

1 **Layers of latency in social networks and their implications**
2 **for comparative analyses**

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27

28 **Abstract**

29 Animal social structures are remarkably diverse, encompassing relationships that
30 range from strong, lifelong bonds to weaker, more transient connections.
31 Understanding the drivers of this variation is a key question in behavioural ecology
32 and has been the focus of numerous studies linking social structure to ecological,
33 demographic, and life history patterns within groups, populations, and species.
34 Equipped with this information, researchers are now turning to investigations of
35 social structure that are comparative in nature. However, comparing social networks
36 remains a considerable logistical and analytical challenge. Here, we present the
37 *layers of latency framework*, which outlines how observed social networks are linked
38 to the two underlying latent networks that are of interest for most research questions:
39 the real social network (the actual pattern of social interactions), and the social
40 preferences network driving these interactions. This conceptual framework provides

41 a clear and unified approach to understand *when* and *why* differences in network
42 properties and sampling protocols can introduce discrepancies between observed
43 and latent networks, potentially biasing or confounding statistical inference. We then
44 use this conceptual framework to outline some of the central challenges to
45 comparing animal social networks, focusing on differences between networks in
46 behaviour type, sampling effort, sampling type, network size and network scale. For
47 each of these focus points, we describe why and how they create challenges for
48 comparative analyses, and we suggest potential directions for solutions. The layers
49 of latency framework can help researchers to identify networks and features they can
50 (or cannot) compare. In doing so, this framework facilitates advances in cross-species
51 social network studies with the potential to generate new and important insights into
52 the ecological and evolutionary drivers of variation in social structure across the
53 animal kingdom.

54

55 **Keywords**

56 comparative analysis; network analysis; social network; social system; social
57 evolution; generative models; latent networks; Bayesian methods

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59 **Introduction**

60 The animal kingdom features a remarkable diversity of social systems, from solitary
61 individuals to large cooperative groups (Clutton-Brock, 2016; Rubenstein & Abbot,
62 2017). Yet, our understanding of the ecological and evolutionary causes and
63 consequences of this diversity remains incomplete (Kappeler et al., 2019; Kurvers et
64 al., 2014). Comparing animal populations facing distinct environmental challenges
65 can provide insights into the influence of ecological variables such as predation and
66 food availability on social patterns (Barsbai et al., 2021; Krause & Ruxton, 2002; Lukas
67 & Clutton-Brock, 2018), and reciprocally, how these social patterns impact ecological
68 factors, such as pathogen transmission (Albery et al., 2021; Bansal et al., 2007; White
69 et al., 2017). Comparative analyses can also reveal how social systems evolve
70 alongside life history traits (Silk & Hodgson, 2021) and interact with demographic
71 mechanisms (Clements et al., 2022; Shizuka & Johnson, 2020).

72 As a result of countless long-term efforts to collect social data (Clutton-Brock, 2021;
73 Sheldon et al., 2022), numerous animal social datasets exist, capturing social
74 structure across diverse species and environments. With the emergence of large
75 databases bringing together these data across taxa (e.g. MacaqueNet, De Moor et
76 al., 2023; Animal Social Network Repository (ASNR), Sah et al., 2019; DomArchive,
77 Strauss et al., 2022), attention has turned to the statistical methods with which such
78 datasets can be compared (Albery et al., 2024; Ellis et al., 2021).

79 Comparative social network analysis offers a holistic approach to draw inference
80 about the drivers and consequences of animal social structure (Albery et al. 2023;

81 Croft et al., 2016; Pinter-Wollman et al., 2013; Webber & Vander Wal, 2019). By
82 explicitly representing social structure as an emergent property of social interactions
83 between individuals (Hinde, 1976), social network analysis can be used to ask
84 questions about social evolution at the level of individuals, dyads, social groups and
85 populations. However, despite the value of comparative social network analysis, only
86 a relatively small body of literature compares social networks across species and
87 taxonomic groups (Albery et al., 2024). A major reason for the lack of such studies is
88 the viability of comparing networks that are generated using different
89 methodologies, and that may diverge widely in key properties such as network size
90 and behaviour types (Faust & Skvoretz, 2002; Ogino et al. 2023; Pinter-Wollman et
91 al., 2013).

92 Here, we offer an overview of five key challenges that create disparities between
93 social networks and provide guidance on what to consider when designing
94 comparative analyses to minimise these challenges. A common theme to these
95 challenges is that the observed networks we compare are most often different from
96 the underlying, latent (i.e. unobservable) networks we want to make inferences
97 about. We therefore begin by introducing the *layers of latency framework* that
98 provides a unified representation of how different biological and observational
99 processes interact to influence the social structures we observe. A clear
100 understanding of how these processes contribute to variation in observed social
101 networks will help researchers to make principled decisions on how best to compare

102 networks. While we introduce the *layers of latency framework* in the context of
103 comparing networks, it contains valuable concepts for all social network analyses, be
104 they comparative or not.

