

# 1 Indirect genetic effects should make group size more evolvable than 2 expected

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## 8 Abstract

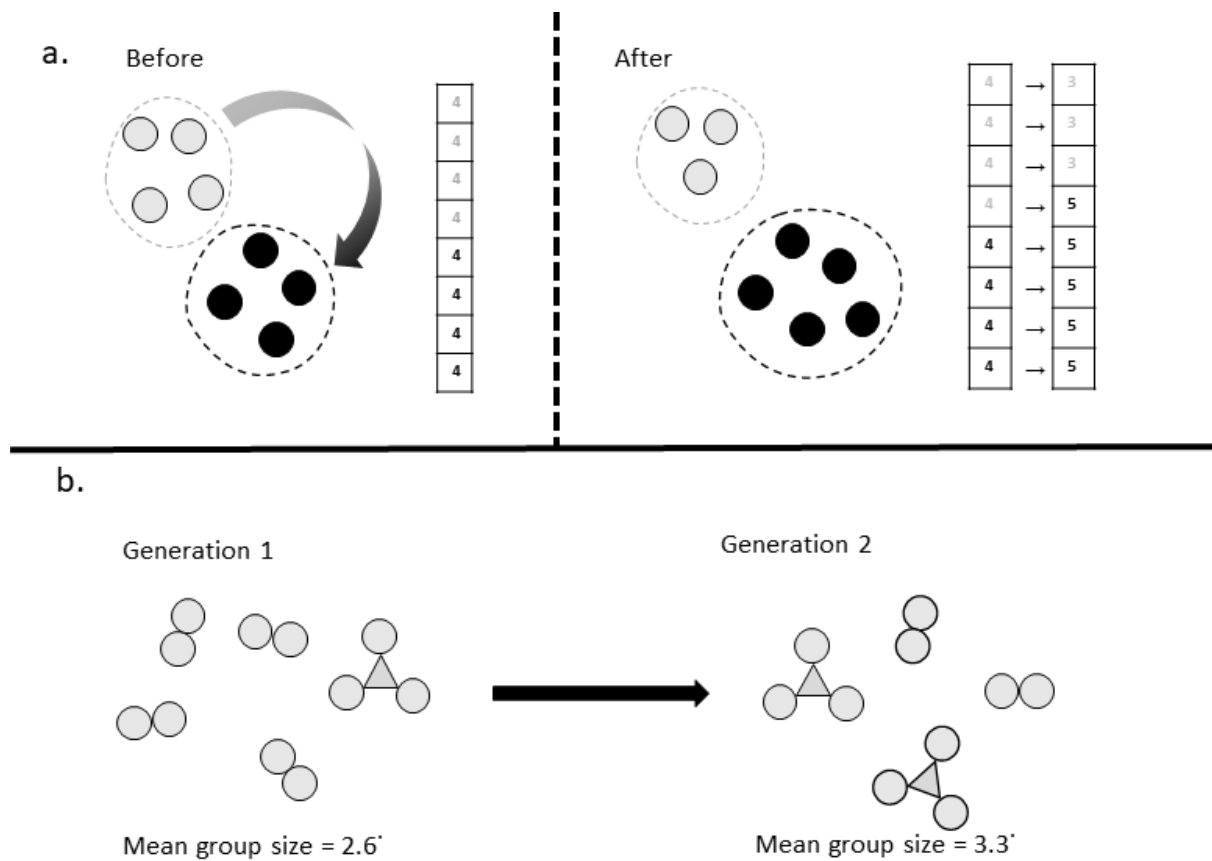
9 Group size is an important trait for many ecological and evolutionary processes. However, it is not a  
10 trait possessed by individuals but by social groups, and as many genomes contribute to group size  
11 understanding its genetic underpinnings and so predicting its evolution is a conceptual challenge.  
12 Here I suggest how group size can be modelled as a joint phenotype of multiple individuals, and so  
13 how models for evolution accounting for indirect genetic effects are essential for understanding the  
14 genetic variance of group size. This approach makes it clear that 1) group size should have a larger  
15 genetic variance than initially expected as indirect genetic effects always contribute exactly as much  
16 as direct genetic effects and 2) the response to selection of group size should be faster than  
17 expected based on direct genetic variance alone as the correlation between direct and indirect  
18 effects is always at the maximum positive limit of 1. Group size should therefore show relatively  
19 rapid evolved increases and decrease, the consequences of which and evidence for I discuss.

