Detecting context-dependence in the expression of life history tradeoffs

Louis Bliard [1 *], Jordan S. Martin [2 *], Maria Paniw [1,3], Daniel T. Blumstein [4,5], Julien G.A. Martin [6], Josephine M. Pemberton [7], Daniel H. Nussey [7], Dylan Z. Childs [8], Arpat Ozgul [1]

1 Department of Evolutionary Biology and Environmental Studies, Zurich University, Zurich, Switzerland

2 Institute of Evolutionary Medicine, Zurich University, Zurich, Switzerland

3 Department of Conservation Biology, Estación Biológica de Doñana (EBD-CSIC), Seville, Spain

4 Department of Ecology and Evolutionary Biology, University of California Los Angeles, Los Angeles, California, USA

5 The Rocky Mountain Biological Laboratory, Crested Butte, Colorado, USA

6 Department of Biology, University of Ottawa, Ottawa, Ontario, Canada

7 Institute of Ecology and Evolution, University of Edinburgh, Edinburgh, UK

8 Department of Animal and Plant Sciences, University of Sheffield, Sheffield, UK

* Shared first authorship

Corresponding author: bliard.louis@gmail.com / louis.bliard@uzh.ch

Abstract

Life history tradeoffs are one of the central tenets of evolutionary demography. Tradeoffs, depicting negative covariances between individuals' life history traits, can arise from genetic constraints, or from a finite amount of resources that each individual has to allocate in a zero-sum game between somatic and reproductive functions. While theory predicts that tradeoffs are ubiquitous, empirical studies have often failed to detect such negative covariances in wild populations. One way to improve the detection of tradeoffs is by accounting for the environmental context, as tradeoff expression may depend on environmental conditions. However, current methodologies usually search for fixed covariances between traits, thereby ignoring their context dependence. Here, we present a hierarchical multivariate 'covariance reaction norm' model, adapted from Martin (2023), to help detect context dependence in the expression of life-history tradeoffs using demographic data. The method allows continuous variation in the phenotypic correlation between traits. We validate the model on simulated data for both intraindividual and intergenerational tradeoffs. We then apply it to empirical datasets of yellow-bellied marmots (*Marmota flaviventer*) and Soay sheep (*Ovis aries*) as a proof-of-concept showing that new insights can be gained by applying our methodology, such as detecting tradeoffs only in specific environments. We discuss its potential for application to many of the existing long-term demographic datasets and how it could improve our understanding of tradeoff expression in particular, and life history theory in general.

Introduction

Demographic tradeoffs, which are characterized as negative covariances between fitness components such as somatic or reproductive traits, are central to life history theory (Stearns, 1989), and are thought to constrain and organize much of the life history diversity that exists (Bielby et al., 2007; Healy et al., 2019; Salguero-Gómez et al., 2016; Stearns, 1984). They originate from the basic fact that the total amount of resources or energy acquired by any one individual is limited, and has to be shared among several of the individual's fitness-related traits. In such a zero-sum game and in the absence of change in the total amount of resources acquired, any increase in the allocation of resources towards a specific fitness component will have to be at the expense of another fitness component. While tradeoffs stem from individual processes, these covariances can scale up to different levels of organization (Agrawal, 2020; Bliard et al., 2024). If tradeoffs did not exist, selection would maximize all fitness-related traits simultaneously and would lead to the impossible "darwinian demons" (Law, 1979). Therefore, tradeoffs should be faced by all organisms and are, in theory, ubiquitous (Stearns, 1989, 1992; Williams, 1966). They can come in several forms (Stearns, 1989), being either intraindividual (traits involved relate to the fitness of the same individual) or intergenerational (traits involved relate to the fitness of a parent-offspring pair; e.g., offspring quantity-quality tradeoff). Despite their expected universality and being sought-after by evolutionary ecologists and biodemographers alike, life-history tradeoffs have been surprisingly hard to detect in wild populations (Chang et al., 2023; Metcalf, 2016; van Noordwijk & de Jong, 1986), with successful probes too often confined to experimental approaches.

Several reasons could explain why tradeoffs are hard to detect in wild populations. First, we often expect traits to covary in a simple bivariate manner following the Y-model of resource

allocation, where any resources diverted from a trait will be allocated to the other one (de Jong & van Noordwijk, 1992). Thus while we are often analyzing a single pair of traits at a time, tradeoff structures are often more complex. For instance, many more than two traits are likely to be involved in the resource allocation process (Cressler et al., 2017; de Jong, 1993; Pease & Bull, 1988), sometimes leading to complex hierarchical allocation trees, potentially resulting in some pairs of traits not covarying negatively (Gascoigne et al., 2022). Second, life history traits can covary at different levels. While tradeoffs result from individuals' resource allocation processes, biodemographers often study tradeoffs as the temporal correlations among demographic rates at the population level (Compagnoni et al., 2016; Fay et al., 2020; Fay, Hamel, et al., 2022; van Tienderen, 1995). Tradeoffs can occasionally scale up to cause negative temporal covariances at the population level (van Tienderen, 1995), but in most cases these covariances are the results of environmental stochasticity and demographic reaction norms to shared ecological drivers (Fay, Hamel, et al., 2022; Knops et al., 2007; Paniw et al., 2020). Third, even though tradeoffs might be present, individual heterogeneity can mask their presence among individuals. This specific ecological version of Simpson's paradox (Simpson, 1951) has been demonstrated by van Noordwijk and de Jong (1986): when the among-individual variance in resource acquisition is greater than the among-individual variance in resource allocation, the tradeoff is not expressed among individuals — even though it is theoretically present within individuals. In addition, expression of a tradeoff among individuals can also be influenced if the allocation and acquisition processes are not independent (Descamps et al., 2016; Fischer et al., 2009; Robinson & Beckerman, 2013). Altogether, this makes the detection of tradeoffs in wild populations difficult.

How much individuals vary in acquisition and allocation of resources determines if a tradeoff is detected among individuals (Metcalf, 2016; Reznick et al., 2000; van Noordwijk & de Jong, 1986). Part of this variance might be fixed, stemming from genetic, developmental, or consistent behavioral differences that constrain how much resources are acquired and allocated to somatic vs. reproductive functions (Réale et al., 2007; Wilson & Nussey, 2010). The remaining variance is likely to be plastic (Spigler & Woodard, 2019), where acquisition vs. allocation likely depends on the environmental context (Cohen et al., 2020; Sgrò & Hoffmann, 2004; Stearns et al., 1991). For instance, in several species, no tradeoffs were found among captive animals fed *ad libitum* (Kengeri et al., 2013; Landes et al., 2019; Ricklefs & Cadena, 2007). Similarly, controlled laboratory experiments on several species have shown that tradeoffs detection and strength were dependent on resource abundance (Gebhardt & Stearns, 1988; Messina & Fry, 2003; Messina & Slade, 1999; Spigler & Woodard, 2019). However, despite evidence that tradeoff expression depends on the environmental context, statistical methods to detect this context dependence in wild populations have, to date, rarely been applied.

Multivariate models are commonly employed to detect tradeoffs in wild populations (Cam et al. 2002, 2013; Hamel et al. 2018; Paterson et al. 2018; Fay et al. 2022a). In quantitative genetics, such models allow for the simultaneous analysis of multiple dependent variables like fecundity, growth, and survival (Kruuk et al. 2008; Wilson et al. 2010). These variables each have their own predictors, and the models estimate the correlated residual variances unaccounted for by the primary predictors. These models can be used to study residual correlations between traits at different levels, such as among-year correlation and among-individual correlation. For example, after accounting for primary predictors, such models quantify whether years with high

survival in a population are also years with high recruitment; or whether individuals with higher fecundity have lower or higher growth rates. However, these correlations among residual variances are estimated as fixed. Estimating fixed correlations might not necessarily be problematic in the case of experimental work, in which environmental conditions can be held constant within each treatment. However, wild populations are unlikely to experience fixed conditions, as the environmental context will vary in a continuous fashion, hence influencing the expression of tradeoffs. Therefore, there is a need to analyse and predict continuous variation of phenotypic correlations.

Here, we repurpose a hierarchical multivariate 'covariance reaction norm' (hereafter CRN) model recently developed by Martin (2023), which allows the incorporation of continuous predictors directly on the covariance matrix, for application to sampling designs typical in population ecology, enabling the study of the context-dependent expression of tradeoffs. As a proof-of-concept, we first validate this model on two simulated datasets, respectively focusing on an intergenerational tradeoff and an intraindividual tradeoff. We then apply our model on two empirical datasets of wild populations of yellow-bellied marmots *Marmota flaviventer* and Soay sheep *Ovis aries*. Prior studies have explored tradeoffs between vital rates in both species (Kroeger et al., 2020; Tavecchia et al., 2005). For instance, in yellow-bellied marmots, a quality-quantity tradeoff in offspring has been observed for older mothers. In Soay sheep, the costs of reproduction have been particularly evident for breeding ewes in high-density populations or following harsh winters. However, the environmental context-dependence of these tradeoffs has yet to be studied explicitly. In the marmots, which inhabit high-altitude, highly seasonal environments, and the sheep, which face severe winter storms and fluctuating population

densities, we hypothesize that tradeoffs are more likely to manifest under unfavorable ecological conditions (Cohen et al., 2020; Sgrò & Hoffmann, 2004).

Methods

The model

In this study, we employ a newly introduced CRN model (Martin, 2023), which has been developed as a quantitative genetic model to predict continuous changes in trait associations when either genetic data or repeated individual measurements are available for all phenotypes of interest. A key assumption of multivariate models thus far has been that phenotypic correlations caused by tradeoffs are fixed through time or space (Cam et al., 2002; Hamel et al., 2018). The CRN approach provides a solution to this general challenge, by allowing for phenotypic covariances to vary in response to variation in the environment, for example, estimating under which conditions among-individual variance in resources allocation is larger than among-individual variance in acquisition (van Noordwijk & de Jong, 1986). In the present study, we extend application of this general CRN approach to the detection of context-dependent tradeoffs (here defined as among-individual correlations even though both are not always equivalent) between life history traits, with special consideration to sampling conditions typical of long-term field research in population ecology. Specifically, we examine the use of bivariate CRN models to test for the presence of phenotypic tradeoffs when repeated individual measurements are lacking in a given environmental context (e.g., during a specific sampling event such as a breeding season or a year). These are typical situations in field research that motivate further development of the quantitative genetic models proposed by Martin (2023).