105 ***The layers of latency framework***

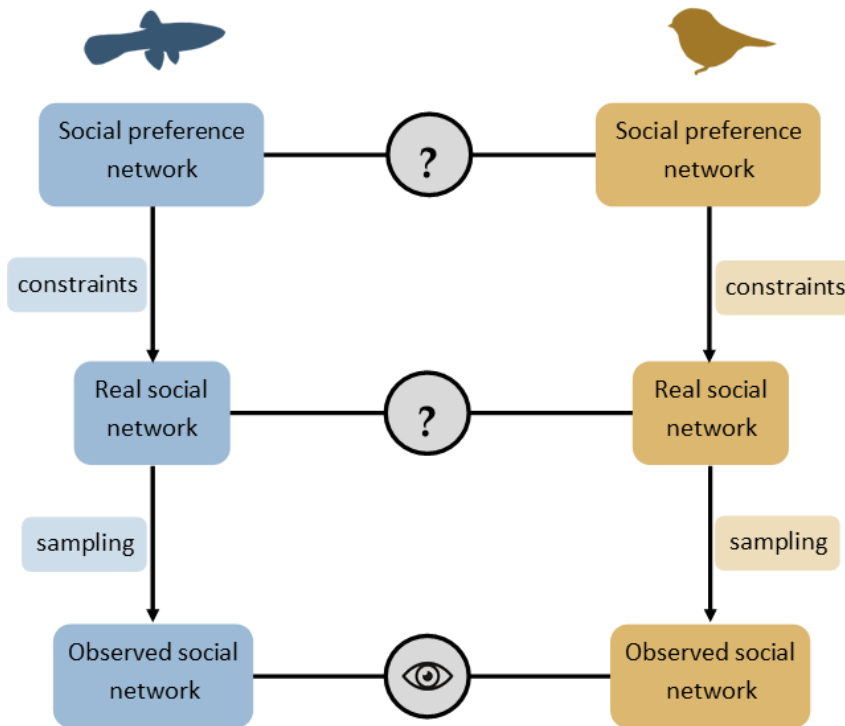
106 One key issue in network analysis is that observed networks often do not directly, or
107 exclusively, correspond to the biological phenomenon of interest. This lack of
108 correspondence is due to two primary reasons. Firstly, the social networks we
109 quantify are usually based on only a subset of interactions – those that have been
110 recorded – and an observed network is therefore an estimation, not exact
111 representation, of the complete or “real” patterning of interactions (Handcock &
112 Gile, 2010). Secondly, even when all interactions that happen in a group are
113 recorded, they are unlikely to correspond directly to individual preferences regarding
114 social partners because of constraints that hinder individuals in realising their
115 preferred relationships. For example, if all individuals in a group prefer high-ranking
116 individuals as partners, only a subset of those individuals may have that preference
117 realised because the time high-ranking individuals have available to socialise is
118 limited (Seyfarth, 1977). Instead, some individuals might end up interacting with their
119 second, third, or even last choice of partner.

120 To provide a structured way of thinking about this, we present the *layers of latency*
121 *framework*, which represents social structure as a hierarchy of networks: an *observed*
122 *social network* to which researchers have access, and two layers of latent networks -

123 the *real social network* and the underlying *social preference network* (Fig. 1). An
124 *observed network* represents a sample of the *real network*. The *real network* is the
125 actual pattern of all interactions or associations between individuals. In turn, the *real*
126 *network* is itself a (likely partial) realisation of the individuals' social preferences.
127 These preferences can also be represented as a network (e.g. a directed network
128 representing the strength of preference that each individual has for others): the *social*
129 *preference network*.

130 Mismatches between an *observed network* and the two latent networks (or indeed
131 between the two latent networks) are the result of two main processes: *sampling*
132 *biases* and *constraints* (Fig. 1). Common examples of *sampling biases* include cases
133 where certain individuals or interactions are better sampled than others (Altmann,
134 1974; Bateson & Martin, 2021). For example, a researcher using biologgers to record
135 proximity between pairs of animals may not be able to afford to put a bilogger on
136 every individual, or a researcher visually observing social interactions cannot
137 simultaneously watch all individuals at once. *Constraints* include factors that prevent
138 individuals from realising their social preferences. These constraints may come from
139 different sources, including incompatible preferences between potential partners,
140 social factors such as dominance structure, and environmental constraints such as
141 spatial distances and barriers in the physical environment (Fisher et al., 2021; Webber
142 & Vander Wal, 2018).

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Fig 1. The *layers of latency framework*. Social structure can be considered a hierarchy of networks: an *observed social network* to which researchers have access, and two layers of latent networks - the *real social network* and the *social preference network*. When we compare networks across species (e.g. here a fish and a bird), we typically compare *observed social networks* (the eye icon), but our research questions typically concern differences between *real social networks* or between *social preference networks* (the question mark icons). To ensure that analyses of the *observed networks* accurately reflect the latent networks of interest, it is important to consider the factors along the path from the relevant question mark to the eye that could result in differences between the *observed* and the *real* and *social preference networks*. This includes accounting for *sampling biases* when the focus is on comparing *real social networks* and accounting for both *sampling biases* and *constraints* when comparing *social preference networks*.

158 Research questions are almost always about the latent network layers rather than the
159 *observed network* (Lundberg et al., 2021). The *social preference network* is usually
160 the level of interest when researchers seek to understand the *causes* of social
161 behaviours, such as how kinship, age and sex impact partner choice, or the role of
162 life history or ecology in shaping the types of social relationships individuals form
163 (Chakrabarti et al., 2020; De Moor et al., 2020; Silk & Hodgson, 2021; Siracusa et al.
164 2022, Smith, 2014; Snyder-Mackler et al., 2016). On the other hand, the *real social*
165 *network* is usually the level of interest for investigations into the *consequences* of
166 social behaviours, such as the influence of social structure on disease or information
167 transmission (Aplin et al., 2012; Collier et al., 2022; Silk & Fefferman, 2021) and on
168 fitness outcomes (Ellis et al., 2017; Ellis et al., 2019; Riehl & Strong, 2018; Sabol et
169 al., 2020; Strauss & Holekamp, 2019). However, analyses are typically run on the level

170 of the *observed network* (Fig 1). Understanding which latent network layer is of
171 interest for a given question, and how an *observed network* relates to that latent
172 layer is therefore essential for reliable social network analyses.

173 ***Challenges of comparative social network analysis***

BOX 1: MOVING BETWEEN LAYERS

Recent developments in Bayesian network analysis provide methods to move between the network layers depicted in Fig. 1 (De Bacco et al., 2023; Hart et al., 2023; Redhead et al., 2023). These generative modelling approaches estimate the latent network layers based on the observed data, while incorporating information about the processes that generate the *observed networks*. This information is used to quantify how well the *observed network* is expected to reflect the underlying latent network, which is translated into uncertainties in the estimated edge weights (Ross et al. 2023). For instance, within the BISO framework (Hart et al., 2023), network metrics are calculated from draws of the Bayesian posterior distribution of the latent *real network* edge weights, while accounting for sampling effort. Doing so generates a posterior distribution of network metric values (instead of a single value, or point estimate), therefore explicitly including uncertainty in the metric estimates, where higher sampling effort leads to narrower distributions. Once network metric posteriors have been generated, they can be passed to downstream statistical analyses thereby carrying uncertainty forward into statistical analyses, such that networks with higher observation effort carry more weight on inference.

