# 1 "A history of the world imperfectly kept": Will we ever know how biodiversity has2 changed over deep time?

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# 14 Abstract

15 The fossil record is our only direct source of evidence for how life on Earth has waxed and 16 waned over its long history. However, the fossil record is also incomplete and biased in many 17 ways, after passing through biological, geological, and socio-economic filters. This means that 18 we only possess snapshots of information, relating to specific places and times in Earth history, 19 from which to try and understand large-scale biodiversity patterns. Over the last fifty years, a 20 wide variety of methods have been developed to try and elucidate macroevolutionary patterns 21 by accounting for fossil record structure or bias, with varying levels of success. Here we review 22 the different approaches that have previously been applied to this problem, and discuss their 23 strengths and weaknesses. We illustrate this by applying a selection of these methods to the 24 global brachiopod fossil record of the Permian and Triassic. Finally, we highlight some avenues 25 for future improvement, including (1) using simulations to investigate method efficacy, (2) 26 designing studies around testable hypotheses, (3) embracing uncertainty, and (4) improving the 27 integration of data from fossil and modern organisms. Although we cannot know exactly how 28 biodiversity has changed over life's history, it is clear that new innovations in computational 29 palaeontology are helping us to improve the trustworthiness of our estimates of biodiversity

30 through deep time.

### 31 The fossil record and its biases

32 Fossils, defined as biological presence, activity or signatures preserved in the rock record, are 33 our sole direct source of evidence for how life existed in the geological past, with the fossil 34 record comprising our knowledge of fossil data collectively. We know that these data are 35 incomplete - the vast majority of organisms ever to have lived did not enter the fossil record 36 (e.g. Marshall 2017; Žliobaitė & Fortelius 2022). Charles Darwin, when discussing the fossil 37 record in On the Origin of Species by Means of Natural Selection, wrote "I look at the natural 38 geological record as a history of the world imperfectly kept" (1859). 39 Among the many processes serving as filters to fossilisation, many are selective or 40 systematic, meaning that the resulting fossil record is biased in favour of some organisms above 41 others (Shaw et al. 2020). To what extent the nature of the fossil record is perceived as 42 "structured" or "biased" depends on how well we understand these filtering processes, and how 43 systematic we consider them to be (Smith 2007; Holland 2017). Regardless, it is clear that 44 preservation in the fossil record is uneven, and this manifests in almost any possible analysis 45 we might want to conduct using it (Kidwell & Holland 2002). For example, fossilisation potential 46 is highly variable between palaeoenvironments, with some broadly unrepresented (e.g. Shaw et 47 al. 2020). The soft parts of animals tend not to preserve (Shaw et al. 2020), except in 48 Lagerstätten, meaning our perception of largely soft-bodied and/or fragile animals is highly 49 skewed towards windows of exceptional preservation (Dean et al. 2016; Walker et al. 2020). 50 Bias in the distribution of fossil-bearing rocks across time and space limits our potential to find 51 fossils (Raup 1972; Smith & McGowan 2007; Wall et al. 2009). A wide range of socio-economic 52 factors also determine where fossils are found, kept and studied, leading to major inequalities in 53 data collection worldwide (Raja et al. 2022; Dunne et al. 2025). 54 As such, it is difficult to quantify diversity in the fossil record, especially to make 'fair'

55 comparisons across space and time, or between clades (e.g. Dunne 2018; Dillon et al. 2023; 56 Hammer & Harper 2024). A wide range of methods have been developed and applied over the 57 last 50 years which attempt to do this. With the emergence of conservation paleobiology (Dillon 58 et al. 2022; Pimiento and Antonelli 2022; Kiessling et al. 2023), and the increasing application of 59 the fossil record to make informed predictions about current and future extinction risk (Harnik et 60 al. 2012; Raja et al. 2021; Finnegan et al. 2024), there is particularly strong motivation to 61 scrutinise our methods for estimating extinction rates in the past. Here, we briefly recap the 62 main schools of thought behind methods for estimating palaeodiversity, demonstrate how some 63 of these methods can be applied, and suggest future directions for our efforts to quantify 64 biodiversity from the fossil record.

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### 66

### 67 Inferring biodiversity in deep time

68 In this paper, we use the terms "diversity" and "richness" to describe the number of discrete

69 taxonomic units present within the biological system of interest (usually globally). Approaches to

estimating palaeodiversity aim to take into account the fact that we know our fossil sampling to

51 be incomplete (e.g. Hunt & Slater 2016). They can be placed into two categories, distinguished

by the key metrics(s) they aim to infer: (1) diversity estimators, which seek to infer true or

- 73 relative diversity through time, and (2) rate estimators, which seek to infer changes in
- 74 diversification rates, origination (or specifically speciation, when data resolution allows) and

extinction, through time or across lineages (see Table 1). This major distinction determines thetypes of hypotheses which these different approaches can be used to test.

77 Typically, the raw data used to infer biodiversity in deep time are lists of fossil 78 occurrences, denoting the presence of specific taxa in a particular place, at a particular point in 79 geological time. Often, these data are sourced from large community databases, such as the 80 Paleobiology Database (Uhen et al. 2023), Geobiodiversity Database (Fan et al. 2013) or 81 Neotoma (Williams et al. 2018). The quality of such data can be suboptimal, and it is important 82 to verify that the data are as correct and clean as possible prior to subsequent analyses (Jones 83 et al. 2025). Even after data cleaning, the accuracy and precision of taxonomic, spatial and 84 temporal information can be highly variable (e.g. Hopkins et al. 2018; Buffan et al. 2023) (but 85 note model-based efforts to increase temporal data resolution, such as CONOP [Sadler & 86 Cooper, 2008; Fan et al. 2020] and HORSE [Chu et al. 2025]). Alternatively, phylogenies can be 87 inferred in conjunction with evolutionary rates, or be used as a template from which to estimate 88 past diversity (e.g. Wright et al. 2022; Mulvey et al. 2025). The occurrence birth-death model 89 combines both phylogenetic and occurrence data to infer taxonomic richness trajectories 90 (Andréoletti et al. 2022).