Before delving into the specifics of the model, note that in all the following models presented, measurements of the same individuals observed in different contexts are considered independent (see supplementary materials Section S1 for more details). This necessary simplification has potential consequences when searching for the phenotypic manifestation of tradeoffs, as fixed heterogeneity across ecological contexts cannot be properly disentangled from context-dependent heterogeneity, which might lead to issues especially in long-lived species that are observed across many different contexts. Nonetheless, this simplification does not impede our ability to detect context-dependence of among-individual correlations (supplementary materials Section S1). Consider a CRN model investigating how environmental contexts C and individual factors affect the phenotypic means of $\beta_{\mu 1}$and $\beta_{\mu 2}$ and among-individual correlations β_r between two Gaussian life history trait measures $\mathbf{z_1}$ and $\mathbf{z_2}$ with repeated individual measurements in each environmental context. $\mathbf{X_1}$ and $\mathbf{X_2}$ are N x P matrices of *N* measurements of *P* predictors. We begin by focusing on linear models to simplify notation and aid comprehension, with generalized models for non-Gaussian distributions discussed further below. Following Martin (2023) in the absence of genetic data, our bivariate phenotypic model is given by

$$\begin{aligned} \boldsymbol{z_1} &= \boldsymbol{X_1}\,\boldsymbol{\beta_{\mu 1}} + \boldsymbol{W}\boldsymbol{\alpha_{1(C)}} + \boldsymbol{\epsilon_{1(C)}} \\ \boldsymbol{z_2} &= \boldsymbol{X_2}\,\boldsymbol{\beta_{\mu 2}} + \boldsymbol{W}\boldsymbol{\alpha_{2(C)}} + \boldsymbol{\epsilon_{2(C)}} \end{aligned} \qquad (1.1)$$

$$\begin{aligned} \left[\boldsymbol{\alpha_{1(C)}}, \boldsymbol{\alpha_{2(C)}}\right] &\sim \boldsymbol{N}\left(\mathbf{0}, \boldsymbol{P}_{(C)}\right) \\ \left[\boldsymbol{\epsilon_1}, \boldsymbol{\epsilon_2}\right] &\sim \boldsymbol{N}\left(\mathbf{0}, \boldsymbol{\Sigma}_{(C)}\right) \end{aligned}$$

Trait values are expressed as a function of the average effects $\boldsymbol{\beta_{\mu 1}}$ and $\boldsymbol{\beta_{\mu 2}}$ of $\mathbf{X_1}$ and $\mathbf{X_2}$ on each phenotype, as well as among-individual effects $\boldsymbol{\alpha_{1(C)}}$ and $\boldsymbol{\alpha_{2(C)}}$ that are repeatable across measurements and within-individual effects $\boldsymbol{\varepsilon_{1(C)}}$ and $\boldsymbol{\varepsilon_{1(C)}}$ that are variable across measurements. The model matrix **W** (an N x J matrix for *J* subjects) structures the among-individual effects $\boldsymbol{\alpha_{(C)}}$ across repeated measurements. (Co)variances between independent among- and within-individual effects are respectively described by **P** and $\boldsymbol{\Sigma}$ covariance matrices. To detect context-dependent tradeoff expression, we use environmental information in $\mathbf{X_3}$ (an C x P matrix of *C* environmental contexts of *P* predictors) to predict the among-individual trait covariance matrix $\mathbf{P_{(C)}}$.

$$\boldsymbol{P}_{(C)} = \begin{bmatrix} \sigma^2_{\alpha_1(C)} & r_{\alpha(C)}\,\sigma_{\alpha_1(C)}\sigma_{\alpha_2(C)} \\ r_{\alpha(C)}\,\sigma_{\alpha_2(C)}\sigma_{\alpha_1(C)} & \sigma^2_{\alpha_2(C)} \end{bmatrix} \qquad (1.2)$$
$$\operatorname{atanh}\left(r_{\alpha(C)}\right) = \boldsymbol{X_3}\,\boldsymbol{\beta_r}$$

where the inverse hyperbolic tangent function atanh(r)=logit($[r + 1]/2$)/2 is used as a link function to model additive environmental effects $\boldsymbol{\beta_r}$ on the logit scale while retaining the [-1,1] scaling of the correlation coefficient *r*. This is akin to a logistic regression with bounds in [-1,1] instead of [0,1]. The same approach can be taken to describe changes in within-individual variation across environmental contexts.

$$\boldsymbol{\Sigma}_{(C)} = \begin{bmatrix} \sigma^2_{\epsilon_1(C)} & r_{\epsilon(C)}\,\sigma_{\epsilon_1(C)}\sigma_{\alpha_2(C)} \\ r_{\epsilon(C)}\,\sigma_{\epsilon_2(C)}\sigma_{\epsilon_1(C)} & \sigma^2_{\epsilon_2(C)} \end{bmatrix} \qquad (1.3)$$
$$\operatorname{atanh}\left(r_{\epsilon(C)}\right) = \boldsymbol{X_3}\,\boldsymbol{\beta}_{r_\epsilon}$$

Direct prediction of the transformed correlation coefficient is useful because we are principally interested in $r_{(C)}$ as an indicator of putative tradeoffs, rather than the covariance $P_{1,2(C)} = r_{(C)}\sigma_1\sigma_2$ per se. Changes in the scale $\sigma_1\sigma_2$ of life history trait variation may occur

188 independently of changes in positive or negative trait association among individuals, but these
189 effects will be confounded together in the covariance $P_{1,2(C)}$. In contrast, the correlation
190 coefficient $r_{(C)}$ is standardized relative to the scale of each phenotype, providing a more robust
191 quantity for directly predicting and comparing estimates of life history tradeoffs across
192 phenotypes and species. Our model also assumes that phenotypic variances can vary across
193 environmental contexts, but no predictions are made on this variation. Greater plasticity is
194 instead expected in the strength of tradeoff expression caused by fluctuating environmental
195 factors (e.g., environmental harshness, resource availability, local predator density). See Martin
196 (2023) for further details on relaxing these assumptions to model environmental effects on
197 among- and within-individual variances.

198 ***Non-repeated measures***

199 Estimating **Eq 1** with empirical data requires multiple measurements of the same subjects
200 to effectively partition trait correlations due to sources of among- $\mathbf{P}_{(C)}$ and within-individual $\mathbf{\Sigma}_{(C)}$
201 phenotypic variation, relative to a given window of sampling (i.e., a given environmental context
202 C). Repeated individual measurements are often inconsistent or unavailable in a given
203 environmental context (e.g., a single fecundity measurement for individuals in a given year) in
204 long-term field studies, which otherwise provide invaluable datasets for investigating context-
205 specific tradeoffs in the wild. Fortunately, we can still take advantage of long-term environmental
206 variation in such studies to detect variation in tradeoff expression without repeated
207 measurements in a given environmental context. This requires simplifying the CRN model to
208 predict observation-level phenotypic associations across environmental contexts.

$$\boldsymbol{z_1} = \boldsymbol{X_1}\,\boldsymbol{\beta_{\mu 1}} + \boldsymbol{o_{1(C)}} \qquad (2)$$
$$\boldsymbol{z_2} = \boldsymbol{X_2}\,\boldsymbol{\beta_{\mu 2}} + \boldsymbol{o_{2(C)}}$$

$$\left[\boldsymbol{o_{1(C)}}, \boldsymbol{o_{2(C)}}\right] \sim \boldsymbol{N}\left(\mathbf{0}, \mathbf{P}_{\boldsymbol{o(C)}}\right)$$
$$\boldsymbol{P_{o(C)}} = \begin{bmatrix} \sigma^2_{o_1(C)} & r_{o(C)}\,\sigma_{o_1(C)}\sigma_{o_2(C)} \\ r_{o(C)}\,\sigma_{o_2(C)}\sigma_{o_1(C)} & \sigma^2_{o_2(C)} \end{bmatrix}$$
$$\operatorname{atanh}\left(r_{o(C)}\right) = \boldsymbol{X_3}\boldsymbol{\beta_r}$$

Here, the lack of repeated measurements mean that we cannot decompose the variance between among- and within-individual variation. Therefore, $\boldsymbol{o_{1(C)}} = \boldsymbol{\alpha_{1(C)}} + \boldsymbol{\varepsilon_{1(C)}}$ and $\boldsymbol{o_{2(C)}} = \boldsymbol{\alpha_{2(C)}} + \boldsymbol{\varepsilon_{2(C)}}$ are observation-level random effects aggregating variation due to among- and within-individual differences across measurements, within a given environmental context defined by C (e.g., a given year, position in space, level of resource abundance). Note that the **W** matrix from **Eq 1** is no longer necessary in **Eq 2** in the absence of repeated measurements. As a consequence, we expect that the observation-level correlation $r_{o(C)}$ between these random effects to reflect the combined effect of the among- and within-individual correlations between life history traits, weighted by the geometric mean of their repeatability R (Dingemanse & Dochtermann, 2013; Searle, 1961).

$$r_{o(C)} = r_{\alpha(C)}\sqrt{\frac{\sigma^2_{\alpha 1}}{\sigma^2_{z1}}\frac{\sigma^2_{\alpha 2}}{\sigma^2_{z2}}} + r_{\epsilon(C)}\sqrt{\frac{\sigma^2_{\epsilon 1}}{\sigma^2_{z1}}\frac{\sigma^2_{\epsilon 2}}{\sigma^2_{z2}}} = r_{\alpha(C)}\sqrt{R_1 R_2} + r_{\epsilon(C)}\sqrt{(1-R_1)(1-R_2)} \qquad (3)$$

Where phenotypic variances are adjusted for the mean effects of $\boldsymbol{X_1\beta_{\mu 1}}$ and $\boldsymbol{X_2\beta_{\mu 2}}$. We can see that inferences about among-individual tradeoffs from the non-repeated measures model (**Eq. 2**) will be at greatest risk of bias when sign(r_α)≠sign(r_ϵ) and $\sqrt{R_1 R_2} << \sqrt{(1-R_1)(1-R_2)}$. Figure 1 shows these general relationships across correlation and repeatability ranges, identifying

regions of sign bias. Fortunately, researchers will generally be able to judge their risk of inferential bias based on *a priori* knowledge about the repeatability of life history traits, which tends to be medium to high (Dingemanse et al., 2021). For example, observation-level correlations of behavioral traits will tend to be dominated by within-individual associations (Bell et al., 2009; Cauchoix et al., 2018; Holtmann et al., 2017), while morphological associations will tend to be dominated by among-individual variation (Dingemanse et al., 2021). We reiterate that our models consider measurements of the same individuals observed in different contexts as independent (see supplementary materials Section S1). In addition, our model considers no measurement errors, as we are not able to disentangle it from true within-individual variation using non-repeated measures. Such considerations regarding trait repeatability and measurement error should be explicit when interpreting results without repeated measures.

