## Coexistence theory for microbial ecology, and vice versa

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#### Abstract

Classical models from theoretical ecology are seeing increasing uptake in microbial ecology, but there 2 remains rich potential for closer cross-pollination. Here we explore opportunities for stronger integration of 3 ecological theory into microbial research (and vice versa) through the lens of so-called "modern" coexistence 4 theory. Coexistence theory encompasses a body of theory for disentangling the contributions of different 5 fluctuation-independent (e.g., resource partitioning) and fluctuation-dependent (e.g., environmental 6 variability) mechanisms to species coexistence. We begin with a short primer on the fundamental concepts 7 of coexistence theory, with an emphasis on the relevance to microbial communities. We next present 8 a systematic review, which highlights the paucity of empirical applications of coexistence theory in 9 microbial systems. In light of this gap, we then identify and discuss ways in which: i) coexistence 10 theory can help to answer fundamental and applied questions in microbial ecology, particularly in 11 spatio-temporally heterogenous environments, and ii) experimental microbial systems can be leveraged 12 to validate and advance coexistence theory. Finally, we address several unique, but often surmountable, 13 empirical challenges posed by microbial systems, as well as some conceptual limitations. Nevertheless, 14 thoughtful integration of coexistence theory into microbial ecology presents a wealth of opportunities for 15 the advancement of both theoretical and microbial ecology. 16

## 17 Introduction

18 Sustained improvement in sequencing technologies, database integration, and bioinformatics are accelerat-

<sup>19</sup> ing the accumulation of microbial community census data. At the same time there is growing awareness

20 that these empirical developments have outpaced advancements in our mechanistic understanding of

<sup>21</sup> microbial community dynamics (Prosser, 2020). To address this imbalance, there has been a recent push

to integrate models and frameworks from theoretical ecology into microbial ecology (Picot, Shibasaki,
Meacock, & Mitri, 2023; van den Berg et al., 2022; Prosser et al., 2007; Meroz, Livny, & Friedman, 2024),

<sup>24</sup> with theory-driven research already providing deep insights into the assembly (Goldford et al., 2018;

<sup>25</sup> Friedman, Higgins, & Gore, 2017), functioning (Skwara et al., 2023), and stability (Hu, Amor, Barbier,

<sup>26</sup> Bunin, & Gore, 2022) of microbial communities.

Understanding species coexistence and competition has been a central goal of theoretical ecology for over
a century (Gause, 1935; MacArthur & Levins, 1967; Tilman, 1982; Chesson, 2000b). With growing insight
into the essential role microbes play in regulating organismal and ecosystem health, understanding the

<sup>30</sup> causes and consequences of species coexistence has become increasingly relevant to applied and fundamental

<sup>31</sup> microbiology. For instance, the maximization of ecosystem functioning (e.g., starch degradation) in

<sup>32</sup> bacterial communities can require the coexistence of specific combinations of species (Sanchez-Gorostiaga,

<sup>33</sup> Bajić, Osborne, Poyatos, & Sanchez, 2019), and the evolution of antimicrobial resistance can be shaped by

<sup>34</sup> how different environmental conditions influence the coexistence of susceptible and resistant strains (Nev,

<sup>35</sup> Jepson, Beardmore, & Gudelj, 2020; Letten, Hall, & Levine, 2021). A number of different overlapping

<sup>36</sup> frameworks have been developed in ecology for understanding species coexistence (Chase & Leibold,

2003; Hubbell, 2011; Abrams, 2022; Clark et al., 2024), some of which (e.g., resource competition theory)

<sup>38</sup> are especially well suited to microbial systems (Grover, 1997). However, one approach that has become

<sup>39</sup> popular amongst plant and animal ecologists, but that has seen far less uptake in microbial ecology, is

40 so-called 'modern coexistence theory' (Chesson, 2000b; Barabás, D'Andrea, & Stump, 2018).

The prefix *modern* (dropped in the remainder of the text) is something of a misnomer in the sense 41 that many of the core ideas date back several decades (Chesson & Warner, 1981; Chesson, 1990, 1994; 42 May, 1973) (albeit with continuous development to the present) and that it has not superseded other 43 approaches (Abrams, 2022). Nevertheless, its rapid uptake in recent years can be understood, at least in 44 part, as a reaction to the confusing morass of system- and scale-specific coexistence mechanisms that 45 theoretical and empirical ecologists had offered up by the end of the 20<sup>th</sup> century. It was against this 46 backdrop that John Lawton famously described community ecology as "a mess, with so much contingency 47 that useful generalisations are hard to find" (Lawton, 1999). Coexistence theory, developed primarily 48 by Peter Chesson and colleagues (hence also referred to as 'Chesson's coexistence theory') emerged as a 49 unifying framework that brought a welcome degree of order to the study of species coexistence (Chesson, 50 1994, 2000b; Barabás et al., 2018; Adler, HilleRisLambers, & Levine, 2007). More specifically, coexistence 51 theory provides a quantitative framework for sorting the many low-level (e.g. system-specific) coexistence 52 mechanisms into a small number of high-level umbrella categories. As such, it concentrates and links many 53 disparate processes, by showing how, for example, temporal fluctuations in temperature, nectar chemistry 54 and rainfall, can mediate coexistence in aquatic plants, floral yeasts, and annual grasses, respectively, via 55 the same underlying mechanism (Armitage & Jones, 2019b; Letten, Dhami, Ke, & Fukami, 2018; Angert, 56 Huxman, Chesson, & Venable, 2009). 57

 $_{58}$  The purpose of this review is to highlight the wealth of opportunities for applications of coexistence theory

<sup>59</sup> in microbial ecology, and the equally rich potential for testing coexistence theory with microbial systems.