These methodological developments hold great promise for comparative social network analysis. They enable researchers to make inferences at the latent network level relevant to specific research questions, while also explicitly accounting for differences between networks that could potentially confound or bias comparisons (Fig 1). However, such models require information on the *generative processes* giving rise to the *observed networks*, which include both biological (e.g., *social preferences* and social and/or physical *constraints* in realising those preferences) and observational (e.g., sampling protocols and effort) factors. Understanding these generative processes is still very much in development in animal social network analysis (Brask et al. 2023; Hobson et al. 2021), and is an area where significant methodological advancements are needed to fully enable reliable comparative social network analysis. The *layers of latency framework* offers a clear and structured approach to understanding these generative processes. It makes explicit how the *observed networks* used in research are generated by underlying *social preferences* and are modulated by *constraints* and *sampling biases*.

174 Comparative social network analysis faces significant challenges due to the variability
175 in how networks are constructed. Networks can be based on different behaviours,
176 sampled using diverse data collection methods with varying degrees of effort, and
177 sampled at different biological scales (Albery et al., 2024; Canteloup et al., 2020;
178 Davis et al., 2018; Faust & Skvoretz, 2002). These differences can create disparities
179 between the *observed networks*, reflecting *sampling biases* and *constraints* rather
180 than true differences, thus confounding comparative analysis (Gagliardi et al., 2023;
181 Ogino et al., 2023).

182 Here, we consider five key challenges in comparative social network analysis:
183 comparing networks that differ in 1) behaviour type, 2) sampling method, 3) sampling
184 effort, 4) network size, and 5) biological scale. We summarise these challenges in
185 Table 1 and discuss in greater detail how these differences introduce *sampling biases*
186 and *constraints*, generating discrepancies between the observed and latent networks
187 and affecting the comparisons of observed networks. Additionally, we provide
188 guidance on how best to handle each of these challenges.

189 While we present these challenges independently here for clarity, it is key to note
190 that these challenges are closely linked (Fig. S2). For example, the size of the *real*
191 *network* (in combination with the research questions being addressed) may influence
192 the scale at which sampling is undertaken, which can then influence the size of the
193 *observed network*.

194 **Table 1:** Summary of five key challenges faced when comparing animal social networks.

Challenge	Description
Behaviour type	Networks vary in the behaviours used to construct them. Whether networks based on different (or the same) behaviours can be compared depends on the biological functions of the behaviours in the given populations and the research question.
Sampling effort	Sampling effort can vary substantially between networks, influencing how reliably an <i>observed network</i> represents the <i>real network</i> . Bayesian models that estimate the <i>real network</i> from observed data can account for sampling effort as uncertainty in the estimated network properties (Box 1).
Sampling type	Networks constructed using various sampling methodologies pose two main challenges: 1) different sampling protocols generate different sampling biases, and 2) how edge weights are quantified may not be directly comparable. Recent methodological advancements, such as mixture models and Bayesian models that estimate the <i>real or social preference network</i> from an <i>observed network</i> while explicitly accounting for sampling type, offer promising solutions (Box 1).
Network size	Networks can vary substantially in their size, which can influence network structure. Whether or not to account for network size depends on whether network size is central to the relationship between network structure and biological variables of interest. If controlling for network size is warranted, doing so correctly can be challenging as it requires knowledge of the generative

	process underlying the network (Box 1), which determines how size impacts the network property of interest.
Network scale	Networks can be sampled at various scales, resulting in <i>observed networks</i> representing different parts of <i>real networks</i> . The scale of sampling significantly influences network structure, making networks sampled at different scales generally incomparable, particularly for global network properties. Bayesian models that impute missing data for networks sampled at smaller scales may provide a solution, but they necessitate an understanding of the generative process underlying the network at the larger scale (Box 1).

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196 1. Differences in behaviour type

197 The first factor determining the comparability of networks is the type of behaviour
 198 used to construct them. For most comparative analysis, networks compared should
 199 be constructed on behaviours with similar biological functions, therefore reflecting
 200 similar *social preferences* or representing *real networks* with similar outcomes. While
 201 it might seem obvious that an affiliation network based on huddling should not be
 202 directly compared to an agonism network based on physical aggression, determining
 203 which behaviours *can* be compared often requires more nuanced considerations. For
 204 example, various behaviours have been used to quantify social relationships in
 205 different studies and species, ranging from direct interactions such as grooming and
 206 allopreening, to spatial associations and co-membership of a group (Webber &

207 Vander Wal, 2019). Whether these behaviours can be considered to represent the
208 same biological function is contingent on the research question and the biology of
209 the study species to be compared (Carter et al. 2015, Farine & Whitehead, 2015). In
210 addition, the same behaviour can serve different functions in different systems and
211 might reflect different information depending on the context. For instance, pairs of
212 animals sitting within a 5m range of one another could be indicative of a close
213 association in wild populations, whereas that same distance might not carry the same
214 information in a captive population where individuals have less space over which to
215 spread.

216 Moreover, behaviours will differ in how strongly individuals are *constrained* in
217 realising their *social preferences*. For example, certain behaviours like sex and
218 grooming are often difficult to direct at more than one partner at a time. In contrast,
219 individuals can sit near or vocalise to multiple partners at once and as such these
220 types of behaviours are likely to be less constrained by limitations related to social
221 preferences. Similarly, environmental constraints are more likely to impact
222 behaviours that involve physical contact than behaviours that do not. Different
223 behaviours are also influenced by *sampling biases* to different extents, so that an
224 *observed network* of one behaviour might better represent the *real network* than
225 another behaviour. Rare or less visible behaviours tend to be more heavily affected
226 by *sampling biases* (Martin & Bateson, 2021). Moreover, the degree of *sampling bias*
227 can vary for the same behaviours depending on the system or context. For example,

228 recording aggression in a terrestrial species may be easier than in an aquatic one.
229 Consequently, a smaller proportion of interactions may be observed for the aquatic
230 species compared to the terrestrial one.

231 *Considerations for comparing networks*

232 Any comparative study whose question depends on comparing 'like to like' will need
233 to carefully evaluate whether the networks are constructed based on behaviours with
234 comparable biological functions and facing similar *sampling biases* and *constraints*
235 in their given context (or whether differences can be accounted for in the analyses).
236 This is important because behaviours should either reflect similar *social preferences*
237 or represent a *real network* with similar outcomes. Determining which behaviour
238 types can be reliably compared is a critical first step in comparative social network
239 analysis, which requires thoughtful consideration tailored to the specific research
240 question and informed by knowledge of the species' biology under study.