Hybrid scenarios

Variation in repeated sampling is also likely to occur across phenotypes due to factors such as difficulty of measurement and the rate of trait expression. While a single measure of age at first reproduction or fecundity in a given environmental context may be available per individual, multiple individual measures may be available for traits such as offspring quality. Such scenarios require a hybrid modeling approach. For example, consider a model with a single predictor for an intergenerational tradeoff between fecundity (e.g., clutch size) and offspring quality, but other traits could equally be studied. The model structure for offspring quality $\mathbf{z_1}$ (depicted as offspring body mass), a gaussian trait, is given by

$$\boldsymbol{z_1} = \boldsymbol{X_1\beta_{\mu 1}} + \boldsymbol{W\alpha_{1(C)}} + \boldsymbol{\epsilon_{1(C)}} \quad (4.1)$$

The linear predictor for $\mathbf{z_1}$ (mass of an offspring of a given mother) in year C includes a year-specific mother random effect $\boldsymbol{\alpha_{1(C)}}$ and $\boldsymbol{\varepsilon_{1(C)}}$ being the within-brood/litter variance.

The model for fecundity $\mathbf{z_2}$ follows the same basic structure, with a single fecundity measurement per female per year. We can use a Poisson distribution where we model the expected rate of offspring production using a log link function, but other distributions could equally be used.

$$\boldsymbol{z_2} = \boldsymbol{X_2\beta_{\mu 2}} + \boldsymbol{o_{2(C)}} \tag{4.2}$$

Without repeated measures, the random effect $\boldsymbol{o_{2(C)}}$ is specified at the observation-level, accounting for any overdispersion in the Poisson process across measurements of each female.

The context-dependent tradeoff will be estimated between the among-mother random effect in offspring quality and the observation-level random effect in fecundity.

$$\left[\boldsymbol{\alpha_{1(C)}}, \boldsymbol{o_{2(C)}}\right] \sim \boldsymbol{N}\left(\mathbf{0}, \mathbf{P}_{(C)}\right) \tag{4.3}$$

$$\boldsymbol{P}_{(C)} = \begin{bmatrix} \sigma^2_{\alpha_1(C)} & r_{(C)}\,\sigma_{\alpha_1(C)}\sigma_{o_2(C)} \\ r_{(C)}\,\sigma_{\alpha_1(C)}\sigma_{o_2(C)} & \sigma^2_{o_2(C)} \end{bmatrix}$$

$$\operatorname{atanh}\left(r_{(C)}\right) = \boldsymbol{X_3\beta_r}$$

Reducing **Eq. 3**, the correlation r_C between the individual- $\boldsymbol{\alpha_{1(C)}}$ and observation-level $\boldsymbol{o_{2(C)}}$ effects will necessarily be proportional to the among-individual correlation across life history traits.

$$r_{o(C)} = r_{\alpha(C)}\sqrt{\frac{\sigma^2_{\alpha 2}}{\sigma^2_{z2}}} = r_{\alpha(C)}\sqrt{R_2} \tag{5}$$

Note that this method does not allow the inclusion of non-continuous traits (e.g., Bernoulli traits) in the absence of repeated measurements within a given environmental context C (e.g., a given year).

Validation on simulated datasets

We validated the CRN model on two different types of tradeoffs. First, we used the hybrid CRN model to study an intergenerational tradeoff between fecundity and quality. The hybrid model is well suited because fecundity (i.e., clutch/litter size) has a single measurement per mother per year, while offspring quality (i.e., offspring mass) has repeated measurements per mother per year (one measurement for each offspring produced). Second, we used the non-repeated measures CRN model to study an intraindividual tradeoff between fecundity (clutch/litter size) and parental growth (the change of mass from a year to the next). The non-repeated measures CRN model is well suited as both traits are expressed only a single time per year (one fecundity and one parental growth measure per individual per year). Note that tradeoffs are described as intergenerational or intraindividual depending on which traits are studied (as explained in Stearns, 1989), and both type of tradeoff can be decomposed into among- and within-individual covariation. We simulate data for these two tradeoffs using the individual-based simulation described in Bliard et al. (2024), whereby the among-individual correlation between life history traits can be made dependent on the environmental context. The code to generate data from the individual-based simulation can be found on github (https://github.com/lbiard/detecting_tradeoffs_crn_models). This model validation is only intended to show that context-dependent among-individual correlations (i.e., context dependent tradeoffs) can be successfully recovered. For a more extensive simulation-based calibration of CRN models over a broad range of parameter values, see Martin (2023).

Intergenerational tradeoff (offspring quantity-quality)

We first focused on an intergenerational tradeoff between offspring quantity and quality (hybrid CRN model). This quantity-quality tradeoff has been the focus of numerous studies since Lack's pioneering work on bird clutch sizes (Einum & Fleming, 2000; Fischer et al., 2011; Gillespie et al., 2008; Lack, 1947; Williams, 1966). We simulate 30 years of individual-based data in which 25 new individuals enter the population each year, reproduce with an average clutch/litter size of 2.5, and then have a probability to survive to next year of 0.6. This yielded a final simulated dataset of 750 individuals, totaling 1578 reproductive events and 4783 offspring. An observation-level correlation was included between offspring mass and clutch size, and this correlation was made dependent on a single climatic predictor. The same climatic predictor was also included to influence both clutch size and offspring mass.

Intraindividual tradeoff (fecundity-growth)

We then simulated data for an intraindividual tradeoff between fecundity and growth (non-repeated measures CRN model). This simulated dataset is also made of 30 years and 750 individuals, for a total of 1974 reproductive events, with a variable observation-level correlation between individual growth and fecundity, which is itself dependent on a single climatic predictor.

Study systems and application on empirical datasets

Marmots

We applied the hybrid CRN model (one trait with repeated individual measurements within a year and one trait without) on data from a yellow-bellied marmot population monitored at the Rocky Mountain Biological Laboratory in Gothic, Colorado (38°57'N, 106°59'W) during the summer season each year, whereby extensive individual-based data is collected (Armitage, 2014;

Blumstein, 2013). In Alpine marmots *Marmota marmota*, an offspring quality-quantity tradeoff has been found (Berger et al., 2015), while it remained mostly elusive in yellow-bellied marmots, being only found for older mothers (Kroeger et al., 2020), whereby within-cohort selection has likely reduced the amount of among-individual variance in resource acquisition, thus making the tradeoff visible (Kendall et al., 2011; van Noordwijk & de Jong, 1986). Therefore, we searched for an intergenerational tradeoff between mothers' fecundity and offspring estimated mass (offspring quality-quantity tradeoff). We used repeated measurements of offspring mass for each mother (one mass estimate for each offspring in a given litter). The offspring weaning mass was imputed based on the date of emergence for each litter and mass measurements from captures later in the season, following the method of Ozgul et al. (2010). We considered two measures quantifying environmental conditions for a given year. First, the total amount of snow during the preceding winter, with years of little overwinter snow considered harsher for marmots as it offers limited thermal insulation during the hibernation (Barash, 1973; Cordes et al., 2020; Wells et al., 2022). Second, the average daily maximum temperature during the month of June, with warmer summer temperatures considered unfavorable conditions for marmots as they are prone to overheating, hence limiting the time that can be allocated to foraging (Cordes et al., 2020; Krajick, 2004; Melcher et al., 1990). Note that we used temperature in June and not July as commonly used in this system (Cordes et al., 2020), because this is more likely to represent the conditions experienced for most offspring before emergence and weaning, since most offspring emerge in July. We expected tradeoffs to be more strongly expressed among individuals in years with little overwinter snow or high summer temperature. In total, we used 2540 offspring mass from 597 reproductive events, from 279 females across 42 years.

We modeled offspring mass using a normal distribution (**Eq. 6.1**), and we included as covariates (i.e., in $\mathbf{X_1}$) the total amount of snow during the winter, June average maximum temperature, age of the mother and its quadratic effect, and mother's estimated mass in early June as a proxy of mother's quality. A year random effect δ_1 was also included.

$$\boldsymbol{offpsring\ mass} = \boldsymbol{X_1\beta_1} + \boldsymbol{\delta_1} + \boldsymbol{W\alpha_{1(Y)}} + \boldsymbol{\epsilon_{1(Y)}} \quad (6.1)$$

With $a_{1(Y)}$ being a year-specific mother random effect and $\epsilon_{1(Y)}$ the within-litter variance.

We modeled the second trait, fecundity (i.e., litter size), using a Poisson distribution (**Eq. 6.2**), as a function of the same covariates ($\mathbf{X_2}$), except June average maximum temperature, since it cannot affect fecundity as pregnancies mostly occur before this period. A year random effect δ_2 was also included.

$$\log(\boldsymbol{litter\ size}) = \boldsymbol{X_2\beta_2} + \boldsymbol{\delta_2} + \boldsymbol{o_{2(Y)}} \quad (6.2)$$

For the observation-level correlation (**Eq. 6.3**), the two environmental variables (winter snow and June temperature) were added as covariates ($\mathbf{X_3}$).

$$\left[\boldsymbol{\alpha_{1(Y)}}, \boldsymbol{o_{2(Y)}}\right] \sim \boldsymbol{N}\left(\mathbf{0}, \mathbf{P}_{(Y)}\right) \quad (6.3)$$

$$\boldsymbol{P}_{(Y)} = \begin{bmatrix} \sigma^2_{\alpha_{1(Y)}} & r_{(X)}\,\sigma_{\alpha_1(Y)}\sigma_{o_2(Y)} \\ r_{(Y)}\,\sigma_{\alpha_1(Y)}\sigma_{o_2(Y)} & \sigma^2_{o_2(Y)} \end{bmatrix}$$

$$\operatorname{atanh}\left(r_{(Y)}\right) = \boldsymbol{X_3\beta_3}$$

We performed posterior predictive checks, showing a good concordance between the litter size data, and data generated under the model (see Figure S3). However, the model slightly underestimates the variance in offspring mass. Overall, posterior predictive checks highlight that

346 the use of a Normal distribution to model offspring mass, and a Poisson distribution with an
347 observation random effect to model litter size, were appropriate in this system.
348
349 ***Soay sheep***
350 We applied the non-repeated measures CRN model on Soay sheep data, as we have no repeated
351 individual measurement within a given year available for neither of the traits studied. We used
352 data from an unmanaged population of feral sheep in the Village Bay area of the island of Hirta
353 (57°48'N, 8°37'W), which has been monitored since 1985 (Clutton-Brock & Pemberton, 2004). In
354 Soay sheep, survival costs of reproduction were found for breeding ewes, particularly in
355 populations at high densities or following stormy winters (Tavecchia et al., 2005). Therefore, we
356 searched for an intraindividual tradeoff between ewes' fecundity defined as the number of lambs
357 born in Spring (ranging from 0 to 2) and their log mass in the following summer, with both traits
358 conditional on ewes surviving the winter. We considered two environmental variables to
359 characterize the ecological harshness faced by the sheep in a given year: population density and
360 NAO (North Atlantic Oscillation) in the winter preceding parturition, with high NAO values
361 corresponding to wet and stormy winters (Coulson et al., 2001; Regan et al., 2022). In total, we
362 used data from 2497 reproductive events across 37 years, for 861 ewes with known mass in the
363 summer preceding the reproductive event, as well as known mass in the following summer. We
364 expected tradeoffs to be more strongly expressed in years of high population density or high
365 NAO.
366 As ewes' fecundity in a given year is restricted to [0,2], we could not use a Poisson
367 regression. This is due to the count data being underdispersed relative to a Poisson distribution.