60 We begin with "A coexistence theory primer", which provides a brief summary of the fundamental concepts

of coexistence theory, but point readers wishing to go deeper to existing reviews detailing the mathematical

intricacies of coexistence theory and guidelines for its empirical implementation (see Barabás et al., 2018; Godwin, Chang, & Cardinale, 2020; Spaak, Ke, Letten, & De Laender, 2023; Chesson, 2018; Ellner, 63 Snyder, Adler, & Hooker, 2019; E. C. Johnson & Hastings, 2023). Next in "Empirical applications" we 64 present the results of a systematic review of existing empirical studies employing coexistence theory in 65 microbial systems. Then in "Mutual benefits of coexistence theory and microbial ecology" we discuss how 66 coexistence theory is well suited to tackling a range of fundamental and applied problems in microbial 67 ecology, and conversely how the tractability of microbial systems makes them ideal for testing and 68 developing emerging branches of coexistence theory. Finally, in "Cautionary notes" we identify some of 69 the empirical challenges and fundamental limitations of coexistence theory, especially in the context of 70 microbial study systems. Indiscriminately applying coexistence theory as an additional "off-the-shelf" 71 analysis risks losing sight of the ecological questions and processes of interest. Nevertheless, thoughtful 72 integration of coexistence theory and microbial ecology holds great promise for generating new insights in 73 both fields. 74

#### A coexistence theory primer 75

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The framework of coexistence theory is best understood as two related approaches for expressing 76 competitors' invasion growth rates as a small combination of mechanisms fundamental to coexistence. 77 Here, invasion growth rates are a species' (or genotype's) long term average growth rate when introduced 78 at very low density into an established (resident) community of potential competitor species at equilibrium 79 or within a dynamic attractor. If invasion growth rates are positive for all species within a community, 80 then they are said to be able to coexist. The critical information recovered from these invasion growth 81 rates are generally either: 1) competitors' niche differences and fitness differences; or 2) competitors' 82 responses to average environments and fluctuations around this average. 83

The first thread provides a higher-level framing of the requirements for coexistence along two fundamental 84 axes. Specifically, stable coexistence among species depends on niche differences exceeding any inherent 85 fitness differences (Chesson, 2000a, 2013; Letten, Ke, & Fukami, 2017; Spaak & De Laender, 2020). Niche 86 differences capture the extent to which competitors use different resources (e.g. consumption of citrate 87 versus glucose by different strains of E. coli in the long-term evolution experiment (Blount, Borland, 88 & Lenski, 2008)) or are targeted by different predators or pathogens (e.g. specificity of bacteriophages 89 to different bacterial strains or species (Koskella & Brockhurst, 2014)). In contrast, fitness differences 90 reflect how well adapted competitors are to their shared environment. It follows that if two or more 91 species are characterised by large fitness differences they can only coexist if their niches are sufficiently 92 differentiated (Figure 1D). Conversely, when species have small fitness differences, even small niche 93 differences can facilitate coexistence (note that a combination of infinitesimal fitness and niche differences 94 can yield so-called neutral coexistence (Adler et al., 2007)). In the jargon of coexistence theory, a process 95 that increases niche differences is referred to as a stabilizing mechanism while one that reduces fitness 96 differences is referred to as an equalizing mechanism (Chesson, 2000a, 2003). 97

The second thread of coexistence theory is concerned with identifying the contributions of different 98 stabilizing mechanisms to coexistence and partitioning them into additive terms reflecting various types 99 of fluctuation-independent and fluctuation-dependent mechanisms (Chesson, 1994; Barabás et al., 2018; 100 Ellner et al., 2019; Letten et al., 2018; E. C. Johnson & Hastings, 2023). Fluctuation-independent 101 mechanisms promote coexistence in a constant environment, while fluctuation-dependent mechanisms act 102 through environmental fluctuations to strengthen, weaken, or even reverse coexistence outcomes. The 103 emphasis on stabilizing mechanisms reflects the prepotent role they play in mediating stable coexistence; 104 stable coexistence is impossible in the absence of a stabilizing mechanism, and sufficient stabilization 105 may depend on environmental fluctuations. Nevertheless, most mechanisms will also have an equalizing 106

component, as these two axes are not orthogonal. Under the standard partition, all fluctuation-independent mechanisms (including resource, predator and pathogen partitioning) are grouped into a single category. The fluctuation-dependent mechanisms capture the effects of both temporal *and* spatial heterogeneity on coexistence (hence they are also commonly referred to as variation-dependent mechanisms). The two main types of fluctuation-dependent mechanisms are the *storage effect* and *relative nonlinearity of competition*, both of which have temporal and spatial analogues (a third, exclusively spatial, mechanism

113 is termed fitness-density covariance (Chesson, 2000a; Barabás et al., 2018)).

The temporal storage effect can facilitate coexistence when species exhibit different growth responses to 114 density independent environmental factors (e.g., temperature or pharmaceutical antibiotics) that vary 115 across space or fluctuate across time (Chesson, 1994; Letten et al., 2021). The emphasis on variation 116 in density-independent environmental factors, which to a first approximation are not influenced by the 117 focal species, is a distinguishing feature of the storage effect. In the jargon of coexistence theory, these 118 species-specific responses can lead to density-dependence in environment-competition covariance (Chesson, 119 1994; Yuan & Chesson, 2015; Barabás et al., 2018). This is simply to say that when a species is rare in the 120 system it will experience little covariance in the strength of competition and environmental favourability 121 across space or time, which allows it to take full advantage of good conditions. Conversely when a species 122 is dominant in the system it will experience high positive covariance between these two factors, which 123 should limit its ability to take advantage of favourable conditions. Provided rare species are also able to 124 buffer the negative effects of high competition during unfavourable periods (e.g. via dormant life stages or 125 overlapping generations), this process can drive the requisite negative frequency dependence underpinning 126 species coexistence. 127

In contrast with the storage effect, relative nonlinearity relies on species exhibiting trade-offs in their 128 per capita growth responses to competitive factors (cf. density-independent environmental factors), such 129 as nutrient resources, which fluctuate through time (note that although there is a spatial analogue of 130 relative nonlinearity, we focus on the more canonical temporal mechanism here) (Chesson, 1994; Yuan 131 & Chesson, 2015; Barabás et al., 2018). These fluctuations may be driven endogenously (e.g., cyclic 132 predator-prey dynamics) or via exogenous resource pulsing (e.g., in the animal gut). The classic trade-off 133 permitting coexistence via relative nonlinearity is between gleaner and opportunists, which tend to be 134 better competitors in continuous versus fluctuating resource environments (the name relative nonlinearity 135 refers to the required difference in the nonlinearity of the per capita growth responses that permit this 136 trade-off) (Yamamichi & Letten, 2022). Alongside the trade-off, stable coexistence via relative nonlinearity 137 additionally requires that each species feedback on the magnitude of fluctuations in a direction that 138 favours its competitor (Chesson, 1994; Yuan & Chesson, 2015; Barabás et al., 2018). For example, 139 for coexistence of gleaners and opportunists, the former needs to increase temporal resource variability 140 relative to that imposed by the opportunist. These negative feedbacks typically emerge as a natural 141 byproduct of each strategist's per-capita growth response, but it is also possible for positive feedbacks, 142 and hence priority effects, to occur when competitors change the temporal pattern of resource availability 143 in a direction which favours their own competitive ability (Ke & Letten, 2018). 144

