- Wang, X., & Sobel, M. E. (2013). New Perspectives on Causal Mediation Analysis. In S. L. Morgan (Ed.), *Handbook of Causal Analysis for Social Research* (pp. 215–242). Springer Netherlands. https://doi.org/10.1007/978-94-007-6094-3_12
- Wauchope, H. S., Amano, T., Geldmann, J., Johnston, A., Simmons, B. I., Sutherland, W. J., & Jones, J. P. G. (2021). Evaluating Impact Using Time-Series Data. *Trends in Ecology & Evolution*, 36(3), 196–205. https://doi.org/10.1016/j.tree.2020.11.001
- Weigel, C., Harden, S., Masuda, Y. J., Ranjan, P., Wardropper, C. B., Ferraro, P. J., Prokopy, L., & Reddy, S. (2021). Using a randomized controlled trial to develop conservation strategies on rented farmlands. *Conservation Letters*, 14(4), e12803. https://doi.org/10.1111/conl.12803
- Wermuth, N., & Lauritzen, S. L. (1990). On Substantive Research Hypotheses, Conditional Independence Graphs and Graphical Chain Models. *Journal of the Royal Statistical Society Series B: Statistical Methodology*, *52*(1), 21–50. https://doi.org/10.1111/j.2517-6161.1990.tb01771.x
- West, T. A. P., Caviglia-Harris, J. L., Martins, F. S. R. V., Silva, D. E., & Börner, J. (2022).

 Potential conservation gains from improved protected area management in the Brazilian Amazon. *Biological Conservation*, 269, 109526.

 https://doi.org/10.1016/j.biocon.2022.109526
- Westreich, D., & Cole, S. R. (2010). Invited commentary: positivity in practice. *American Journal of Epidemiology*, 171(6), 674–677; discussion 678-681. https://doi.org/10.1093/aje/kwp436

- White, H., & Chalak, K. (2009). Settable Systems: An Extension of Pearl's Causal Model with Optimization, Equilibrium, and Learning. *Journal of Machine Learning Research*, 10(61), 1759–1799.
- White, H., Chalak, K., & Lu, X. (2011). Linking Granger Causality and the Pearl Causal Model with Settable Systems. In F. Popescu & I. Guyon (Eds.), *Proceedings of the Neural Information Processing Systems Mini-Symposium on Causality in Time Series* (Vol. 12, pp. 1–29). PMLR. https://proceedings.mlr.press/v12/white11.html
- Wiik, E., Jones, J. P. G., Pynegar, E., Bottazzi, P., Asquith, N., Gibbons, J., & Kontoleon, A. (2020). Mechanisms and impacts of an incentive-based conservation program with evidence from a randomized control trial. *Conservation Biology*, 34(5), 1076–1088. https://doi.org/10.1111/cobi.13508
- Wooldridge, J. M. (2010). *Econometric analysis of cross section and panel data* (2nd ed). MIT Press.
- Wu, J., Zhou, Y., Wang, H., Wang, X., & Wang, J. (2023). Assessing the Causal Effects of Climate Change on Vegetation Dynamics in Northeast China Using Convergence Cross-Mapping. *IEEE Access*, 11, 115367–115379. https://doi.org/10.1109/ACCESS.2023.3325485
- Wu, X., Sverdrup, E., Mastrandrea, M. D., Wara, M. W., & Wager, S. (2023). Low-intensity fires mitigate the risk of high-intensity wildfires in California's forests. *Science Advances*, 9(45), eadi4123. https://doi.org/10.1126/sciadv.adi4123
- Wu, Y., Zhang, L., & Wu, X. (2019). Counterfactual fairness: unidentification, bound and algorithm. *Proceedings of the 28th International Joint Conference on Artificial Intelligence*, 1438–1444.

- Xie, Y., Brand, J. E., & Jann, B. (2012). Estimating Heterogeneous Treatment Effects with Observational Data. *Sociological Methodology*, 42(1), 314–347. https://doi.org/10.1177/0081175012452652
- Yang, A. C., Peng, C.-K., & Huang, N. E. (2018). Causal decomposition in the mutual causation system. *Nature Communications*, 9(1), 3378. https://doi.org/10.1038/s41467-018-05845-7
- Ye, H., Deyle, E. R., Gilarranz, L. J., & Sugihara, G. (2015). Distinguishing time-delayed causal interactions using convergent cross mapping. *Scientific Reports*, *5*(1), 14750. https://doi.org/10.1038/srep14750
- Yongmei, D., & Yulian, L. (2024). Causal Linkage Effect on Chinese Industries via Partial Cross Mapping Under the Background of COVID-19. *Computational Economics*, 63(3), 1071–1094. https://doi.org/10.1007/s10614-023-10408-0
- Yu, Y., Chen, J., Gao, T., & Yu, M. (2019). DAG-GNN: DAG Structure Learning with Graph Neural Networks. In K. Chaudhuri & R. Salakhutdinov (Eds.), *Proceedings of the 36th International Conference on Machine Learning* (Vol. 97, pp. 7154–7163). PMLR. https://proceedings.mlr.press/v97/yu19a.html
- Yuan, A. E., & Shou, W. (2022). Data-driven causal analysis of observational biological time series. *eLife*, 11, e72518. https://doi.org/10.7554/eLife.72518
- Zeldow, B., Lo Re, V., & Roy, J. (2019). A semiparametric modeling approach using Bayesian Additive Regression Trees with an application to evaluate heterogeneous treatment effects. *The Annals of Applied Statistics*, *13*(3), 1989–2010. https://doi.org/10.1214/19-AOAS1266
- Zeng, Y., Cai, R., Sun, F., Huang, L., & Hao, Z. (2025). A Survey on Causal Reinforcement Learning. *IEEE Transactions on Neural Networks and Learning Systems*, *36*(4), 5942–5962. https://doi.org/10.1109/TNNLS.2024.3403001

- Zhang, C., Mohan, K., & Pearl, J. (2023). Causal Inference under Interference and Model
 Uncertainty. 2nd Conference on Causal Learning and Reasoning.

 https://openreview.net/forum?id=TYKk9SWhke0
- Zhao, A., & Ding, P. (2022). Regression-based causal inference with factorial experiments: estimands, model specifications and design-based properties. *Biometrika*, 109(3), 799–815. https://doi.org/10.1093/biomet/asab051
- Zheng, K., Yu, S., & Chen, B. (2024). CI-GNN: A Granger causality-inspired graph neural network for interpretable brain network-based psychiatric diagnosis. *Neural Networks*, 172, 106147. https://doi.org/10.1016/j.neunet.2024.106147
- Zheng, L., & Yin, W. (2023). Estimating and evaluating treatment effect heterogeneity: A causal forests approach. *Research & Politics*, 10(1), 20531680231153080. https://doi.org/10.1177/20531680231153080
- Zhu, S., Ng, I., & Chen, Z. (2020). Causal Discovery with Reinforcement Learning.

 International Conference on Learning Representations.

 https://openreview.net/forum?id=S1g2skStPB