We therefore modeled the ewe's fecundity using an ordinal regression (also called cumulative logistic regression; **Eq. 7.1**), and we included as covariates ($\mathbf{X_1}$) the individual's log mass preceding the reproductive event as a proxy of quality, age and its quadratic effect, and population density.

$$\text{logit}\left(\Pr\left(\boldsymbol{N_{offspring}} \leq i\right)\right) = \theta_i - \left(\boldsymbol{X_1\beta_1} + \boldsymbol{\delta_1} + \boldsymbol{o_{1(Y)}}\right) \quad (7.1)$$

Where the cumulative probability of having at most *i* offspring is given as a function of the threshold θ_i and the matrix of covariates $\mathbf{X_1}$, as well as a year random effect δ_1 and a year specific observation random effect $o_{1(Y)}$.

We modeled the ewe's log mass in the following summer using a normal distribution (**Eq. 7.2**), and included in $\mathbf{X_2}$ the same covariates as in $\mathbf{X_1}$, as well as NAO in the winter preceding parturition. A year random effect δ_2 was also included.

$$\boldsymbol{mass} = \boldsymbol{X_2\beta_2} + \boldsymbol{\delta_2} + \boldsymbol{o_{2(Y)}} \quad (7.2)$$

For the observation-level correlation (**Eq. 7.3**), the two ecological variables (winter NAO and density) were added as covariates ($\mathbf{X_3}$).

$$\left[\boldsymbol{\alpha_{1(Y)}}, \boldsymbol{o_{2(Y)}}\right] \sim \boldsymbol{N}\left(\mathbf{0}, \mathbf{P}_{(Y)}\right) \quad (7.3)$$

$$\boldsymbol{P}_{(Y)} = \begin{bmatrix} \sigma^2_{\alpha_{1(Y)}} & r_{(Y)}\,\sigma_{\alpha_1(Y)}\sigma_{o_2(Y)} \\ r_{(Y)}\,\sigma_{\alpha_1(Y)}\sigma_{o_2(Y)} & \sigma^2_{o_2(Y)} \end{bmatrix}$$

$$\text{atanh}\left(r_{(Y)}\right) = \boldsymbol{X_3\beta_3}$$

The posterior predictive checks we performed highlighted a good fit between the data and data generated under the model. This confirms that using a normal distribution to model ewe's mass, and using a cumulative logistic regression to model ewe's number of offspring, were appropriate (see Figure S4).

386

387 Model implementation

388 We implemented all multivariate models described above in a Bayesian framework using the Stan
389 statistical language (Carpenter et al., 2017), through the software R (R Core Team, 2021) using
390 the R package *CmdStanR* (Gabry & Češnovar, 2020). Stan was preferred for model
391 implementation because of its flexibility. Common regularizing priors were used for all model
392 parameters: normal distributions of mean 0 and standard deviation of 1 for intercepts and slopes
393 coefficients, and exponential distributions of rate 2 for variance parameters. Each model ran on
394 3 chains, with a burn-in period of 1000 iterations, sampling for 3000 iterations, keeping all the
395 sampled iterations (Link & Eaton, 2012). Convergence of parameter estimates was assessed
396 visually and using the Gelman-Rubin diagnostic (Gelman & Rubin, 1992). We report the full
397 posterior distributions, alongside their mean, 50%, and 89% credible intervals (McElreath, 2020).
398 The Stan code to implement all the CRN models presented in this study is archived on GitHub
399 (https://github.com/lbiard/detecting_tradeoffs_crn_models) and Zenodo
400 (https://doi.org/10.5281/zenodo.12800618).

401

402 **Results**

403 The model validation performed on simulated datasets showed that parameters were correctly
404 recovered for both intergenerational tradeoffs (Figure 2) and intraindividual tradeoffs (Figure 3).
405 While these simulation examples do not quantify bias of estimations (more details from a
406 simulation-based calibration of CRN models are available in Martin (2023)), they still confirm that

407 the model presented in the methods is able to detect context-dependence in the expression of
408 tradeoffs.

409 The model applied to yellow-bellied marmot data shows trends towards tradeoffs being
410 more strongly expressed in years with harsh environmental conditions, albeit with high
411 uncertainty in the estimates (Figure 4). We found a positive mean effect of the amount of
412 overwinter snow on the correlation (Figure 4), meaning that the tradeoff between fecundity and
413 offspring quality was more strongly expressed after winters with little snow. We also found a
414 negative mean effect of the average maximum June temperature on the correlation (Figure 4),
415 where females with more offspring were more likely to have lighter offspring during warmer
416 summers. Estimated effects of covariates on either fecundity or offspring mass can be found in
417 Figure 4, as well as in Figure S5.

418 Estimated effects of covariates on the correlation also had high uncertainty in the Soay
419 sheep dataset (Figure 5). Overall, we found that the correlation tended to be negative across
420 most environments, which means that ewe's growth was lower for the ones that weaned
421 offspring (Figure 5). Contrary to our expectations, while we hypothesized that the tradeoffs
422 should be more strongly expressed in wet and stormy winters (high NAO index), we found a
423 positive effect of winter NAO on the correlation between fecundity and growth (Figure 5). We
424 also found a positive effect of population density on the expression of the tradeoff (Figure 5).
425 Estimated effects of covariates on either fecundity or ewe's mass can be found in Figure 5, as
426 well as in Figure S6.

427

428 **Discussion**

Our proof-of-concept study demonstrates that hierarchical multivariate CRN models (Martin, 2023) can be used successfully to detect and estimate context-dependent changes in tradeoff expression, though estimation uncertainty can be large. In agreement with theoretical predictions and despite large uncertainty, we found that reproductive tradeoffs in yellow-bellied marmots tend to be more strongly expressed under unfavorable climatic conditions. In Soay sheep, we found some context-dependence in the expression of the tradeoff, but effect directions were opposite to our initial prediction. This hierarchical model has the potential to be used on many long-term individual-based datasets and could help improve our understanding of tradeoff expression and life history theory.

Although the initial motivation to use this method partly rested on the observed difficulty of finding tradeoffs in empirical datasets, we found that in both sheep and marmots, the tradeoffs tend to be expressed across most environments, with mean phenotypic correlations being negative overall. Thus, ironically, in these two empirical datasets, tradeoffs might have been detected using simpler multivariate methods without the need for context dependence. However, this should not come as a surprise for Soay sheep, as this negative correlation between growth and fecundity was already found on a smaller dataset (Fung et al., 2022). Nonetheless, the results still highlight that context-dependence has the potential to hinder our ability to detect tradeoffs in some cases. For instance, when marmots experience favorable environmental conditions, the average correlation is closer to null with credibility intervals nearing or overlapping zero (Figure 4), while this intergenerational tradeoff is found to be more strongly expressed during harsh years. In Soay sheep, context dependence appears to be marked for the expression of the tradeoff, but opposite to our predictions. Indeed, we found a positive

451 correlation between growth and fecundity only under the harshest environmental conditions
452 (high population density and high winter NAO, Figure 5). Since ewes' mass is measured in the
453 following summer and not directly after parturition, harsh winter conditions are expected to
454 increase overwinter mortality (Milner et al., 1999), lowering spring population density and
455 reducing competition. This could potentially help surviving ewes to recover their body condition
456 between spring and summer, which is the period of greatest grass growth, hence potentially
457 explaining our counter-intuitive results. We can also speculate that the result could have arisen
458 from two potential pitfalls due to idiosyncrasies of the Soay sheep data. First, among-individual
459 variation in fecundity is limited in sheep, ranging from no offspring to twins, potentially making
460 it more complicated for the model to estimate variances accurately (Fay, Authier, et al., 2022;
461 Kain et al., 2015). Second, both ewes' growth and fecundity are conditional on survival in the
462 data, hence individuals who suffered most from the cost of reproduction and did not survive are
463 not present in the analysis, potentially biasing the results (Hadfield, 2008). Finally, while we
464 expected more negative phenotypic correlations under harsh conditions, where among-
465 individual variance in resource allocation is greater than among-individual variance in acquisition,
466 it is theoretically possible that in population facing adverse conditions, a few robust individuals
467 monopolize most resources, thus increasing the among-individual variance in resource
468 acquisition (Chambert et al., 2013), hence leading to positive estimates of phenotypic
469 correlations.

