Open integrated distance sampling for modelling age structured population dynamics

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10 Abstract

- 11 Estimation of abundance and demographic rates for populations of wild species is a
- 12 challenging but fundamental issue for both ecological research and wildlife management. One
- 13 set of approaches that has been used extensively to estimate abundance of wildlife populations
- 14 is Distance Sampling (DS) for line or point transect survey data. The first implementations of
- 15 DS models were only available as closed population models, and did not allow for the
- 16 estimation of changes in abundance through time. The advent of open population
- 17 formulations based on the DS framework greatly extended the scope of the models, but much
- 18 untapped potential remains in models that estimate temporal dynamics not only in abundance
- 19 but also in the underlying demographic rates. Here, we present an integrated distance
- 20 sampling approach that utilizes age-structured survey data and auxiliary data from marked
- 21 individuals to jointly estimate population density and the demographic rates (recruitment
- 22 rate and survival probability) that drive temporal changes in density. The resulting model is
- 23 equivalent to an integrated population model with a two age classes: juveniles and adults. The
- 24 integrated framework allows making full use of the available data by effectively combining
- 25 line transect and telemetry data, and can easily be adapted to include additional and/or
- 26 different data types. Moreover, as demographic rates often respond to environmental
- 27 variation, our approach also supports direct estimation of the effects of such environmental
- 28 covariates on demographic rates. Through a comprehensive simulation study we show that
- 29 the model is able to adequately recover true population and vital rate dynamics. Subsequent
- 30 application to data from a study of willow ptarmigan (Lagopus lagopus) in Norway showcases
- 31 the frameworks ability to recover both fluctuations and trends in population dynamics and 22 highlights its potential applies bility to a wide range of maximum during distances.
- 32 highlights its potential applicability to a wide range of species surveyed using distance
- 33 sampling approaches.
- 34

35 **1. Introduction**

- 36 Estimating abundance and demographic rates for wildlife populations is an integral part of
- 37 basic and applied ecology (Skalski, Ryding, and Millspaugh 2005; Williams, Nichols, and
- 38 Conroy 2002). Over the last few decades, tremendous progress has been made towards this
- 39 end. This progress is partly driven by development and application of new field data
- collection methods and approaches, such as citizen science data (Danielsen et al. 2022). 40
- 41 camera trap data (Hamel et al. 2013) and the collection of environmental DNA data (Beng
- 42 and Corlett 2022). In addition, developments of novel statistical methods alongside
- 43 decreases in computational costs now allow researchers to estimate abundance and
- 44 demographic rates in situations where it was not feasible before (Zipkin et al. 2021).
- 45 Combined, these advances put us in a much better position for estimating quantities needed
- for population management (Williams, Nichols, and Conroy 2002) and indices relevant for 46
- 47 large scale policy applications, e.g. Essential Biodiversity Variables (Kissling et al. 2018).
- 48 Until recently, joint estimation of population dynamics and demography has relied mostly
- 49 on data from marked individuals and associated open-population capture-mark-recapture
- 50 models (Schaub and Kéry 2021). While such methods can provide valuable information for
- 51 both ecological research and management, collecting the necessary data is typically costly
- 52 and logistically challenging to implement over large areas. Monitoring programmes
- 53 focusing on abundance trends over larger areas, on the other hand, are typically based on
- 54 data from unmarked animals. One often used approach for such surveys is distance
- 55 sampling (DS). DS has been used for estimating animal abundance in a wide range of
- 56 contexts and for a variety of taxa (Buckland et al. 2015). One reason for the method's
- popularity is that it requires neither marking of individuals nor repeated visits to the same 57 58 sites for estimating detection probability. This makes DS particularly useful for
- 59
- implementation in participatory monitoring programs, allowing stakeholders to take part in
- 60 the data collection process.
- 61 Classical implementations of DS models have used closed-population formulations,
- i.e. models that treat estimates of population density or abundance at different time points 62
- 63 as independent and do not including an explicit formulation of the process model that links
- abundance across years based on estimates of population growth rate (λ) or underlying 64
- demographic rates (Buckland et al. 2015). In recent years, DS approaches have been 65
- 66 extended in many ways, including applications that estimate changes in abundance over
- time in open populations via a hidden state model representing population dynamics 67
- (Moore and Barlow 2011; Sollmann et al. 2015; Schaub and Kéry 2021). This has greatly 68
- 69 extended the potential of DS approaches for studying ecological dynamics across time and
- 70 space. However, while these latter frameworks may allow to accurately quantify population
- changes, they typically provide little information on the drivers of these changes, i.e. the 71 72 underlying vital rates. In fact, if the data does not contain information about the age (and/or
- 73 sex-) structure of the surveyed population, there is no straightforward way to estimate
- 74 demographic rates from such data. On the contrary, if age (and sex) of detected individuals
- 75 can be determined, this information can be used to provide information on recruitment
- rates and survival probabilities. Nilsen and Strand (2018), for example, used a model based 76
- on harvest statistics and observations of population age structure to estimate population 77