20 **Key words:** evolvability, group size, indirect genetic effects, joint phenotypes

## 22 Introduction

23 Understanding the evolution of traits that are jointly contributed to by multiple different organisms  
24 and genomes is difficult (Queller, 2014). For example, group size represents how many organisms  
25 are acting together within a limited space at a given time. Types of groups include shoals of fish and  
26 flocks of birds moving cohesively, offspring and their parent(s) associating prior to dispersal, and  
27 even long-term bonds in a monogamous pair can be thought of as groups of two individuals. Group  
28 size is an important trait as it impacts various ecological and evolutionary processes that are density  
29 dependent (e.g., sexual selection; Kokko & Rankin, 2006; McDonald, 2023). However, group size is  
30 not the property of one individual, and so its evolution cannot be modelled in the way we might  
31 model the trait of an individual such as its body mass e.g., by quantifying the narrow-sense

32 heritability and measuring selection on it. Multiple, potentially 1000s, of individuals contribute to  
 33 group size, with each individual contributing a small and equal amount to the overall size of the  
 34 group. Further, individuals impact both their own group size and the group size of others when they  
 35 join and leave groups. For instance, consider two groups of four. If one individual leaves one group  
 36 and joins another, it changes its own group size from four to five, increases the group size of its four  
 37 new groupmates from four to five, and decreases the group size of its old groupmates from four to  
 38 three (Fig. 1a). An individual’s underlying sociability therefore impacts both the group sizes it  
 39 experiences and those of others in the population. Understanding the genetic variation  
 40 underpinning the trait at the population level, and so being able to predict the evolutionary change  
 41 of the sizes of animal groups (depending on the association with fitness), therefore represents an  
 42 important but difficult task (see also: Radersma, 2020 for a similar problem for social network  
 43 phenotypes).



44

45 **Figure 1.** a. Plastic changes in group membership affect many individuals in the population, not  
 46 just the focal individual. In “Before”, we have two groups of four, coloured in grey and black. One  
 47 of the grey individuals moves into the black group, changing colour as it does, giving the “After”  
 48 situation. This single movement changes the group size of every individual in the two groups,  
 49 demonstrating how individuals affect each other’s group sizes. b. Evolved changes in sociability