These methods for partitioning invader-resident growth differences into an additive sum of contributing mechanisms have also been generalised into a method for assessing the role of any interspecific difference on coexistence. This has been called "trait-decomposition" in recent literature and quantifies the sensitivity of invasion growth rates to interspecific differences in model parameters such as nutrient uptake rates or mortality rates, all else being equal (Ellner et al., 2019).

#### **Empirical applications** 150

A variety of experimental and observational approaches have been used by researchers to confront the 151 predictions and inference of coexistence theory with empirical data. Typically this involves the direct 152 measurement of invasion growth rates via mutual invasion tests (Figure 1B), or the parameterization of 153 dynamical models (e.g., Lotka-Volterra or consumer-resource models) using timeseries datasets (Figure 154 1C) or "response surface" experiments that manipulate species' densities (Figure 1A) (Grainger, Levine, 155 & Gilbert, 2019; Terry & Armitage, 2024). The obtained estimates of invasion growth rates or model 156 parameters may then be used to predict (or explain) coexistence based either on the partitioning of fitness 157 and niche differences in equilibrium system (Figure 1D) or on the partitioning of different fluctuation-158 dependent and -independent mechanisms (Figure 1E) (Godwin et al., 2020; Ellner et al., 2019). Most 159 empirical research employing coexistence theory has been conducted in plant systems with few studies in 160 microbial systems; of the 49 studies that quantified niche and fitness differences reviewed by Terry & 161 Armitage (2024), 39 focused on plant communities and just six studied microbial communities. 162

To confirm the rarity of empirical explorations of coexistence theory in microbial systems we performed a 163 systematic review (see Supplementary Materials) that identified studies in two ways. First, we screened 164 174 empirical coexistence studies compiled in previous systematic reviews of the field (Buche, Spaak, 165 Jarillo, & De Laender, 2022; Terry & Armitage, 2024; Hawlena, Garrido, Cohen, Halle, & Cohen, 2022) 166 and found nine studies that applied coexistence theory to microbial systems. Second, we performed an 167 additional search of the literature in May 2024 and used a machine learning framework to screen abstracts 168 (Van De Schoot et al., 2021). From an initial search that returned 2,164 records we found just 12 relevant 169 studies (Table 1), including all nine relevant studies that had been identified from previous reviews. 170

This low number of studies precludes a formal analysis, but it does demonstrate how rarely coexistence 171 theory has been applied in microbial systems. The 12 studies were published between 2013 and 2022 172 (with no obvious increase over time) and they used bacteria (n = 5), phytoplankton (n = 3), protists (n = 3)173 2), or yeasts (n = 2). Most studies (9/12) used mutual invasion tests (Figure 1B) and species sensitivity 174 to competition (sensu Carroll, Cardinale, & Nisbet, 2011) to calculate niche and fitness differences. Two 175 studies tracked the density of monocultures and multi-species communities over time (Figure 1C) and 176 fitted population models to the timeseries data to either quantify niche and fitness differences (Hogle, 177 Hepolehto, Ruokolainen, Cairns, & Hiltunen, 2022) or to quantify the relative contributions of different 178 coexistence mechanisms (Letten et al., 2018). No studies used the response surface approach (Figure 1A) 179 which dominates plant and animal empirical coexistence study designs (Terry & Armitage, 2024), and 180 one study observed natural communities and used "performance proxies" (sensu Grainger, Levine, & 181 Gilbert, 2019 for niche and fitness differences (Zufiaurre et al., 2021).

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Some studies focused on the coexistence of just one pair of species (e.g., Tan, Rattray, Yang, & Jiang, 183 2017; Hogle et al., 2022), while other studies investigated the coexistence of over 20 pairs of species 184 (e.g., Li, Tan, Yang, Ma, & Jiang, 2019; Narwani, Alexandrou, Oakley, Carroll, & Cardinale, 2013). The 185 tractability of these microbial systems result in the numbers of independent replicates far exceeding 186 typical animal or plant experiments, with some studies having more than 500 experimental units (e.g., Li 187 et al., 2019; Grainger, Letten, Gilbert, & Fukami, 2019). This increase in experimental units was not used 188 to increase the replicates per treatment to gain more robust predictions (across the 12 relevant studies the 189 maximum number of replicates was eight and the median was three). Instead, the additional experimental 190 units were used to increase the number of species pairs examined (e.g., Li et al., 2019; Narwani et al., 191 2013) or to test the effects of additional factors such as the effect of environmental variables (e.g., Letten 192 et al., 2018; Grainger, Letten, et al., 2019), trait diversity (eg., Hogle et al., 2022), or evolutionary history 193 (e.g., Zhao, Zhang, & Zhang, 2016; Tan, Rattray, et al., 2017). 194



#### **EMPIRICAL APPROACHES**

**ANALYTICAL APPROACHES** 

Figure 1: Approaches to data acquisition (A-C) and analysis (D-E) taken in empirical applications of coexistence theory. The arrows between panels show the number of studies in our systematic review that used that combination of empirical and analytical approaches. The numbers in superscripts refer to row numbers of Table 1. (A) Response surface designs, which can not always be applied in microbial systems (see emphEmpirical challenges), are used to parameterize population models. (B) Invasion tests can be performed to test the mutual invasion criterion (i.e., coexistence predicted if all species can invade the community from low densities). (C) Timeseries datasets can be used to parameterize population models or to test coexistence theory predictions. (D) The most common analytical approach for applying coexistence theory is quantifying niche and fitness differences, either directly from the data through model-agnostic approaches or from parameterized population models using mathematical approaches. Communities can then be placed in a "coexistence plane" with axes defined by niche and fitness differences where different regions indicate either competitive exclusion (pale grey zones on top and bottom), stable coexistence (mid grey zone on the right), or priority effects (dark grey zone on the left). (E) Coexistence theory can also be used to partition the effects of different coexistence mechanisms either using analytical techniques or using simulation-based approaches. In this hypothetical example, there is stable coexistence between the blue and yellow species (both have positive invasion growth rates) primarily due to large contributions from fluctuation-dependent mechanisms.

