Beyond sex differences in mean: meta-analysis of differences in skewness, kurtosis, and
 correlation

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34

36 Abstract

37 Biological differences between males and females are pervasive. Researchers often focus on sex 38 differences in mean or, occasionally, in variation, albeit other measures can be useful for 39 biomedical and biological research. For instance, differences in skewness (asymmetry of a 40 distribution), kurtosis (heaviness of a distribution's tails), and correlation (relationship between 41 two variables) might be crucial to improve medical diagnosis and to understand natural processes. 42 Yet, there are currently no meta-analytic ways to measure differences in these metrics between 43 two groups while accounting for sampling error. We propose three effect size statistics to fill this 44 gap: Δsk , Δku , and ΔZr , which measure differences in skewness, kurtosis, and correlation, 45 respectively. Besides presenting the rationale for the calculation of these effect size statistics, we 46 illustrate their potential using a large dataset of mice traits. For example, we found that females 47 show, on average, greater skewness and kurtosis than males in both fat mass and heart weight. 48 Although calculating Δsk , Δku , and ΔZr may require large sample sizes of individual data, 49 technological advancements in data collection create increasing opportunities to use these effect 50 size statistics. Importantly, Δsk , Δku , and ΔZr can be used to compare any two groups, allowing a 51 new generation of meta-analyses that explore such differences and potentially leading to new 52 insights in multiple fields of study.

53

54 Key-words: covariance, individual participant meta-analysis, meta-regression, nonnormality,
55 normal distribution, sex characteristics

56 Background

57 Sex is a biological attribute that can strongly impact organisms' traits, with differences between 58 males and females being central to questions in the biological sciences (e.g., [1,2]). In contrast, 59 biomedical research has primarily focused on male subjects [3], posing a danger to female health 60 [4,5]. Aware of these issues, the US National Institutes of Health and other health agencies have 61 demanded the use of multiple sexes in animal studies when possible [6]. As a consequence, the 62 number of biological and biomedical studies using both female and male animals as research 63 subjects has increased in the last decade [7], leading to the accumulation of data that can be used 64 to synthesise and quantify sex differences across biological domains.

65 Realising the accumulation of sex-specific data, many perspective pieces have encouraged researchers to investigate sex differences more carefully (e.g., [8–10]). Yet, some of these pieces, 66 67 and most of the biological literature, focus exclusively on mean differences between males and 68 females. A fixation on mean differences has been present for a long time in science because of an 69 obsession with dimorphism in trait averages (e.g., [11]), a lack of sufficiently powerful data, or 70 limited (or difficult to use) statistical tools available to researchers. Yet, measures such as variance, 71 correlation, skewness, and kurtosis can be critical to understanding sex differences. For example, 72 certain traits in mice may exhibit no disparity in average values between sexes, but substantial differences emerge in terms of variability [12,13]. These differences could be more easily assessed 73 74 because of an effect size statistic that measures differences in variability between two groups 75 (proposed by [14]), illustrating how novel statistical tools can expand possible research questions and provide new scientific insights, such as identifying sex differences in trait selection or 76 77 canalisation.

78 Beyond variability, the relative shape of trait distributions to the normal distribution 79 (measured by skewness and kurtosis, i.e. asymmetry of a distribution and heaviness of a 80 distribution's tails, respectively; Fig. 1A-B) can also be crucial to understanding ecological and 81 evolutionary processes and patterns (e.g., [15–19]), as well as improving medical diagnostics (e.g., 82 [20,21]). For instance, skewness can bias heritability estimates because evolutionary biologists 83 assume that phenotypic components (genetic and environmental) are normally distributed [18]. 84 Furthermore, kurtosis can be used to understand community assembly processes (e.g., [16]). 85 Besides the shape of trait distributions, evolutionary biologists and quantitative geneticists can 86 quantify correlation matrices to understand trait plasticity and evolvability (e.g., [22–24]), which 87 could then be used for group comparisons (as in [25]; Fig.1C). Despite this, there are no effect size 88 statistics that can easily measure between-group differences (e.g., males and females) in skewness, 89 kurtosis, or within-group correlations.



90

Figure 1. Simulated trait distributions for two groups with different shapes (A: distinct skewness,
B: distinct kurtosis), and different correlations between two traits for two groups (C).

93

Here, we propose three new effect size statistics to evaluate between-group differences in skewness (Δsk), kurtosis (Δku), and correlation (ΔZr), key moments of a distribution that are usually unexplored. These effect size statistics will be valuable to explore sex differences but can 97 also be applied in other fields of study and used to compare differences between any two groups 98 of interest. Meta-analyses using these new effect sizes will create multiple avenues for novel 99 biological enquiries. The time is particularly ripe for analyses using these new effect sizes because 100 the individual-level data (e.g., individual participant data [26,27]) required for their calculation are 101 increasingly available from new technological advances that allow faster data collection and 102 sharing (e.g., automated phenotyping).