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91 Below, we discuss the philosophy behind each of the main "families" of metrics, as well 92 as the criticisms that have been levelled against them.

94 Range-through analysis

95 One of the most apparent ways in which fossil occurrence lists are incomplete is the presence of "gaps" in taxon stratigraphic ranges, sometimes called "ghost ranges", due to the fact that the 96 97 rock record is not continuous across space and time. A simple way to account for gaps in 98 species ranges is to "range-through" taxon occurrences between their first and last appearance 99 in the fossil record (Sepkoski et al. 2002; Sepkoski 1984). This method is based on the 100 fundamental evolutionary assumption that a taxon is highly unlikely to have originated twice and 101 thus must have been extant during each interval between its first and last occurrence, even if it 102 is not sampled in all of those time bins. Although ranged-through richness accounts for gaps in 103 ranges, it does not assess the extent to which first and last occurrences deviate from the true 104 origination or extinction times, which may well be considerably older or younger than is 105 preserved in the fossil record (Signor & Lipps 1982; Holland & Patzkowsky 2002) (although see 106 methods for estimating confidence intervals on first and last occurrences, e.g. Marshall 1990, 107 1997; Wang et al. 2012). Because the metric relies on a cohesive taxonomic (species) concept, 108 taxonomic uncertainty and violations of this taxonomic concept (for example, cryptic species) 109 can lead to errors. It is also vulnerable to the pull of the recent (Raup 1972, 1979), and is 110 inappropriate for use on regional or local data sets, as it cannot account for regional extinction. 111 112 Fair sampling

- 113 One of the first trains of thought concerning the impact of fossil record bias on estimates of
- 114 biodiversity relates to "fairness". If we want to make comparisons of taxonomic diversity across
- space, time or clades, we ideally want to be making estimates based on equivalent samples
- 116 from each of our groups of interest. The first step in this direction was a simple one: perhaps an
- equal number of fossils could be sampled from each time bin, with the number of taxa
- 118 represented by those fossils illustrating the relative diversity through time. This approach, first

implemented using the fossil record by Raup (1975), is now known as "classical rarefaction",

although the term "subsampling" is also commonly used to refer to methods that purposefully

121 use less than the total available data. Given that the fossil record is already sparse, the

- discarding of data when using these methods has been a major source of criticism in their use.
- 123 The opposite approach, extrapolation, has also been implemented, with the idea being that
- statistical models can be used to estimate biodiversity by extrapolating from low to higher
- sampling levels, such as by Dodson (1990) and Russell (1995). Here, criticism rests on the fact
- that extrapolation beyond what we know from data is heavily reliant on the correctness of the assumptions of the model and data used, which can be difficult to evaluate.
- 128 While rarefaction and extrapolation remain a viable approach for estimating past 129 diversity, ways of determining "fair" samples have become more sophisticated. In particular, 130 coverage-based approaches use more robust quantifications of sampling effort to determine 131 equivalent fossil subsamples between which to compare species diversity (Wang & Dodson 132 2006). Shareholder quorum subsampling (Alroy 2010) uses this approach, with Hill numbers 133 (Hill 1973) used to evaluate when equivalent levels of sampling effort (or "guorum levels") have 134 been sampled from each temporal or spatial bin (see Roswell et al. 2021 for a neontological 135 review on this topic). Hill numbers are calculated using species abundance distributions, and 136 therefore this approach utilises the abundance of each taxon, not just its presence. In the R 137 package iNEXT (Chao & Jost 2012; Hsieh et al. 2016), coverage-based subsampling and 138 extrapolation can both be used to estimate species diversity at a range of quorum levels. 139 Although an improvement on simple equal subsamples, coverage-based approaches interpret 140 the abundance of common versus rare species in taxon samples, and are therefore reliant on a 141 fairly standardised curve relating abundances to diversity when estimating sampling effort. As a 142 result, this approach may perform poorly if the true community possessed a relative abundance 143 distribution which differed from that assumed by the model, or if sampling filters have 144 substantially skewed relative abundance distributions, both of which are difficult to evaluate 145 (Close et al. 2018).
- 146
- 147 Cohort analysis

148 Some of the most popular methods for estimating origination and extinction rates in deep time 149 are those which rely on cohort analysis. First developed by Raup (1978), cohort analysis 150 considers fossil occurrences within a series of discrete time bins. Any changes in taxonomic 151 lists between adjacent time bins are used to determine taxon gains or losses across the bin 152 boundary, and deemed to be indicative of speciation and extinction events. The approach has 153 particular appeal because it fits well with the natural temporal structure of fossil data: often 154 occurrences are dated to a named geological interval, rather than a specific numerical age, and 155 these data are therefore suited to cohort analysis without the need for additional refinement of 156 fossil ages. A series of metrics have been developed based on these approaches, including the 157 boundary-crosser (Alroy 1996; Foote 1999), three-timer (Alroy 2008), gap-filler (Alroy 2014) and 158 second-for-third (Alroy 2015) metrics. Over time, these metrics have been developed to quantify 159 ghost ranges in increasingly sophisticated ways, and use this information to estimate (and 160 correct for) incomplete fossil sampling; however, these developments have also resulted in the 161 discarding of increasing amounts of occurrence data (Warnock et al. 2020). Regardless, there is 162 large appeal in these methods because they are somewhat intuitive, and because they are

relatively easy to implement, particularly since their inclusion in the R package *divDyn* (Kocsis et al. 2019).