Table 1: The twelve empirical coexistence studies using microbial systems identified by our systematic review. *Empirical Approach* describes what type of experimental design was used; mutual invasion tests ("invasion"), densities tracked over time ("timeseries"), or empirical studies where natural communities are observed and proxies are used to estimate niche and fitness differences ("proxies"). For *Analytical Approach*, "ND-FD" indicates studies that quantified niche and fitness differences and "partitioning" indicates studies that quantified the relative contributions of different coexistence mechanisms to invasion growth rates. *Model* indicates the population model used, *Pairs* records the number of species pairs for which coexistence was estimated, *Replicates* records the number of replicates per species pair (for each treatment), and *Units* records the number of distinct experimental units used in the coexistence part of the study.

Study	Taxa	Empirical Approach	Analytical Approach	Model	Pairs	Replicates	Units
Narwani et al., 2013	algae	invasion	ND-FD	none	28	3	168
Tan et al., 2016	bacteria	invasion	ND-FD	none	6	3	57
Zhao et al., 2016	bacteria	invasion	ND-FD	none	5	3	180
Tan, Rat- tray, et al., 2017	bacteria	invasion	ND-FD	none	1	5	60
Tan, Yang, & Jiang, 2017	bacteria	invasion	ND-FD	none	6	6	78
Letten et al., 2018	yeast	timeseries	partitioning	consumer- resource	6	4	160
Gallego et al., 2019	cyanobacteria	invasion	ND-FD	none	15	3	126
Grainger, Letten, et al., 2019	yeast	invasion	ND-FD	none	6	8	576
Li et al., 2019	bacteria	invasion	ND-FD	none	24	3	540
Jackrel et al., 2020	algae	invasion	ND-FD	none	6	3	72
Zufiaurre et al., 2021	protists	proxy	ND-FD	none	n/a	2	22
Hogle et al., 2022	protists	timeseries	ND-FD	lotka- volterra	1	4	24

### <sup>195</sup> Mutual benefits of coexistence theory and microbial ecology

To facilitate closer integration of coexistence theory and microbial ecology, in this section we explore the mutual benefits between the two areas of research. We first highlight how coexistence theory can provide a fresh perspective on key challenges in the study of microbial communities. We then argue that microbial communities provide unique opportunities for novel tests of coexistence theory that would otherwise be intractable (i.e., in macro-organisms).

#### <sup>201</sup> How coexistence theory can benefit microbial ecology

Many mechanisms, some general to all ecological systems (e.g., resource and natural enemy partitioning) 202 and others more common to microbial systems (e.g., cross-feeding, horizontal gene transfer), have been 203 proposed to explain the high levels of microbial diversity commonly encountered in metabarcoding studies 204 (Thompson et al., 2017). Coexistence theory can help microbial ecologists move beyond verbal theories 205 and intuitions for how species coexist by quantifying the relative importance of these mechanisms and 206 by relating different mechanisms to each other. Coexistence theory might be leveraged to synthesize 207 disparate models in microbial ecology, and it holds particular promise for guiding the growing interest in 208 how spatio-temporal variability impacts microbial communities. The remainder of this section will use 209 three high-level examples to outline how different aspects of coexistence theory described in the primer 210 section - (i) niche and fitness differences, (ii) fluctuation-dependent mechanisms of coexistence, and (iii) 211 trait-decomposition simulations – can shine light on open problems in fundamental and applied microbial 212

213 ecology.

A common approach taken by microbial ecologists (albeit one that is not unique to microbial ecology) is 214 to infer species interactions and community assembly processes from the observed covariances between 215 taxa in metagenomic/metabarcoding inventories (Armitage & Jones, 2019a). This includes characterizing 216 communities as being under stochastic versus deterministic regulation, depending on the functional (or 217 phylogenetic) distribution of co-occurring taxa (Stegen, Lin, Konopka, & Fredrickson, 2012). Although 218 this data undoubtedly provides a valuable starting point for more mechanistic predictions, inference of 219 assembly processes from observational data is well known to be fraught (Barner, Coblentz, Hacker, & 220 Menge, 2018), not least because of the confounding effects of spatial and temporal scale dependence 221 (Blanchet, Cazelles, & Gravel, 2020; Armitage & Jones, 2019a). Viewed from the perspective of niche and 222 fitness differences it is apparent that all systems must fall along a continuum from stochastic (weak niche 223 and fitness differences) to deterministic (strong fitness differences or strong niche differences), and that the 224 magnitude of niche and fitness differences is going to be highly dependent upon the spatial and temporal 225 scale at which they are evaluated. However, it is likewise unclear how the traditionally pairwise niche and 226 fitness difference metrics relate to observed covariation among species in complex multispecies communities. 227 Thus, we envision at least one way in which these approaches can complement one another. By tracking 228 experimental or observational low density growth rates derived through metagenomic, metabarcoding, or 229 plate count timeseries, we can begin to relate stabilising niche differences (a key requirement of invasion 230 growth rates) to the topological properties of a community's statistical correlational structure or its 231 position along a predicted niche-neutral continuum. By benchmarking the inferential accuracy of these 232 methods in experimental microbial communities in which each species' invasion abilities are already 233 known, we can identify the inferential ability of such approaches and their specific failure modes. 234