- abundance and demographic rates without the need for any additional data from marked
- 79 individuals.
- 80 Concurrent with the development of more sophisticated DS models, another group of
- 81 models has emerged and rapidly gained popularity, not least for their ability to disentangle
- 82 demographic processes underlying population dynamic: integrated population models
- 83 (IPMs, Schaub and Kéry 2021). Through joint analysis of multiple datasets (or multiple
- 84 components of the same dataset), IPMs allow simultaneous estimation of population size
- and composition, as well as all vital rates that form part of an underlying age- or stage-
- 86 structured population model. Since both DS models and IPMs estimate population
- 87 size/density, a combination of the two frameworks has the potential to provide good
- estimates of both population- and demographic parameters by maximizing knowledge
 gained from transect surveys by augmenting them with other available data (e.g. Schmidt
- 90 and Robison 2020).
- 91 In this study, we present a new integrated distance sampling model (IDSM) which
- 92 integrates data from line transect distance sampling survey data and survival data from
- 93 marked animals. The model's core is a stage-structured matrix population model that
- 94 projects population size from one time step to the next based on underlying survival and
- 95 recruitment rates. We first present the model and assess its robustness and performance
- 96 through applications to simulated data. By doing so, we showcase how distance sampling
- 97 models can be used to not only estimate population density but also demographic rates in
- 98 an IPM setting. Finally, we proceed to highlight the potential of this new modelling
- 99 framework by applying it to a case study involving data collected on willow ptarmigan
- 100 (Lagopus lagopus) in Central Norway.
- 101

102 **2. Methods**

103 2.1 Integrated distance sampling model

104 Our open population integrated distance sampling model (IDSM) consists of two major

- 105 components: a latent structured population model and a set of likelihoods for data
- 106 originating from distance sampling surveys and auxiliary survival monitoring of marked
- 107 birds. In the example case, these auxiliary data come from a radio-telemetry study, but in
- 108 principle other types of capture-recapture data can also be used.

109 2.1.1 Age-structured population model

- 110 The population model follows a post-breeding census and includes two age classes:
- 111 juveniles (young of the year) and adults (> 1 year of age, Figure 1). This structure
- 112 commonly used for populations of passerine and game birds (Williams, Nichols, and Conroy
- 113 2002; Schaub and Kéry 2021). In the context of our willow ptarmigan case study (see
- below), the population census is set in late summer which is when the annual distance-
- sampling survey takes place. At this time, the juvenile class is about 1 2 months old.
- Both juveniles and adults survive from year *t* census to year t + 1 census with survival
- 117 probability S_t . We assume that individuals can reproduce already as 1-year olds, meaning
- all survivors may produce offspring in late June which recruit into the population as
- juveniles just prior to the census in year t + 1 according to a recruitment rate R_{t+1} . The
- 120 changes in densities of juveniles and adults in the population, D_{juv} and D_{ad} , can thus be
- 121 expressed as

122
$$D_{juv,t+1} = D_{ad,t+1} * R_{t+1}$$
$$D_{ad,t+1} = S_t * (D_{juv,t} + D_{ad,t})$$

123 or, alternatively, in matrix notation as

124
$$\begin{bmatrix} D_{juv,t+1} \\ D_{ad,t+1} \end{bmatrix} = \begin{bmatrix} S_t * R_{t+1} & S_t * R_{t+1} \\ S_t & S_t \end{bmatrix} \begin{bmatrix} D_{juv,t} \\ D_{ad,t} \end{bmatrix}$$

125 Note that recruitment rate *R* is defined as juveniles/adult (not juveniles/female). We

126 assume no stochasticity beyond time-variation in vital rates in the model for population

127 density itself, but instead treat local population sizes (numbers of birds in age class *a* in

- 128 year *t* within the area of each transect *j*, $N_{a,j,t}$), as outcomes of a Poisson process with an
- expected average equaling $D_{a,t}$ times the transect area (see below). We also make the
- 130 simplifying assumption that there is no age- or sex-dependence of vital rates, but this
- assumption could be relaxed by including additional auxiliary data (Israelsen et al. 2020;
- 132 Sandercock et al. 2011).



Figure 1: Graphical representation of the annual ptarmigan life cycle with two age classes under a post-breeding census and the data sources included in the integrated distance sampling model. Solid arrows represent relationships within the ptarmigan life cycle; dotted arrows visualize information flow from data sources to parameters. Blue and pink data nodes originate from distance sampling and line transect surveys, respectively. Juvenile_t = juveniles in year t. Adult_t = adults in year t. R_t = recruitment rate in year t. S_t = survival probability from year t to t + 1.