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### 166 Residual modelling using sampling proxies

167 Difficulties in determining how to implement "fair" subsampling methods led to the concept that 168 additional data could be used to quantify differences in sampling intensity between time bins. A 169 methodology was proposed by Smith and McGowan (2007), and refined by Lloyd (2012), to use 170 a sampling proxy, i.e. an indirect measure of sampling effort, to "correct" raw palaeodiversity 171 curves using a regression model-fitting approach. In this method, the sampling proxy is used to 172 identify times of relatively poor and good sampling, and a regression model is fitted to determine 173 how well the sampling signal predicts the biodiversity curve. The residuals of the regression 174 model indicate periods of time where the model does not perfectly predict biodiversity (hence 175 the name "residual modelling"), and can be used to highlight time periods that are more diverse 176 or less diverse than would be expected given the level of sampling for that time interval (Smith & 177 McGowan 2007; Lloyd 2012). Residual modelling does not require large amounts of occurrence 178 data, has therefore been particularly popular in vertebrate palaeontology, for exploring the 179 impact of sampling bias on raw diversity curves (e.g. Barrett et al. 2009; Benson et al. 2010;

180 Butler et al. 2012).

181 The most commonly used sampling proxies have focused on geological biases, such as 182 rock outcrop area (Smith & McGowan 2007; Dunhill et al. 2012, 2013, 2014a). However, it is 183 unclear whether the close correlation between the amounts of rock preserved and palaeodiversity through time (Raup 1972; Na et al. 2023; Ye & Peters 2023) result from 184 185 geological megabias or "common cause", whereby Earth system changes drive trends in both 186 the rock and fossil records simultaneously (Peters 2005; Hannisdal & Peters 2011). The number 187 of fossiliferous formations has also been a popular proxy (Barrett et al. 2009; Benson et al. 188 2010; Butler et al. 2012), and has been claimed capture aspects of rock volume, facies 189 heterogeneity, geographical and temporal dispersion, and research effort (Benson & Upchurch 190 2013). Despite this, many studies have been critical of the use of formation counts in residual 191 modelling, particularly when only considering formations that bear the fossil group in question, 192 due to inherent redundancy between formation counts and the biodiversity signal which it seeks 193 to correct (Crampton et al. 2003; Benton et al. 2011; Dunhill et al. 2014b; Benton 2015; Dunhill 194 et al. 2018). It has been demonstrated that "correcting" palaeodiversity curves using residual 195 modelling based on formation counts can lead to richness estimates that are further from the 196 truth than the raw fossil record (Brocklehurst 2015; Dunhill et al. 2018). Residual modelling also 197 performs poorly when both low diversity and poor sampling occur simultaneously, such as after 198 a mass extinction event.

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### 200 Mechanistic model-based approaches

201 Mechanistic models aim to describe the processes which generated our fossil data, using model

202 parameters that have a tangible biological or geological interpretation, such as rates of

sampling, origination, and extinction (e.g. Warnock et al. 2020). Each process is defined based

- 204 on expectations, also known as assumptions, of how it behaves. Model performance therefore
- hinges on (1) whether all of the important processes have been included in the model, and (2)

whether the processes have been modelled in a way which adequately represents how theywork.

208 The most straightforward mechanistic modelling approach is to model the fossil sampling 209 process only, without making any assumptions about the evolutionary processes. For example, 210 TRIPS (True Richness estimated using Poison Sampling) models sampling using a Poisson 211 process (Starrfelt & Liow 2016). Per-interval sampling rates are quantified from fossil 212 occurrence data, then transformed into per-interval probabilities, to extrapolate an estimate of 213 true richness. A major advantage of modelling the sampling process explicitly is that very sparse 214 sampling, including singletons, can be an expected outcome of the process, meaning fossil 215 occurrence data does not have to be subsampled a priori.

216 More complex models include the demographic or diversification processes, in addition 217 to sampling. Capture-mark-recapture (CMR) models are a class of models largely used by 218 ecologists to estimate population size dynamics from incomplete samples of contemporary 219 populations (Nichols & Pollock 1983; Liow & Nichols 2010). CMR has been adapted for use in 220 paleobiology, and although not yet widely applied, there have been several model extensions 221 relevant to fossil data, such as allowing for variation in sampling across time, space and 222 lineages (Liow & Nichols 2010; Laake 2013). In contrast, the widely used program PyRate 223 implements a range of birth-death process models (Silvestro et al. 2014; Silvestro et al. 2019). 224 Birth-death models have a long history in paleobiology (e.g. Raup 1985; Huelsenbeck & Wagner 225 1996; Foote 2000) and provide an intuitive approach for modelling branching processes 226 resulting from origination and extinction events. These can also be combined with a model 227 describing how the evolutionary process has been sampled. In PyRate, origination, extinction 228 and fossil sampling are considered independent Poisson processes, with parameter values 229 estimated from fossil occurrence data. PyRate also includes model variants that allow for 230 different combinations of rate variation. Both CMR and PyRate allow users to test explicitly 231 whether there has been a change in diversification rates across interval boundaries, making it 232 easy to compare their results with those generated from simpler cohort models.

