1	Evolutionary rate incongruences in squamates reveal contrasting patterns of
2	evolutionary novelties and innovation
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#### 16 SUMMARY

17 Understanding the rate of phenotypic evolution can reveal fundamental aspects of organismal 18 evolutionary trajectories. Hence, several studies have attempted to detect the tempo of evolution 19 for multiple organisms, although based on radically different datatypes (e.g., discrete and 20 morphometric) and methods (phylodynamic vs comparative methods). Here, we ask whether 21 these competing approaches provide comparable rate trajectories using an expanded squamate 22 phylogenetic dataset that is matched (to the species-level) with new geometric morphometric 23 data, while also assessing method robustness to fossil sampling. Our new squamate total-24 evidence time-tree suggests a new placement for putative stem iguanians while matching 25 divergence time estimates of recent phylogenomic studies. We show that low fossil sampling 26 inadvertently removes entire regions of the morphospace and contraction of crown clade 27 phenotypic diversity, as morphospace boundaries are frequently delimited by transitional fossils. 28 Critically, different datatypes produce radically incongruent rate patterns, which are further 29 exacerbated by methodological differences. We suggest that phylogenetic discrete data (i.e., 30 characters) are strongly influenced by neomorphisms and reveal phenotypic novelties, while 31 morphometric data (i.e., shape) reflects changes in phenotypic refinement leading to phenotypic 32 innovation. This conceptual distinction conciliates discrepant macroevolution trajectories across 33 squamates, which we expect to be generalizable to other systems across the Tree of Life. 34 35 **Keywords**: evolutionary rates; macroevolution; phylogenetic comparative methods; 36 phylodynamics; squamates; morphospace

#### **38 INTRODUCTION**

39

40 Inferring rates of phenotypic evolution at macroevolutionary scales provide fundamental insights 41 into the tempo of adaptive changes governing the origin of new body plans and other major 42 evolution transitions across the tree of life<sup>1-3</sup>. Phenotypic rate inference has a long tradition in evolutionary biology and paleobiology<sup>1,2</sup>, but it has undergone an overhaul over the last two 43 44 decades due to the increasing availability of new data and quantitative phylogenetic tools<sup>4-8</sup>. The 45 result has been a proliferation of studies that have provided insights into phenotypic 46 macroevolutionary rate dynamics across various taxonomic and timescales<sup>3,9-15</sup>; thus inferring 47 events of major phenotypic novelties and innovations<sup>3,16-19</sup>, and their role in macroevolutionary 48 phenomena such as adaptive radiations<sup>3,17,18</sup>. Further, evolutionary rate estimates can also be 49 used to assess the mode and strength of natural selection across various subdivisions of the 50 phenotype, and thus enabling such insights into extinct species for which molecular data is unavailable<sup>20-22</sup>. 51

52 Despite these technical advances and new empirical implementations, important 53 theoretical and practical differences in estimating evolutionary rates have historically remained 54 uninvestigated. Recently, however, these have captured broader scientific interest, such as a 55 suggested pervasive relationship between evolutionary rates and chronological branches lengths in evolutionary trees (i.e. time-trees), potentially biasing rate estimates<sup>2,23</sup>, but which was 56 subsequently demonstrated to be the result of mathematical<sup>24,25</sup> or taxon sampling artifacts<sup>26</sup>. 57 58 From both a theoretical and practical perspective, another key aspect (but which has seldomly 59 been explored) is whether different approaches to infer evolutionary rates produce comparable 60 results and how they perform under different empirical conditions. If competing approaches do 61 not produce comparable results, in which specific way do they differ from each other in terms of performance and usefulness to test different kinds of hypotheses? 62

The two main approaches of evolutionary rate inference for phenotypic data are
phylodynamic methods (sensu Stadler *et al.* <sup>4</sup>) and phylogenetic comparative methods (PCM).
Phylodynamic rate inference uses complex mechanistic models, including diversification and
clock models, to jointly estimate phylogenetic trees and many evolutionary parameters, such as
rates of phenotypic and/or molecular evolution, speciation, extinction, among others. PCM
approaches, on the other hand, assume a (or a set of) fixed tree topology and map trait evolution

69 under a stochastic model, most commonly Brownian Motion<sup>8</sup>. Furthermore, phylodynamic 70 approaches almost always take as input discrete data (e.g., as morphological characters, 71 nucleotides, amino acids), whereas PCM can utilize both datatypes, although most studies have 72 used continuous data, such as body mass or multivariate traits (e.g., obtained from geometric 73 morphometrics—GMM). These approaches have been well-described in the evolutionary literature<sup>4,7</sup>, and applied to several study systems over the past decade (e.g., <sup>3,12,14,15,27-31</sup>), with 74 75 important conclusions regarding their macroevolutionary trajectories, such as the timing and 76 processes behind the origin of phenotypic novelties and innovations in fishes, early reptiles, 77 squamates, non-avian dinosaurs, birds, and placental mammals <sup>3,9-15,32</sup>.

78 Here, we apply phylodynamic and PCM methods for estimating the rate of phenotypic 79 evolution, test their robustness, and impact on interpretations regarding the tempo, mode of 80 selection, and patterns of phenotypic novelty and innovation for the largest group of terrestrial 81 vertebrates on Earth today—squamates (lizards and snakes). Squamates have been the recent 82 focus of attention in using phenotypic rates to identify major evolutionary novelties and innovations, using both phylodynamics and PCM methods <sup>3,9,10,12,33</sup>. These studies have 83 84 produced radically different conclusions on their rates of evolution and inferred patterns of 85 phenotypic change, making them the perfect study system to address the questions put forward herein. We start by substantially expanding a total-evidence phylogenetic dataset<sup>3,34-38</sup> of 86 87 squamates and their closest lepidosaurian relatives (i.e., 60% taxonomic sampling increase, and 88 21% increase in morphological discrete characters). This dataset was used to produce a new 89 time-calibrated tree of squamates and their kin, including ample sampling of both living and 90 fossil species, that was used to infer phylodynamic rates of evolution. We complemented this by 91 also collecting geometric morphometric (GMM) data on the same species—in fact, most of the 92 data obtained from the same specimens. The latter was used for inferring evolution rates using 93 the only two PCM methods that implement branch-by-branch evolution rate inference (thus 94 comparable to phylodynamic inference) using multivariate data (BayesTraits<sup>39</sup> and RRphylo<sup>40</sup>). 95 To our knowledge, this is the first time that rates of evolution based on phylodynamics and 96 GMM data are directly compared to each other while including the fossil record. 97 Our results reveal a major discrepancy between clock-based phylodynamic and PCM rate

98 inferences. Many of those differences are dependent on data type (i.e. discrete anatomical
99 characters vs. continuous shape variables), with each data type providing answers to

100 ontologically different aspects of phenotypic evolution. Moreover, we find that the methods

101 tested here vary greatly in robustness to fossil sampling, with the phylodynamic approach being

102 more consistent than PCM methods. Further, BayesTraits was the least robust and with much

103 greater disparity of rate estimates than either clocks or RRphylo, for all clades analyzed

separately or together and regardless of fossil sampling effort. We conclude by proposing a

105 conceptual complementarity between rate estimates using different data types and guidelines on

106 how downstream conclusions can be obtained from each of them.