Understanding the impact of environmental fluctuations on eco-evolutionary dynamics is another increasingly active area of inquiry in microbial ecology (e.g. Abreu, Andersen Woltz, Friedman, & Gore,
2020; Nguyen, Lara-Gutiérrez, & Stocker, 2021; Shibasaki, Mobilia, & Mitri, 2021). Microbial systems
are rarely homogeneous, particularly at the temporal and spatial scales relevant in applied microbiology
(Nguyen et al., 2021). This spatio-temporal variability – from periodic antibiotic dosing, to drying

and wetting of soils, to daily and seasonal fluctuations in temperature and light – undoubtedly plays 240 a critical role in the eco-evolutionary dynamics of microbial systems. As opposed to most commonly 241 applied ecological theory that assumes homogeneous environments (Meroz et al., 2024; Picot et al., 242 2023), coexistence theory offers a mathematically rigorous framework to systematically study the role of 243 fluctuating environments and to partition the relative effects of different variation-dependent mechanisms 244 on microbial coexistence. Furthermore, the stabilizing effects of spatio-temporal fluctuations may be 245 leveraged to help engineer microbial communities for the optimization of ecosystem function (Letten & 246 Ludington, 2023). Functional landscape approaches can be used to predict which combinations of species 247 have the maximum performance for a given function across different applications from food and beverage 248 production to waste management (Sanchez-Gorostiaga et al., 2019; Sanchez et al., 2023). However, these 249 optimal communities may not have sufficient niche differences to overcome any fitness differences under 250 standard conditions, so their coexistence might require the introduction of temporal or spatial fluctuations, 251 which could be designed based on coexistence theory predictions. If, on the other hand, fluctuations are 252 an unavoidable feature of the process, they will need to be considered in the design of microbial consortia. 253 Using coexistence theory to better understand fluctuating environments therefore has the potential to 254 advance both basic and applied microbial ecology. 255

As is common in many nascent fields, microbial ecology has seen a wide proliferation of alternative 256 hypotheses and theories, with limited conceptual integration between them to date. Consider two popular 257 theories concerning microbial coexistence: the seed bank and kill-the-winner models (Thingstad & Lignell, 258 1997; Winter, Bouvier, Weinbauer, & Thingstad, 2010; Lennon & Jones, 2011; Lennon, den Hollander, 259 Wilke-Berenguer, & Blath, 2021). The seed bank model posits that persistent populations of dormant or 260 sporulated microbial cells can respond rapidly to transiently favourable environmental conditions and 261 buffer their populations against losses they would incur if otherwise active and competing for resources 262 (Lennon & Jones, 2011; Lennon et al., 2021). Although it has been loosely linked with the temporal 263 storage effect in the past, recent work shows that microbial dormancy may also mediate coexistence 264 via relative nonlinearity of competition when dormancy is adaptive under under periods of resource 265 starvation (cf. density-independent stressors such as temperature, osmostic stress or antimicrobials) 266 (Letten, Yamamichi, Richardson, & Ke, 2024). The "kill-the-winner" model, on the other hand, is a 267 proposed fluctuation-independent mechanism by which lytic bacteriophage viruses – each specific to a 268 single strain of bacterial competitor – act to suppress the abundance of otherwise competitively dominant 269 bacteria (e.g. by virtue of being better resource competitors) (Thingstad & Lignell, 1997). It is reasonable 270 to assume that trade-offs between growth and dormancy, and growth and phage resistance, frequently 271 occur side-by-side, but we are aware of no efforts to theoretically synthesise them and assess their joint 272 contributions to microbial coexistence. By unifying existing models of kill-the-winner and seed bank 273 dynamics into a single community dynamics model, growth rate partitioning approaches could be used to 274 evaluate their relative contribution to community average stabilization and fitness equalization (Ellner 275 et al., 2019). This "trait-decomposition" approach (recently developed by Ellner et. al (2019)) would 276 not only provide high-level inference on the importance of these two prominent microbial coexistence 277 mechanisms, but would also allow for the further partitioning of the fluctuation-independent (e.g. classic 278 resource competition vs. trade-offs in phage susceptibility) and fluctuation-dependent contributions (i.e. 279 temporal storage effect vs relative nonlinearity). 280

#### <sup>281</sup> How microbial ecology can benefit coexistence theory

The development of coexistence theory has undoubtedly outpaced its empirical validation (Godwin et al., 282 2020; Terry & Armitage, 2024). This lag is at least in part due to the comparatively technical nature 284 of early presentations of the theory, but it is also due to the challenges of testing the theory in plant 285 and animal systems. Most empirical coexistence studies of animal and plant communities are conducted

over a single generation due to logistical constraints (Terry & Armitage, 2024, but see Terry, 2024), 286 which means coexistence theory can only be used to produce (error-prone) predictions rather than to 287 explain observations. However, the short generation times and rapid dynamics of microbes allow for 288 direct observations of coexistence, competitive exclusion, or priority effects (i.e., through invasion tests or 289 timeseries). As such, with microbes, it is much easier to both make and test predictions informed by 290 coexistence theory. This tight connection between theory and experiments places microbial systems in an 291 excellent position to rigorously test and to develop emerging theory on a range of themes in coexistence 292 theory, including, but not limited to, spatiotemporal fluctuations as coexistence mechanisms, evolutionary 293 effects on coexistence, and coexistence in diverse multispecies communities. 294

The challenges of manipulating environmental variability at meaningful temporal and spatial scales 295 in animal and plant systems has hindered empirical research on fluctuation-dependent mechanisms of 296 coexistence – e.g., the storage effect and relative non-linearity of competition. Firstly, as environmental 297 fluctuations must occur on timescales longer than generation times to act as stabilizing mechanisms, 298 studies of temporal storage effects and related mechanisms in plant and animal systems have typically 299 relied on simulation approaches with parameterized models (e.g., Armitage & Jones, 2019b; Hallett, 300 Shoemaker, White, & Suding, 2019). In contrats, empirical tests of fluctuation-dependent coexistence 301 mechanisms, that require multi-year experiments for annual plants, can be done in days for bacteria. It is 302 unsurprising then that the few direct empirical tests (cf. simulation-based predictions) of fluctuation-303 dependent coexistence have mostly been carried out in microbial systems (e.g., Descamps-Julien & 304 Gonzalez, 2005; Jiang & Morin, 2007; Ellner, Snyder, & Adler, 2016; Letten et al., 2018). Secondly, 305 removing or manipulating spatial heterogeneity in plant and animal experimental systems is often not 306 feasible. Experimental arenas for microbial communities, on the other hand, can be easily modified to 307 create or remove spatio-temporal variability in environmental conditions (e.g., using a chemostat). One of 308 the few studies that has empirically quantified spatial coexistence mechanisms used found higher diversity 309 of Pseudomonas strains in static (heterogenous) compared to shaken (homogenous) environments when 310 dispersal between environments was permitted (Tan, Rattray, et al., 2017). Modified chemostats with 311 gradients of environmental conditions (i.e., "gradostats", sensu Lovitt & Wimpenny, 1981), complex 312 artificial "micro-landscapes" (Larsen & Hargreaves, 2020), or biofilm model systems (O'Brien & Fothergill, 313 2017) all offer more sophisticated and highly controllable approaches for testing the effects of spatial 314 heterogeneity on species coexistence. 315