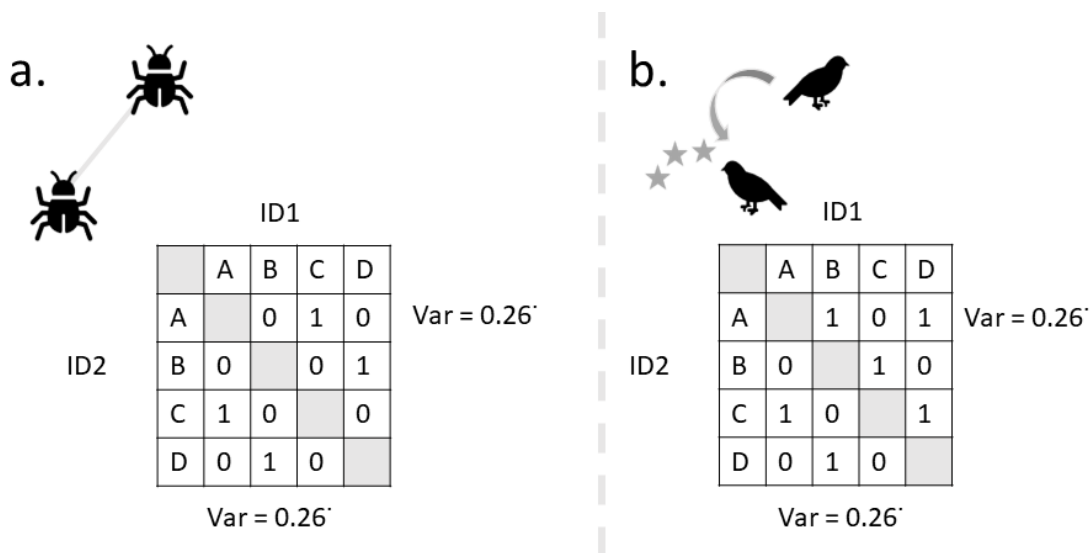
50 can lead to a rapid evolved change in mean group size. In Generation 1 there is a single sociable  
51 individual (the triangle) who associates with three others, while the remaining eight unsociable  
52 individuals associate in pairs, giving a mean group size of 2.6'. In Generation 2, one of the  
53 unsociable individuals has been replaced by a sociable individual, meaning there are now two  
54 groups of four and two pairs, and a mean group size of 3.3'; a rapid evolved increase. These two  
55 examples show how small changes in sociability can lead to large changes in group sizes.

56

57 One approach is to consider group memberships at each time point that a population is surveyed.  
58 This assumes that groups can be strictly defined at a given moment in time or for a set period and  
59 does not apply to fleeting or ephemeral associations. For each possible pair of individuals in the  
60 population, the individuals are either in the same group as each other or not (hereafter "paired or  
61 not", named distinctly to distinguish from the general concept of being in groups of any size). Being  
62 paired or not at a given point in time is therefore a binary trait under control of two individuals (even  
63 when overall groups are larger than two, paired or not always refers to two individuals). Note that  
64 we are not considering individual's preferences for particular others here, just their general  
65 tendency to be with other individuals in the most general sense. We expect that an individual's  
66 tendency to be paired or not will be influenced by its underlying sociability or gregariousness  
67 (Gartland *et al.*, 2022), a latent trait we cannot directly observe but through how often an individual  
68 is paired with others. Additionally, what is key is that, unlike traits that are completely under the  
69 control of the focal individual (such as eye colour), the phenotypic and genetic variance of traits  
70 influenced by two (or more) individuals, such as being paired or not, has both direct sources,  
71 stemming from the focal individual, but also indirect sources, stemming from the partner. In the  
72 case of being paired or not, an individual's trait will be influenced by both its own sociability (and  
73 genetic variance for that) and the sociability of its partner (and the genetic variance for that; note  
74 that the designation of focal and partner is arbitrary). In fact, in this formulation both individuals  
75 contribute exactly equally to the trait of being paired or not, and therefore the variance attributable  
76 to focal and partner individuals is identical.

77 For a population of size  $k$  at a given point in time, it is instructive to represent the paired status as a  
78 binary and symmetrical matrix  $\mathbf{K}$  of  $k \times k$  dimensions, where cells  $i, j$  and  $j, i$  are coded as "1" if  
79 individuals  $i$  and  $j$  are paired in the same group and coded as "0" if they are not (the diagonal itself is  
80 left blank; Fig. 2a). Mean group size can be recovered from this matrix by  $1 + \left[ \frac{\sum \mathbf{K}}{k} \right]$ , allowing  
81 comparison between the paired or not phenotype and groups size, a more common summary of  
82 population social structure. In Fig. 2a names of the columns indicate the (arbitrarily defined) focal,