107

### 108 **RESULTS**

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### 110 Total evidence time-tree of early lepidosaurs and squamates

111 The total-evidence dating (TED) phylodynamic analyses using a single morphological 112 and a single molecular partition produced topological results and divergence times (Fig. 1a, 113 Suppl. Fig. S1) that are broadly congruent with previous phylogenomic and TED studies<sup>3,38,41</sup>. 114 Among the contending areas of discordance between previous phylogenomic and TED studies, 115 and which are of greater relevance to broader squamate systematics, we find Dibamidae as the 116 sister group to Unidentata—as in<sup>42,43</sup>—rather than at the earliest crown squamate clade<sup>44</sup> or as a sister to gekkotans<sup>45</sup>. We also find snakes as the earliest diverging toxicoferan clade along with 117 118 Mosasauria, which has been a trend in several recent TED analyses, even when using highly distinct morphological data sets<sup>3,38,41,46,47</sup>. 119

120 Among the placement of important fossil taxa, we highlight the recovery of the fossil 121 taxa Palaeagama, Taytalura, Sophineta, and Fraxinisaura as stem lepidosaurs and great 122 uncertainty in the relationships among the stem fossil squamates Bellairsia, Oculudentavis, and 123 Huhuecuetzpalli. The latter, instead of being recovered as stem squamates as in recent 124 studies<sup>41,48</sup>, are inferred herein as early diverging taxa within crown squamates—forming a sister 125 clade to gekkotans (although with very low support). We find great uncertainty surrounding the 126 internal relationships within early diverging mosasaurians, but we recover a monophyletic 127 Dolichosauridae (inclusive of the once-proposed "four-legged snake" *Tetrapodophis*, supporting recent findings<sup>49</sup>) and a strongly supported clade formed by *Aigialosaurus* and mosasauroids. 128 129 Contrary to all previous squamate trees inclusive of fossil taxa, we find most iguanians from the 130 Late Cretaceous of Mongolia (except for *Saichangurvel*) as sister taxa to acrodontans, instead of

their traditionally placement as part of an early pleurodontan radiation (e.g.,<sup>50,51</sup>), This is driven by many (and previously overlooked) similarities between these (specially *Ctenomastax*) and acrodontans regarding their mode of tooth attachment (see Suppl. Fig. S2).

134 Divergence time estimates are broadly consistent with previous TED and phylogenomic 135 results. This is true for the time of origin for total group Squamata—252.5 Ma herein, and 250.3 136 Ma in Simões *et al.*<sup>3</sup>—and for crown group Squamata—214.6 Ma herein and in the most recent 137 phylogenomic time-tree by Title et al.<sup>9</sup> at 213.2 Ma (Norian, Late Triassic). Both results also push back the crown age relative to most other previous estimates, which were between 186 and 138 206 Ma<sup>3,45,52,53</sup>. Agreement with recent results is also found for Unidentata—194 Ma herein, and 139 140 between 189.5 to 203.7 Ma (latest Triassic to Early Jurassic,) in most previous TED and phylogenomic studies<sup>3,45,46,52</sup> (except for 176 Ma in <sup>46</sup>). Toxicofera is found to have originated at 141 142 182.6 Ma herein and between 170 to 184.6 Ma (Toarcian-Aalenian; Early-Middle Jurassic) in previous studies<sup>3,45,46,52,53</sup>. These results demonstrate an increasing consensus on age estimates 143 144 for the deepest nodes on the squamate tree of life, despite using radically different datasets and 145 dating methods. Notably, these results are also consistent across different iterations of this same 146 dataset, despite changes in taxonomic sampling and placement of some fossils, thus providing 147 empirical support to recent theoretical work suggesting that uncertainty in fossil placement does 148 not significantly impact the accuracy of divergence time estimates<sup>54</sup>.

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#### 150 Morphospace occupation and the impact of fossil sub-sampling

151 Using GMM data from the dorsal skull surface, we tested changes in morphospace 152 occupation for each clade while systematically reducing the total number of fossil taxa in the 153 dataset (from 24.5%, to 14%, then to 0%). The results (Fig. 1b-d, Suppl. Fig. S3) indicate that, 154 for all PC comparisons, reduction in fossil sampling creates two main effects. The first, as 155 expected, is that fossil removal generates the disappearance of regions of the morphospace that 156 are exclusively occupied by extinct clades—e.g., upper right quadrant in Fig. 1b is occupied by 157 fossil sphenodontians and stem lepidosaurs only. We considered this to be a Type II bias in 158 morphospace representation-a false indication of unoccupied areas of the morphospace that are 159 in fact occupied.

Second, the edges of the morphospace occupied by crown squamate families are
frequently delimited by fossils taxa—e.g., polyglyphanodontians for Lacertoidea; stem fossil

snakes for early snakes ("Haenophidia") (Fig.1b). Therefore, iterative fossil removal contracts 162 163 crown clade morphospaces (Figs. 1b-d, Suppl. Fig. S3). This can be explained by the fact that 164 early fossil members of a clade should present a suit of plesiomorphic and derived phenotypes, 165 which in practice, represent transitional body plans between crown clades. This pattern is most 166 likely not exclusive to squamates and might represent a generalizable property of low fossil 167 sampling that should also be expected for other groups. Importantly, however, we find that the 168 relative positions of crown clade morphospaces are almost unaffected even by complete removal 169 of fossils (Figs 1b-d, Suppl. Fig. S3). This indicates that even studies focusing on extant taxonomic sampling for squamates, or with low fossil sampling (e.g., <sup>9,12</sup>), are still able to 170 171 provide an accurate depiction of relative morphospace occupation of their main respective sub-172 clades.

173

### 174 Clock rates across clades and morphological partitions

175 Our TED phylodynamic inference applying multiple morphological clocks for all 176 sampled species and across morphological partitions of the squamate phenotype revealed an 177 interesting mosaic of rates of change across body regions (Fig. 2a-d). This approach enables a 178 more detailed assessment of the mosaic of rate patterns across the phenotype than inferring rates 179 for the phenotype as a whole, such as a single "global morphological clock" (Suppl. Fig. S4). For 180 instance, phenotypic rates are slower on mandibles, dentition and postcranial characters relative 181 to skull surface, palate and braincase (Fig. 2e). Additionally, the fast rates of evolution detected 182 in the earliest branches leading up to early snakes and scolecophidians (blind-snakes) using a 183 global morphological clock (Suppl. Fig. S4) are detected here as driven by fast rates of change 184 across many body subdivisions, but proportionately less by mandibular and dentition characters 185 (Fig. 2c). In amphisbaenians (worm-lizards), we see a global pattern of accelerated rates early in 186 their evolution, which partitioned clocks revealed to be mostly driven by high rates of change in 187 the palate and braincase, and postcranial partitions, with proportionately much slower rates in 188 skull surface, or in their mandible and dentition. Faster rates of evolution in the mandible and 189 dentition occur later in amphisbaenians, during the origin of the "acrodont-like" dentition of 190 trogonophids (Fig. 2c). A final example comes from dibamids, which do not have particularly 191 accelerated phenotypic rates in most body regions (Fig. 2a,b,d), also reflected in the global 192 morphological clock (Suppl. Fig. S4), but have fast rates of change in the palate and braincase

193 (Fig. 2b).

194

#### 195 Congruence and conflicts between data types and methods

We compared phenotypic rates of change inferred from phylodynamic approaches with
those recovered from phylogenetic comparative methods (PCM) on our GMM dataset—using
BayesTraits<sup>39</sup> and RRphylo<sup>40</sup>—two widely implemented approaches in macroevolution over the
last decade<sup>12,31,39,55,56</sup>. Our results indicate a drastically different pattern of rate inferences across
these different methods and data types that, to our knowledge, have never been previously
detected (Figs. 3-5, Suppl. Fig. S5-26).