233 Birth-death processes, or closely related approximations, also underpin most recent 234 phylogenetic approaches used to infer diversification history, since phylogenetic trees directly 235 capture the inferred branching history (Wright et al. 2022; Morlon et al. 2024). Phylogenetic 236 approaches for estimating past diversity include the software BAMM, which can be used to 237 estimate lineage-specific evolutionary rates based on a fixed tree (Rabosky 2014; Mitchell et al. 238 2019), and the fossilized birth-death (FBD) process family of models (Stadler 2010; Heath et al. 239 2014), which can be applied in a wide range of simulation and inference contexts (see Mulvey et 240 al. 2025 for a review of applications). Phylodynamic models can be used to infer the tree and 241 estimate the parameters associated with the underlying tree-generating processes 242 simultaneously (e.g. Close et al. 2015, Andréoletti et al. 2022). Being able to estimate the tree 243 and divergence (origination) times also means we can quantify the extent of ghost lineages 244 more comprehensively within the same model. Different variants of birth-death process models 245 can be applied to trees with extant taxa only, trees that combine both extant and extinct taxa, or 246 trees that include extinct taxa only (see MacPhearson et al. 2022 for an overview of the theory). 247 While questions have been raised as to whether these models are fully identifiable (Louca & 248 Pennell 2020, 2021), theoretical work indicates that phylogenies containing fossils should only 249 be compatible with a single set of evolutionary rate trajectories (Truman et al. 2025). Another

class of phylodynamic models are coalescent processes, based on a model of branching history
in which lineages coalesce backwards in time, which have only recently been explored in the
context of paleobiology (Allen et al. 2024). While phylodynamic models have mainly been used
to estimate diversification rates, they can also be used to infer richness using an emerging suite
of tools (Vaughan et al. 2019; Andréoletti et al. 2022; Vaughan & Stadler 2024).

255 Model-based approaches are often straightforward to implement in a Bayesian 256 framework, allowing uncertainty to be guantified naturally during inference, and allowing us to 257 take advantage of existing (prior) knowledge (Wright et al. 2022). The use of prior parameter 258 constraints allows us to include data beyond the fossil occurrences in our models, such as 259 information about how sampling has varied through time (see section Residual modelling using 260 sampling proxies). However, these approaches tend to be more computationally expensive than 261 their non-model-based counterparts, and can be much more difficult to use (e.g. Barido-Sottani 262 et al. 2024). Any results are sensitive to the model assumptions, meaning that violation could 263 lead to false conclusions, but the importance of assumptions in mechanistic modelling means 264 they are more often explicitly stated, and can be scrutinized with more rigor using approaches 265 like model adequacy (e.g. Duchêne et al. 2019).

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### 267 Machine learning

268 Some of the newest techniques available to computational palaeobiologists use machine 269 learning. This includes text mining approaches to collate fossil occurrences (e.g. Peters et al. 270 2014, Kopperud et al. 2019), using decision trees to infer extinction drivers (e.g. Foster et al. 271 2023), and identifying and discriminating morphological features using image recognition (He et 272 al. 2024). Deep learning methods also exist for estimating species diversity in deep time. 273 DeepDive (Cooper et al. 2024a, b) simulates species-through-time curves before and after the 274 influence of incomplete sampling to emulate the fossil record, and trains a neural network to 275 understand the relationship between the two. The trained network can then be applied to real 276 fossil occurrence data, in order to infer the shape of the complete diversity curve. In contrast, 277 the birth-death neural network (BDNN; Hauffe et al. 2024) model infers trajectories of 278 speciation, extinction and fossilisation rates through time. The model uses a neural network to 279 estimate these trajectories in light of a range of time series, such as environmental or sampling 280 proxy data, providing insight into which were most influential in driving the estimated speciation 281 and extinction rates. The limitations of these approaches lie in their complexity: they can be 282 difficult to set up, and require more computational resources than the simpler metrics. Further, 283 neural networks are reliant on the simulations they are trained on; should the simulations be 284 substantially incorrect, this will also feed through into the inferred trajectories. In an attempt to 285 address this latter point, DeepDive conducts autotuning (Cooper et al. 2024b), during which the 286 parameters used in simulation are iteratively corrected in order to produce sampled diversity 287 curves more in line with the provided fossil data.

288

### 289 Understanding geographic biases

290 Temporal bias has long been considered the main facet of unevenness in the fossil record.

- However, recent debate has turned to spatial biases as a major way in which our perception of diversity in deep time is skewed (e.g. Close et al. 2020a, Jones et al. 2021, Flannery-Sutherland
- et al. 2022, Raja et al. 2022, Antell et al. 2024). This includes highlighting that supposedly

"global" analyses infer metrics using a set of sampled regions, which is unlikely to produce fair
estimates as long as sampling is incomplete (Benson et al. 2021). Russell (1995) made an early
attempt to correct for uneven geographic sampling, by estimating the amount of land area from
which dinosaur fossils had already been collected, and using this information to extrapolate to
the total number of dinosaurs which might have existed, should the whole Earth be sampled
equivalently.

300 One approach to this problem is subsampling, with equivalent numbers of fossils 301 selected from different geographic areas in order to more fairly estimate differences in 302 biodiversity across space (e.g. Close et al. 2020a, b). The R package divvy aims to make this 303 easier to implement (Antell et al. 2024). Thus far, this approach has been implemented as a 304 data treatment, with geographic subsampling performed prior to species diversity estimation 305 using one of the other described metrics. This means that temporal and spatial biases are 306 typically handled in different steps within an analytical pipeline for inferring palaeodiversity: how 307 we can consider these biases simultaneously is an important area of future research.

308 Another useful approach for understanding geographic sampling bias is occupancy 309 modelling (Foote et al. 2007; Foote 2016; Kiessling & Kocsis 2016; Dean et al. 2025). This 310 conceptual framework has been developed and applied by neontologists for decades (e.g. 311 MacKenzie et al. 2002), but is yet to be widely used in palaeontology. Within repeatedly-312 sampled geographic regions (such as multiple stratigraphic levels or localities in a grid square), 313 the model aims to differentiate between taxa missing from occurrence lists due to incomplete 314 sampling, compared to those missing due to true (biological) absence. The model outputs 315 provide an estimate of relative sampling adequacy between geographic regions. More 316 sophisticated occupancy models can also be used to determine the relative importance of 317 different drivers of sampling incompleteness, such as geological versus collection processes 318 (Dean et al. 2025). Although useful for understanding differences in fossil sampling across 319 space, there is currently no clear way to translate these insights into improved estimates of 320 palaeodiversity.