Amidst growing interest in the role of rapid evolution in regulating community dynamics and coexistence 316 on ecological time scales (Lankau, 2011; Hiltunen, Kaitala, Laakso, & Becks, 2017; Wittmann & Fukami, 317 2018; Yamamichi & Letten, 2021), several recent studies have shown that evolution can shift niche or 318 fitness differences through changes in species traits and competitive abilities. However, with only a 319 few exceptions (e.g., Bernhardt et al., 2020) these are limited to studying sorting of standing genetic 320 variation rather than de novo evolution (Sakarchi & Germain, 2023; Hart, Turcotte, & Levine, 2019). 321 The rapid generation times and large population sizes of microbes permit observation of evolutionary 322 impacts on species coexistence over relatively short timescales. In two rare examples, Zhao et al., (2016) 323 studied coexistence between allopatrically and sympatrically evolved pairs of bacteria, while Hogle et 324 al., (2022) observed community dynamics and species coexistence over 70 generations of ciliates (a study 325 that would have taken an annual plant ecologist 70 years). Furthermore, precise genetic manipulation of 326 microbial populations (e.g., transfer of antimicrobial resistant genes) could deepen our understanding of 327 the molecular basis of traits that shape species coexistence. Expanding coexistence studies into microbial 328 systems also has the potential to refine our understanding of the processes responsible for the persistence 329 or loss of allelic diversity in evolving populations, as the framework's ideas naturally map to population 330 genetic processes such as clonal interference and negative frequency-dependent selection (Maddamsetti, 331

The small-scale nature of microbial systems also allows the use of far more experimental units than 333 realistically achievable in animal and plant study systems. This is to say that the "combinatorial explosion 334 problem", where the number of species combinations increases exponentially with species richness, is 335 far less of a limiting factor in microbial systems. Indeed, Li et al., (2019) used over 500 experimental 336 units to quantify niche and fitness difference between 24 pairs of bacterial species. High-throughput 337 robotic or droplet-based systems, which can rapidly assemble and observe the dynamics of many different 338 microbial communities (e.g., Diaz-Colunga, Catalan, San Roman, Arrabal, & Sanchez, 2024; Kehe et al., 339 2019), would be especially powerful tools for testing emerging theory on species coexistence in diverse 340 communities where indirect interactions can significantly complicate predictions of species coexistence 341 (Spaak & Schreiber, 2023). 342

#### Cautionary notes 343

There are inherent features of microbial systems that introduce novel challenges for applying coexistence 344 theory. Moreover, this framework is not a silver bullet for investigating all problems related to species 345 coexistence. As such, awareness of the constraints and limitations in implementing coexistence theory is 346 essential for its effective use in microbial ecology. 347

#### **Empirical challenges** 348

While the fast growth and short generations of microbes are a convenience in many circumstances (see 349 above), they can also present unique challenges for empirical application of coexistence theory. For 350 response surface experiments, where species' densities must be finely controlled (Inouye, 2001), the 351 fast dynamics of microbial systems are potentially prohibitive. It is therefore unsurprising that our 352 systematic review found no studies applying this approach. For mutual invasion tests, where a key 353 assumption is that the resident community is at equilibrium when the invader is introduced, batch 354 culture experiments are inappropriate as they do not allow for community dynamics to establish a stable 355 equilibrium. High-frequency serial transfer, or better still, chemostat systems, should instead be used to 356 ensure that resident communities are indeed at equilibrium (Picot et al., 2023), so that invader growth 357 rates can be accurately estimated. For timeseries approaches in microbial systems, it may be important 358 to consider eco-evolutionary dynamics when fitting population models to estimate species interaction 359 coefficients. Rapid evolution may cause species interactions to change over time and dramatic shifts 360 in population structure of a given species can even occur between different growth stages (Zambrano, 361 Siegele, Almirón, Tormo, & Kolter, 1993). 362

Microbial communities also generally exhibit much higher phylogenetic and biochemical diversity than 363 animal and plant communities (Prosser et al., 2007). While understanding the coexistence of two 364 macroorganisms (e.g., endangered wolves and common coyotes) is often critical for conservation and 365 ecosystem management, it is less common for the coexistence of just two microbial taxa to have significant 366 implications in applied settings (but see, for example, the balance of Bacterioidetes and Firmicutes in the 367 mammalian gut). As such, the diversity of microbial communities may seem at odds with coexistence 368 theory, which has traditionally used species pairs as the focal study unit. Indeed, the concepts of niche 369 and fitness differences were originally formulated for two competitors from the same trophic level, and 370 the limitations of invasion analysis when studying more than two species have long been acknowledged 371 (MacArthur & Levins, 1967; Spaak & Schreiber, 2023). Extensions of coexistence theory to multi-trophic 372 systems, or to systems with three or more competitors from the same trophic level, are therefore at the 373 forefront of theoretical work on coexistence theory (Chesson, 2018; Spaak & Schreiber, 2023; Song & 374 Spaak, 2024; Ranjan, Koffel, & Klausmeier, 2024), and are likely to be important for microbial applications 375 of this framework.