133 2.1.2 Likelihoods for distance sampling data

134 The implementation of the modelling framework we present assumes that the distance

- 135 sampling survey data have the following characteristics: 1) the survey consists of line
- transects, 2) animals may be detected alone or in groups, and 3) juveniles and adults can be
- 137 distinguished during surveys. These characteristics are inspired by our willow ptarmigan
- 138 case study (details below). Our model includes three likelihoods for different components
- 139 of the age-structured distance sampling data. First is the likelihood for the perpendicular
- 140 detection distances from line transect, *y*, which are linked to distance-dependent detection
- 141 probability p_y through a half-normal detection function:

142
$$p_y = exp\left(-\frac{y^2}{2\sigma^2}\right)$$

- 143 where σ is the half-normal detection parameter. We assumed σ to vary among years (index
- 144 *t*) but not between transect lines or animal group sizes. Following Moore and Barlow
- 145 (2011), the resulting σ_t can be used to calculate effective strip width (*esw*_t) and,

146 consequently, average detection probability per line transect with a truncation distance W147 according to:

$$esw_t = \sqrt{\frac{\pi * \sigma_t^2}{2}}$$
$$\widehat{p}_t = esw_t/W$$

- 149 The estimated average detection probability \hat{p}_t is an integral part of the second data
- 150 likelihood which relates the observed number of animals in each age class *a*, $obsN_{a,j,t}$ (*j* =
- 151 transect) to the corresponding true number per transect, $N_{a,j,t}$:

152
$$obsN_{a,j,t} \sim Poisson(\hat{p}_t * N_{a,j,t})$$

153 $N_{juv,j,t}$ and $N_{ad,j,t}$ are then linked back to the population model by converting them to

- 154 densities through multiplication by $2L_{j,t}W$ (where $L_{j,t}$ is length of transect *j* in year *t*, and 155 *W* is the truncation distance).
- 156 The third data likelihood focuses on the counts of adults ($obsAd_{i,t}$) and juveniles ($obsJuv_{i,t}$)
- 157 observed during the distance sampling surveys and links them to the estimated year-
- 158 specific recruitment rate:

148

- 159 $obsJuv_{i,t} \sim Poisson(\widehat{R_t} * obsAd_{i,t})$
- 160 2.1.3 Likelihood for radio-telemetry data
- 161 The final likelihood is for the auxiliary telemetry data. It is set up under the assumption of 162 perfect detection, and hence known fates, of animals bearing transmitters and links the
- 163 numbers of animals released at the start of season k of year t to the number of survivors at
- 164 the end of the same season:
- 165 $survivors_{k,t} \sim Binomial(released_{k,t}, \widehat{Sk}_t)$
- 166 Here, Sk_t is the survival probability over the relevant time interval k in year t. The length 167 and definition of k will be specific to any given study. For the remainder of this article, we 168 define k as 6-month seasons to be consistent with our ptarmigan case study. Consequently, 169 the annual survival probability, S_t that appears in the population model above is calculated
- 169 the annual survival probability, S_t that appears in the population mode 170 as the product of two seasonal survival probabilities, $S1_t$ and $S2_t$.
- 171 2.1.3 Hierarchical models with time-variation in parameters
- 172 Vital rates (survival probabilities S_t , recruitment rates R_t) and detection parameters (half-173 normal detection parameters σ_t) can all be modelled as time-dependent in our framework.
- For both the tests with simulated data and the case study described below, we implemented
- 174 For both the tests with simulated data and the case study described below, we implemented 175 log-normally distributed random year effects on recruitment rate and detection probability.
- 176 In the case study, we additionally included a covariate effect (see details below) on log
- 177 recruitment rates, resulting in the following model:

178
$$log(R_t) = log(\mu_R) + \beta * cov_t + \epsilon_t$$

- 179 μ_R represents the mean recruitment rate if the covariate cov_t is centered around 0 (e.g. z-
- 180 standardized) or a baseline recruitment rate corresponding to $cov_t = 0$ if the covariate is
- 181 not centered. β the slope of the covariate effect, and ϵ_t the normally distributed random
- 182 effects.
- 183 In both simulations and the case study, we treated survival as time-invariant. This was
- 184 motivated by our case study: previous research has relatively low interannual variation in
- survival of our focal ptarmigan population (Israelsen et al. 2020) and the telemetry data
- 186 used in this study has limited potential for accurately estimating time-variation as it is
- 187 relatively sparse. We note, however, that also survival could be modelled as time-
- 188 dependent if sufficient data is available.

189 2.2 Model testing with simulated data

- 190 We assessed the model's overall performance and ability to estimate abundance,
- 191 demographic rates, and detection parameters without bias by testing it on simulated data.
- 192 We generated a total of 10 simulated datasets in five steps. First, we simulated 15-year
- 193 time-series of survival and recruitment rates from biologically plausible values for averages
- and in the case of recruitment among-year variation in demographic rates (survival was
- held constant across years). Second, we used the yearly demographic rate and realistic
- initial population densities to simulate stochastic population dynamics in 50 distinct sites.Third, we simulated the grouping of individuals in each site by first determining the
- 197 Find, we simulated the grouping of individuals in each site by first determining the 198 expected number of groups in a site (based on the average group size of 5.6 from our
- 199 ptarmigan data) and then distributing individuals among groups via multinomial trials.
- 200 Fourth, we assigned a distance from transect line to each group and simulated the line
- transect survey in all 50 sites across 15 years. Finally, we simulated 5-year time-series of
- radio-telemetry data (= survival from one year to the next) for a subset of individuals (30
- 203 per year on average) using the simulated survival probabilities for each relevant year. We 204 then fit the IDSM to each of the 10 simulated datasets three times, using distinct seeds for
- both simulating initial values and initiating and running the MCMC. Model implementation
- 206 for simulated data tests was largely identical to that for real data and is described in detail
- 207 below. For assessing model performance, fit, and bias, we 1) compared model estimates to
- the true values of parameters used for data simulations visually, 2) correlated estimated
- and true values, and 3) calculated two metrics to measure bias: the proportion of samples
- above the true value (corresponding to Bayesian p-values) and the root-mean squaredeviation (RMSD).