83 while names of the rows indicate the (arbitrarily defined) partner. Note how the matrix in Fig. 2a is  
 84 symmetrical; there is exactly the same pattern of 0s and 1s on either side of the diagonal. Therefore,  
 85 the variances of direct and indirect effects for the trait of paired or not are identical. This can be  
 86 extended to cases where we have data on the number of times two individuals are paired. If there  
 87 are  $t$  observations, we have a symmetrical matrix  $K_t$  where valued terms replace the 1s. Mean group  
 88 size in this case is recovered through  $1 + [\frac{\sum K_t}{kt}]$ . For both the binary and the valued cases, because  
 89 an individual that is paired as a focal will also be paired as a partner, the correlation between a focal  
 90 individual's scores and those of its partners must be exactly 1. The fact that we have exactly identical  
 91 direct and indirect variances and a perfect, positive correlation between them has interesting  
 92 consequences when we consider the evolutionary potential of the trait of paired or not, and  
 93 therefore of group size.



94

95 **Figure 2.** a. When modelling group size using an indirect genetic effects model, individuals  
 96 contribute both to their own values for being paired, and to the values of others. Their  
 97 contributions as the focal (ID1) and partner (ID2) are identical, and so the variances are the same  
 98 and their correlation is exactly 1. B. When modelling the outcome of dyadic contests for  
 99 dominance in the same way, we see that individuals contribute to the outcome both as a focal  
 100 and as a partner, but in this case their contributions are exactly opposite, and so, while the  
 101 variances are equal, the correlation is exactly -1.

102

103 The evolutionary potential of a trait is defined by its additive genetic variance. Typically, we only  
 104 consider the *direct* additive genetic variance, i.e., how the genes in a focal organism influence its  
 105 own trait. However, when other individuals influence the trait value, then we must also account for

106 *indirect* additive genetic variance i.e., how the genes in others influence the focal's trait value (Scott  
 107 & Fuller, 1965; Griffing, 1967; Moore *et al.*, 1997). Indirect genetic effects can contribute substantial  
 108 additional genetic variance to morphological, life history, physiological, and behavioural traits (Ellen  
 109 *et al.*, 2014). Further, as I have argued above, indirect genetic effects must contribute exactly as  
 110 much to the total genetic variance of the trait of paired or not as direct genetic effects do. In  
 111 essence, individuals with genetic variants that increase their sociability will join groups more often,  
 112 and therefore will increase the group sizes of other individuals in the population. This greatly  
 113 increases the evolutionary potential of the trait, as a small increase (decrease) in sociability across  
 114 generations will increase (decrease) the frequency at which individuals are with others, altering the  
 115 group size of large portions of the population (Fig. 1b).

116 To quantify the change in evolutionary potential brought about by indirect genetic effects, we can  
 117 consider the total heritable variance in a trait with and without indirect genetic effects. The trait we  
 118 are considering here is whether an individual is paired or not with each other individual in the  
 119 population (giving  $k(k - 1)$  measures), rather than mean group size or total number of individuals  
 120 in the group. The total heritable variance ( $\hat{\sigma}_H^2$ ) reflects the amount of variation of a trait in a  
 121 population which is underpinned by genetic variation, rather than environmental or stochastic  
 122 variation.  $\hat{\sigma}_H^2$  in the absence and presence of indirect genetic effects is shown in eqs. 1 & 2  
 123 respectively (Bijma, 2011). In eq. 1 it is simply equal to the direct additive genetic variance ( $\sigma_{A_D}^2$ ).

$$124 \quad \hat{\sigma}_H^2 = \sigma_{A_D}^2 \quad \text{eq. 1}$$

125 In eq. 2 (including indirect genetic effects)  $\hat{\sigma}_H^2$  includes  $\sigma_{A_D}^2$ , the indirect additive genetic variance  
 126 ( $\sigma_{A_I}^2$ ), and twice the covariance between direct and indirect effects ( $\sigma_{A_{DS}}$ ).

$$127 \quad \hat{\sigma}_H^2 = \sigma_{A_D}^2 + 2 \sigma_{A_{DS}} + \sigma_{A_I}^2 \quad \text{eq. 2}$$