322 **Table 1.** A list of methods for inferring biodiversity metrics from the fossil record which take

323 sampling bias into account in some way. Starred citations are the first description, or

324 application, of the method specifically relating to palaeontological data.

Name	Metric type	Data needed	Citation	Description	Implementations
(Classical) Rarefaction	Diversity	Taxon occurren ces	Sanders (1968) *Raup (1975)	Uses subsampling to the size of the smallest sample to compare species richness between samples	divDyn R package (Kocsis et al. 2019)
Range-through	Diversity	Taxon occurren ces	Raup (1972)	Corrects estimates of diversity through time by filling in ghost ranges (gaps in the temporal distribution of taxa)	
Coalescent model	Diversifi cation rates	Phyloge ny (or cladistic matrix)	Kingman (1982) *Allen et al. (2024)	Uses the branching (or "coalescence") times in a phylogeny to infer the diversification rate, based on a Wright- Fisher population model of exponential growth	BEAST2 (Bouckaert et al. 2019)
Capture-mark- recapture (CMR)	Diversity Originati on/extin ction rates	Taxon occurren ces (Proxy data optional)	*Nichols & Pollock (1983)	Uses comparison of repeated samples from the same pool to infer sampling probabilities, which are used to estimate total diversity	MARK (White & Burnham 1999) RMark R package (Laake 2013)
(Simple) Extrapolation	Diversity	Taxon occurren ces Proxy data	Dodson (1990) Russell (1995)	Uses a metric of collection effort to estimate the asymptote of total diversity	
Abundance-based coverage estimator (ACE)	Diversity	Taxon occurren ces	Chao & Lee (1992) *Anderson et al. (1996) Wang & Dodson (2006)	Uses the abundance counts of rare taxa to estimate sampling coverage (completeness) and therefore the total number of taxa	

Boundary-crosser	Originati on/extin ction rates	Taxon ranges	Alroy (1996) Foote (1999, 2000)	Uses cohort analysis (Raup 1978) to count the taxa which do and do not cross temporal boundaries	divDyn R package (Kocsis et al. 2019)
Three-timer	Originati on/extin ction rates	Taxon occurren ces	Alroy (2008)	Builds on boundary- crosser by correcting based on proportion of "three-timers" (taxa that are present, absent, then present again)	divDyn R package (Kocsis et al. 2019)
Coverage-based rarefaction and extrapolation, or Shareholder quorum subsampling (SQS)	Diversity	Taxon occurren ces	Alroy (2010) Chao & Jost (2012)	Uses Hill numbers (Hill 1973) to estimate sampling completeness, or "quorum", and uses this to subsample or extrapolate to a consistent level of completeness	iNEXT R package (Hsieh et al. 2016)
Phylogenetic generalized linear mixed models	Originati on/extin ction rates	Phyloge ny (Proxy data optional)	Hadfield (2010) *Sakamoto et al. (2016)	Estimates speciation and extinction rates from the branching times and tip dates in a fixed phylogeny	MCMCglmm R package (Hadfield 2010)
Fossilised birth- death model (FBD)	Originati on/extin ction rates	Phyloge ny (or cladistic matrix)	Stadler (2010) Stadler et al. (2018) *Heath et al. (2014) Gavryushki na et al. (2014)	Estimates branching times and tip dates in a phylogeny, in concert with constant speciation and extinction rates, in a Bayesian framework	See review by Mulvey et al. (2025)
Gap-filler	Originati on/extin ction rates	Taxon occurren ces	Alroy (2014)	Builds on three-timer by allowing for longer gaps between occurrences	divDyn R package (Kocsis et al. 2019)
Fossilised birth- death model, skyline version	Originati on/extin ction rates	Phyloge ny (or cladistic matrix)	Gavryushki na et al. (2014)	Estimates branching times and tip dates in a phylogeny, in concert with piecewise-constant speciation and	See review by Mulvey et al. (2025)

	I				
				extinction rates, in a Bayesian framework	
PyRate	Originati on/extin ction rates	Taxon occurren ces (Proxy data optional)	Silvestro et al. (2014)	Uses a range of models describing speciation, extinction, and fossil sampling, that can be used to infer rates in a Bayesian framework	PyRate Python library (Silvestro et al. 2014, 2019)
Second-for-third	Originati on/extin ction rates	Taxon occurren ces	Alroy (2015)	Builds on gap-filler by quantifying specific temporal gaps separately	divDyn R package (Kocsis et al. 2019)
True Richness estimated using Poison Sampling (TRiPS)	Diversity	Taxon occurren ces	Starrfelt & Liow (2016)	Models fossil sampling using a Poisson process to extrapolate estimates of total diversity	Supplemental R code from Starrfelt & Liow (2016)
Squares	Diversity	Taxon occurren ces	Alroy (2018) *Allen et al. (2020)	Uses abundance structure within samples to determine how to extrapolate total diversity	Supplemental R code from Allen et al. (2020)
Fossilised birth- death model, treeless version	Originati on/extin ction rates	Taxon occurren ces	Stadler et al. (2018) *Warnock et al. (2020)	Estimates speciation, extinction, and fossil sampling rates, accounting for the underlying phylogenetic branching process	DPPDiv (Heath et al. 2012; Warnock et al. 2020)
Fossil Bayesian Analysis of Macroevolutionary Mixtures (BAMM)	Speciati on/Extin ction rates	Phyloge ny	Mitchell et al. (2019)	Estimates speciation and extinction rates from the branching times and tip dates in a fixed phylogeny, within a Bayesian framework	BAMM (Rabosky 2014) BAMMtools R package (Rabosky et al. 2014)
Occurrence birth- death model	Diversity Originati on/extin ction rates	Phyloge ny (or cladistic matrix) Taxon occurren ces	Andréoletti et al. (2022)	Estimates branching times and tip dates in a phylogeny, in concert with piecewise-constant speciation and extinction rates, plus a	OBD model in RevBayes (Höhna et al. 2016; Andréoletti et al. 2022)