103

104 **Difference in skewness and kurtosis**

105 The mean and variance represent the first and second moments of a distribution, respectively. 106 However, the third and fourth moments of a distribution (i.e. skewness and kurtosis, respectively) 107 can also be valuable as they characterise the distribution's shape. More specifically, skewness 108 reflects the distribution's asymmetry around its mean. While positive skewness indicates an 109 elongated right tail with an excess of high values, negative skewness suggests an elongated left 110 tail with an excess of low values. This asymmetry can influence the interpretation of means and 111 variation, as the mean tends to be larger than the median in positively skewed distributions, while 112 the mean tends to be smaller than the median in negatively skewed distributions. Note that a 113 perfectly normal distribution is symmetric (i.e. skewness = 0), where the mean is equal to the 114 median. Skewness (*sk*) can be expressed as:

115
$$sk = \frac{\frac{1}{n}\sum_{i=1}^{n}(x_i - \bar{x})^3}{\left[\frac{1}{n}\sum_{i=1}^{n}(x - \bar{x})^2\right]^{\frac{3}{2}}} \frac{\sqrt{n(n-1)}}{n-2} (eq. 1)$$

116 where x_i is a raw data value, \bar{x} is the sample mean, and n is the sample size. Skewness 117 sampling variance (s^2_{sk}) can then be expressed as:

118
$$s_{sk}^2 = \frac{6n(n-1)}{(n-2)(n+1)(n+3)} (eq. 2)$$

119 On the other hand, kurtosis measures tail heaviness: high kurtosis distributions have 120 heavier tails (i.e., proportionally more extreme values than central values), whereas low kurtosis 121 distributions have lighter tails. For comparison, a normal distribution is expected to have kurtosis 122 = 3. Kurtosis (ku) can be expressed as:

123
$$ku = \frac{n(n+1)(n-1)}{(n-2)(n-3)} \frac{\sum_{i=1}^{n} (x_i - \bar{x})^4}{\left[\sum_{i=1}^{n} (x_i - \bar{x})^2\right]^2} - \frac{3(n-1)^2}{(n-2)(n-3)}$$
(eq. 3)

124 and its with sampling variance (s^{2}_{ku}) as:

125
$$s_{ku}^2 = \frac{24n(n-1)^2}{(n-3)(n-2)(n+3)(n+5)} (eq. 4)$$

Evaluating skewness and kurtosis provides valuable insights into a variable distribution, which is crucial for interpreting means, assessing variability, and making informed decisions in statistical analyses. Although meta-analyses can use skewness (eq. 1) and kurtosis (eq. 3) to investigate single variables, effect size statistics that compare these metrics between two groups are lacking. Thus, we propose the difference between two groups in skewness (Δsk), expressed as:

131
$$\Delta sk = sk_1 - sk_2 \text{ (eq. 5)}$$

132 and its sampling variance $(s^2 \Delta sk)$ as:

133
$$s_{\Delta sk}^2 = s_{sk_1}^2 + s_{sk_2}^2 - 2\rho_{sk}s_{sk_1}s_{sk_2} \text{ (eq. 6)}$$

134 Where ρ_{sk} represents the sampling correlation in skewness between the two groups (zero if 135 assumed to be independent). Similarly, we propose the difference between two groups in kurtosis 136 (Δku), expressed as:

137
$$\Delta ku = ku_1 - ku_2 \text{ (eq. 7)}$$

138 and its sampling variance $(s^2_{\Delta ku})$ as:

139
$$s_{\Delta ku}^2 = s_{ku_1}^2 + s_{ku_2}^2 - 2\rho_{ku}s_{ku_1}s_{ku_2} \text{ (eq. 8)}$$

140

141

where ρ_{ku} represents the sampling correlation in kurtosis between the two groups (zero if assumed to be independent).

142

143 **Difference in correlation**

144 Numerous meta-analyses measure correlation between two variables (e.g., [28,29]). To do so,
145 researchers use the effect size statistic *Zr*, which can be expressed as:

146
$$Zr = \frac{ln(\frac{1+r}{1-r})}{2}$$
 (eq. 9)

147 and its sampling variance (s^2_{Zr}) as:

148
$$s_{Zr}^2 = \frac{1}{n-3} (\text{eq. 10})$$

149 where *r* is Pearson's correlation coefficient between two variables and *n* is the sample size. 150 Although Zr alone remains extremely useful to test correlational hypotheses, researchers 151 from all fields would benefit from being able to compare Zr values between two groups. Although 152 Cohen [30] proposed the difference between two groups in Zr as q, he did not provide an equation 153 to calculate its sampling variance. Consequently, this effect size statistic has not been used despite 154 its potential. We therefore propose the difference between two groups in Zr with a new name 155 (ΔZr), as:

156
$$\Delta Zr = Zr_1 - Zr_2 \text{ (eq. 11)}$$

157 and its sampling variance $(s^2 \Delta Z_r)$ as:

158
$$s_{\Delta Zr}^2 = s_{Zr_1}^2 + s_{Zr_2}^2 - 2\rho_{Zr}s_{Zr_1}s_{Zr_2} \text{ (eq. 12)}$$

159 where ρ_{Zr} represents the sampling correlation in Fisher's Zr between the two groups (zero 160 if assumed to be independent).

162 Worked examples: sex differences in mice

163 To illustrate the application of our proposed effect size statistics, we used data compiled by the 164 International Mouse Phenotyping Consortium (IMPC, version 18.0; [31]: 165 http://www.mousephenotype.org/). We examined differences between male and female mice 166 regarding two pairs of traits from distinct functional domains: morphology (fat mass and heart 167 weight) and physiology (glucose and total cholesterol). We selected these traits because they are 168 widely understood traits, even by non-specialists, and had a large sample size. More specifically, 169 we assessed differences between the sexes in mean (using the natural logarithm of the response 170 ratio [32], hereby *lnRR*), variability (using the natural logarithm of the variance ratio [14], hereby 171 *lnVR*), skewness (using Δsk), and kurtosis (using Δku) for each trait, as well as in the difference in 172 correlation for each trait pair (using ΔZr). The IMPC dataset contains data from multiple 173 phenotyping centres and mice strains, so we selected the ones with the most data points for our 174 analyses here, computing the aforementioned effect size statistics separately for each one of them. 175 We performed a meta-analysis for each effect size statistic to obtain a mean effect size for 176 each trait (or pair of traits, in the case of ΔZr), using 'phenotyping centre' and 'mice strain' as 177 random factors in meta-analytical models. In these analyses, positive effect sizes denoted a greater 178 estimate (mean, variability, skewness, kurtosis, or correlation) for males than females. We 179 conducted all statistical analyses in the software R 4.4.0 [33]. We fitted meta-analytical models 180 using the *rma.mv* function from the package *metafor* [34]. All methodological details and 181 additional information can be found in our tutorial, at 182 https://pietropollo.github.io/new_effect_size_statistics/.

183 We found that males, on average, had greater fat mass and heart weight than females 184 regardless of phenotyping centre and mice strain (Fig. 2A, B, F, G). The variability among

185 individuals regarding these traits was also greater for males than for females, except for fat mass 186 from one specific phenotyping centre and mice strain (Fig 2C). By contrast, females tended to have 187 greater skewness in fat mass and heart weight than males (i.e., negative Δsk values, but note they 188 overlap zero; Fig. 2D, I). Most importantly, Δsk values for fat mass and heart weight varied across 189 phenotyping centres and mice strains, with negative and positive values present (Fig. 2D, I). Sex 190 differences in kurtosis for fat mass and heart weight followed a very similar pattern to the one 191 described for skewness: negative mean Δku values (i.e., greater kurtosis for females than for males, 192 but overlapping zero) with some variation across individual effect sizes (Fig. 2E, J). Moreover, the 193 correlation between fat mass and heart weight was, on average, greater for females than males 194 (Fig. 3A, B). However, this difference in correlation was absent for some phenotyping centres and 195 mice strains (Fig. 3A, B).

196 We also found that male and female mice were, on average, similar in terms of blood 197 glucose levels (Fig. 4A, B), although males had higher total cholesterol than females (Fig. 4F, G). 198 We observed the same pattern regarding the variability of these traits: on average, the sexes were 199 similarly variable in glucose (Fig 4C), but the variability of total cholesterol was greater in males 200 than in females (Fig. 4H). Contrasting with morphological traits, sex differences in skewness and 201 kurtosis were mostly absent (Fig. 4D, E, I, J). Lastly, males and females showed a similar 202 relationship between glucose and total cholesterol, albeit this relationship was stronger for males 203 than for females in some instances (Fig. 3C, D).

Our findings that females have, on average, lower (Fig. 2B, G), less variable (Fig. 2C, H), more concentrated at low values (higher skewness; Fig. 2D, I), and more extreme values (higher kurtosis; Fig. 2E, I) of fat mass and heart weight compared with males may contribute to sexrelated differences in the development of diseases associated with these traits and their biomarkers 208 (e.g., QTc interval length [35]). Moreover, a stronger relationship between fat mass and heart 209 weight in females than in males (Fig. 3B) may represent a greater risk of cardiohypertrophy arising 210 from obesity in the former compared with the latter [36]. Meanwhile, absent or less pronounced 211 sex differences in glucose and total cholesterol (Fig. 4) may suggest other sources of variation may 212 contribute to sex differences in the symptomology of diseases associated with these measurements 213 (e.g., [37-39]). Characterising sex differences in biological traits, as we have done here, can 214 provide new perspectives on evolutionary, ecological, and medical patterns, possibly improving 215 healthcare and environmental interventions.