212 2.3 Case study

- To demonstrate the applicability of the IDSM to real data, we applied it to a case study of
- willow ptarmigan, a small grouse species with a has a circumpolar distribution (Fuglei et al.,
 2020). In Norway, there has been a long-term decline in willow ptarmigan abundance
- across more than a century (Hjeljord and Loe 2022), but in the last few decades abundance
- 216 across more than a century (njenoru and Loe 2022), but in the last lew decades abundant 217 trends have fluctuated substantially both across time and space. Willow ptarmigan is a
- valued game species (see e.g. Andersen et al. (2014)), and there have been several long-
- term research projects devoted to understanding how they respond to environmental
- variation and harvest management (Israelsen et al. 2020; Sandercock et al. 2011). A key

- insight from across several study areas is the the annual recruitment rate (i.e. R_t in our
- 222 model, as outlined above) is highly variable, and is affected both by spring conditions
- 223 (Eriksen et al. 2023) and the abundance of small rodents, which constitute alternative prey
- for common predators (i.e. the Alternative Prey Hypothesis; see Hagen (1952); Kausrud et
- al. (2008); Bowler et al. (2020)). Adult survival show less inter-annual fluctuations
- (Israelsen et al. 2020), although variation due to e.g. harvest management is evident when
- comparing across studies (Israelsen et al. 2020; Sandercock et al. 2011).
- 228 Our case study was based on an ongoing long-term research project on willow ptarmigan in 229 Lierne municipality in Central Norway (approximately 62.4 degrees north and 13.2 degrees
- 230 east). The study area is located in a sub-alpine ecosystem, and the landscape is a mosaic of
- 231 open heath and shrub vegetation (dominated by Ericacea, willow shrub *Salix spp.*, and
- 232 dwarf birch *Betula nana*), interspersed with bogs and forest patches (mainly birch *Betula*
- *spp.*). The climate is strongly seasonal, with snow typically covering the ground from
- 234 October/November through April/May.
- From this study system, two datasets were used for the case study:
- 2361.Data from a line transect survey program targeting willow ptarmigan operated237under the natural resources management authorities (2007-2021, ongoing)
- 238 2. Data from an individual-based monitoring programme based on radio collared
 239 willow ptarmigan (2015-2021, ongoing)
- 240 Line transect survey data were collected in August each year, prior to the annual autumn 241 harvest season, as part of the program "Hønsefuglportalen". Hønsefuglportalen is a national 242 program for line transect surveys of tetraonid birds, and the effort is directed mainly 243 towards willow ptarmigan habitats. In our case study, we used data from the western part 244 of Lierne municipality. Line transects are surveyed by trained volunteers that use pointing 245 dogs to locate the birds. When located, the geographical coordinate, perpendicular distance from the sampling line, the number of birds in the group, as well as the age (juvenile or 246 247 adult) and sex of the birds are recorded. As the surveys are conducted in early August, 248 juveniles can be distinguished from adults by their smaller body size. Males and females are 249 mainly distinguished by sound (males often make a characteristic sound when being 250 flushed). Observers are trained to distinguish age classes and sexes, but incomplete 251 identification can occur. In this application we assumed that the resulting "unknown" age 252 and/or sex class birds were in fact juveniles (see discussion for further considerations). 253 Besides bird observations, field workers also record whether (1) or not (0) they encounter 254 small rodents on any transect line, allowing the proportion of transect lines with small 255 rodent detection to be used as measure of rodent occupancy (covariate ranging from 0 to 256 1). After data are collected they undergo quality control, get standardized based on the Darwin-Core standard (Wieczorek 2012), and made publicly available as a sampling-event 257 258 data set published through GBIF (Nilsen et al. 2023). For additional description of the data 259 collection procedures, see (Bowler et al. 2020; Kvasnes, Pedersen, and Nilsen 2018; Nilsen 260 et al. 2023).
- The radio-telemetry data is the result of an individual-based longitudinal study over the period 2015-2021. Each winter (in February-March), willow ptarmigan were located at