				species richness trajectory through time, in a Bayesian framework	
DeepDive	Diversity	Taxon occurren ces	Cooper et al. (2024)	Trains a neural network on simulated data matching the real data, to infer total diversity	DeepDive Python library (Cooper et al. 2024a) DeepDiveR R package (Cooper et al. 2024b)
Birth-Death Neural Network (BDNN)	Speciati on/extin ction rates	Taxon occurren ces Proxy data	Hauffe et al. (2024)	Trains a neural network on simulated data matching the real data, alongside proxy time series, to infer speciation and extinction rates, and their drivers	PyRate Python library (Silvestro et al. 2014) Simulations in BDNNsim Python library (Hauffe et al. 2024)
Fossilised birth- death model, multi- type version	Originati on/extin ction rates	Phyloge ny (or cladistic matrix)	Barido- Sottani & Morlon (2025)	Estimates branching times and tip dates in a phylogeny, in concert with per- branch speciation and extinction rates, in a Bayesian framework	MSBD package in BEAST2 (Barido- Sottani et al. 2020a; Barido- Sottani & Morlon 2025)
Fossilised birth- death diffusion model	Diversifi cation rates	Phyloge ny	Quintero et al. (2025)	Uses data augmentation to infer viable complete trees, allowing per-branch diversification rates to be estimated, using a model where these rates evolve along the tree under a diffusion process	Tapestree Julia package (Quintero & Landis 2020; Quintero et al. 2025)

### 327 Case study: brachiopod diversity in the Permian and Triassic

- 328 Methods
- 329 To illustrate the differences between diversity estimates generated by the different metrics
- described here, we applied a range of them to the fossil record of brachiopods across the
- 331 Permian and Early/Middle Triassic. Brachiopod occurrences from this time interval identified to 332 the species level were downloaded from the Paleobiology Database (Uhen et al. 2023).
- the species level were downloaded from the Paleobiology Database (Uhen et al. 2023).
   Occurrences were placed into stage-level bins, with any dated to a coarser temporal reso
- 333 Occurrences were placed into stage-level bins, with any dated to a coarser temporal resolution 334 discarded. Collections allocated to the same stage and location (matching modern-day latitude
- and longitude to two decimal places) were pooled into a single "locality". The resulting dataset
   included 25,678 occurrences across 4,404 pooled collections, containing 4,710 species within
   948 genera.
- The different metrics were then calculated in R (R Core Team, 2024), on a per-stage basis, at both species and genus levels, using the following approaches:
- 340 1) *Raw*. A raw diversity curve was calculated by counting the number of unique taxa341 sampled within each stage bin.
- *Range-through.* The R package *palaeoverse* (Jones et al. 2023) was used to calculate
  ranged-through diversity. First, the function *tax\_range\_time()* was used to convert the
  occurrence data into stratigraphic ranges for each unique taxon. Then, the function *tax\_expand\_time()* was used to create pseudo-occurrences for each taxon within each
  stage of their temporal range. The total number of pseudo-occurrences for each stage
  was then counted.
- 3) Simple rarefaction. Simple rarefaction was conducted by calculating diversity within an
   equal number of pooled collections for each stage bin. First, the stage with the smallest
   number of collections was identified: this was the Olenekian, with 93 collections. For
   each stage bin, 93 pooled collections were sampled (without replacement), and the
   taxonomic diversity within this sample was quantified; this was repeated 100 times for
   each stage.
  - *4) Squares.* Diversity within each stage bin was estimated using the Squares extrapolator (Alroy, 2018) based on the code of Allen et al. (2020).
- 5) Coverage-based rarefaction and extrapolation. The function estimateD() in the R
  package *iNEXT* (Hsieh et al. 2016) was used to estimate diversity, at a quorum level of
  0.8, for each stage bin. Hsieh et al. (2016) recommend that extrapolated values above
  twice the observed sample size are discarded; 0.8 was the highest quorum level at
  which this was not necessary.
- *Residual modelling.* The number of geological formations included within the occurrence
   dataset for each stage was counted, for use as the sampling proxy for residual
   modelling. Code from Lloyd (2012) was then used to calculate residual diversity between
   the raw taxon curve and the number of formations through time.
- 365 For each metric (except residual modelling), the proportional change in diversity across each 366 stage boundary was also calculated.

368 Results

367

354

- 369 The different metrics produce comparable trends at the broad scale, showing roughly constant
- diversity throughout the Permian, followed by a steep drop at the end of the Permian, with some

371 limited recovery during the Middle Triassic (Figure 1). However, the timing, strength, and even 372 direction of diversity fluctuations varies considerably based on the metric chosen. All metrics 373 show a comparably-severe mass extinction at the end of the Permian (species losses of 92% 374 for raw data, 92% for range-through, 86% for rarefied, 90% for Squares, and 92% for coverage-375 based estimates; see Table 2). By contrast, the metrics vary considerably in their estimates of 376 diversity trends at the end of the Capitanian (species gains of 32% for raw data, losses of 51% 377 for range-through, gains of 1% for rarefied, gains of 2% for Squares, and losses of 25% for 378 coverage-based estimates; see Table 2). The curve produced by residual modelling also shows 379 comparable diversity loss between the Early and Middle Triassic, and across the Permian-380 Triassic boundary (Figure 1). These overall trends are observable at both species and genus 381 level (Figure 1, 2). Clapham et al. (2009) also reported that sampling standardisation of fossil 382 occurrences resulted in observing a gradual diversity decline from the Wordian to the Induan for 383 marine invertebrates, due to reduced origination rates in the Capitanian and Wuchiapingian. 384