202 Overall, clock rates using discrete data from the skull surface result in comparatively 203 slower rates of change relative to PCM approaches with geometric morphometric data (Fig. 3a-204 f). Besides the difference in rate magnitude, there is also no linear relationship on rate estimates 205 for each node between estimates obtained from clock rates and PCM methods (Fig. 5a,b, Suppl. 206 Fig. S25a,b,d,e). Even among the two PCM methods tested here, some of the rate patterns can be 207 somewhat different from each other (Fig. 3c.e), with only a weak linear relationship between 208 their results (Fig. 5c, Suppl. Fig. S25c,f). These differences thus impact rate-based inferences for 209 their mode of selection (Fig. 3g-i).

210 More specifically, we find congruence between clock and both PCM estimates only in the 211 snake family Elapidae (Fig. 3g-i, branch 5), all indicating significantly accelerated rates on this 212 branch and strong evidence of directional selection in dorsal skull surface characters and shape. 213 Contrasting results between clock and PCM rates (but still congruent among PCM methods) can 214 be found in the stem of Afrophidia, stem of Scolecophidia, early pleurodontan branches, and 215 early gekkotan branches (Fig. 3 a,c,e, g-i, branches 3, 4, 8, 9). The stem of Afrophidia undergoes 216 strong rate acceleration based on discrete data and clock rates, characteristic of directional 217 selection (Fig. 3g), whereas the same branch undergoes substantially decelerating rates measured 218 from geometric morphometrics and PCM rate inference, characteristic of stabilizing selection 219 (Fig. 3h-i). A similar rate acceleration happens at the stem of Scolecophidia under clock rates 220 (Fig. 3g), but which is nonsignificant under GMM/PCM rates (Fig. 3h-i). Finally, clock rates do 221 not find significant rate changes in early pleurodontan and early gekkotan branches (Fig. 3g), but 222 these are found to undergo significant deceleration under GMM/PCM rates (Fig. 3h-i). 223 Congruence between results from clock rates and RRphylo only, but different from

224 BayesTraits, can be found in Dibamidae, and the stem teiioid fossil Dalinghosaurus (Fig. 3 g-i,

branches 10, 11). Finally, we find many instances of contrasting results among all methods

employed, such as in the earliest snake branch, the stem fossil snakes (*Najash* and *Dinilysia*),

227 early Neoanguimorpha branches, early acrodontan branches, and several gymnophthalmid

branches (Fig. 3 g-i, branches 1, 2, 6, 7, and 12). These are differences that may represent a

229 conflation of differences in both data type and method performance.

230

### 231 Robustness of rate methods to fossil sub-sampling

In order to assess which factor is driving the inconsistencies in rate inference across methods, we tested the impact of fossil sub-sampling, as performed above for its impact on morphospace (see Methods for details). Although we cannot test for accuracy, which can only be achieved using simulated datasets where the true answer is known a priori—e.g.,<sup>57,58</sup>, it can provide an estimate of method robustness to variations in tree size and proportion of fossil inclusion.

238 Our results indicate that clock rate inferences were the most robust approach to fossil 239 sub-sampling (which also led to changes in total tree size), with similar rate profiles across 240 sampling categories for all morphological partitions (Fig. 4a, Suppl. Fig. S23). Among 241 GMM/PCM methods, using both standard and phylogenetically corrected PCs, RRphylo is 242 somewhat robust to fossil subsampling and tree size (Fig. 4c, Suppl. Fig. S24c,d). In contrast, 243 BayesTraits shows radically different results across different sub-sampling categories (Fig. 4b, 244 Suppl. Fig. S24a,b), suggesting it is quite dependent on fossil sampling and tree size. This much 245 greater variation in results reported by BayesTraits relative to RRphylo and clock rates can also 246 be detected when comparing the overall range of rate values inferred by each method pooled 247 across all clades through different sub-sampling categories (Fig. 5d, Suppl. Fig. S26a,c); this also 248 revealed the presence of strong outliers, especially when sampling is reduced to 0% of fossils 249 (Fig. 5d). The same is observed when comparing each method's output across individual clades 250 and pooled across all taxon sub-sampling categories (Fig. 5e, Suppl. Fig. S26b,d). Finally, these 251 patterns are also observed when plotting rates across all individual tree branches for each 252 category of fossil sub-sampling (Supplementary Figs. S5-S22).

253

## 254 **DISCUSSION**

We find here a remarkable consistency of phenotypic clock rates inferred across different levels of fossil sampling for multiple subdivisions of the phenotype, and with clock rates consistently more robust than rates of evolution based on phylogenetic comparative methods (PCM). This supports recent simulation-based studies that have revealed a higher accuracy of clock models to infer molecular evolutionary rates compared to alternative approaches in molecular evolution<sup>59</sup> (note that PCM methods were not tested in the simulation study, as these are typically only applied to phenotypic data).

263 Among PCM approaches, RRphylo is somewhat consistent across subsampling strategies 264 whereas Bayes Traits demonstrates substantial volatility of rate inference patterns depending on 265 the proportion of fossil sampling and tree size. Despite such differences between PCM 266 approaches, we still find important areas of agreement between both that make their results more 267 similar to each other than they are to phylodynamic rate inference (Fig. 5). These include at least 268 five important clades (Fig. 3g-i, branches 3, 4, 8, 9), besides an overall similar pattern of rate 269 differences among clades—e.g., despite differences in magnitude, overall mean clade rates 270 follow a similar pattern among clades for PCM methods compared to clock rates (Fig. 5e). 271 Collectively, these findings suggest a strong influence on results due to the nature of the data 272 types used by each approach (discrete data by phylodynamics vs GMM data by PCM), despite 273 several differences in inference procedure and robustness among PCM methods. Our results are 274 in agreement with other studies that have shown how inferring evolutionary mode (e.g., 275 Brownian vs Ornstein-Uhlenbeck models) can be strongly impacted by the proportion of fossil inclusion<sup>60,61</sup> and data type (discrete and continuous traits)<sup>62</sup>. 276

277 We propose that such discrepancy in phenotypic rates estimated from different datatypes 278 should not be seen as a limitation of available methodologies, but rather as expected as they 279 reflect the distinct ontological nature of each data type and the biological information conveyed 280 by them. For instance, phylogenetic morphological datasets typically include discrete features 281 (i.e., characters) that represent the gain or loss of important anatomical structures or their sub-282 components (e.g., neomorphisms). They may also capture variation that can be directly or 283 indirectly linked to shape (e.g., characters related to certain structures becoming wider or 284 narrower), color, ecology, among others. For technical reasons, however, the artificial 285 discretization of continuous variation—such as shape data—can introduce important logical

biases in morphological phylogenetics <sup>63</sup>, and recent guidelines suggest that morphological 286 287 datasets should treat continuous variation as such and only categorical features should be coded as discrete characters<sup>63,64</sup>. Hence, morphological datasets following this premise (including ours 288 289 used herein—see Star+Methods), can be useful to explore rates associated with (mostly) discrete 290 (e.g., neomorphic) character changes. Such changes are linked to the concept of evolutionary 291 novelties in the phenotype—i.e., the origin of new, individuated and quasi-independent phenotypic characters, rather than variations upon preexisting characters<sup>16-18</sup>. Geometric 292 293 morphometric data on the other hand are, by definition and design, used to quantify continuous 294 variation in shape rather than gains or losses of discrete anatomical structures. These changes in 295 shape can be interpreted as phenotypic innovations (sensu <sup>16-18</sup>)—i.e., the refinement of pre-296 existing structures to better integrate novel aspects of the phenotype into new ecological contexts<sup>16-18</sup>. 297

298 Embracing this distinction allows us to reconcile the apparently highly discrepant 299 patterns of phenotypic rates of evolution detected here. For instance, an acceleration on the rate 300 of phenotypic novelties associated with the origin of total group Serpentes and Scolecophidia 301 (Fig. 3a,g, branches 1 and 3) is mostly driven by the loss of several skull and limb elements, 302 besides major gains or losses in subcomponents of skull in these branches—see further details in these morphological changes in<sup>34,65,66</sup>. In terms of shape changes, however, these are not 303 304 significantly different from background rates of evolution. Instead, substantial shape changes 305 associated with rate shifts happen elsewhere, such as in the skull of early fossil snakes (Fig. 3e,i, 306 branch 2). This shows a pattern of accelerated phenotypic refinement in fossil snakes on top of 307 the main (discrete) changes that defined the snake body plan at their origin.