- 263 night using snowmobiles and large hand nets with prolonged handles, as described in
- 264 (Israelsen et al. 2020). High-powered head lamps were used to dazzle the birds and allow
- 265 capture. Captured birds were fitted with a uniquely numbered leg ring (\sim 2.4g) and a
- 266 Holohil RI-2BM or Holohil RI-2DM radio transmitter (~ 14.1g) and subsequently released.
- The radio transmitters had an expected battery lifetime of 24 months (RI-2BM) or 30
- 268 months (RI-2DM), and included a mortality circuit that was activated if a bird had been
- 269 immobile for 12 hours. We monitored the birds throughout most of the year by
- triangulation from the ground at least once a month for 10 months of the year (February –
- November) by qualified field personnel. A number of birds dispersed out of the main study areas and was thus out of signal range for field personnel on the ground. To avoid loss of
- 272 areas and was thus out of signal range for neid personnel on the ground. To avoid loss of 273 data, we conducted aerial triangulation using a helicopter or airplane three times a year
- 274 (May, September and November) in the years 2016-2020. In the analysis here, we assume
- that the telemetry data is representative for the entire duration of study period (2007-
- 276 2021), despite its collection only starting in 2015.

277 2.4 Bayesian model implementation

- 278 We implemented the model in a Bayesian framework using NIMBLE version 1.0.1 (Valpine
- et al. 2017) in R version 4.3.1 (R Core Team 2023). The likelihood for line transect
- 280 observation distances was set up using a custom half-normal distribution developed by
- 281 Michael Scroggie as part of the "nimbleDistance" package
- 282 (https://github.com/scrogster/nimbleDistance). We used non-informative uniform priors
- 283 (with biologically reasonable boundaries where possible) for all parameters. We assumed
- constant survival and time-varying recruitment rate in models fit to both simulated and realdata.
- For the model fits to simulated and real data we ran 3 (simulated) or 4 (real) MCMC chains
- with NIMBLE's standard samples for 100k iterations. 40k thereof were discarded as burn-in
- prior to thinning with factor 20, leaving us with 3k posterior samples per chain (total of 12k
- samples per run). MCMC parameters were chosen to yield a representative number of
- samples from converged chains, and convergence was determined based on visual
- 291 inspection of trace plots. Posterior samples from the model fitted to real data are available
- at Nilsen and Nater (2024) (in folder PosteriorSamples_LierneCaseStudy).
- 293

294 **3. Results**

295 **3.1 Model performance on simulated datasets**

296 Models fit to simulated datasets reached MCMC convergence within the given number of

- iterations. Chain mixing was good for all parameters except average recruitment rate (μ_R);
- for this parameter, an elevated degree of autocorrelation was visible in the MCMC chains in
- some of the replicate runs, but models still produced posterior distributions that well
- 300 represented the true value used in simulations (Figure 2).
- 301 Posterior estimates relative to true values, Bayesian p-values, and RMSD for parameters
- 302 estimated in three model fits to each of 10 simulated data sets are shown in Figure 2 and
- Figure 3. Overall, the IDSM was able to correctly estimate the majority of parameters from
- all 10 simulated datasets without substantial systematic bias. The replicate runs for each
 dataset resulted in very similar posterior distributions, demonstrating that the models
- 306 converged towards the same posterior distributions irrespective of starting values. This
- 306 converged towards the same posterior distributions irrespective of starting values. This 307 may not seem to be the case for survival parameters (Figure 2), but this is largely due to the
- relatively low number of individuals in the simulated telemetry data; estimated posteriors
- 309 match up well with simulated numbers of survivors in each datasets, and the averages of
- 310 Bayesian p-values fell very close to 0.5 (= no bias). For time-variation in recruitment rate
- 311 (σ_R) , on the other hand, the average Bayesian p-value indicated a potential for
- 312 overestimation (p = 0.6966667), and this is consistent with the relatively large spread of
- Bayesian p-values for year-specific recruitment rates (Figure 3). Across all years, the
- 314 correlation between predicted and true recruitment rates was very high (slope = 0.981), yet
- closer inspection showed that slight over- and under-estimation was present for certain
- 316 years across all replicates (see supplementary figures in folder SimCheck_byDataSet in
- Nilsen and Nater (2024)). This was also the case for year-specific estimates of population
- 318 density and detection probability, but both were slightly more likely to be underestimated
- than overestimated (Figure 3).



Figure 2: Vital rate and detection parameter averages estimated from 10 distinct sets of simulated data (= colors) using three model fits each. First row depicts posterior densities from each model run relative to the true value used to simulate data (black dashed line). Second and third rows visualize the distributions of Bayesian p-values (proportion of samples > true value) and root-mean square deviations (RMSD) for all model runs, respectively. Purple lines and numbers mark the mean values across all model runs; dashed black line (second row only) marks the ideal Bayesian p-value of 0.5.



Figure 3: Annual population density (D_t) , detection probability (p_t) , and recruitment rate (R_t) estimated from 10 distinct sets of simulated data (= colors) using three model fits each. First row depicts the relationship between posterior medians from each model run and the true value used to simulate data (purple solid line = relationship estimated from linear model with a = intercept and b = slope; black dashed line = perfect correlation). Second and third rows visualize the distributions of Bayesian p-values (proportion of samples > true value) and root-mean square deviations (RMSD) for all model runs, respectively. Purple lines and numbers mark the mean values across all model runs; dashed black line (second row only) marks the ideal Bayesian p-value of 0.5. And equivalent figure showing posterior samples instead of posterior means is available in the supplementary material on OSF.