385

386 Figure 1. Brachiopod diversity through the Permian and Triassic estimated using different 387 methods. Black (or dark grey) lines show the species-level data, while grey (or light grey) lines 388 show the genus-level data. Panels show (a) raw diversity, (b) range-through diversity, (c) 389 diversity rarefied using locality counts, with line showing median values and error envelope 390 showing full range across 100 repetitions, (d) diversity estimates using the Squares 391 extrapolator, (e) diversity estimated using coverage-based rarefaction and extrapolation, to a 392 guorum level of 0.8, with 95% confidence intervals, and (f) model-detrended diversity based on 393 the number of formations sampled through time, with error envelope showing standard 394 deviation. The geological timescale axis was added using *deeptime* (Gearty, 2024). 395

- Figure 2. Brachiopod generic diversity through the Permian and Triassic estimated usingdifferent methods. See caption for Figure 1 for panel details.
- 398







**Table 2.** Change in diversity estimates across stage boundaries, as a percentage of diversity in

402 the older stage.

Stages	Level	Raw	Range- through	Rarefied	Squares	Coverage- based
Asselian	genera	11.32	37.74	-15.38	-1.73	4.94
to Sakmarian	species	17.85	39.35	-21.21	-1.44	15.91
Sakmarian	genera	26.69	27.4	17.42	41.24	16.81
to Artinskian	species	33.03	34.41	15.1	62.22	23.9
Artinskian	genera	22.41	37.1	26.45	10.16	0.95
to Kungurian	species	49.38	109.07	52.09	25.17	5.55
Kungurian	genera	-10.93	-18.24	-1.28	-13.31	-5.31
to Roadian	species	-13.68	-37.78	4.38	-27.27	-1.95
Roadian	genera	1.23	16.07	1.29	2.48	12.28
to Wordian	species	13.62	52.43	-0.24	21.42	31.45
Wordian	genera	-19.39	3.51	-12.24	-14.25	-22.18
to Capitanian	species	-34.74	17.49	-19.33	-17.01	-34.77
Capitanian	genera	4.14	-38.32	-13.95	-5.95	-20.86
Wuchiapingian	species	31.85	-50.62	0.74	1.86	-25.18
Wuchiapingian to Changhsingian	genera	-14.8	-22.33	13.85	-18.99	8.29
	species	-19.48	-25.95	19.65	-22.6	14.23
Changhsingian	genera	-86.02	-84.58	-81.01	-84.1	-84.16
to Induan	species	-91.89	-91.78	-85.68	-90.44	-91.87
Induan	genera	-18.18	-5.41	-15.62	-2.43	-18.11
to Olenekian	species	-38.33	-36.07	-36.21	-24.28	-39.75
Olenekian	genera	251.85	182.86	153.7	176.73	216.48
to Anisian	species	508.11	479.49	240.54	458.62	477.88
Anisian	genera	-34.74	-37.37	-29.93	75.53	-26.29
to Ladinian	species	-57.78	-57.96	-45.63	44.88	-37.99

#### 405 The future of palaeobiodiversity metrics

#### 406 Utilising simulations

407 Although all of the aforementioned methods and metrics were proposed with a logical basis, a

- 408 major barrier to reliable inference of past biodiversity is that we have a poor understanding of
- 409 whether any of these methods work well, i.e. we do not know if they bring us closer to the truth
- 410 than the raw data. An increasing number of studies have attempted to compare the
- 411 performance of different biodiversity metrics (e.g. Lane et al. 2005; Warnock et al. 2017; Close
- 412 et al. 2018; Smiley, 2018; Alroy 2020), but it is clear that there is scope for much more rigorous testina.
- 413

414 While we might not know how true biodiversity changed over deep time as a marker 415 against which to test our metric performance, we can use the next best thing, which is

- 416 simulations (Barido-Sottani et al. 2020b). Simulations enable us to generate believable
- 417 biodiversity data, often using a mechanistic model describing hypothesised evolutionary
- 418 processes, that can then be compared to trends in empirical data (e.g. Saupe et al. 2019, 2020;
- 419 Dunne et al. 2023). We can also subsample this data, illustrating how the fossil record may
- 420 obscure our view (Liow et al. 2010; Dunhill et al. 2014; Brocklehurst 2015; Barido-Sottani et al.
- 421 2019). We can then apply our metrics to the simulated fossil data, and compare the inferences
- 422 to the true values used in simulation. As well as generally enabling us to quantify how correct
- 423 our metrics are, a particular advantage of this approach is that simulations can be designed to 424 emulate data from different clades or preservational systems, allowing us to investigate the
- 425 contexts in which different metrics perform better or more poorly (e.g. Allen et al. 2023). In fact,
- 426 tuning simulations to replicate specific empirical datasets, prior to or within analyses, can be a
- 427 powerful tool for exploring uncertainty (e.g. Cooper et al. 2024b; Quintero et al. 2025).
- 428