216



Figure 2. Examples of morphological sex differences in mice (fat mass, A-E; heart weight, F-J) for various phenotype centres (each with a different colour in panels B-E and G-J) and mice strains (each with a different shape in panels B-E and G-J), with the bottom estimate in panels B-E and G-J (turquoise) representing the mean effect size. While A and F show distributions of these traits for males (black with dashed borders) and females (white with solid borders), panels B-E and G-J

show effect sizes (*lnRR*: natural logarithm of the response ratio; *VR*: variance ratio; Δsk : difference in skewness; Δku : difference in kurtosis).

226



Figure 3. Relationship between fat mass and heart weight (A, B) and glucose and total cholesterol (C, D) in mice. Panels A and C show these relationships separately for males (dashed line) and females (solid line), each panel representing a different phenotyping centre and/or mice strain.

Panels B and D then show differences in correlation (ΔZr) between males and females, where each colour represents a distinct phenotype centre and each shape represents a distinct mice strain, with the bottom estimate in each panel (pink) representing the mean effect size. Note that panels A and C contain individual data points, which may appear as background shading in cases with large sample sizes.



Figure 4. Examples of physiological sex differences in mice (glucose, A-E; total cholesterol, F-J) for various phenotype centres (each with a different colour in panels B-E and G-J) and mice strains (each with a different shape in panels B-E and G-J), with the bottom estimate in panels B-E and G-J (turquoise) representing the mean effect size. While A and F show distributions of these traits for males (black with dashed borders) and females (white with solid borders), panels B-E and G-J show effect sizes (*lnRR*: natural logarithm of the response ratio; *VR*: variance ratio; Δsk : difference in skewness; Δku : difference in kurtosis).

245

246 Limitations

247 Despite the enormous potential of the effect size statistics we proposed here, they are not free of 248 limitations. For instance, skewness and kurtosis (and therefore the difference in these estimates 249 between two groups; i.e., Δsk and Δku , respectively) are more likely to become extreme with small 250 sample sizes and with variables with few unique values, either because the variable is discrete or 251 because it is naturally constant (e.g., number of vertebrae in mice). We thus recommend 252 researchers only to compute Δsk and Δku for continuous variables with a minimum sample size of 253 50 for each group. Lastly, although Δsk , Δku , and ΔZr can be calculated, respectively, from 254 reported skewness, kurtosis, or within-group correlations for different samples, empirical studies 255 rarely report these estimates. Thus, the calculation of these effect sizes will probably require raw 256 data, which are only now fortunately becoming more easily available.

257

258 **Future opportunities**

The effect size statistics proposed in the present study can be useful across the life sciences, social sciences, and medicine. This is because skewness and kurtosis, and consequently differences

261 between any two or more groups in these estimates (i.e., Δsk and Δku), may help researchers to 262 understand epidemiological trends [40], genetic patterns relevant to medical diagnosis [20,21], 263 disruptive selection on quantitative traits [41], body size patterns across individuals [42] and 264 species [43], reproductive patterns [44], regime shifts in ecosystems [45], heritability [18], 265 community assembly processes [16], and possibly many other topics. Meanwhile, comparisons 266 regarding correlations have been used to explore memory processing during sleep [46], 267 physiological patterns in patients with certain medical conditions [47], and selection patterns [22– 268 24], to name a few. Because ΔZr can be used in virtually any comparison between two groups of 269 correlational data, the opportunities for its use are endless. Most importantly, Δsk , Δku , and ΔZr 270 are unitless measures, so they can be meta-analysed to uncover patterns between two groups (e.g. 271 males and females). Moreover, the growing availability of raw data and big data approaches, 272 facilitated by technological advances, make these effect size statistics particularly valuable for 273 modern research.

274

275 Data and code availability

All data and code used in this study are available at:
https://github.com/pietropollo/new_effect_size_statistics.

278

279 **Declaration of AI use**

The authors declare that they occasionally used GPT-4-turbo (OpenAI) to improve the clarity and readability of this work. After using these tools, the authors reviewed and edited the content as needed and took full responsibility for the content of the publication.

284	Author contributions
285	Conceptualisation: PP, SN; data curation: PP; formal analysis: PP; funding acquisition: SN;
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288	all authors.
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