321 **3.2** Case study on willow ptarmigans in Central Norway

- 322 Having evaluated the overall performance of our model on simulated data, we used data
- 323 from our case study in Lierne to estimate abundance, vital rates and detection probabilities
- from a real-world data set. Like the model fits to simulated data, convergence was reached
- within the fiven amount of iterations and mixing was good, albeit with somewhat higher
- 326 chain autocorrelation for the intercept in the recruitment model. Ptarmigan population
- 327 density was estimated with a marked increase across the study period, from < 10 ptarmigan

- 328 $/ km^2$ in 2007 to > 35 ptarmigan $/ km^2$ in in 2021 (Figure 4). The increase was most 329 distinct from 2016 and onward.
- 330 The average probability of detecting individuals and groups of ptarmigan within transect
- 331 line areas was 0.61 (95% C.I = 0.57 0.65), and estimated with a detection decay parameter
- 332 σ of 95.3 (95% C.I = 82.18 110.43). Detection probabilities were highest in the start of the
- study and in the period 2016-2019 and lowest from 2010-2012. The relationship between
- detection probability and distance and changes in detection over time are visualized in
- 335 supplementary figures "DetectionProb_distance.png" and "TimeSeries_pDetect.png" in
- 336 Nilsen and Nater (2024).



Figure 4: Estimated density of willow ptarmigans in Lierne from 2007 to 2021. Solid line represents the posterior median, ribbon marks 95% credible interval.

- Average survival probability for August January (S_1) was estimated at 0.46 (95% C.I = 0.42
- 338 0.5) while average survival probability for February July (S_2) was estimated as 0.64
- 339 (95% C.I = 0.59 0.7) (Figure 5 A). Annual survival probability *S*, given by the product of S_1
- 340 and S_2 , was estimated at 0.3 (95% C.I = 0.29 0.31), Figure 5 A).
- 341 Recruitment (R_t) was allowed to vary across years (see model specification), and estimates
- 342 displayed large inter-annual variability (Figure 5 C, Figure S1). While the mean (baseline)
- recruitment μ_R was estimated as 2.7 (95% C.I = 2.3 3.2) the yearly recruitment rates
- 344 ranged from 1.2 in year 2012 to 4.9 in year 2007.
- Given the available data, the IDSM was not able to estimate a clear effect of small rodent
- 346 abundance on ptarmigan recruitment (slope-paramater for the z-standardized rodent
- 347 occurrence data = 0.062 ; 95% C.I. = -0.2 0.31, see supplementary figure "Rep_betaR.R.png"
- in Nilsen and Nater (2024)).

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Figure 5: Posterior densities of A) seasonal survival, B) average annual survival, and C) recruitment rate. For the latter, the yellow distribution is for the intercept, representing a baseline recruitment rate when rodent occupancy is low. The turquoise distributions are for year-specific estimates or recruitment rate, with darker colors indicating later years. For a visualization of the time-series of recruitment rates, see supplementary figure "TimeSeries_rRep" on OSF.

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350

351 **4. Discussion**

352 We developed an integrated population model that jointly analyses line transect distance

- 353 sampling survey data and data from marked individuals to estimate population abundance,
- 354 survival probabilities, and recruitment rates over time. We first used simulated data to
- examine the model's ability to recover the underlying parameters when they were known.
- We then fitted the model to data from an ongoing field study on willow ptarmigan in
- 357 Norway to showcase its applicability to real wildlife monitoring data.
- 358 Open population formulations of the distance sampling model have previously been
- 359 presented and applied to various ecological systems(Sollmann et al. 2015; Bowler et al.
- 360 2020; Moore and Barlow 2011). The model presented here extends those previous
- 361 applications by formulating the underlying population process model as a stage-structured
- matrix model (Caswell 2000) in which the matrix elements are represented by annual
- 363 survival probabilities and recruitment rates. While this has been the common approach for
- a range of other statistical modelling frameworks, including the growing suite of models
- falling into the category of integrated population models (Schaub and Kéry 2021), the
- integration of mechanistic population models into distance sampling frameworks is rathernew. The resulting modelling framework allow us to make maximum use of distance
- new. The resulting modelling framework allow us to make maximum use of distance
 sampling data in combination with auxiliary information both from the distance sampling
- 369 survey itself (i.e. information on age, sex, etc. of observed animals) and from other types of
- 370 monitoring, and enables estimation not only of changes in population density but also of
- 371 underlying vital rates over time.