Interestingly, both clock and PCM approaches find a strong mosaic of evolutionary patterns across all snakes, with both strongly accelerating and decelerating rates. This is in stark contrast with recent findings suggesting a "macroevolutionary singularity" of snakes, as a reference to their inferred sustained high rates of evolution across all snakes<sup>9</sup>. It is possible that such difference in results between this and previous studies<sup>9</sup> can be explained by methodological differences. Unfortunately, we could not test for this as the previous study used a new rate statistic<sup>9</sup> that has yet to be implemented in a software package.

315 In another major squamate group, Scincoidea (with > 2,000 extant species) there are not 316 many substantial discrete changes (i.e., no substantial phenotypic novelties, Fig. 3a,g), but we 317 detect several independent instances of evolutionary innovation of their skull (Fig. 3e,i). This 318 conclusion is supported by a recent study also finding substantial evolutionary elaboration in this 319 clade<sup>10</sup>. Furthermore, in Dibamidae, a mysteriously long branch of limbless and fossorial 320 squamates, both clock and RRphylo estimate accelerated rates of evolution, thus suggesting 321 substantial phenotypic novelties and innovation occurring jointly in the evolution of this lineage 322 (note that this pattern is contradicted by BayesTraits results, but as illustrated above, this method 323 is less robust to fossil sub-sampling, which might be biasing estimates for dibamids, for which 324 there are no fossils currently known). Finally, in amphisbaenians, there are major discrete 325 changes in their early evolution associated with gains and (mostly) losses of skull elements, as in 326 dibamids and early snakes. However, both PCM methods indicate no substantial shift in skull 327 shape rates in the group, suggesting evolutionary innovation occurred rather gradually within this 328 group compared to the more drastic (early-on) rate shifts detected in dibamids and many snake 329 lineages.

330 In conclusion, we suggest that fundamental differences in data type are expected to 331 generate discrepant evolutionary patterns (such as phenotypic rates), which can be further 332 exacerbated by the nature and accuracy of the methodologies employed. However, many of such 333 discrepancies may actually capture important differences in biological information carried by 334 distinct data types. Whereas discrete character rates captures variation that is compatible with 335 phenotypic novelties, shape changes provide estimates of refinement (or elaboration) leading to phenotypic innovation—see also<sup>19</sup> for a recent and more restrictive definition of phenotypic 336 337 elaboration and innovation, defined by the direction of shape change in morphospace. This 338 important (but previously overlooked) conceptual distinction enables a better understanding of 339 the differences observed in evolutionary rate patterns detected here, and which we predict to be 340 common across other study systems outside of squamates. Hence, it raises the necessity for 341 phenotypic rate studies to be self-aware regarding the conclusions that can be drawn with the 342 data at hand, and whether their results produce patterns that are more compatible with 343 phenotypic novelties or innovation.

344

#### 345 **RESOURCE AVAILABILITY**

- 346
- 347 Lead contact

348	Requests for further information and resources should be directed to and will be fulfilled by the
349	lead contact, Tiago R. Simões (simoes@princeton.edu).
350	
351	Materials availability
352	This study did not generate new unique reagents.
353	
354	Data and code availability.
355	• All data, scripts and command blocks are available online as Supplementary Data at
356	NNNNNNN
357	• Updated functions for the R package <i>BTprocessR</i> is also available at
358	https://github.com/tiago-simoes/BTprocessR2 and for R package EvoPhylo v.0.3.3 <sup>20</sup>
359	available at <u>https://github.com/tiago-simoes/EvoPhylo</u> .
360	
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373	
374	DECLARATION OF INTERESTS
375	
376	The authors declare no competing interests.
377	

# 378 DECLARATION OF GENERATIVE AI AND AI-ASSISTED TECHNOLOGIES IN THE

## 379 WRITING PROCESS

- 380
- 381 During the preparation of this work, the authors used ChatGPT to assist on the creation of R
- 382 code.
- 383

## 384 SUPPLEMENTAL INFORMATION

385 Supplemental information can be found online at XXX.

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## **KEY RESOURCES TABLE**

<b>REAGENT or RESOURCE</b>	SOURCE	IDENTIFIER					
Biological samples							
Specimen list with metadata:	this study (online); Supplementary	https://dataverse.harvard.edu/api/ac					
morphological and molecular	Tables S1-S7	cess/datafile/10838345					
Deposited data	1						
Supplementary Tables with PCA	this study (online); Supplementary	https://dataverse.harvard.edu/api/ac					
results	Tables S8-S37	cess/datafile/10838345					
Supplementary Tables with	this study (online); Supplementary	https://dataverse.harvard.edu/api/ac					
summary statistics results	Tables S38-S44	cess/datafile/10838345					
Supplementary Figures	this study (online); Supplementary	Supplementary Information					
	Information						
Output files of phylodynamic and	this study (online)						
PCM analyses		https://dataverse.harvard.edu/api/ac					
		cess/datafile/10843419					
Software and algorithms							
R v. 4.2.1	R Core Team	https://www.r-project.org/					
<i>R</i> package <i>geomorph</i> v. $4.0.8 \frac{83}{2}$	CRAN	https://cran.r-project.org/					
<i>R</i> package <i>phytools v. 2.3-0</i> $\frac{85}{2}$	CRAN	https://cran.r-project.org/					
R package <i>RRphylo</i> v. 2.8.1 <sup>48</sup> .	CRAN	https://cran.r-project.org/					
R package BTprocessR2	github	https://github.com/tiago-					
		simoes/BTprocessR2					
R package <i>EvoPhylo</i> v.0.3.3 <sup>20</sup>	github	https://github.com/tiago-					
		simoes/EvoPhylo					
BayesTraits v. 4.1.1 47	BayesTraits website	https://www.evolution.reading.ac.u					
		k/BayesTraitsV4.1.3/BayesTraitsV					
		<u>4.1.3.html</u>					
Mr, Bayes 3.2.7* (*developer's	github	https://github.com/NBISweden/Mr					
version) <sup>55,73</sup>		Bayes					
3D Slicer v. 5.2.2 <sup>72</sup>	3D Slicer image computing	https://www.slicer.org/					
	platform						