470 Despite the potential of this modeling approach to study context-dependent tradeoffs, a
471 few methodological limitations are to be considered. A recent study conducted by Fay et al.
472 (2022) highlighted that multivariate models with correlated random effects for Bernoulli traits

performed rather poorly, resulting in a potentially large bias and imprecise estimates of variances and covariances. This is in part because Bernoulli traits contain less information than continuous variables, making estimations of variances complicated (Fay, Authier, et al., 2022), but also because the data available to estimate individual heterogeneity is usually scarce (Browne et al., 2007). The model we present suffers from this limitation, and even more so when there is only a single individual observation per individual per sampling occasion (e.g., parental survival), and when the trait is not repeatable (death can only occur once). This issue renders the model, as well as any other multilevel model, unable to meaningfully estimate distinct mean and variance parameters for Bernoulli traits, due to the fact that the mean p of a Bernoulli variable determines its variability $p(1-p)$ without scope for overdispersion. Therefore, environmental effects on the mean of Bernoulli measures will necessarily change their variances (Skrondal & Rabe-Hesketh, 2007). However, when repeated Bernoulli observations or a binomial measure are available within each sampling occasion (e.g., survival of each offspring within a litter), the CRN model can then be used to partition distinct environmental effects on trait means and (co)variances. As we have shown in the present study, despite this limitation, the CRN remains applicable to single measures of continuous traits and count measures (e.g., growth, fecundity, phenology, behavioral traits), as well as proportions and various other kinds of non-Gaussian measures. Another limitation of the proposed method is that sample sizes needed are likely to be large, with enough individuals in each environmental context, and importantly enough sampling occasions across which to estimate the context dependence of tradeoff expression. Nonetheless, many long-term individual-based studies should have enough data to fulfill these requirements (de Villemereuil et al., 2020).

Despite the abovementioned caveats and limitations of the methodology in the absence of repeated measurements, this new model is a development that could be useful for many datasets. Thanks to its implementation in a Bayesian framework using Stan (Carpenter et al., 2017), it offers great flexibility and can be easily repurposed and modified to fit the idiosyncrasies of a given dataset or species life history. It is also straightforward to extend the model by adding a pedigree for quantitative genetic analysis (see Martin, 2023), even though phenotypic correlations should be good approximations of genetic correlations in most cases (Cheverud, 1988; Dochtermann, 2011; Roff, 1995). While we presented a bivariate model, this model is not necessarily limited to two traits, and more continuous traits and their covariances could also be analyzed simultaneously. We also restricted our proof-of-concept study to the reaction norm of the correlation between traits, but researchers interested in the canalization of traits variances as a response to the environmental context could also benefit from this modeling approach (Péron et al., 2016).

Life history tradeoffs have long been sought after, but difficult to detect in observational data due to individual heterogeneity (Metcalf, 2016; Reznick et al., 2000; van Noordwijk & de Jong, 1986). Previous studies have also highlighted that life history tradeoffs could be expressed only under unfavorable ecological conditions (Cohen et al., 2020; Stearns, 1989). Yet, despite our knowledge of the issues hindering tradeoff detection, we still lacked a statistical framework that permits the detection of context-dependence in tradeoff expression. Our proof-of-concept study shows that this context dependence can be detected. This method has the potential to be applied by demographers and evolutionary ecologists having long-term individual-based datasets at hands, with many study systems having the required data (Culina et al., 2021; de Villemereuil et

al., 2020). Altogether, this method has the potential to help us improve our understanding of life history theory, and in part resolve van Noordwijk and de Jong's (1986) conundrum of tradeoff detection, by accounting for the context-dependence of their expression.

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Authors contributions

LB, JSM, AO, MP, DZC conceived the study. JSM designed the initial modeling framework and LB analyzed the data. DTB, JGAM, JMP, DHN collected and curated the data. LB and JSM wrote the first draft with input from AO, MP, DZC. All authors contributed to the editing of the manuscript.

Data and code availability

The data, as well as the R and Stan code necessary to reproduce the results are available on GitHub https://github.com/lbiard/detecting_tradeoffs_crn_models and are archived on Zenodo https://doi.org/10.5281/zenodo.12800618.

Figures

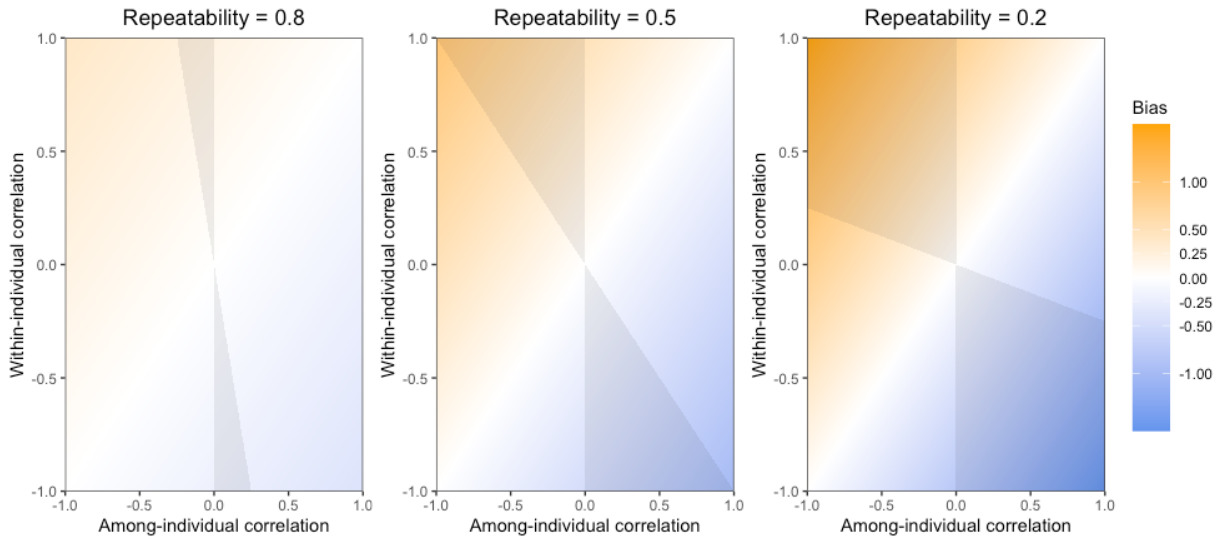
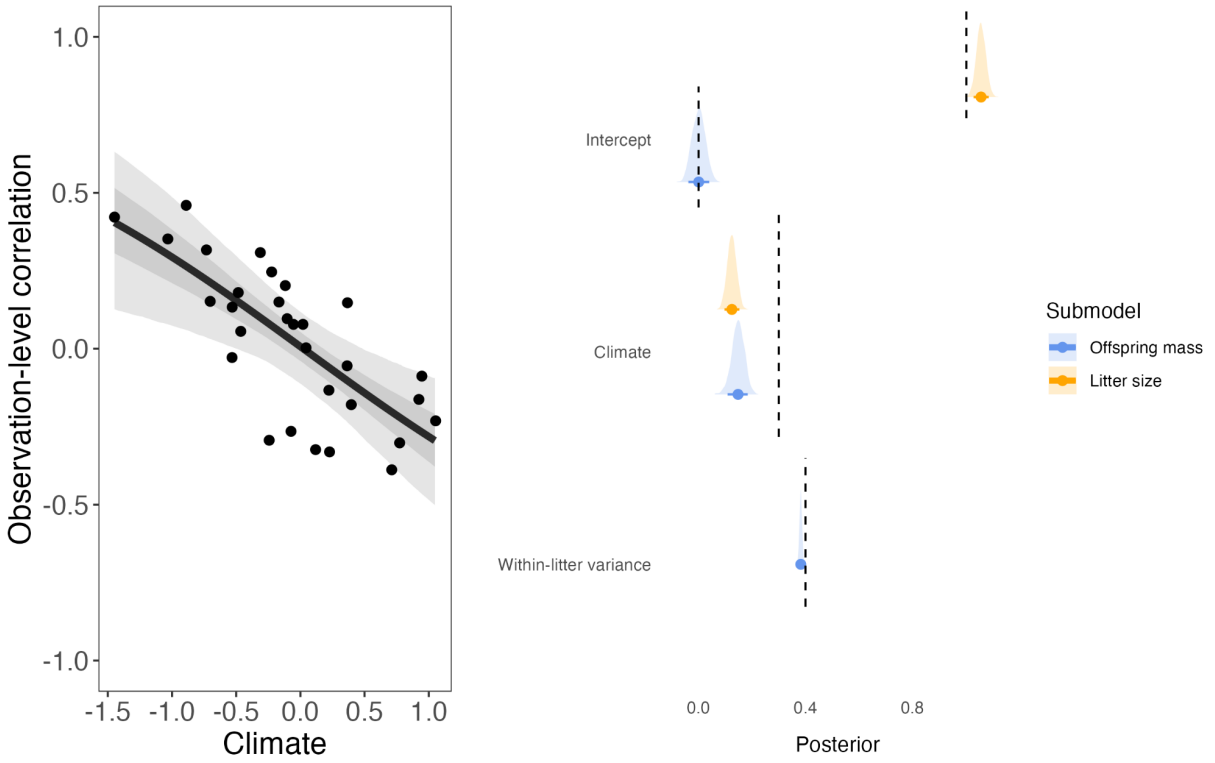


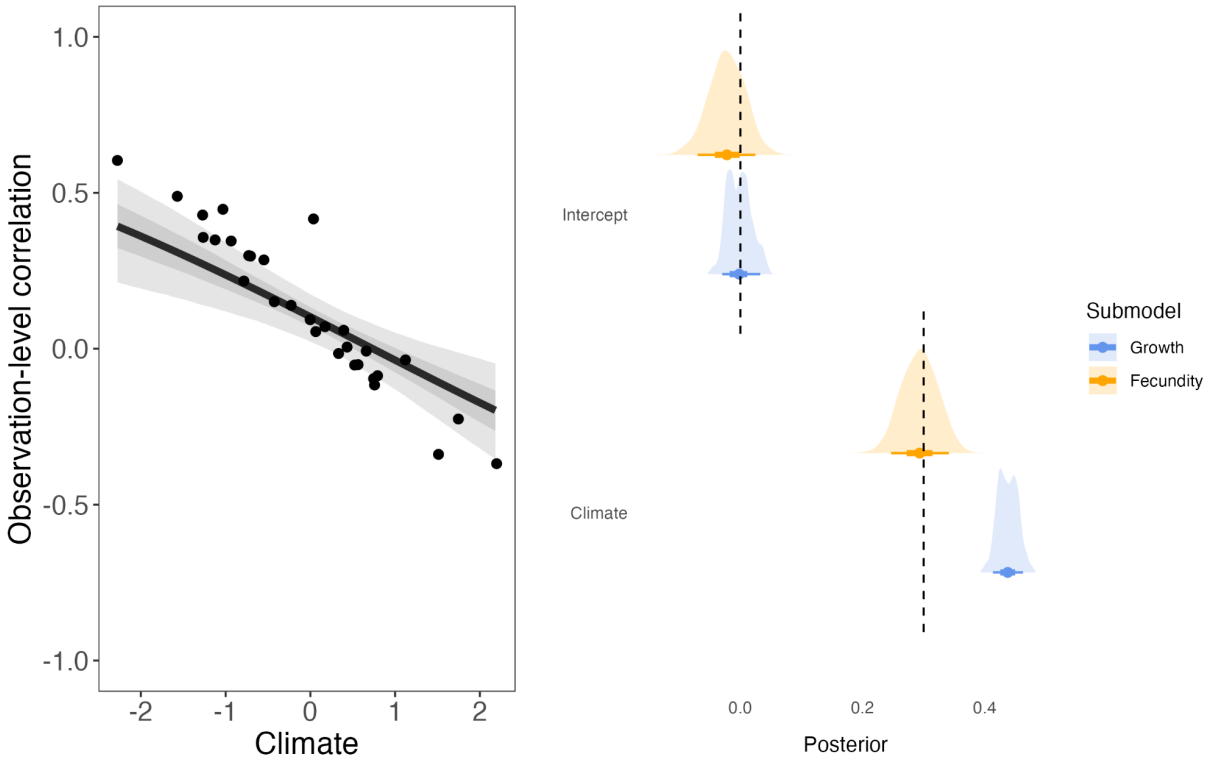
Figure 1: General relationships across correlations and repeatability ranges based on **Eq 3** for a non-repeated measures CRN (model of **Eq 2**), identifying the magnitude of correlation bias and the regions of sign bias. The bias is here defined as the difference between the observation-level correlation and the among-individual correlation, using the latter as a reference. Parameter spaces in gray represent the regions of sign bias, where the observation-level correlation has a sign opposite to the among-individual correlation. This highlights that the observation-level correlation is mostly influenced by the among-individual correlation for traits with high repeatability, while it is mostly influenced by the within-individual correlation for traits with low repeatability.