In general, the model did a good job at recreating the underlying parameters when fitted to 372 373 simulated data with known underlying true parameter values. The simulated data sets were 374 based relatively wide ranges of parameter values, yet model posteriors included the true 375 values in almost all cases. While there seems to be potential for overestimating time 376 variation in recruitment rates, this bias did not propagate into estimates of year-specific 377 recruitment rates (Figure 3), and may be related to the subpar mixing of the intercept of the 378 recruitment model. The model was more likely to under- than overestimate detection 379 probabilities and population densities, but bias in these estimates was generally small and 380 spread out across time-series, i.e. bias did not seem to arise disproportionately at e.g. the 381 starts or ends of time-series. Simulated data tests also revealed that telemetry data 382 simulated with an average of 30 individuals may be too sparse to obtain robust and 383 generalisable estimates of seasonal survival probabilites. This could be investigated further by repeating simulated data runs with different average numbers of individuals in the 384 385 telemetry data, but we chose not to go down this path here as we were primarily interested 386 in model performance given the amounts of data that are currently available for our 387 ptarmigan case study. Based on the simulated data tests presented here, we conclude that 388 the IDSM is able to provide meaningful and sufficiently accurate and robust estimates of 389 demographic parameters from age-structured distance sampling data, provided that the 390 input data are unbiased (with respect to the underlying model formulation).

Real data, however, are likely to be subject to certain biases, which may result in biased
 parameter estimates unless accounted for. One type of bias that is likely to be common for
 age-structured distance sampling data arises from failure to (correctly) classify the age

394 class of observed individuals. In our case study on willow ptarmigan in Norway, such 395 misclassification is likely to happen at an unknown rate, even if the size difference between 396 adult and juvenile birds are quite substantial during the survey. Moreover, The probability 397 for misclassificiation might be related to both the timing of the survey (e.g. mid August 398 rather than early August), it might vary between observers, and even by survey conditions. 399 Observations with incorrectly classified age have the potential to introduce bias in the IDSMs relative estimates of survival and recruitment. This is due to the way it uses the 400 401 distance sampling data to estimate survival and recruitment rates. In our process model. 402 the population growth rate (λ) is determined by the survival and recruitment rate in the 403 following way: $\lambda = S + (S * R)$, and this creates a dependence between the demographic parameters. If the age ratio in the data are biased or contain frequent misclassifications, this 404 405 is likely to affect the relative contribution of survival and recruitment to the growth rate. To 406 get an idea of the potential effect of this on parameter estimation, we checked the 407 sensitivity of the output of the model fit to real data with regard to the treatment of birds 408 classified as "unknown sex and age" by the field personnel (see Methods). In the model 409 version presented in the results section, we made the assumption that these birds were in fact juveniles. Comparing estimates to an alternative scenario in which we discarded all 410 411 birds classified as "unknown sex and age" (see supplementary figures in Nilsen and Nater 412 (2024)) we found that – as expected – estimated population density was virtually 413 unaffected by the treatment of "unknown sex and age" observations, while the annual 414 demographic parameters shifted proportional to the amount of "unknown sex and age" 415 observations in the given year (towards higher recruitment and lower survival). Thus, biases in the reported age ratios may affect estimated of demographic rates, but not so 416 417 much population density. Since the proportion of "unknown sex and age" observations in 418 our ptarmigan case study was low (< 3% of observations), potential biases in estimates 419 resulting from age misclassification are expected to be small. Nonetheless, future 420 developments of the IDSM modelling framework should focus on ways of accounting 421 explicitly for misclassification of age class in the field.

422 The density estimates that we derived from the case study on Willow ptarmigan in Norway 423 is comparable to previous estimates from across Norway (see e.g. Sandercock et al. (2011); Kvasnes, Pedersen, Solvang, et al. (2014)). Throughout the study period from 2007 - 2021, 424 425 the density increased markedly, but the reason for this increase is not known. Compared to 426 previous studies on ptarmigan (see e.g. (Israelsen et al. 2020; Sandercock et al. 2011)), we could have expected somewhat higher estimates of survival probability. One potential 427 428 reason for the overall lower estimates obtained here is that our IDSM analysis assumed 429 constant survival over the period 2007-2021 while survival, in reality, may have changed 430 over time. If survival in more recent years, when telemetry data was collected (and the 431 study of e.g. Israelsen et al. (2020) was carried out) was higher than in earlier years -432 something that seems likely given population increase over recent years - an average over the entire time period is expected to be lower. On a different note, we can also not exclude 433 434 the possibility of a small degree of bias in survival estimates due to misclassification of age 435 in the data (see above), especially seeing as the IDSM's recruitment rate estimates also appear somewhat high compared to other studies on willow ptarmigan (Eriksen et al. 2023; 436 437 Kvasnes, Pedersen, Storaas, et al. 2014; Steen et al. 1988). As the ptarmigan case study 438 served as an illustrative example for the IDSM framework in this article, we did not further

439 investigate alternative models, such as implementations with time-varying survival or

440 different treatment of uncertainty in age and/or sex. The model lends itself easily to such

441 extensions, however, and methods such as posterior predictive checks and WAIC will be

442 useful for assessing and optimizing the fit of the model to data from relevant case studies

443 (Hooten and Hobbs 2015; Conn et al. 2018).