### **EXPERIMENTAL MODEL AND STUDY PARTICIPANT DETAILS**

669

#### 670 Morphological phylogenetic data.

671 Morphological data consists of a considerable expansion of the diapsid-lepidosaur dataset of 672 Simões *et al.* <sup>38</sup>, which was later expanded especially in number of taxa (up to 145 species) by multiple studies—e.g., <sup>3,34-37</sup>. Most recently, this dataset was reconfigured as a lepidosaur-only 673 dataset and with increased sample of stem squamates <sup>41</sup>, totaling 101 (95 lepidosaurs and 6 non-674 lepidosaurian outgroups). The present morphological dataset was built by first using this last 675 676 iteration <sup>41</sup> as a starting point for a substantial increase in the sampling of both characters and 677 taxa across extant and fossil squamates with the goal of building a squamate focused dataset. 678 Specifically, we added 63 additional squamates (both fossil and extant), totaling 164 species: 95 679 extant squamates, 48 fossil squamates, 12 sphenodontians (including the single extant 680 Sphenodon punctatus), and nine stem lepidosaurs and non-lepidosaurian reptiles—sampled taxa 681 and accession numbers for morphological data are provided in Supplementary Table S1. 682 We used a relatively large number of non-squamatan species (21 taxa) to break the exceptionally 683 long (240myr) branch between the only living outgroup (Sphenodon punctatus) and squamates. 684 Substantial revisions of characters used in this dataset and applicable across lepidosaurs were performed by Brownstein et al.<sup>41</sup>, totaling 325 characters therein. Here, we expanded the 685 686 sampling of characters that are variable across squamates given the expanded taxonomic 687 sampling here by adding 69 characters, totaling 394 characters scored for all 164 taxa. This 688 followed character construction guidelines, such as utilization of contingent coding schemes and 689 homology assessment to avoid logical and biological biases in character construction, or artificial 690 splitting of continuous traits <sup>58,63</sup>. Importantly, here we provide 180 detailed character illustrations for easy reproducibility of character scoring for this dataset. 691

692

#### 693 Molecular phylogenetic data.

694 Molecular data for total evidence dating (TED) analyses and relaxed clock inference must

695 necessarily consist of a small number of molecular loci due to the exceptionally demanding

696 computing requirements of such inferences. Here, we focused on molecular loci that yield a

697 species tree consistent with much larger phylogenomic datasets—e.g., <sup>30-32,39</sup>—but matching our

698 morphological taxon sample and also small enough for TED.

As a result, we sampled 11 genetic markers (eight nDNA, two mDNA, and one rRNA) for all 95
extant taxa obtained from GenBank (Supplementary Data)— sampled taxa and accession
numbers for molecular data are provided in Supplementary Table S2. The sampling was
performed to match the morphological data to the species level as much as possible, which was

achieved in most cases. In a few instances where species did not match the morphological data, a

congeneric taxon was used.

Sequences were aligned in MAFFT 7.490<sup>67</sup> online server using the global alignment 705 706 strategy with iterative refinement and consistency scores (G-INS-i). For the protein-coding 707 genes, MAFFT alignments were further verified by translating nucleotide sequences to amino 708 acids and visually inspecting and trimming regions of poor alignment with Geneious Prime (v. 709 2023.2.1). The final multiple sequence alignment was concatenated for phylogenetic inference, but both concatenated and individual locus alignments are provided as supplementary 710 711 information. Molecular sequences from all extant taxa were analyzed for the best partitioning 712 scheme and model of evolution using the PartitionFinder algorithm as implemented in IO-TREE 713 <sup>68</sup> under Akaike information criterion (AIC).

The molecular tree, despite much smaller than existing phylogenomic trees based on various marker types—e.g.,<sup>9,43-45</sup>—, recovers the same overall topology and relationship among major squamate clades as the latter (Supplementary Fig. S28). The only three exceptions are the placement of the homalopsid *Hypsicopus* with the dipsadid *Diadophis*, the gekkonid *Gehyra* within phyllodactylids, and *Gonatodes* not forming a clade with other sphaerodactylids. For these three cases, in the subsequent total evidence analyses we used a topological constraint fixing their placements following the results of Burbrink *et al.* <sup>45</sup> based on AHEs.

721

#### 722 Morphological shape data.

There have been few previous studies using high dimensional shape data from geometric morphometrics (GMM) to understand macroevolutionary and macroecological aspects across all major groups of squamates<sup>12,33,69,70</sup>. This includes one study <sup>12</sup> that focused on obtaining 3D data (with several hundred landmarks) on the cranium which provides more shape variables and thus a finer scale resolution of evolutionary changes. However, 3D data imposes a strong limit in the availability of fossil species that can be assessed as fossil vertebrates are rarely preserved in three dimensions and relatively uninformed. This limited the 3D GMM study to a nearly all extant dataset (174 extant and seven fossil species). On the other hand, 2D GMM limits the total

number of variables and phenotypic dimensions, but it enables a much larger taxonomic

sampling for fossil species, which is especially relevant when addressing deep time

733 macroevolutionary questions. This larger taxonomic sampling thus provides a denser sampling of

morphological diversity within and across squamate families, besides better capturing shape

variation across important evolutionary transitions by directly including fossil specimens within

those transitions.

737 The most extensive study on skull shape evolution across all major groups of squamates 738 using 2D GMM to date <sup>70</sup> included data from 20 homologous landmarks from published 739 photographs, hand drawings, and firsthand obtained photographs and CT scans, culminating in 740 skull samples for 279 extant and 23 fossil species. Despite the large sampling of extant and fossil species using 2D data in Da Silva *et al.*<sup>70</sup> (total = 302 taxa), only 193 were available in their 741 742 combined evidence phylogenetic tree used to correct for the phylogenetic signal for statistical 743 analyses when including both extant and fossil data <sup>47</sup>. Also, all landmarks were obtained in 744 lateral view of the skull as in a previous study of skull shape change across lizard families <sup>69</sup>. 745 However, there is a substantially larger amount of fossil squamates and other lepidosaurs better 746 (or exclusively) preserved in dorsal view (see Supplementary Table S4) and the symmetric 747 nature of the skull bones in dorsal view makes it easier to detect taphonomic distortions, and 748 retro-deform skulls in some instances. Finally, all previous studies have focused on sampling 749 data from within squamates, only sampling a single outgroup species (the modern tuatara, 750 Sphenodon punctatus), from the sister lineage to squamates—sphenodontians—which diverged 751 from the squamate branch at  $\sim 260$  million years ago<sup>3,52</sup>.

In order to maximize sampling of fossil species for geometric morphometric (GMM) analyses, we opted for the collection of 2D landmark data, since the vast majority of squamate fossils are not preserved in three-dimensional articulation, and those that have 3D preservation, most do not have CT scan data openly available for 3D landmarking. Therefore, 2D landmarking maximizes the collection of observational data points, despite being limited by the number of variables compared to 3D GMM approaches.

To assess the best candidate cranial region and aspect of cranial morphology for 2D geometric morphometrics, we conducted a survey of 88 fossil lepidosaur species (including 6 non-lepidosaurian outgroups used for all analyses) represented by 272 specimens 761 (Supplementary Table S4). Our results indicate that the skull in dorsal view is the most 762 commonly preserved aspect (dorsal = 75 occurrences, lateral = 48, ventral = 45), and that the 763 mandible is far more frequently observed in lateral view than medial view (73 and 51 764 occurrences, respectively). Our personal evaluation also indicated that specimens preserved 765 exclusively in lateral view were frequently more distorted than those preserved only in dorsal 766 view. Therefore, despite previous attempts to quantify squamate skull shape in lateral view using 767 2D GMM <sup>70</sup>, we opted here for a new landmark data collection focusing on dorsal view only for 768 maximizing sample size and minimizing distortion.