554

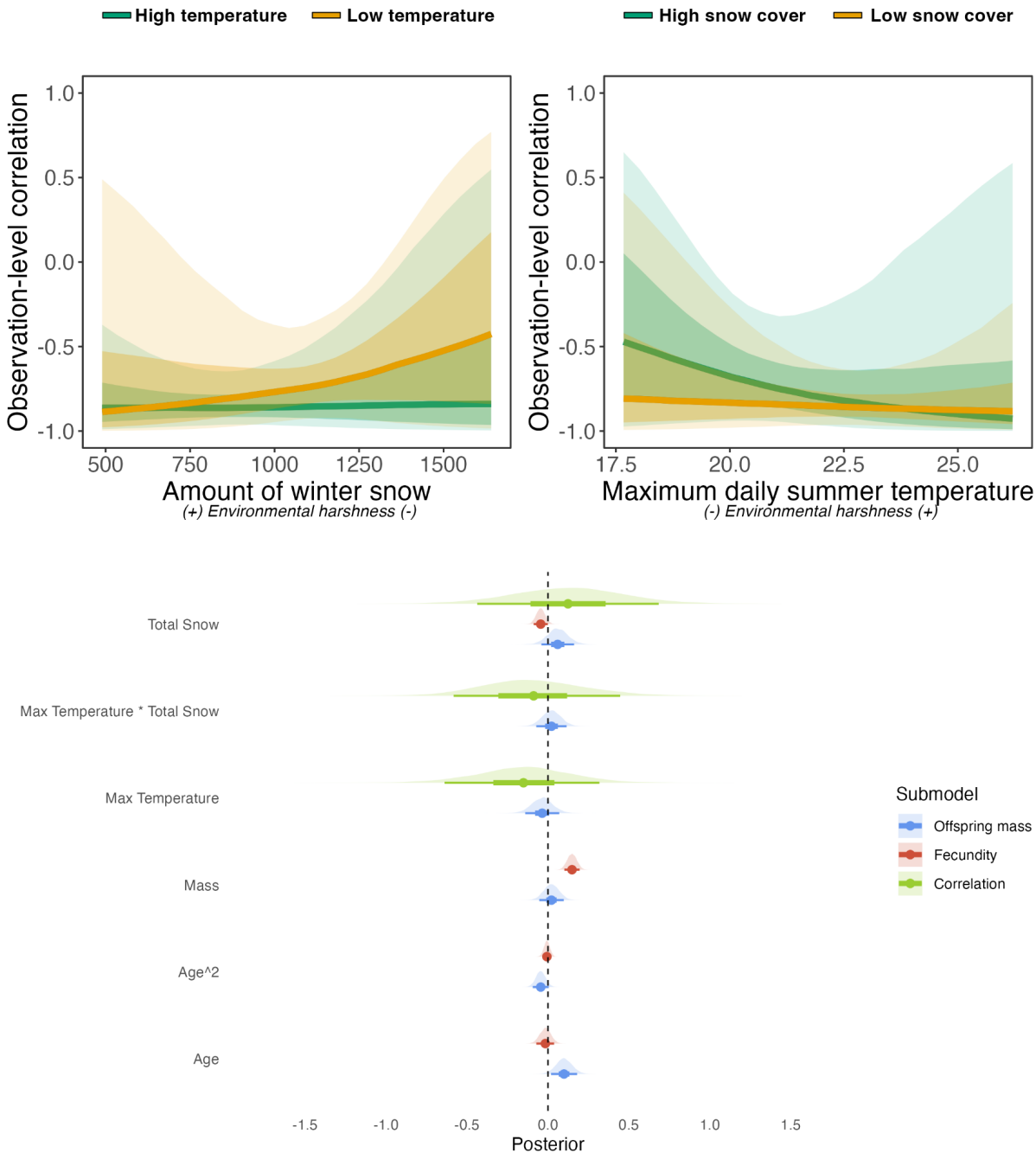
555 Figure 2: Left panel: estimated vs. simulated observation-level correlation between litter size and
556 offspring mass as a function of climate, after accounting for the effect of climate on both traits.
557 The regression line indicates the mean effect of climate on the correlation, while the shaded
558 areas depict the 50% and 89% credible intervals predicted by the model. Each black dot
559 represents the simulated observation-level correlation between both traits in a given year
560 depending on climate. Right panel: estimated vs. simulated intercepts and slopes for the
561 offspring mass and litter size sub-models. Dashed lines represent the value used to simulate the
562 data, while the distributions and intervals represent the posterior distributions estimated by the
563 model, alongside the median, 50%, 89% credible intervals. Litter size estimates are presented on
564 the log scale.

565



566

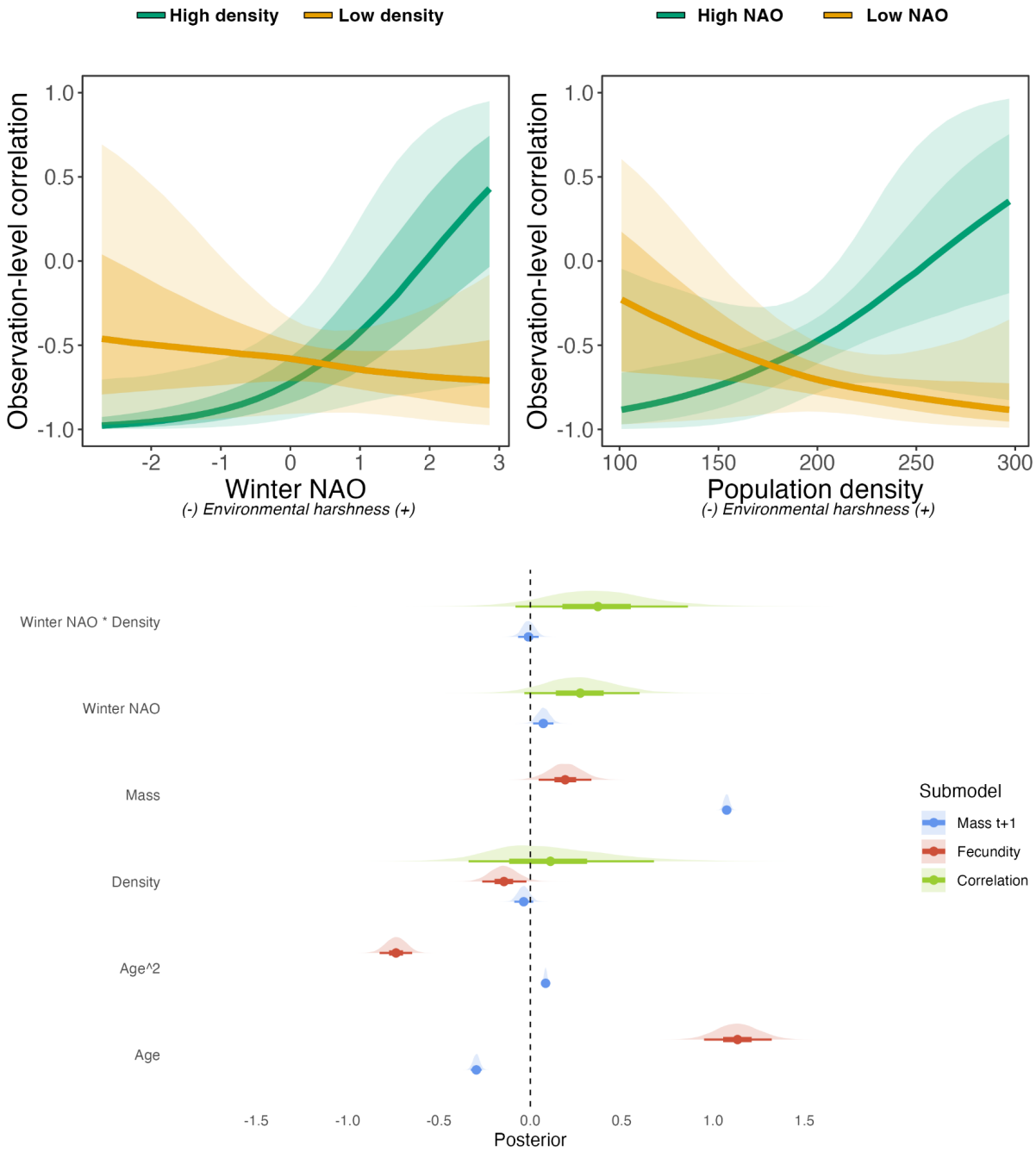
567 Figure 3: Left panel: estimated vs. simulated observation-level correlation between fecundity and
568 growth as a function of climate, after accounting for the effect of climate on both traits. The
569 regression line indicates the mean effect of climate on the correlation, while the shaded areas
570 depict the 50% and 89% credible intervals predicted by the model. Each black dot represents the
571 simulated observation-level correlation between both traits in a given year depending on climate.
572 Right panel: estimated vs. simulated intercepts and slopes for the growth and fecundity sub-
573 models. Dashed lines represent the value used to simulate the data, while the distributions and
574 intervals represent the posterior distributions estimated by the model, alongside the median,
575 50%, 89% credible intervals. Fecundity estimates are presented on the log scale.