444 In addition to estimating demographic rates from line transect data, the IDSM also allows 445 including relevant environmental effects on the demographic rates themselves, and not just on population growth rate as a whole (λ). In the ptarmigan case study we thus attempted to 446 447 investigate the effect of small rodent abundance (approximated as the proportion of 448 transect lines on which rodents were reported each year) on recruitment rate. We were not 449 able to detect a clear effect of rodent abundance due to large uncertainty associated with 450 the estimate (see Supplementary Figures "Rep_betaR.R.png" in Nilsen and Nater (2024)). 451 This may seem somewhat surprising given that such a pattern has been reported repeatedly in the literature (see e.g. Bowler et al. (2020)). We speculate that there are at 452 453 least three potential and not mutually exclusive explanations to this result. The first is that 454 our covariate data may not have been well suited for estimating effects on recruitment. The data on rodent abundance was heavily zero-inflated, and the annual variation in the index 455 456 was rather small otherwise, making for a covariate with relatively little information 457 content. While this may be partially a consequence of how these data are collected, it is also 458 well known that the amplitude and regularity of the rodent cycles has been fading in recent 459 decades (Kausrud et al. 2008; Cornulier et al. 2013), and our study area might be no exception. Lack of peak rodent years in the time series to which we fitted the model may 460 thus also have contributed to making effect estimation challenging. Second, it is possible 461 that rodent effects were obscured by other, potentially stronger, covariate effects. Previous 462 463 research has shown that ptarmigan recruitment is also sensitive to the weather in the late 464 winter and spring (before and during the breeding season); as we did not fit any weather covariates to the model, there is a possibility that effects of spring conditions in certain 465 466 vears may have masked any remaining effects of small rodent abundance. Finally, the data 467 set used in this analysis is relatively short (15 years), leaving us with somewhat limited 468 statistical power to detect effects of temporal covariates. Taken together we therefore do not consider this study as a particularly strong test of the underlying effect of small rodent 469 470 fluctuations on ptarmigan recruitment rates. It is worth noting that future applications 471 could increase statistical power by including either more years of data or capitalizing on space-for-time substitution as the Norwegian ptarmigan monitoring programme spans 472 473 many more locations beyond Lierne. Bowler et al. (2020), for example, used data from the 474 same sampling program but from more areas using a simpler open population DS model. 475 and detected a very clear signal from small rodent abundance on ptarmigan population 476 growth rate. An extension of our IDSM to include data from multiple areas therefore 477 constitutes a promising approach for investigating to which extent similar results emerge by linking environmental covariates to the actual demographic rates and not only just to the 478 479 resulting population growth rates.

480 The new IDSM framework presented here is relevant for many wildlife populations that are

- 481 surveyed using line transect sampling that includes additional information on age, sex,
- 482 and/or life stages of the observed individuals. Following the integrated modelling

- 483 philosophy, the IDSM also allows for the integration of auxiliary data. In our application
- 484 here, we integrated data from radio-telemetry of marked birds, which explicitly supported
- the estimation of survival probabilities. The IDSM framework is very flexible, however, and
- 486 open to the inclusion of additional/other auxiliary data that contains information on
- 487 demographic rates or population size/density. Moreover, the hierarchical nature of the
- 488 model makes is straightforward to adapt to different species and to include different suites
- of environmental covariates on the demographic rates. Finally, it constitutes a modelling
 framework that is well suited for extension to multiple areas and thus able to capitalize on
- 490 Inamework that is wen suited for extension to multiple areas and thus able to capitalize on 491 space-for-time substitution (Lovell et al. 2023) to produce large-scale and spatially explicit
- 492 estimates of population density, demographic rates, and environmental effects from large-
- 493 scale (participatory) monitoring.
- 494 Author contributions
- 495 Erlend B. Nilsen: Conceptualization, Methodology, Software, Formal analysis, Investigation,
- 496 Data Curation, Writing Original Draft, Writing Review & Editing, Project administration,
 497 Funding acquisition.
- 498 Chloé R. Nater: Conceptualization, Methodology, Software, Validation, Formal analysis,
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- 511 Conflict of interest disclosure
- 512 The authors declare that they comply with the PCI rule of having no financial conflicts of
- 513 interest in relation to the content of the article
- 514 Data and code availability
- 515 The raw data from the line transect surveys is deposited on GBIF and can be accessed freely
- 516 via the Living Norway Data Portal (https://data.livingnorway.no). The work here is based
- 517 on version 1.7 of the dataset "Tetraonid line transect surveys from Norway: Data from
- 518 Fjellstyrene" (Nilsen et al. 2023).

- 519 The auxiliary radio-telemetry data and rodent occupancy data, all code used for wrangling,
- 520 analysing, and visualizing data and results, as well as vignettes providing rich text
- 521 documentation of all steps in the workflows for simulated and real data analysis, can be
- 522 found in the project's repository on GitHub:
- 523 https://github.com/ErlendNilsen/OpenPop_Integrated_DistSamp. The results presented in
- this paper were created using version 1.5 of the code (Nater et al. 2024).
- 525 Supplementary figures and posterior samples from the model run on the real data are
- 526 available as a time-stamped open archived on Open Science Framework (Nilsen and Nater 527 2024).
- 528
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