128 Note that this is the same calculation as for the more familiar maternal genetic effects model  
 129 (Mousseau & Fox, 1998). Note also that in models where more than two individuals interact the  
 130 number of interacting individuals (or the group size,  $n$ ) minus one is included in the calculation  
 131 (Bijma & Wade, 2008), but since we are modelling our phenotype as a product of only and always  
 132 exactly two individuals interacting,  $n-1$  always equals 1 and so does not affect the sum. What is clear  
 133 in the case of being paired or not is that, as  $\sigma_{A_{DS}}$  is guaranteed to be positive, eq. 2 will always be  
 134 larger, and potentially much larger, than eq. 1. Therefore, being paired or not, and so group size, will  
 135 have a larger total heritable variance than initially expected based on  $\sigma_{A_D}^2$  alone and therefore could  
 136 have substantial potential for evolution.

137 Further, when predicting the response to selection, the covariance between direct and indirect  
138 genetic effects can radically alter our estimates (Moore *et al.*, 1997). The response to selection  
139 (change in mean phenotype across a single generation;  $\Delta\bar{P}$ ) in the absence of indirect genetic effects  
140 is given in *eq. 3*; it is simply the product of the selection gradient ( $\beta$ ) and the direct additive genetic  
141 variance (Muir, 2005; Bijma & Wade, 2008):

$$142 \quad \Delta\bar{P} = \beta\sigma_{A_D}^2 \quad \text{eq. 3}$$

143 Meanwhile, the response to selection in the presence of indirect genetic effects includes the direct  
144 indirect genetic covariance:

$$145 \quad \Delta\bar{P} = \beta[\sigma_{A_D}^2 + \sigma_{A_{DS}}]$$
 eq. 4

146 Positive values of  $\sigma_{A_{DS}}$  greatly enhance the response to selection, speeding evolution, while negative  
147 values can reduce, remove, or even reverse the response to selection (Bijma *et al.*, 2007; Bijma &  
148 Wade, 2008), potentially causing evolutionary change to move in the opposite direction to selection  
149 (Fisher & Pruitt, 2019). In the case of being paired or not, as I have argued above, we must have a  
150 strong (the strongest possible) positive covariance between direct and indirect genetic effects.  
151 Individuals with genes that predispose them to join others and so make groups larger also cause  
152 other individuals to be with others and so be in larger groups (or be in a group at all). Therefore,  
153 group size has a larger evolutionary potential than initially expected, as both direct and indirect  
154 genetic effects must contribute to its total genetic variation, and evolutionary responses will be  
155 especially rapid as these direct and indirect effects are also perfectly positively correlated.

156 Interestingly, this is the exact inverse situation to that of another trait expressed jointly: outcomes in  
157 dyadic contests for dominance. In the case of dyadic contests, each contest must have one winner  
158 and one loser. These outcomes are therefore perfectly *negatively* correlated, as if the focal  
159 individual wins its partner always loses, and vice versa. As Wilson *et al.* (2011) have highlighted, the  
160 indirect genetic variance for outcomes in dyadic contests must equal the direct genetic variance, as  
161 designation of focal and partner is again arbitrary and so both contribute equally to the outcome.  
162 Further, the direct-indirect genetic correlation must be -1, as individuals with genes that predispose  
163 them to win contests cause other individuals to lose contests. Another way of thinking about this is  
164 to consider the matrix in Fig 2b, which shows the outcomes of dyadic contests in a population. This  
165 matrix is asymmetrical; if there is a “1” in a cell in the top right half, there is a “0” in the  
166 corresponding cell on the opposite side of the diagonal in the bottom left half, and vice versa. The  
167 consequences for the predicted evolution of average dyadic contest outcome are stark: evolutionary  
168 change in the trait mean becomes *impossible* as predicted increases through direct effects are  
169 always exactly cancelled out by changes in the opposite direction in indirect effects (this appeals to

170 our common sense, half of all in the individuals participating in dyadic contests must lose [trait value  
171 of 0], while half win [trait value 1], and so the mean trait value can never differ from 0.5, and so  
172 should never be able to evolve; Wilson *et al.*, 2011).