241 **2. Differences in sampling effort**

242 Sampling effort can significantly impact how reliably an *observed network* represents
243 the *real network*, with increasing effort improving reliability (Farine & Strandburg-
244 Peshkin, 2015; Franks et al. 2021). Accounting for uncertainty in the estimated
245 network metrics is important for any social network analysis but becomes especially
246 crucial when comparing networks constructed with varying sampling efforts. These
247 networks inherently differ in the uncertainty surrounding their observed edge

248 weights and consequently any estimated network metrics. Failing to account for this
249 uncertainty might lead to wrong conclusions. For instance, in a network constructed
250 based on just one hour of observation, a dyad may appear to spend most of their
251 time together. Yet, this estimate could be a highly uncertain representation of this
252 dyad's edge in the *real network*. Extending to 100 hours of sampling effort would
253 provide a more accurate estimate of the weight of this edge in the *real network* and
254 would lower the level of uncertainty around that estimate. Comparing a low
255 observation effort network to a high observation effort network might falsely suggest
256 that individuals in the low observation network spend more time together compared
257 to those in the high observation network, but in reality the difference is due to
258 sampling effort rather than actual differences in behaviour. One effective solution to
259 address the challenge of variable sampling effort when comparing networks is to use
260 models that estimate the *real network* based on the *observed network* as a latent
261 structure, with an explicit degree of uncertainty (Box 1).

262 *Considerations for comparing networks*

263 When comparing networks, researchers should account for differences in sampling
264 effort, which can strongly impact how well an *observed network* represents the *real*
265 *network*. An effective solution to do so is to consider the *real network* as a latent
266 structure, which is estimated with a degree of uncertainty, determined by the
267 observation effort. Recent frameworks provide tools to estimate the *real network*

268 from an *observed network*, while explicitly estimating uncertainty in the estimated
269 latent network based on sampling effort (Box 1).

270 3. Differences in sampling type

271 Many challenges are associated with comparing networks constructed using different
272 sampling methodologies (Albery et al., 2024). The two we focus on here are
273 differences in sampling protocol and differences in how data are summarised into
274 edge weights.

275 Different sampling protocols can impact how an *observed network* relates to the *real*
276 *network*. Some of the most commonly used sampling protocols include focal
277 continuous sampling (recording social interactions and/or associations, referred to
278 collectively as ‘interactions’ from here on, that include a given individual for a set
279 amount of time), group scan sampling (recording the social interactions of each
280 individual in a group instantaneously at regular time intervals) and gambit of the
281 group sampling (recording group compositions during repeated surveys, where
282 individuals observed in the same group are taken to be associating with each other;
283 Altmann, 1974; Whitehead, 2008). More recently, technologies such as camera traps,
284 biologgers, or drones have been used to observe and record animal behaviour
285 remotely (Webber & Vander Wal, 2019). Each of these sampling protocols have
286 inherent biases in the interactions that are recorded (Altmann 1974). For instance,
287 focal continuous sampling provides rich, detailed data on the focal individual and its

288 social partners for a given time but overlooks social interactions between all other
289 individuals during that time. Similarly, sampling using biologgers is often limited to
290 a subset of individuals in the group because of their high cost and deployment
291 schedules (e.g., not all animals can have a bilogger deployed at the same date).
292 Sampling the whole group at regular time intervals (using scan sampling or camera
293 traps), on the other hand, can capture the overall occurrence of interactions across
294 group members to a greater extent, but misses interactions occurring between
295 sampling intervals.

296 A second challenge is that networks are built based on different measures of edge
297 weights, which are not always directly comparable and can even sometimes
298 represent different aspects of the *social preference network*. Raw data on social
299 interactions typically comes from a count of the number of interactions and/or the
300 duration of each interaction observed (Martin and Bateson, Altmann 1974). Which of
301 these raw data are used is determined, in part, by the selected sampling protocol,
302 although certain protocols permit the collection of multiple types of raw data. Edge
303 weights may then be represented as the rate of social interactions per unit of time
304 (rates, the count of the number of social interactions over observation time), as the
305 proportion of observation time two individuals spend engaged in a social interaction
306 (proportions), or as the likelihood of a social interaction occurring between two
307 individuals within a specific time frame (probabilities, the ratio of samples during
308 which an interaction is recorded over the total samples). Probabilities and

309 proportions are both unitless measurements bound between zero and one. Rates,
310 on the other hand, are the expected number of events per unit time (e.g. associations
311 per hour), with a lower bound of zero and no upper bound. Because the probability
312 of being in a particular state at a point in time is equal to the proportion of time
313 spent in that state, a unit increase in a probability is equivalent to a unit increase in a
314 proportion, allowing direct comparisons between probabilities and proportions, all
315 else being equal. However, comparing probabilities or proportions to rates is not as
316 simple, as there is no natural way to interpret these two distributions of data on the
317 same scale. This also relates to a more conceptual point: how often individuals
318 interact with a given partner (rates), and how much of their social time they spend
319 on a given partner (proportions/probabilities) are meaningful aspects of the *social*
320 *preference network*, which do not necessarily carry the same information (Dunbar,
321 1976). For instance, animals might interact frequently for brief amounts of time with
322 certain types of partners and interact less often but for long amounts of time with
323 others.

324 Selecting an appropriate interaction index can help mitigate issues related to
325 sampling type to a certain extent. Various indices have been devised to address
326 different *sampling biases*, making networks built from different sampling protocols
327 more comparable (Franks et al., 2010). Moreover, some network metrics, such as
328 unweighted network metrics, or metrics that are expressed relative to the mean edge
329 weight of the group, are less sensitive to differences in sampling type. In addition,

330 using a standardisation such as Z-scoring makes edge weights (or derived measures
331 of network structure) interpretable in terms of standard deviations, thereby making
332 rates and proportions/probabilities more comparable. However, these approaches
333 do not account for the different *sampling biases* inherent to these distinct sampling
334 processes, which may introduce disparities between an *observed network* and the
335 *real network*. Nor do they account for how different measures of edge weights might
336 capture different aspects of the *social preference network*.