#### 429 Acknowledging and embracing uncertainty

430 Methods which provide an estimate of uncertainty around their average value should ultimately

- 431 be preferred over those which do not. Such error bars or confidence intervals are essential for
- 432 making informed interpretations concerning the reliability of our diversity estimates. All methods
- 433 that involve subsampling data can be repeated on multiple samples, producing a range of
- 434 estimates which can then be summarised. Methods that use a Bayesian approach produce
- 435 posterior distributions for each model parameter, describing the range of values obtained over 436 the course of a Markov chain Monte Carlo (MCMC) inference (Barido-Sottani et al. 2024).
- 437 Estimates of uncertainty can be interpreted in many useful ways. First, they can be used 438 to understand the range of values obtained across an analysis. A wide range might suggest a
- 439 low amount of certainty in a mean or median value, and cast doubt on the fact that this average 440 should be interpreted at face value. However, the range of values can also be viewed as a way
- 441 of excluding extremes. For example, if we assume that our model is performing well, we can
- 442 have relatively high certainty that the true diversity does not lie outside of our confidence 443 interval. Second, particularly for Bayesian analyses, we can interpret the shape of the posterior
- 444 distribution obtained for our focal parameters. Closer investigation might reveal a multimodal
- 445 distribution, in which case a mean or median might be a poor representation of the distribution
- 446 as a whole, instead placing considerable likelihood on two or more different values. Such
- 447 distributions may result from nonidentifiability, meaning that the priors and data are insufficient
- 448 to be able to determine a single best-fitting mode (e.g. Louca & Pennell 2020). In this case,

further analysis with a larger dataset and/or an alternative model may converge on a singlemode (Barido-Sottani et al. 2024).

451

### 452 Having a clear, testable hypothesis

453 Sometimes deep time diversity is investigated in a manner closer to an open question, e.g. 454 "What was the diversity of my clade through time?" Answering such a guestion requires diversity 455 estimates that are both accurate and precise, across a large number of data points, which is 456 ambitious given the sparsity of data we have available to us. However, most computational 457 analyses aim to either support or disprove a given hypothesis concerning the system which the 458 data describe (e.g. Hammer & Harper 2024), and adhering to this in the case of diversity 459 estimation is also a good idea. For example, we can investigate whether diversification was 460 positive (net speciation) or negative (net extinction) within a given interval (e.g. Allen et al. 461 2024). Although our exact estimate of the diversification rate might be inaccurate, or vary across 462 different methods, our conclusion will only be incorrect if this inaccuracy means that the point 463 crosses the zero line. Using methods which provide an estimate of uncertainty can also help us 464 to evaluate the probability with which diversification was positive or negative, including whether 465 one of these solutions is fully excluded from the posterior.

Comparison can also be a useful approach: for example, we could test whether our clade was more diverse in interval X or interval Y. Although sampling incompleteness affects the known fossil record in both intervals, any bias only becomes concerning if it substantially differs between the two time bins. If desired, we can also interpret this further, such as considering that the larger the difference between estimates for the two intervals, the more certainty we might have in which was more diverse.

472

### 473 Improving the quality and volume of data

Ultimately, having more data will give us more statistical power for estimating diversity in deep
time. Alongside simply collecting more fossils, we also need these fossils to be described and
identified, before being entered in global databases (Alroy 2003, Marshall et al. 2018). Text
mining shows promise as a method for facilitating biodiversity data collation more rapidly (e.g.
Peters et al. 2014, Kopperud et al. 2019). However, it is important that we maximise efforts to
collate data from across the world, but also that researchers in every country have access to,
and stakeholdership in, this data (Dunne et al. 2025).

481 At present, data limitations are a major influence on the methodologies used to estimate 482 palaeodiversity. For example, many studies focus on generic diversity, as such patterns are 483 perceived to be more robust in comparison with the sparser data available for individual species 484 (Hendricks et al. 2016). However, we cannot assume that generic and species-level patterns 485 are related or a proxy for one another, and this must be considered when making comparisons 486 between clades, and with present-day diversity. Further, differences in data availability 487 contribute to the preferential use of occurrence-based methods for invertebrate studies, and 488 phylogenetic methods for vertebrates (e.g. Mulvey et al. 2025). This contributes to difficulties 489 comparing studies across this divide. In future, increased volumes of vertebrate occurrence 490 data, alongside the development of more morphological matrices for invertebrates, may help to 491 close the gap.

- 492 Integration with modern data, for extant organisms, is also an area which can be further 493 developed (Dillon et al. 2023; Liow et al. 2023). The use of modern diversity estimates to 494 condition inferred diversity curves can have a large impact on richness estimates through time. 495 particularly in the recent past (e.g. Cooper et al. 2024b). Although modern and fossil occurrence 496 data have their own nuances and biases, these can be modelled separately in order to account 497 for any discrepancies: for example, in the fossilized birth-death model, Ψ describes fossil 498 sampling, while  $\rho$  describes extant sampling, allowing these two ways of observing the 499 evolutionary process to be incorporated fairly into the model (Mulvey et al. 2025). In addition, 500 modern data can prove useful as a template through which we can investigate the potential
- 501 influences of sampling bias on diversity estimates (e.g. Barr & Wood 2024, Krone et al. 2024).
- 502

## 504 Conclusions

505 In the absence of a time machine, it is difficult for us to have complete faith in our estimates of 506 biodiversity in deep time. However, a long history of methodological development has provided

- 507 us with an abundance of ideas and approaches for attempting to estimate palaeodiversity.
- 508 Choosing a metric to use depends on the hypothesis being tested, the data available, and the
- 509 computational resources available. It is not guaranteed that different metrics will agree with
- 510 each other, but we do have tools available to us to make an informed choice about which
- 511 metrics to use, and comparison between metrics should be conducted where possible.
- 512 Collecting more data, testing methods with simulations, and being careful about how to interpret
- 513 our results, can all contribute to making better inferences of palaeodiversity. The future
- 514 development of new methods may also yet provide more accurate and precise estimates. Such
- 515 approaches may allow us to address a wide range of questions in macroevolution with 516 increased confidence in our results.
- 516 Increased confidence in our rest
- 517 518

# 519 Data availability

- 520 Data and code for the presented case study are available at <u>https://github.com/bethany-j-</u> 521 <u>allen/brachiopod\_diversity/tree/main</u>.
- 522
- 523

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