376

High frequencies of non-competitive or context-dependent interactions (Kehe et al., 2021; Momeni, 377 Xie, & Shou, 2017; Kost, Patil, Friedman, Garcia, & Ralser, 2023) are additional features of microbial 378 communities that complicate the application of coexistence theory. Facilitation can be challenging to 379 model with traditional tools (e.g., Lotka-Volterra) and most definitions of niche and fitness differences 380 - including the most popular metrics such as Chesson's classic square root equations (Chesson, 1990; 381 Chesson & Kuang, 2008; Chesson, 2013) and the sensitivity to competition formula of Carroll et al. 382 (2011) – do not account for positive interactions between species (Spaak & De Laender, 2020). However, 383 such interactions are seemingly ubiquitous in microbial communities with ample evidence of cross-feeding 384 (Dal Bello, Lee, Goyal, & Gore, 2021), multi-species biofilm formation (Nadell, Drescher, & Foster, 385 2016), and sharing of antibiotic resistance genes (Ellabaan, Munck, Porse, Imamovic, & Sommer, 2021). 386 Further, interspecific interactions among microbes have been shown to readily switch signs from facilitative 387 to competitive depending on the local environmental context (Hoek et al., 2016; Meroz et al., 2024). 388 Non-competitive interactions are not beyond the scope of coexistence theory – new metrics for niche and 389 fitness differences that can accommodate positive interactions have recently been developed (Spaak & 390 De Laender, 2020; Koffel, Daufresne, & Klausmeier, 2021) – but they are nonetheless difficult to integrate 391 with traditional approaches. Indeed, the sign flexibility of interspecific interactions in microbes merits 392 further study as it may be one pathway from which fluctuation-dependent mechanisms can emerge even 393 in the absence of external environmental variation. 394

#### <sup>395</sup> Limitations and conceptual mismatches

Several of the empirical challenges discussed above can be addressed – at least conceptually – through 396 recent extensions to the original theory. However, there are some limitations of the theory that must be 397 treated with caution. One of the most obvious limitations, which has received considerable attention in 398 the ecological literature, is that invasion analysis does not always predict coexistence. The analytical 399 approaches of applying coexistence theory (Figure 1D and E) are built upon the assumption that mutual 400 invasibility predicts coexistence. However, it is easy to imagine cases where all species can invade but 401 will not ultimately coexist or where not all species cannot invade even if they could all coexist (Barabás 402 et al., 2018; E. Johnson & Hastings, 2022; Clark et al., 2024). Although complex ecological dynamics 403 (e.g., Allee effects) and stochasticity (both environmental and demographic) can break the simple logic of 404 invasion analysis, even in multispecies systems, invasion growth rates have been shown to be broadly 405 informative (Chesson, 2018; Schreiber, Levine, Godoy, Kraft, & Hart, 2023; Clark et al., 2024). 406

Another shortcoming of coexistence theory is the (over)emphasis it has traditionally placed on qualitative 407 (e.g. coexistence vs exclusion), rather than the quantitative, community states. Often, however, relative 408 abundances of coexisting species are an equally, if not more, important response variable (Abrams, 2022). 409 If multiple species coexist but one is far more abundant, the community may function like a monoculture. 410 For instance, lakes dominated by toxic algal blooms often have communities where cyanobacteria, diatoms, 411 and green algae are all coexisting, but where the cyanobacteria dominate by orders of magnitude (Scheffer, 412 Rinaldi, Gragnani, Mur, & van Nes, 1997; Grover, 1997; Jankowiak, Hattenrath-Lehmann, Kramer, 413 Ladds, & Gobler, 2019). Similarly, predicting if a pathogenic microbe can coexist with (or be excluded 414 by) beneficial microbes may not be as useful as predicting the abundance of the pathogen (Letten et al., 415 2021). If the pathogen coexists with the other microbes but is held at low density (i.e., below the minimal 416 infective dose), it may be of no material consequence for the host. Nevertheless, with the data required 417 to evaluate qualitative community states informed by coexistence theory, it is usually always possible to 418 quantify other response variables of interest (e.g. relative abundance at equilibrium, invasion growth rates 419 or time to extinction (Clark et al., 2024)) that may be especially relevant in more applied contexts. 420

421 Finally, common uses of coexistence theory – specifically the quantification of niche and fitness differences

tells us if species coexist but not necessarily how they coexist. Niche and fitness differences summarize 422 the combined effects of many underlying mechanisms, so focusing solely on these properties risks obscuring 423 underlying ecological processes. This is particularly true if phenomenological models (e.g., Lotka-Volterra 424 competition) rather than mechanistic models (e.g., resource-consumer models) are used to estimate niche 425 and fitness differences, which has been the dominant approach of applying coexistence theory to date 426 (Chesson, 2013; Godwin et al., 2020). Indeed, phenomenological approaches, such as the widely-used 427 generalized Lotka-Volterra model, are far more common than mechanistic approaches in the microbial 428 literature (Picot et al., 2023). The field of microbiology, however, has a rich history of precisely identifying 429 and manipulating the biochemical processes underlying an organism's ecology, resulting in the development 430 of metabolic models capable of predicting microbial growth from first principles (Delattre, Desmond-431 Le Quéméner, Duquennoi, Filali, & Bouchez, 2019). Incorporating these more sophisticated models 432 into the coexistence framework will be challenging but likely fruitful, expanding our ability to make 433 mechanistically informed manipulations of diverse microbial systems in applied contexts. 434

## 435 Conclusion

With our systematic literature search finding limited uptake of coexistence theory in microbial ecology to 436 date, we hope that the observations and opportunities outlined in this review can act as stimulus for closer 437 cross-pollination between these two fields. This includes leveraging coexistence theory to foster rigour and 438 conceptual synthesis to the study of coexistence and community assembly in microbial systems, as well as 439 taking advantage of the high-throughput of microbial systems to push the frontier of coexistence theory 440 forward. Echoing broader concerns in microbial ecology (Prosser, 2020), it is of course important that 441 coexistence theory is not merely appended to descriptive studies to provide an illusion of theory-driven 442 research. The ever-expanding framework of coexistence theory will only benefit microbial ecology if 443 it is applied appropriately and is used to inform study design as well as data analysis. Nevertheless, 444 thoughtfully incorporating coexistence theory into microbial ecology offers numerous opportunities to 445 explore new research avenues, driving progress in theoretical and microbial ecology alike. 446

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### **Author Contributions**

JAO, DWA, and ADL conceived the research. JAO performed the systematic review and wrote the first draft of the manuscript with input from ADL and DWA. All authors contributed to the final manuscript.