337 Alternatively, mixture models can be used to identify similar interaction levels in the
338 *observed network*, creating categories of individuals that share strong, intermediate
339 or weak social relationships (i.e. estimating the *social preference network*; Ellis et al.,
340 2021; Weiss et al., 2019). These categories are robust to variation in sampling type
341 and can therefore readily be compared. Finally, the sampling process can be
342 integrated into analytical models that estimate the *real network* based on an
343 *observed network* (Box 1). Bayesian models have been developed to reconstruct
344 latent networks by explicitly incorporating assumptions about how the sampling
345 process impacts the relationship between an *observed network* and the *real* or even
346 the *social preference network* (Young et al., 2020).

347 *Considerations for comparing networks*

348 When comparing networks derived from various sampling methods, two main factors
349 need to be considered: 1) biases in the recorded social interactions due to differing
350 sampling protocols, and 2) differences in how edge weights are measured. Although

351 employing suitable indices and Z-scoring edge weights can alleviate some of these
352 concerns, these approaches do not account for the disparities between an *observed*
353 *network* and the *real* or *social preferences network* that differences in sampling can
354 generate (Fig. 1). Recent methodological advancements, including mixture models
355 and models that estimate the *real network* as a latent structure while accounting for
356 the sampling process offer promising avenues to navigate these challenges
357 effectively (Box 1).

358 4. Differences in network size

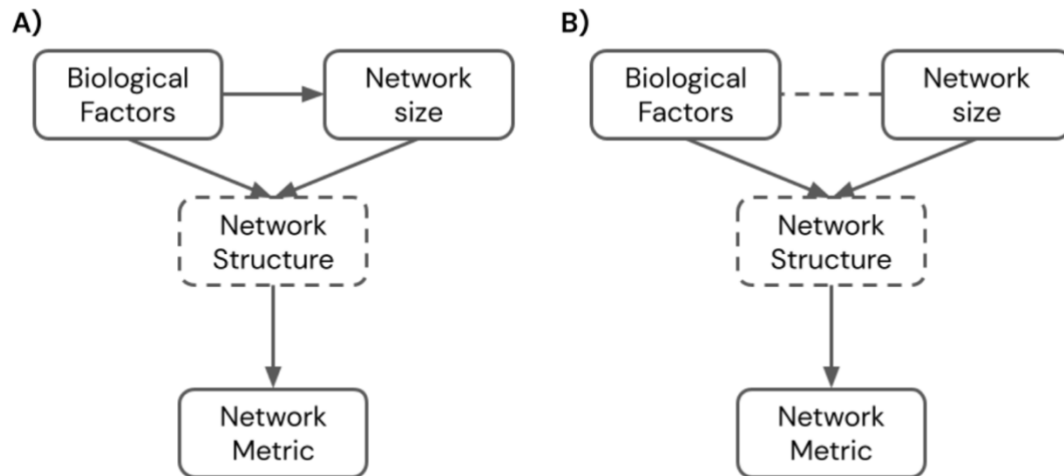
359 Network size, or the number of nodes in a network, varies substantially in animal
360 societies ranging from only a few individuals to large assemblages of several hundred
361 individuals (Webber & Vander Wal, 2019). This variation is shaped in part by
362 differences in social organisation, dispersal patterns, ranging behaviour and/or
363 territoriality (Kappeler, 2019). In addition, *observed networks* can include different
364 subsets of the underlying *real network*, driven by researchers' choices regarding who
365 is observed (for instance focusing only on adults or on habituated individuals).
366 Observed network size therefore depends on the features of the social system being
367 investigated (which determine *real network* size) as well as the decisions made by
368 researchers when designing their study (which determine what subset of the *real*
369 *network* is observed). Here we consider what different network sizes mean for the
370 comparability of network structures. We explore the effects of sampling different

371 subsets of *real networks* in the next section (*Differences in network scale across*
372 *networks*).

373 Comparing networks of different sizes is a complex challenge because network size
374 can greatly influence other aspects of network structure in non-trivial ways. The effect
375 of network size on social structure depends on the nature of the underlying process
376 generating the network (Box 1, Boccaletti et al., 2006; Hobson et al., 2021), and is
377 often not the same for different measures of network structure (Anderson et al.,
378 1999; Naug, 2009). Therefore, controlling for network size (e.g. dividing network
379 metrics by network size, or adding network size as a control predictor in analyses)
380 does not always fully account for size effects, and may even introduce biases.

381 The first question to consider when comparing networks of different sizes is *whether*
382 *it is appropriate* to control for network size. Biological factors may influence key
383 aspects of network structure through their effects on network size (at least in part).
384 Network size can therefore be considered an important feature of social structure
385 itself. For example, if an individual's risk of being infected by a pathogen depends
386 on its number of social partners, then being in a larger group can help explain higher
387 exposure risk. In these cases, conditioning network comparisons on network size
388 would mask effects of biological importance (Fig. 2A). However, for other research
389 questions it may be necessary to condition on network size to make meaningful
390 biological comparisons. For example, to test the hypothesis that forest-living species
391 (typically living in smaller groups) have denser social networks than those in open

392 habitats (typically living in larger groups), conditioning on network size is necessary
393 to demonstrate that habitat influences network structure (density) in a manner that
394 is not solely driven by the relationship between habitat and network size (Fig 2B).