769 After discarding all duplicates, species not included in the phylogeny (due to phylogenetic 770 instability), and only keeping specimens for which all landmarks could be confidently placed, we 771 obtained a final fossil sampling of 30 fossil lepidosaur species (Suppl. Table S3). These were 772 subsequently removed to test for the impact of reduced fossil sampling on inferences of 773 morphological disparity and rates of evolution. Taxon removal for GMM and shape-based rates 774 of evolution was homogeneous across the phylogeny (e.g., one species removed by family), 775 rather than random, in order to reproduce the sampling strategy of most researchers (i.e., 776 maximizing diversity of clade representation). This resulted into four categories of taxonomic

inclusion: 24.5%, 14%, and 0% of sampled taxa as fossils (Suppl. Table S5).

We identified 35 homologous landmarks and 102 semilandmarks (totaling 137 points; see
Suppl. Fig. S27 and Supplementary Table S6). Landmarks were partitioned into premaxilla (4
landmarks), nasals (5), prefrontals (4), frontals (7), parietal (5), supraoccipital (three),

basioccipital (one), quadrates (one), and ectopterygoids (4). They comprise 26 type I landmarks

and 9 type II landmarks *sensu* Bookstein <sup>71</sup>. Semilandmarks were placed on the outline of the

anterior margin of the premaxilla (14 semilandmarks), around the internal margin of the orbital

fossa (22 on each side), and along the lateral margin of the parietal—in snakes, it followed the
sagittal crest, when it was pronounced (22 on each side).

The ectopterygoid landmarks and semilandmarks in the orbital and supratemporal fossae were included to accommodate the absence of the jugal bar in snakes and amphisbaenians, enabling a unified analysis with non-ophidian squamates. Previous studies excluded landmarks in the jugal region for snakes and created a snake subsample in the dataset <sup>12,70</sup>. Here, we chose to use jugal landmarks and only include landmarks comparable across all squamates without subsampling for specific clades for better among clade comparability. Fossil specimens with poorly preserved or asymmetric regions were corrected using side reflection. For all other

- specimens, we followed the recommendation of places landmarks on both sides of the skull to
- take into account the potential impact of skull asymmetry <sup>72</sup>. Landmarks and semilandmarks
- were digitized with tpsDig2 v.2.32 and subsampled with tpsUtil v.1.83<sup>73</sup>, with semilandmarks
- spaced equally along curves.

CT scans of living squamates were obtained from MorphoSource and digitally segmented
with 3D Slicer v.5.2.2<sup>74</sup> (e.g., to remove osteoderms and soft tissue) and exported in dorsal view
using orthographic projection for parallax correction. These were complemented by high
resolution photographs of living and extinct squamates in dorsal view, all collected by the same
individual (TRS) (Supplementary Table S3).

802

## 803 METHOD DETAILS

804

#### 805 Bayesian phylogenetic inference.

806 Bayesian analysis of the morphological data set was performed using Mr. Bayes developers

807 version (future Mr, Bayes 3.2.8) compiled from source code (available at

808 <u>https://github.com/NBISweden/MrBayes</u>)<sup>75,76</sup> using the Della HPC cluster at Princeton

809 University. The software choice was decided based on the diversity of relaxed clock models

810 available (see further information below) and ability to run analyses on a feasible amount of

811 time. Specifically, the alternative software with a wide range of available clock models,

- 812 RevBayes<sup>77</sup>, would take an order of magnitude longer than Mr. Bayes to run the same analyses
- 813 (lasting weeks instead of days).

814 The molecular component of the combined evidence dataset was analyzed under the GTR 815 + gamma model and subdivided into four partitions (see above for partitioning and model 816 testing). For the morphological data, we used the Mkv + gamma substitution model  $^{78}$  (Mk with 817 ascertainment bias correction). The molecular only dataset was run for 30 million generations, 818 under 4 independent runs with 4 chains each, temperature = 0.007, 25% burn-in, and sample 819 frequency at every 1,000 generations. The total-evidence analyses (using morphological and 820 molecular partitions) used similar parameters but ran over 70 mi generations. Stationarity was assessed using standard measures, such as average standard deviation of 821

split frequencies (ASDSF  $\leq 0.05$ ) and potential scale reduction factors (PSRF  $\approx 1$  for all

823 parameters). Effective sample size (ESS) values were assessed using Tracer v.1.6<sup>79</sup>, reaching

824 >200 for all parameters. Our reported summary trees were calculated with standard output tree

825 procedures available in MrBayes: the majority rule consensus tree (MRC) and the maximum

826 compatible tree (MCT).

827

#### 828 Phylodynamic relaxed clock Bayesian macroevolutionary analyses.

829 We implemented total-evidence-dating using the fossilized birth-death tree model (FBD), under relaxed clock models in MrBayes <sup>75,76</sup>. Sampling strategy among extant taxa was set to 830 831 "diversity", which is more appropriate when extant taxa are sampled in a way to maximize diversity (as performed herein) and fossils are assumed to be sampled randomly <sup>76</sup>. Given the 832 833 chronological gap between most species and phylogenetic distance between most taxa— as 834 typical for most total evidence studies of highly diverse groups spending thousands of species-835 we used a no sampled ancestor model (rho = 1) where all fossils are considered to be tips only, and which can avoid overestimates of divergence times for morphological clocks <sup>28</sup>. 836

837 Importantly, for our focal analyses we implemented the Skyline FBD model (SFBD), 838 which enables a piecewise constant inference of speciation, extinction, and fossil sampling parameters, which are allowed to vary across time bins <sup>80</sup>. This provides more biologically 839 840 realistic parameterization of the diversification processes and has been demonstrated to yield more reliable divergence time estimates using empirical data <sup>28,76</sup>. We implemented SFBD with a 841 842 flat prior (uniform distribution: samples  $\in U[0,1]$ ) on the parameters of relative extinction (= 843 turnover) and probability of sampling fossils, whereas the net diversification rate was sampled 844 from an exponential distribution with mean = 1.0.

845 All FBD parameters were allowed to shift in the skyline model at four time frames, 846 creating five distinct time bins for parameter sampling, which are large enough to include 847 sufficient lineages to accurately inform FBD parameters and also matching critical events in the 848 history of squamates: i) the Jurassic-Cretaceous boundary (145 Ma), when a shift is typically 849 observed in the fossil record of lepidosaurs, with the drastic decrease in diversity of 850 sphenodontians and an increase in the diversity of squamates <sup>28,81</sup>; ii) the Early-Late Cretaceous 851 boundary (100.5 Ma), which marks the disappearance of several early squamates and the much 852 higher diversity of crown group squamates observed in the Late Cretaceous <sup>81,82</sup>; iii) the 853 Cretaceous-Paleogene boundary (66Ma), which marks the end Cretaceous mass extinction,

allowing us to account for potential shift in speciation and extinction rates of squamates after that event; iv) the Paleogene-Neogene boundary (23Ma), after which modern genera become abundant in the fossil record of squamates <sup>52,81</sup> and potentially correlates with the exponential increase in the number of squamate lineages in the Cenozoic <sup>82</sup>, thus accounting for a potential shift of this relatively recent diversification history.

The age of the root (node representing the MRCA of  $\dagger$  *Youngina* and crown reptiles) was sampled from an offset exponential distribution with a hard bound for the minimum age (based on the minimum age for  $\dagger$  *Youngina*, at 255 Ma) and a soft maximum age, with the mean of the exponential distribution based on a recent TED analysis for this node (280Ma). This provides a relatively low but nonzero probability for sampling ages older than set the maximum age for the root.