576

577 Figure 4: Observation-level correlation between litter size and offspring mass in marmots as a
578 function of the total amount of snow in the preceding winter at high and low temperature (top
579 left panel) and the maximum daily June temperature of the year at high and low snow cover (top
580 right panel). Estimated effects of standardized predictors (bottom panel) on offspring mass,

fecundity, and the observation-level correlation between both traits in marmots. The regression line indicates the median estimated effect, while the shaded areas depict the 50% and 89% credible intervals predicted by the model.



584

Figure 5: Observation-level correlation between fecundity and mothers' mass in the following year in Soay sheep as a function of the winter NAO at high and low density (top left panel), and as a function of the population density at high and low winter NAO values (top right panel). Estimated effects (bottom panel) of standardized predictors on mother's mass in the following year, fecundity, and the observation-level correlation between both traits in Soay sheep. The figure displays the posterior distributions estimated by the model, alongside the median, 50%, and 89% credible intervals.

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Supplementary materials

Section S1: fixed individual heterogeneity

The models presented in the main text do not include distinct parameters for fixed individual heterogeneity across environmental contexts, hence considering observations from the same individual but in different environmental contexts as independent. Here, we illustrate why this limitation is needed to correctly estimate context-dependent covariation. Using simulated data, we illustrate that it is not possible to estimate the among-individual variation across context, while at the same time estimating among- and within- individual variation within context. However, it is important to note that not accounting for fixed individual heterogeneity should not have any consequences regarding the accuracy of the estimation of the context-dependent correlations.

For this purpose, we simulate demographic data with a tradeoff between parental growth and fecundity, suitable for the non-repeated measures CRN (model of equation 2). We include a fixed heterogeneity component (context-independent individual random effect), as well as the context-dependent component (context-dependent individual random effect) to make the correlation vary across contexts. The data is similar to what is presented in the "validation on simulated datasets" section, with the addition of the fixed heterogeneity component. We then analyze this simulated dataset either with a model that estimates only the context-dependent covariation (model presented in the manuscript, equation 2), or a model that does include fixed (context-invariant) individual random effects in addition to the context-dependent covariation (model of equation 2 with the addition of a context-independent individual random effect).

914 The figures for both scenarios are presented below, with Figure S1 highlighting that the
915 inclusion of a fixed among-individual random effect in the model leads to an erroneous
916 estimation of the context-dependent correlation. This is because the inclusion of this fixed
917 among-individual random effect captures part of the variation from the context-dependent
918 random effects, and therefore the context-dependent term will then only estimate deviations of
919 individuals from the fixed heterogeneity term. However, Figure S2 highlights that not including a
920 fixed among-individual random effect allows the model to properly recover the context-
921 dependent correlation.

922 Our results here reflect a more general theoretical point about the biological
923 interpretation of reaction norms. For any reaction norm model, there will not be a distinct
924 component of fixed individual heterogeneity separated from the process of phenotypic plasticity
925 shaping individual heterogeneity across environments. With simple linear reaction norms,
926 empiricists often conceptualize the intercept of the model as reflecting a fixed, environmentally
927 invariant component of the response, separate from the plastic effects described by reaction
928 norm slopes. However, while this can be heuristically useful for some purposes, it is in a strict
929 sense misleading, as the reaction norm intercept simply describes the variation expected when
930 the environmental variable defining the slope is fixed to 0 (e.g., in the average environment for
931 a mean-centered predictor or in the absence of an environmental exposure). Therefore, the value
932 of the intercept is no more fixed than the expected value at any other position along the slope
933 with respect to a fixed value of the environmental gradient. This thinking applies to the CRN and
934 any other reaction norm model. When sufficient data is available, individual random slopes could
935 also be estimated, which can be used to directly quantify the degree to which individuals' rank

order may shift across environments (Mitchell & Houslay, 2021). However, the depth of repeated sampling required to fit such models for present purposes is unlikely to be achieved by many currently existing datasets, motivating our CRN approach. Moreover, these random individual slopes will generally be of less interest for detecting demographic tradeoffs, as compared to the average shift in among-individual trait covariance across the population as determined by the fixed CRN slopes.

Taking a CRN approach to one's data thus requires taking seriously that there may not be any biologically meaningful sense in which there is a fixed level of individual heterogeneity irrespective of the environment (for traits that exhibit phenotypic plasticity). Rather, there is simply the amount of individual heterogeneity given a particular environment, prior to exposure to the environment, averaged across environments, and/or in the average environment. The parameters from the CRN can always be used to predict any such quantities of interest. For instance, applying the inverse link function to the intercept of the CRN (the first element of $\beta_{\boldsymbol{r}}$) will describe the expected trait correlation under the average environmental conditions.

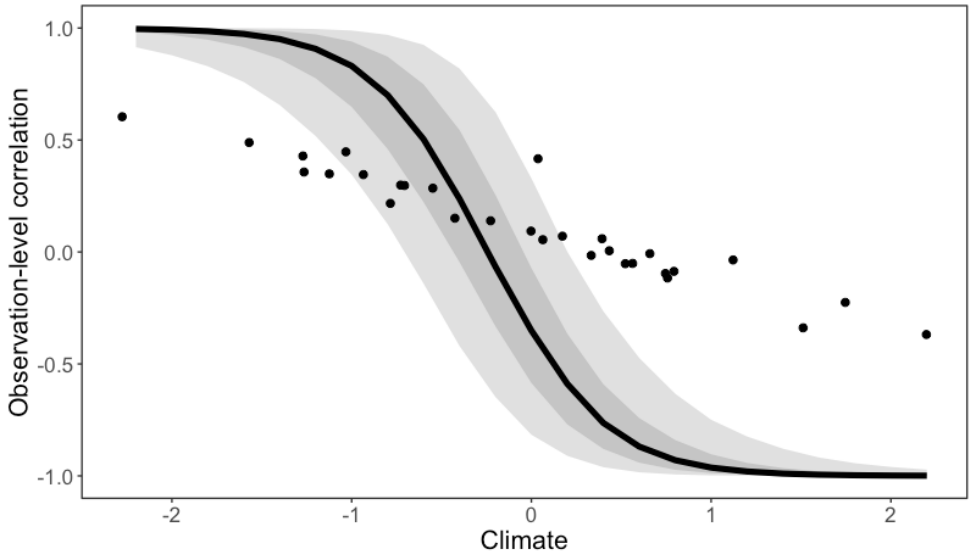


Figure S1: Estimated context-dependent correlation when a fixed individual-random effect is included. The regression line indicates the mean effect of climate on the correlation, while the shaded areas depict the 50% and 89% credible intervals predicted by the model. Each black dot represents the simulated observation-level correlation between both traits in a given year depending on climate. This highlights that the inclusion of a fixed individual random effect leads to a biased estimation of the context-dependent correlation.

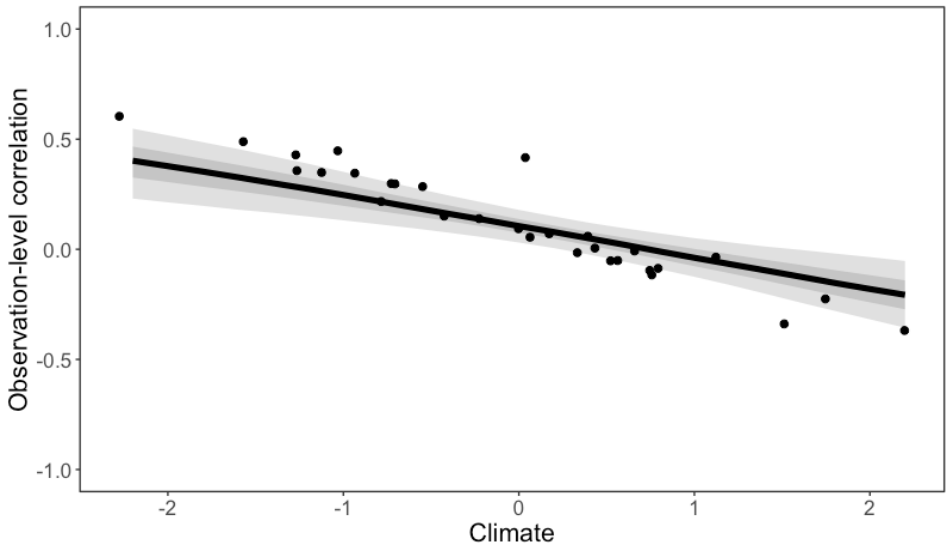


Figure S2: Estimated context-dependent correlation without the inclusion of a fixed individual-random effect in the model. The regression line indicates the mean effect of climate on the correlation, while the shaded areas depict the 50% and 89% credible intervals predicted by the model. Each black dot represents the simulated observation-level correlation between both traits in a given year depending on climate. This highlights that not including a fixed individual random effect leads to an appropriate estimation of the context-dependent correlation.