173 The cases of paired or not and the outcomes of dyadic contests are exact mirrors of each other; in  
174 both cases the direct genetic variance must equal the indirect genetic variance, and for both we  
175 expect perfect correlations between direct and indirect genetic effects. However, for paired or not  
176 this is a perfect positive correlation (Fig. 2a), while for outcomes of dyadic contests it is perfectly  
177 negative (Fig. 2b). Therefore, while for dyadic contest outcome we never expect evolution, for  
178 paired or not (and so group size) we expect relatively rapid evolutionary changes (which could be  
179 increases or decreases in mean group size).

180 While the result for paired or not might seem esoteric, it is actually quite intuitive. If an individual  
181 starts off alone, and then joins a group (of size  $n$ ), they increase not only their own group size (from  
182 1 to  $n + 1$ ) but also the group size of all those already in the group (from  $n$  to  $n + 1$ ). If this initially  
183 lone individual and the group they join are the only animals in the population, the mean group size  
184 in the population goes from  $(1 + n*n) / (n + 1)$  to  $n + 1$ , a rapid increase at the population level given  
185 only one individual changed its behaviour (if  $n$  was 30 this is an increase from 29.06 to 31). If we  
186 imagine the same process, but instead of plastic change within a generation, evolved change across  
187 generations, it is easy to see how rapid changes in group size can occur (see also Fig. 1). Even small  
188 increases in sociability will give a rapid increase in mean group size as not only are the more sociable  
189 individuals in larger groups, but even those with the same underlying tendency to be sociable as the  
190 previous generation have a higher mean group size, as they are more often being joined by the more  
191 sociable individuals (Fig. 1b). This is true independently of the conceptual framework used to  
192 understand it; my use of indirect genetic effects is merely a tool to make accurate predictions about  
193 change across generations. It might seem more straightforward to measure sociability directly, and  
194 to estimate its heritability and selection on it, but sociability is a latent trait that can only be inferred  
195 from observations of individuals interacting with others, and so it always needs untangling from  
196 indirect effects (Fisher, 2023). When we observe individuals forming groups, the phenotypes we are  
197 observing are inherently a product of at least two genomes, a phenomenon that evolutionary  
198 models incorporating indirect genetic effects, which I highlight here, are specifically designed to  
199 account for (see also: Queller, 2014).

200

## 201 Consequences of the higher evolvability of group size

202 The primary consequence of the increased total heritable variance in group size is that we expect to  
203 see relatively rapid increases (decreases) across generations in mean group size when selection  
204 favours (disfavours) larger groups. Note that the initial genetic variation in being paired or not may  
205 still be quite small, especially if environmental variation strongly influences grouping, and so the  
206 total heritable variation in group size may not be large in the absolute sense, but it should always be  
207 larger than that expected from direct genetic effects alone. Group size is commonly linked to fitness,  
208 as it can provide protection for predators and access to mates and other resources, but also be  
209 associated with increased food competition and exposure to disease. Variation in group size may  
210 therefore often be linked to variation in fitness, and so individual sociability may be under selection  
211 in a range of systems (Snyder-Mackler *et al.*, 2020; Gartland *et al.*, 2022; selection on group size is  
212 discussed more below). Given we now expect a higher degree of genetic variation in group size,  
213 evolved changes should be common, albeit I have no general expectations about a direction (i.e., I  
214 do not expect animals to be typically evolving to live in larger or smaller groups). In the presence of  
215 consistent directional selection, we expect group sizes to rapidly evolve in line with selection (*eq. 4*).  
216 Even if selection was weak and highly variable in direction, we would still expect relatively rapid  
217 changes in group size across generations as there is large amounts of genetic variation, but these will  
218 be both increases and decreases, and so mean group sizes should be highly variable around a mean  
219 value over evolutionary time. However, as noted above, the trait of paired or not could have  
220 exceptionally low direct genetic variance if the tendency to be paired is strongly influenced by  
221 environmental effects such as current resource availability or predation risk. In this case, even the  
222 addition of indirect effects may not raise the total heritable variance to a particularly high level,  
223 keeping the rate of evolutionary change low. Directly estimating the direct and indirect genetic  
224 variance in the tendency to be in pairs in wild populations is key for understanding the trait's  
225 evolutionary potential, and therefore the evolutionary potential of group size.