865 The vast majority of our calibrations were based on tip-dating, which accounts for the 866 uncertainty in the placement of fossil taxa and avoids the issue of constraining priors on taxon relationships when implementing bound estimates for node-based age calibrations<sup>75</sup>. The range 867 868 of the stratigraphic occurrence of the fossils used for tip-dating here were used to inform the 869 uniform prior distributions on the age of those same fossil tips, which avoids biases that can be introduced by point age calibrations on the age of the fossils <sup>83</sup>, by using a uniform prior 870 871 distribution on the age range of the stratigraphic occurrence of the fossils (Supplementary Table 872 S7). Complementary to that, in clades for which we lacked some of the oldest known fossils in 873 our analysis and for which there is overwhelming support in the literature (and in all our other 874 analyses), we employed node age calibrations with a soft minimum age. The single clade node 875 calibration for that is Serpentes: based on *†Eophis underwoodi* (Bathonian, Middle Jurassic— UK)  $\rightarrow$  168.3-166.1 MYA (166.1,168.3), as in previous studies<sup>3,38,41</sup>. 876

We assessed the fit of various clock models to our data, including a new suit of clock models available in the developer's version of Mr. Bayes, which was compiled from source code (available at <u>https://github.com/NBISweden/MrBayes</u>). These models include the continuous autocorrelated clock model (TK02) and three uncorrelated clock models: the white noise model (former IGR model up to version 3.2.7a of Mr. Bayes) <sup>84</sup>, and the new independent gamma rate (IGR) and independent lognormal clock (ILN) models <sup>84</sup>. These models represent radically different interpretations of how and where in the tree evolutionary rates are allowed to change across lineages, which can substantially impact divergence time estimates using morphological
 and/or molecular data <sup>28,84</sup>.

886 We tested model fit using the stepping-stone sampling strategy to assess the marginal model likelihoods<sup>85</sup> and calculated Bayes Factors (BF)—30 steps (+5 as burn in) for 100 million 887 888 generations. Due to convergence issues for the computationally heavy stepping-stone strategy, 889 we also compared marginal log likelihoods inferred during empirical analyses reported as 890 harmonic means. Using the significance thresholds of Kass and Raftery <sup>86</sup>, we found a strong 891 support for the ILN clock model relative to all other models (Table 1), with the autocorrelated 892 TK02 model having by far the weakest support (BF>400) and also with one or multiple 893 independent runs not reaching convergency. Our results thus focused on the output from ILN 894 clocks.

895

- 896 **Table 1.** Results of clock and tree model fit using marginal log likelihoods for Bayes Factor
- 897 comparisons. All BF values are reported relative to the best fitting models within each

Clock Model	Tree Model	Free Parameters	ASDSF	lnL (HM)	BF (HM)	lnL (SS)	BF (SS)
ILN	FBD	25	0.014897	-157162.5	0	-150738.7	0
ILN	SFBD	37	0.01336	-157140.8	0	na	na
WN	FBD	25	0.013349	-157231.7	-69.2	-158251.6	-7512.85
WN	SFBD	37	0.014644	-157226.4	-85.61	na	na
IGR	FBD	25	0.015578	-157211.5	-68.14	-152463.9	-1725.16
IGR	SFBD	37	0.030888	-157482.3	-255.92	na	na
TK02	FBD	25	0.055625	-157612.3	-468.91	-158486.7	-7747.93
TK02	SFBD	37	0.074106	-157638.1	-411.69	na	na

comparable category defined by the total number of free parameters.

- 899 Abbreviations: BF, Bayes Factor; HM, harmonic means; LnL, marginal ln-likelihood; SS,
- 900 stepping-stones.

903 The starting value for the prior on the clock rate was given an informative prior as per 904 previous non-clock analysis—the median value for tree height in substitutions from posterior 905 trees divided by the age of the tree based on the median of the distribution for the root prior<sup>3,28</sup> 906 (104.45/267.5= 0.3904). The mean of the lognormal distribution was given the value based on 907 the non-clock tree estimate in natural log scale: ln(0.3904) = -0.9404. Finally, we chose a broad 908 standard deviation around the mean ( $\sigma = 1.0$ ).

909 To account for mosaic evolution across the phenotype and to be able to directly compare 910 rates of phenotypic evolution in the skull using phylogenetic and geometric morphometric 911 inference, we partitioned morphological phylogenetic characters following an anatomy-based 912 partitioning scheme. Specifically, we created four partitions, the first one closely matching the 913 same elements (dermal elements of the skull surface) landmarked for GMM, and for which 914 evolutionary rates were extracted for direct comparison with GMM-based rate inference: skull 915 surface dermal bones (characters 1-113, 393, 394), skull palatal bones and braincase (characters 916 114-208); mandibles and dentition (characters 209-275); postcranium (characters 277-392). We 917 did not further subdivide these categories in order to keep a minimum number of characters that 918 are capable of informing branch lengths. Further, the postcranial partition could not be further 919 subdivided (e.g., axial skeleton and limbs) due to the near-complete absence of appendicular 920 skeleton across limb reduced squamates (most notably, snakes), which represent a substantial 921 portion of the data.

922 The prior on the variance of clock rates (informing individual branch rates) was then 923 unlinked between all molecular and morphological partitions, enabling the inference of branch 924 specific rates for each partition. As this is a heavily parameterized analysis, we maximized 925 convergence and sampling of parameters for clock rates by conducting a two-step procedure. 926 First, we performed a completely unconstrained Bayesian evolutionary inference using the best 927 fit models indicated above (e.g., ILN clock and skyline FBD) with only two clock partitions (one 928 morphological and one molecular) for 70 million generations. Secondly, the resulting tree 929 topology from the first step was used to fix the topology of subsequent multi-clock analyses, 930 with all molecular and morphological partitions unlinked, as described above, for another 70 931 million generations. This ensured a large effective sample size and convergence of all parameters 932 despite the large number of tips and complexity of the models implemented.

#### **QUANTIFICATION AND STATISTICAL ANALYSIS** 934 935 936 Geometric morphometric analyses. 937 For each taxon sampling category, we performed separate Generalized Procrustes Analysis 938 (GPA) on the landmark data using the 'gpagen' function in the R package geomorph v. 4.0.8<sup>87</sup>. 939 Principal component analysis (PCA) and phylogenetically corrected PCA (pPCA) were 940 conducted using the 'gm.prcomp' function in geomorph. The pPCA utilized generalized least-941 squares for series ordination to center and to estimate the covariance matrix, with residuals 942 projected onto an orthogonal projection. To access the phylogenetic signal among Procrustes 943 shape variables, we used the 'physignal' and 'physignal.z' functions in geomorph, with the last 944 estimating effect size using the "front" method for lambda <sup>88</sup>. Morphospace and 945 phylomorphospace projections (based on the first three pPCs) were performed using the R package *phytools* v. 2.3-0<sup>89</sup> with the 'phylomorphospace' and 'contMap' functions. 946 947 948 Skull shape evolutionary rates. 949 Prior studies have used phylogenetically-corrected principal components (pPCs) for subsequent evolutionary mode or rate inference <sup>12,31,90</sup>, or standard PCA <sup>91,92</sup>, or both <sup>15,93</sup>. Here we have 950 951 done both. We used the standard principal components (PCs) representing 95% of variance in 952 skull shape data (38, 41, and 44 highest ranking PCs) and the phylogenetically corrected 953 principal components (pPCs) representing 95% of non-phylogenetic residual variance of skull 954 shape data (40, 43 and 45 highest ranking pPCs) to calculate rates of phenotype evolution. All 955 inferences used the MCT tree obtained from relaxed clock Bayesian inference (the same used 956 preferred clock rates of evolution) the PCs/pPC residuals were used as inputs for shape rate estimates using BayesTraits v. 4.1.1<sup>39</sup> and the R package *RRphylo* v. 2.8.1<sup>40</sup>. 957 958 For BayesTraits, we used the variable rates model of evolution, which assumes a 959 Brownian motion model of rate change across the tree while also allowing for rate shifts across branches, with the number and location of rate shift being inferred with reversible jump 960 MCMC<sup>56</sup>. It also performs branch transformations to detect the overall mode of trait evolution, 961

- 962 using parameters delta (e.g., early burst vs late mode of rate of acceleration), kappa (punctuated
- 963 mode with rates concentrated on speciation events), and lambda (where rates better fit the

phylogenetic structure of the input tree). For this dataset, we used 200 million generations,
sampling at every 20,000 generations and a burn-in of 25% (50M generations), using 2
independent runs.