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# Supplementary Material for

# Coexistence theory for microbial ecology, and vice versa

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## 1 Overview of systematic review

We performed a systematic review to find empirical coexistence theory conducted in microbial systems. First we established three distinct inclusion criteria that a study had to meet in order to be included (Fig. S1). We considered a study relevant if it was primary empirical research and it was conducted in microbial systems and it applied (modern) coexistence theory. We identified relevant studies through previous systematic reviews and by performing our own search of the literature using a machine learning framework for abstract screening (Fig. S2).

The previous systematic reviews that we initially used to identify studies were of: (i) 29 empirical studies where both niche and fitness differences could be quantified (Buche, Spaak, Jarillo, & De Laender, 2022), (ii) 49 empirical studies that empirically applied any form of coexistence theory (Terry & Armitage, 2024), and (iii) 96 empirical studies that generally tested mechanisms of species coexistence (Hawlena, Garrido, Cohen, Halle, & Cohen, 2022). Of the 174 studies identified from previous reviews, 15 studies were potentially relevant based on how they had been labelled by the authors of those reviews (Fig. S2). Six of these studies were excluded at the full text screening stage for not meeting at least one of our inclusion criteria (Fig. S1). The remaining nine studies were included in our systematic review.

Guided by the search terms used by the previous systematic reviews, we then performed our own search of the literature and we used a novel machine learning framework for abstract screening. The methods and results of this AI-aided literature review are outlined below.



Figure S1: Decision tree with our three inclusion criteria. For a study to be included it had to meet all three criteria. This decision tree was also used during abstract screening where "yes" or "maybe" led to a record being marked as (potentially) relevant.



Figure S2: PRISMA-style flow chart summarizing the steps of our systematic review from study identification, to abstract screening to full-text screening, to study inclusion.

## 2 AI-aided literature review

A literature search was performed on *Web of Science* on the  $19^{\text{th}}$  of May 2024 using the following advanced search where a study needed to have a word associated with microbial systems *and* a word associated with modern coexistence theory in either its title, abstract, or keywords:

Web of Science search. TS = Topic (title, abstract, or keyword).

TS = ("microb\*" OR "microorganism\*" OR "bacteri\*" OR "fung\*" OR "yeast\*" OR "alga\*" OR "phytoplankton" OR "diatom\*" OR "cyanobacteria" OR "protozoa" OR "protist\*" OR "ciliate\*" OR "archaea" OR "virus\*" OR "biofilm")

AND

TS = ("coexistence theory" OR "co-existence theory" OR "species coexistence" OR "species coexistence" OR "niche differ\*" OR "fitness diff\*" OR "niche overlap" OR "stabili\$ing mechanism\*" OR "equali\$ing mechanism\*" OR "fitness ratio\*" OR "fluctuation-\*dependent" OR "fluctuation \*dependent" OR "relative non-linearit\*" OR "relative non linearit\*" OR "storage effect\*" OR "lottery effect\*" OR "lottery model\*" OR "invas\* criteri\*" OR "invas\* condition\*")

This broad search returned 2,164 records, including all nine relevant studies that had been identified from previous systematic reviews. We then used a machine learning framework called *ASReview*, where active learning models help to accelerate abstract screening (Van De Schoot et al., 2021). In summary, a human screener will input their unlabelled dataset to the model and they will identify some "training" data (labelled abstracts that are known to be relevant or irrelevant based on prior knowledge). The active learning model then ranks the entire unlabelled dataset in order of relevancy based on the words (or sentences) that are found in the abstracts that were marked by the human as irrelevant or relevant. The paper that the active learning model marks as most relevant is shown to the human screener, who then reads that abstract and uses their inclusion criteria to determine whether to mark it as relevant or irrelevant. The active learning model is then updated based on the decision of the human screener and the order of the remaining records in the unlabelled dataset are updated based on their new relevancy scores. This screening process continues until some *a priori* stopping criterion is met. If the active learning model is working as expected, plotting the number of records screened against the number of relevant records found should return a saturating curve.

This framework requires that all records have abstracts, but there were 16 papers in our search results that did not have abstracts. The full texts of these papers were screened and all 16 were marked as irrelevant. The remaining 2,148 papers were screened using ASReview. The importance of the training data for these active learning models has been shown to be extremely low, given that the models are constantly being updated. Nonetheless, for the relevant training records we chose three studies from the nine relevant studies identified through previous reviews that were diverse in terms of the study organisms and approach of applying coexistence theory (Letten, Dhami, Ke, & Fukami, 2018; Li, Tan, Yang, Ma, & Jiang, 2019; Narwani, Alexandrou, Oakley, Carroll, & Cardinale, 2013), and for the irrelevant training records we randomly selected three records that were confirmed to be irrelevant. Our *a priori* stopping criterion, which was informed by a recent simulation study (Campos et al., 2024), was a combination of time driven and data driven heuristics where screening would stop when at least 20% of the records had been screened and then when the number of records marked as irrelevant in a row equalled at least 5% of the total number of records marked as irrelevant. We used the default active learning model settings (i.e., "Naive Bayes" as the classifier and "Term Frequency-Inverse Document

Frequency" for feature extraction). This combination works well for fields were terminology if well defined (e.g., "niche differentiation" or "temporal storage effect" have very specific meanings) and has been shown to be very efficient and accurate in simulation studies (Van De Schoot et al., 2021; Campos et al., 2024).

By the time our stopping criterion was met, we had marked 50 records as relevant and 399 records as irrelevant. When we stopped the abstract screening process, 65 records had been marked as irrelevant in a row. All nine relevant records from previous studies had been identified during the abstract screening process and the recall curve was clearly saturating (Fig. S3). 1,699 records were automatically excluded as they were not suggested to be relevant by the active learning model before the stopping criterion was met. The 50 records manually marked as relevant progressed to full text screening and all of their full texts were available. Following full-text screening, 38 of these records were excluded (five studies were not empirical, 28 studies did not use coexistence theory, and five studies did not meet multiple inclusion criteria). The 12 studies that passed through full-text screening included the nine relevant studies identified from previous reviews as well as three additional relevant studies (Fig. S2).



Figure S3: Recall curve showing the number of relevant records identified plotted against the number of records screened (green line). The grey line shows the number of relevant records that would have been expected by random sampling of the unlabelled dataset (i.e., traditional abstract screening). The gap between the green and the grey line shows the efficiency of the machine learning abstract screening framework.

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