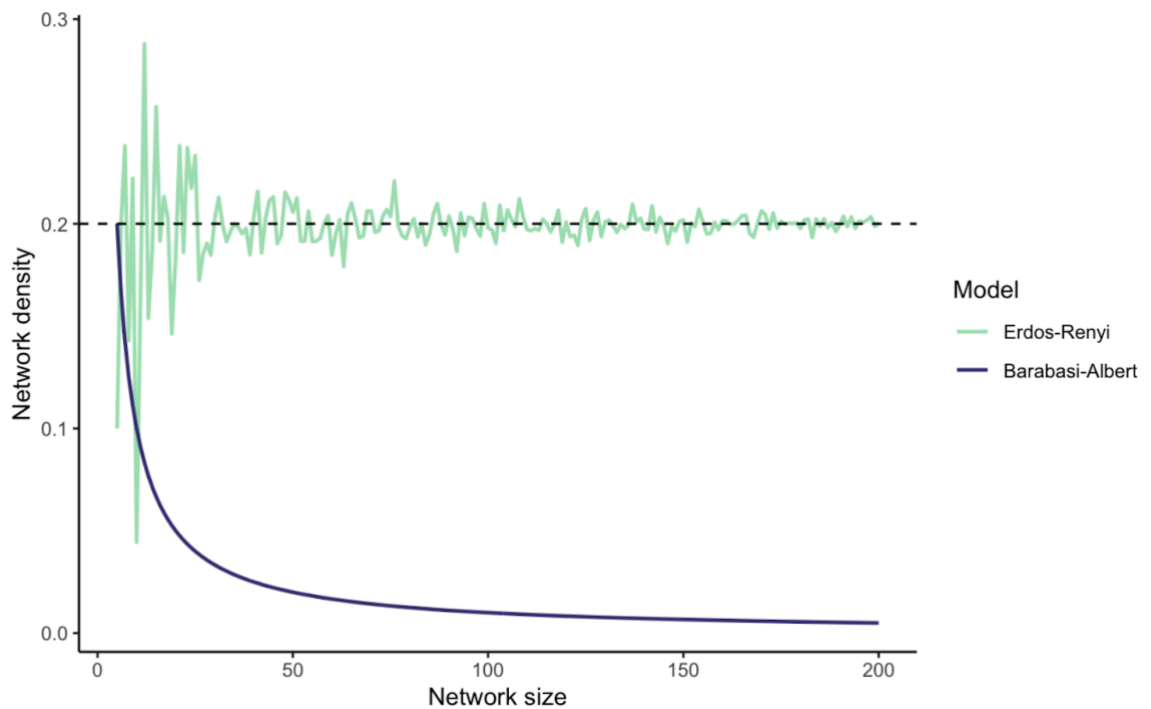


395 **Figure 2: Potential causal mechanisms linking network size to structure.** Note that ‘network’
396 here refers to the *real network* (Fig 1). The solid arrows represent causal relationships. The
397 dashed line between biological factors and network size in panel B indicates a potential non-
398 causal association. The dashed boxes indicate that the structure of the *real network* is a latent,
399 unobservable variable, which can be quantified, but not entirely captured by a network metric,
400 i.e. a measure of network structure. In A, biological factors affect network structure partially
401 via network size, and controlling for network size would mask some of the influence of
402 biological factors on network size. In B, biological factors do not influence network size, but
403 through exogenous variables, biological factors and network size may be correlated. Unless
404 network size can be effectively controlled for, the overall impact of biological processes on
405 network structure cannot be estimated, as network size is a possible confound. In both cases,
406 potential confounds act on the network structure itself, not on the network metric. As long as
407 the chosen network metric is an accurate quantification of network structure, potential
408 challenges do not lie with the metric, but with underlying causal assumptions.

409

410 The next question to consider is *how to control* for differences in network size. Even
411 when controlling for network size is appropriate for a specific question, doing so in
412 a way that correctly removes size effects can be difficult. The relationship between
413 size and network structure depends on the process that generates the network, and
414 these processes are often unknown (Box 1, Brask et al. 2023). For instance,
415 unweighted network density (the ratio of actual to potential connections in a
416 network) is divergently impacted by network size, depending on the process that
417 generates the network (Fig. 3). If individuals choose their interaction partners at
418 random with a fixed probability, then network density stays the same regardless of
419 the size of the network. In contrast, if individuals preferentially interact with their
420 most popular groupmates and each individual forms a fixed number of relationships,
421 then the density of the network declines exponentially with its size. Similarly, the
422 strength of social relationships can depend on network size in different ways. If
423 individuals get more partners when the network is larger but are restricted in the
424 amount of time they have available to socialise, relationship strength will decrease
425 with network size. In contrast, relationship strength can be independent of network
426 size if individuals keep a constant number of partners regardless of network size, or
427 if they get more partners and also increase the amount of time they spend socialising
428 (so that they can spend the same amount of time with each of their partners even
429 when their number of partners increases). Each of these scenarios require different

430 approaches to correctly remove the effect of network size (Hobson et al., 2021). That
431 is, if the networks to be compared have emerged from different generative
432 processes, then correctly controlling for size may involve a different control
433 procedure for each network.



434
435 Figure 3: Measures of network structure can be influenced by network size in different ways,
436 depending on the underlying processes that generate the network. In this example we compare
437 how unweighted network density depends on network size for networks generated from two
438 different processes. If individuals choose their interaction partners at random ('random
439 attachment', captured by the Erdős-Rényi model, Erdős & Rényi 1959) with a fixed probability
440 (e.g. each pair of individuals has a 20% chance of interacting) then the network density stays the
441 same regardless of the size of the network. In contrast, if individuals preferentially interact with
442 their most popular groupmates and each individual contributes with a fixed number of edges
443 ('preferential attachment', captured by the Barabási-Albert model, Barabási & Albert 1999), then
444 the density of the network declines exponentially with its size.

445 Properly accounting for network size in comparative network analysis is often
446 difficult, if not impossible, unless valid assumptions are established about the
447 underlying processes that generate the network (Hobson et al. 2021). Understanding
448 *generative processes* in animal social networks is an area that still needs substantial
449 methodological progress (Box 1, Brask et al. 2023), but one where the *layers of*
450 *latency framework* may be particularly helpful. By explicitly considering the *social*
451 *preferences* driving a given network, we can better understand the expected
452 relationship between network size and relationship strength within the system. This
453 in turn, can inform the design of simulations to predict how network structure varies
454 with changes in size and guide decisions on whether and how to account for network
455 size in subsequent analyses.