Section S2: posterior predictive checks

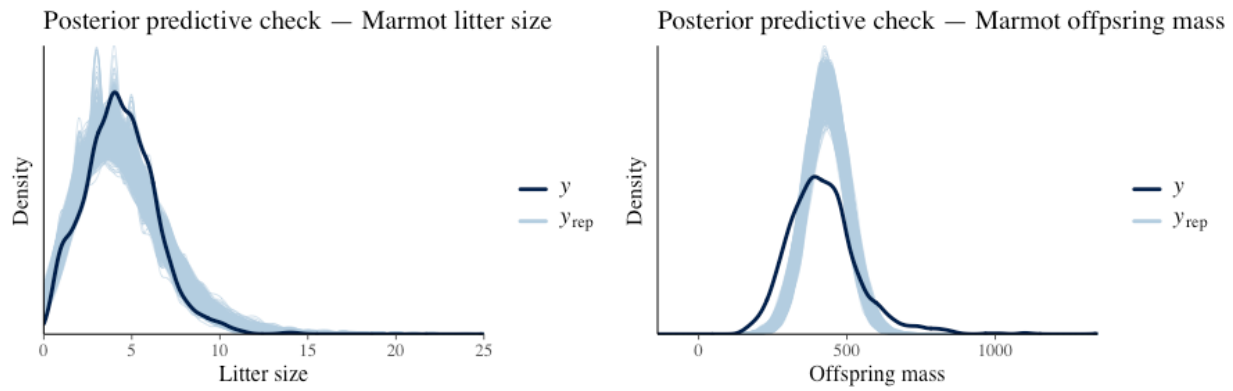
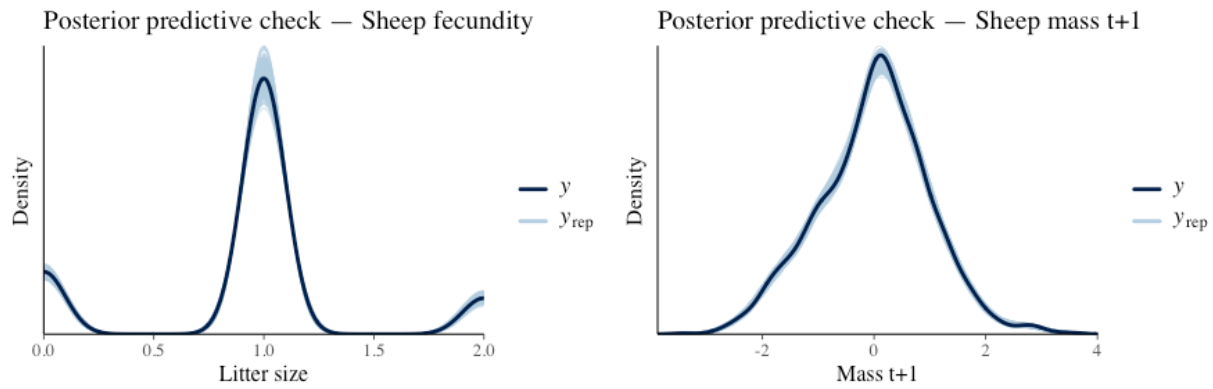


Figure S3: Posterior predictive checks showing the concordance between the distribution of the data (y) and the distribution of data generated under the statistical model (y_{rep}), for litter size (left panel) and offspring mass (right panel). This highlights a good fit for the litter size model. It also highlights that there is a slight overdispersion in offspring mass that is not accounted for by the model.



980

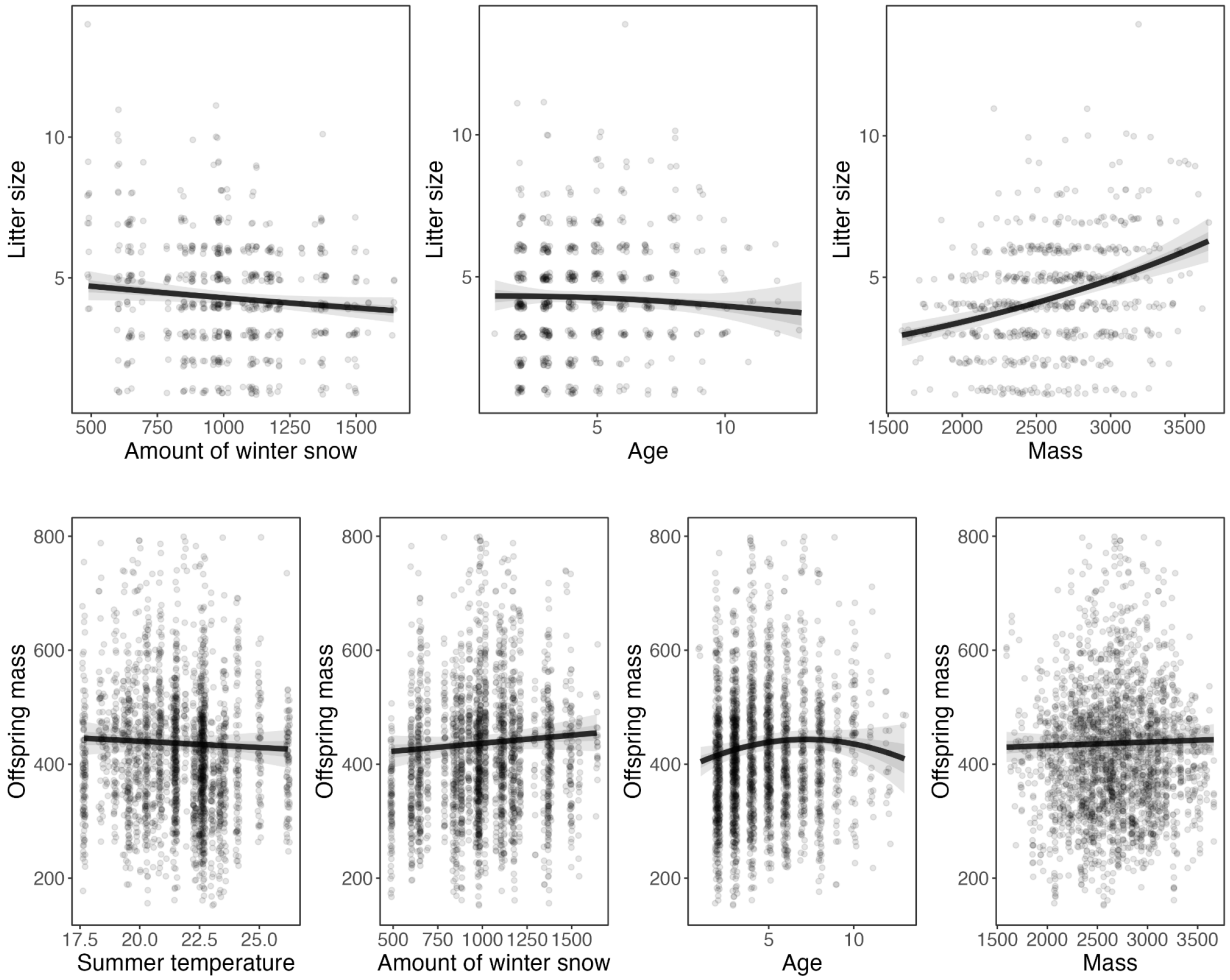
981 Figure S4: Posterior predictive checks showing the concordance between the distribution of the

982 data (y) and the distribution of data generated under the statistical model (y_{rep}), for number of

983 offspring (left panel) and ewe's mass in the following summer (right panel). This highlights a good

984 fit for both the litter size and mass models.

985 **Section S3: associations between the covariates and traits studied**



986

987 Figure S5: Top row: Association estimated by the model between the amount of winter snow,

988 age, and mass (panels from left to right) with litter size. Bottom row: Association estimated by

989 the model between summer temperature, the amount of winter snow, age, and mass (panels

990 from left to right) with offspring mass.

991

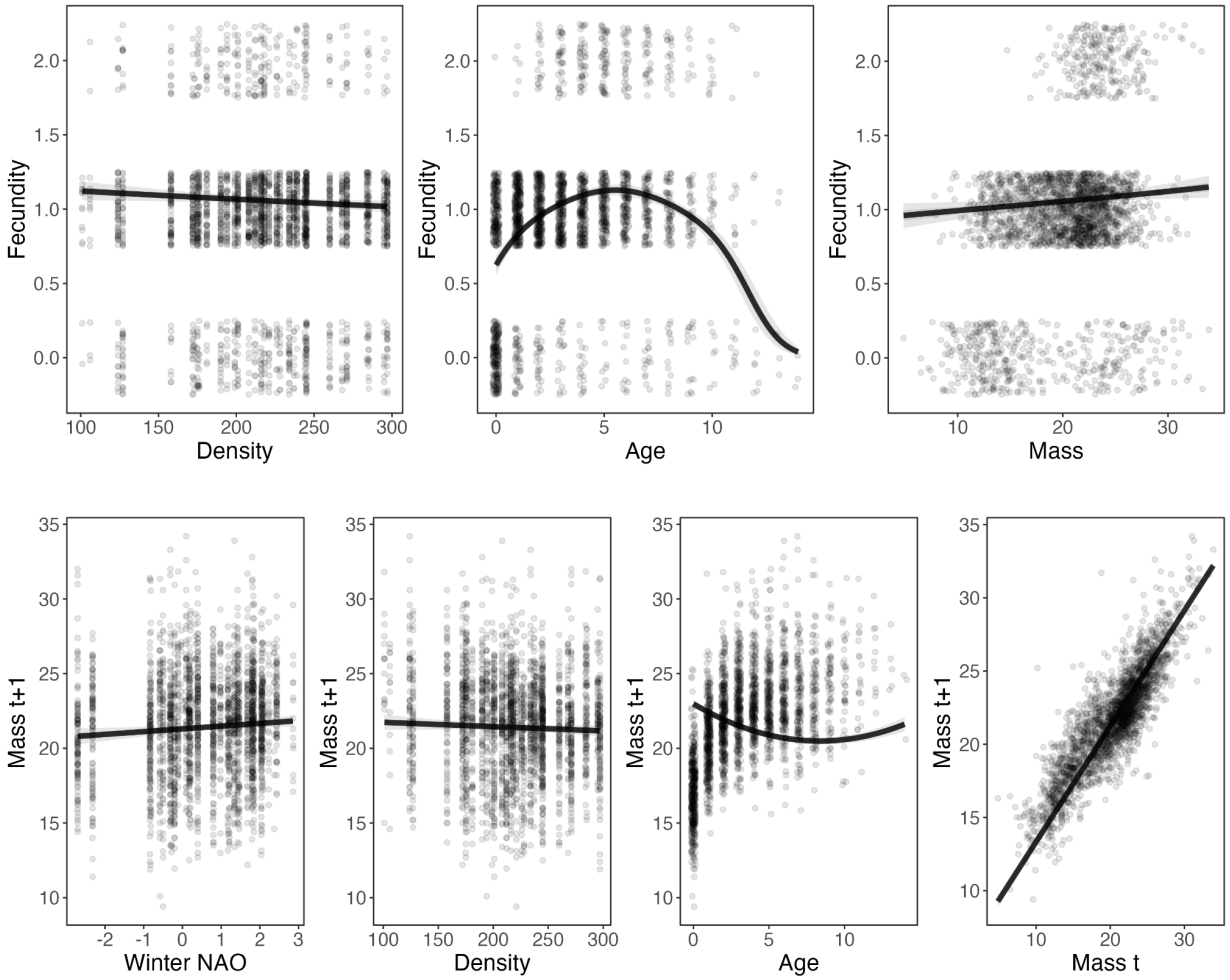


Figure S6: Top row: Association estimated by the model between population density, age, and mass (panels from left to right) with fecundity. Bottom row: Association estimated by the model between winter NAO, population density, age, and mass (panels from left to right) with mass at t+1.