Parameters values across independent runs were assessed using Tracer v.1.6<sup>79</sup>, which 967 indicated stationarity and convergence across runs, with an effective sample size (ESS) values 968 969 reaching >200 for all parameters. Summary statistics and mapping of rates across the tree were 970 conducted using a modified version of functions formally available in the discontinued R 971 package *BTprocessR* — we updated these functions and made them all available again in 972 GitHub: https://github.com/tiago-simoes/BTprocessR2. We used the function 'rjpp' to 973 postprocess the posterior parameter values and posterior trees and generate summary statistics 974 for all posterior parameters. This was followed by mapping inferred mean rate changes across the MCT tree using the ggtree R package 94. 975 976 Skull shape evolution rates were also assessed with the *RRphylo* R package, using yhe 977 function RRphylo0, which uses phylogenetic ridge regression to infer ancestral states for each

978 internal node and calculate rates of evolution. It provides a complementary approach to

979 BayesTraits to test for evolutionary rates taking into account multivariate data types and non-

980 ultrametric trees <sup>40</sup>. Differently from BayesTraits and clock rates, this is a deterministic

approach, and multiple input trees are recommended to account for phylogenetic uncertainty.

However, for purposes of comparability across methods, we used the same input time calibratedtree as used for BayesTraits and clock rate inferences.

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## 987 Figures and Captions



989

Fig. 1. New total evidence dating time-tree of squamates (and other lepidosaurs) and impact
of fossil sampling in morphospace patterns. A, times inferred from relaxed clock phylodynamic
inference for all morphological characters ("global clock") using full dataset (164 species). Node
violin plots indicate 95% HPD divergence times. Values on nodes indicate mean divergence
times (top, in bold), and posterior probabilities (bottom). B, morphospace using 122 species (all
extants + 30 fossils; 24.5% of fossil sampling) based on PC 1 vs PC2 and skull shape plots indicate
direction of skull shape change along PC axes. C, morphospace using 106 species (all extants + 15

- 997 fossils; 14% of fossil sampling) based on PC 1 vs PC2. **D**, morphospace using 92 species (all extants + 0
- 998 fossils; 0% of fossil sampling) based on PC 1 vs PC2. Some regions of the morphospace are occupied
- almost exclusively by completely extinct lineages (e.g., upper right by fossil sphenodontians). Further,
- 1000 morphospace limits for some crown squamate families are represented by fossils (e.g.,
- 1001 polyglyphanodontians among lacertoids, in yellow; stem fossil snakes among early snakes
- 1002 ("Haenophidia"), in cyan). Iterative fossil removal contracts crown clade morphospaces, although the
- 1003 relative positions and overlap are mostly unchanged. For additional results depicting the same changes
- across PC1 vs PC3 and PC2 vs PC3, see Suppl. Fig. S3.
- 1005







- 1016 characters relative to skull surface, palate and braincase. For rates values for all partitions combined
- 1017 (global clock rates), see Suppl. Fig. S4, and with fossil subsampling, see Suppl. Fig. S5-7.



- 1019
- 1020

Fig. 3. Evolutionary rates estimate comparison for skull surface data across inference methods. A,
 relaxed clock phylodynamic inference using discrete characters. B, histogram of clock rates by clade. C,
 BayesTraits rates using geometric morphometric (shape) data based on phyloPCs representing 95% of
 total variation. D, histogram of BayesTraits rates by clade. E, RRphylo rates using geometric

- 1025 morphometric (shape) data based on phyloPCs representing 95% of total variation. **F**, histogram of
- 1026 RRphylo rates by clade. G, selection mode inferred from clock rates. H, selection mode inferred from
- 1027 BayesTraits rates. I, selection mode inferred from RRphylo rates. Node numbers in g-i represent the
- 1028 following focus branches: 1, earliest snake branch; 2, early fossil snakes; 3, stem of Scolecophidia; 4,
- 1029 stem of Afrophidia; 5, Elapidae; 6, stem of Neoanguimorpha; 7, stem of Acrodonta; 8, early Pleurodonta;
- 1030 9, early Gekkota; 10, Dibamidae; 11, Dalinghosaurus; 12, Gymnophtalmidae. All rates mapped on the
- same time-calibrated evolutionary tree of sample size = 122 species (30 fossils; 24.5% fossil sampling).
- 1032 Rate values inferred from GMM data are on average higher than using discrete character data, despite
- 1033 substantial differences in the pattern of rate distributions among branches (see also Fig. 4). For additional

1034 rates mapped on trees across different sample sizes, and using both phyloPCs and standard PCs, see

1035 Supplementary Figs. S8-S22.



1040 Fig. 4. Rate distributions by clade across methods and fossil sampling efforts. A, histogram of clock 1041 rates by clade. **B**, histogram of BayesTraits rates by clade. **C**, histogram of RRphylo rates by clade. Top 1042 row represents full taxon sampling matching GMM data set (122 taxa, 24.5% being fossils), middle row 1043 represents taxon sampling matching GMM data set with 50% of fossils removed (106 taxa, 14% being 1044 fossils), and bottom row represents taxon sampling matching GMM data set with all fossils removed (92 1045 taxa, 0% being fossils). For clock rate distributions for each partition and fossil subsampling category, see 1046 Suppl. Fig. S23. For PCM rate distributions for each method contrasting standard and phylogenetically 1047 corrected PCs, see Suppl. Fig. S24. 1048



1051 Fig. 5. Comparison of rate inferences across methods and fossil sampling efforts. A, linear

1052 regressions between clock and BayesTraits normalized rates. B, linear regressions between clock and

1053 RRphylo normalized rates. C, linear regressions between BayesTraits and RRphylo normalized rates. D,

1054 violin plot of normalized rate distributions by method and three fossil sampling strategies (pooled across

1055 all clades). E, box plots of normalized rate distributions for each major clade (pooled across all fossil 1056 sampling strategies). There is no detectable correlation on a node-by-node comparison between clock

1057 rates and rates using phylogenetic comparative methods (PCMs). However, there is some (although week)

1058 correspondence between the two PCM approaches using GMM data (BayesTraits and RRphylo in c) with

1059 disparity of rate values using BayesTraits being much higher than either clocks or RRphylo, for all clades

1060 analyzed separately or together and regardless of fossil sampling effort (in **D** and **E**). All PCM rates here

- used phyloPCs (see Suppl. Fig. S25 and S27 for similar results using standard PCs.) 1061
- 1062
- 1063
- 1064