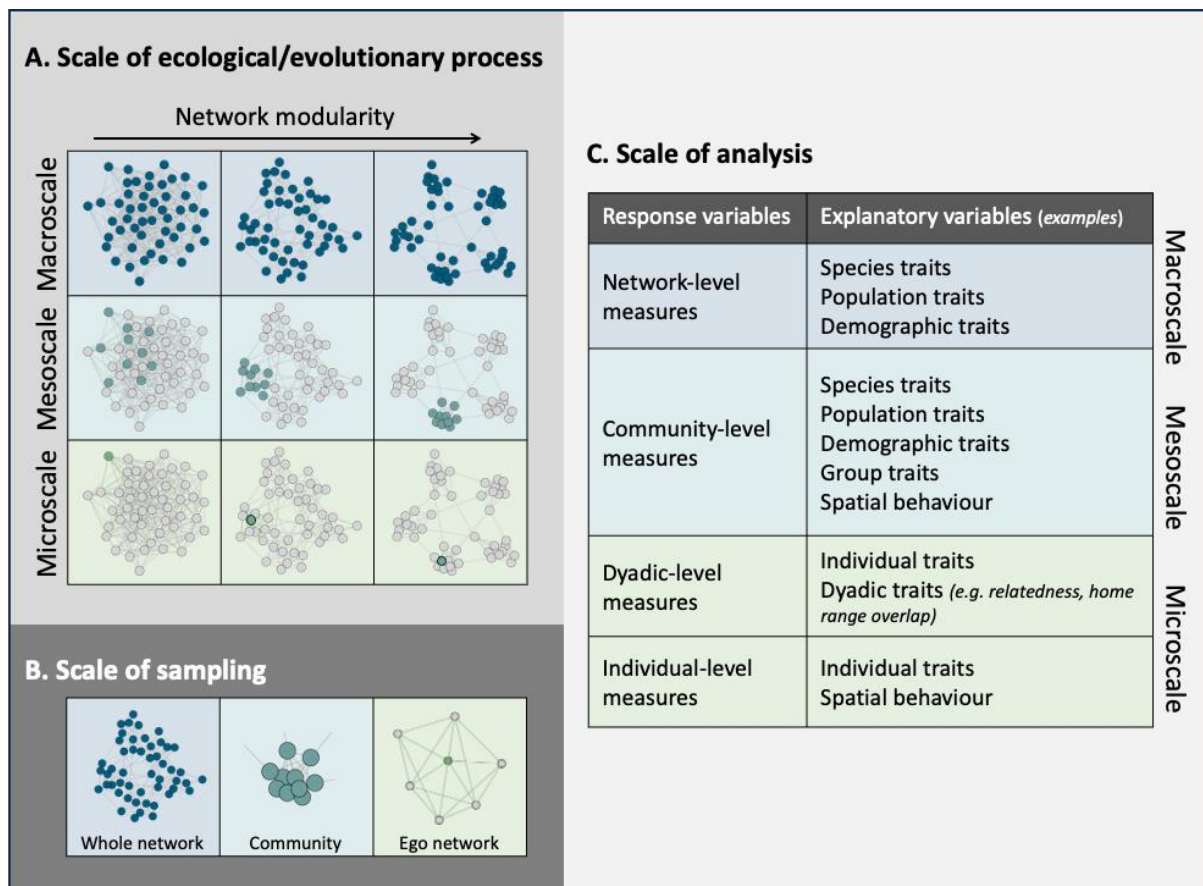
456 *Considerations for comparing networks*

457 When comparing networks, differences in network size are almost inevitable.
458 Whether and how to account for differences in network size is a long-standing
459 challenge in network science, and solutions are often context-dependent. When
460 network size is central to how network structure relates to biological variables of
461 interest, conditioning on network size could mask important effects. When biological
462 factors do not directly influence network size, or when biological effects that go
463 through network size are not of interest, conditioning on network size is warranted.
464 To condition properly requires an understanding of the *generative processes* (i.e. the
465 *social preferences* and *constraints*) underlying the networks, to understand the

466 relationship between network size and measures of network structure (Box 1). As this
467 information is often absent, we suggest restricting comparisons to networks of similar
468 size, or where it is reasonable to assume similar underlying *generative processes* and
469 similar relationships between network size and other components of network
470 structure.

471 5. Differences in network scale

472 Networks can be studied at different social and spatial scales, depending on the
473 ecological or evolutionary process of interest and limitations in data collection. For
474 instance, in some cases a single group may be studied, in others the entire
475 population. As a result, *observed networks* can represent samples of the *real network*
476 at different scales, which can introduce biases in comparative analyses if they are not
477 conducted with appropriate caution (Fig. 4).



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Figure 4. An illustration of the challenges of scale in social network analyses. A. Social network analyses address diverse questions related to various ecological and evolutionary processes for which different scales of network structure are important. Networks can vary considerably between species across these scales. For instance, in species that cluster into groups, network modularity (illustrated), is higher at the population-level (macroscale) than the group-level (mesoscale). B. Research teams make decisions about the scale at which to sample networks based on biological properties of their study system, their research question and time and budget constraints. C. Research teams make decisions about the scale of analysis, focusing on measures that may capture the structure of their sampled network as a whole down to measurements that quantify the network position of single individuals. Any mismatches in the scales at which networks are sampled can generate challenges for subsequent comparative analyses.

491 The extent to which comparing across network scales poses a challenge depends on
492 the scale of analysis required to answer the question of interest (Fig. 4). Measures of
493 network structure that are being compared can vary from measures of the
494 connectedness of individuals (microscale), to measures of the structure of the whole
495 network (macroscale). Meso- and macroscale (whole) network metrics are likely to be
496 particularly susceptible to differences in the scale of sampling between datasets
497 (Ogino et al. 2023). For example, comparing network density (a macroscale measure)
498 from a single social group with that of an entire population can be misleading
499 because the scale of observation affects network density. Individuals within a single
500 group are typically more strongly connected to each other, leading to higher density,
501 while a population-level network includes multiple loosely connected groups,
502 resulting in lower overall density. In contrast, microscale (individual-level) metrics of
503 networks are often less affected by scale and will be more reflective of values in the
504 *real networks* (including non-sampled individuals). However, this will vary according
505 to the *generative processes* underlying the network structure and the specific choice
506 of individual-level metric. For example, in species where individuals interact with
507 others outside their group, an individual will have much higher betweenness
508 centrality when a population- rather than group-level network is considered.

509 In some cases, it may be possible to compare networks sampled at different scales
510 by sub-sampling from the network sampled at a larger scale. But this process is
511 untested and fraught with complex decisions on how best to subsample (e.g., see

512 the previous section *Differences in network size across networks*). Another potential
513 solution is to estimate the *real network* as a latent structure from an *observed*
514 *network* by using imputation to “fill in” missing parts of networks sampled at a
515 smaller scale (Box 1, Young et al., 2020). Doing so requires information about the
516 *generative processes* underlying the network, which currently are not well developed
517 (Box 1). For example, in many studies focused on within-group networks, interactions
518 with members of other groups may not be recorded or may occur so infrequently
519 that they remain unobserved. This means we know little about the *social preferences*
520 and *constraints* generating networks beyond the scale of the group. In these cases,
521 it would be impossible to reliably infer the *real network* beyond the scale of the
522 original study.

523 *Considerations for comparing networks*

524 Networks can be sampled across various scales, and *observed networks* representing
525 different scales usually cannot directly be compared. One solution is to use
526 methodological advancements that can impute missing data to reconstruct the *real*
527 *network* at a larger scale. However, reliable imputation requires an understanding of
528 the *generative processes* underlying the networks, including the processes that drive
529 interactions beyond the scale that was sampled (Box 1). As this understanding is most
530 often lacking, we suggest comparisons be restricted to cases where it is reasonable
531 to assume networks have been sampled at a similar scale.

532 Discussion

533 Comparative social network analysis offers huge potential to answer fundamental
534 questions in ecology and evolution, but this approach comes with a set of major
535 challenges that are yet to be fully resolved (Albery et al., 2023). In this paper, we
536 present the *layers of latency framework* that explains how observed animal social
537 networks are related to the latent social structures and processes of interest to
538 researchers. We then outline five key challenges in comparative analyses of social
539 networks. Using the *layers of latency framework* as a base, we consider how these
540 challenges can lead to erroneous conclusions, and we discuss the current state of
541 solutions to mitigate these challenges. By doing so, we have aimed to offer guidance
542 on factors to consider before embarking on comparative social network analyses and
543 to inspire further developments of methodological tools that enable these types of
544 analysis to be conducted robustly and to their full potential.

545 In addition to giving potential solutions for each specific challenge in the sections
546 above, our summary of our overall current guidance for comparative network analysis
547 is:

- 548 • Identify the latent network layer to which your research question applies (Fig.
549 1) - are you interested in the *real network*, or the *social preference network*?
550 This will shape your analytical decisions going forward.

- 551 • Be clear about the limitations of any approach used. Different networks may
552 have been affected by different inherent *constraints* and *sampling biases*, and
553 this can influence observed differences between them.
- 554 • Consider whether and how differences between networks to be compared
555 can be addressed analytically. Bayesian methodological developments offer
556 promising solutions, by estimating the *real*, or even the *social preference*
557 *network*, while explicitly accounting for key differences in compared networks
558 (Box 1). Maintain uncertainty when moving between network layers, and
559 propagate this uncertainty into subsequent comparisons.
- 560 • Consider the *generative processes* that link the latent networks to the
561 observed network for different sampling methodologies and/or datasets (Box
562 1). Understanding these processes can help identify how to account for
563 methodological differences to make different networks comparable or can
564 help (careful) imputation of missing information.

565 The *layers of latency framework* highlights future theoretical and methodological
566 work that will be central to facilitating analyses that make inferences about latent
567 network layers (both for comparative network analyses and more generally). Moving
568 between network layers necessitates detailed knowledge of the key processes that
569 influence the emergent structure of animal social networks (Box 1). While such
570 knowledge is available for some particularly well-studied species, a combination of
571 theoretical modelling and empirical analyses will often be necessary to identify

572 patterns that can be used to pinpoint the generative processes underlying animal
573 social networks. New statistical tools will then be required to efficiently estimate the
574 latent networks, as well as to tailor existing observation models (e.g. from capture-
575 recapture models) to social network contexts (Silk & Gimenez, 2023). These steps
576 forward will benefit greatly from interdisciplinary collaborations between behavioural
577 ecologists, statisticians, and network scientists (Brask et al., 2021).

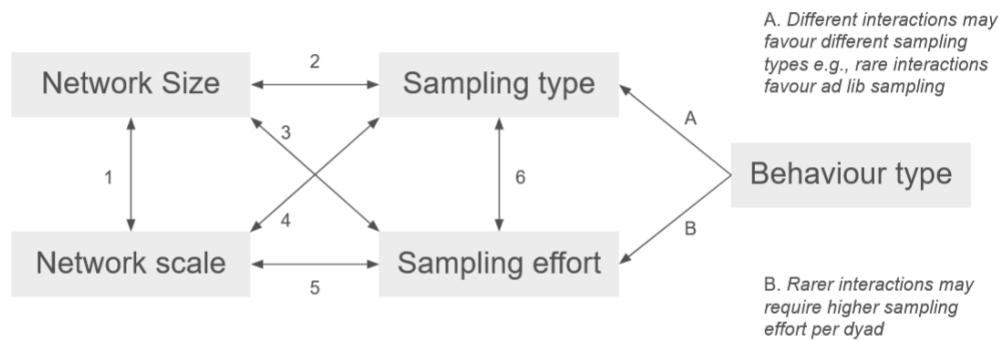
578 We hope the challenges and potential solutions presented here will help to move
579 the field towards a more comprehensive suite of tools for comparing social networks.
580 With further development, comparative social network analysis could become an
581 accessible, reliable and powerful approach to answer long-standing questions in
582 ecology and evolution. We hope that this paper provides a better understanding of
583 the key challenges facing researchers applying these approaches, and some
584 potential ways to address them. Good luck!

585

1. Large real networks might be sampled at smaller scales. Sampling more groups will likely lead to larger sampled networks

2. Some sampling types allow larger sampled networks than others e.g., scan versus focal sampling; pit tags (cheap) versus GPS (expensive)

3. Sampling at lower effort per dyad could allow more nodes to be sampled and so a larger sampled network



4. Cost effective, low-intensity and/or biologist sampling types will often lead to networks sampled at larger scales. Questions posed at larger scales require such methodologies.

5. Sampling fewer groups will likely lead to reduced sample effort per dyad (and vice versa)

6. Sampling type will lead to differences in sampling effort per dyad, e.g. scan vs. focal sampling; GPS tracking vs. behavioural observations. Required sampling effort may inform how to sample.

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587 Figure S2. Links between the five key challenges faced when comparing social networks

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