226 A high variability of group size over evolutionary timescales would mean that other ecological and  
227 evolutionary processes that depend on group size should also be highly variable. For instance, the  
228 spread of an infection through a population can depend on the typical group size, if transmission is  
229 fast within groups and not between them (Nunn *et al.*, 2015). Fewer, larger groups will then allow a  
230 faster spread than many small groups. If group sizes are variable across generations, then the speed  
231 of disease spread, or indeed any processes that is influenced by group size, will also be highly  
232 variable. This high degree of variability means that making predictions for timescales encompassing  
233 multiple generations will be difficult.



234 In the presence of direct selection for larger groups, we would expect to see a rapid increase in  
235 group size. For short-lived species such as some insects, multiple generations can occur in a year or  
236 even season, and so evolved changes in group size might be observably on those timescales. We  
237 already are aware that large aggregations of pest insects such as desert locust (*Schistocerca*  
238 *gregaria*) can appear seemingly from nowhere, with plastic changes in aggregative behaviour  
239 assumed to be behind this (Uvarov, 1921; recently reviewed in: Simpson, 2022). However, evolved  
240 changes in sociability and therefore group size might also contribute if selection for larger groups  
241 emerged, given that those changes could be very rapid. The importance of evolved changes for  
242 outbreaks in desert locust is likely limited due to their generation times (although changes in social  
243 behaviour across generations do appear possible; Roessingh *et al.*, 1993) but in short-lived species  
244 such as *Drosophila spp.* the importance of evolved changes is more plausible (Behrman *et al.*, 2018).

245 The evolution of group size as discussed here may also apply to the evolution of multicellularity. In a  
246 population of unicellular organisms, a mutant cell that adheres to or joins other individuals forms a  
247 multicellular aggregation not just for itself, but for the other individual(s) it has joined (Fig. 1b).  
248 Change in mean phenotype (the number of cells grouped together) could then change relatively  
249 quickly as more “sociable” cells (such as those *Saccharomyces cerevisiae* that express flocculin  
250 proteins that bind cells together; Belpaire *et al.*, 2022) would lead to many cells being involved in  
251 multicellular aggregations, whether the other cells have an innate tendency to group or not. Further  
252 work on facultatively multicellular organisms such as *S. cerevisiae* under artificial selection for “floc”  
253 formation (Fisher & Regenberg, 2019) could test whether the evolution of multicellularity is faster  
254 than that expected based on direct genetic variance for production of flocculin proteins alone.

255

## 256 Selection on group size

257 While this article is focused on the total heritable variation in group size, when considering the  
258 evolution of this trait we must also consider selection on group size, and how that depends on the  
259 type of genetic variation available. For species that form groups, we often expect the relationship  
260 between group size and fitness to be humped, such that fitness for individuals within a group  
261 increases with increasing group size up to an optimum, and then declines (Sibly, 1983). The shape of  
262 this relationship might be due to initial benefits such as detection of predators with increased group  
263 sizes, and but increased costs of group size after a point such as risk of transmission of diseases at  
264 especially high group sizes. In standard models for phenotypic selection, this could be captured  
265 through the use of linear and quadratic selection gradients, where we would expect a positive linear  
266 gradient and a negative quadratic one (Phillips & Arnold, 1989). Note that for group size to have

267 fitness consequences the associations need to be more than simply ephemeral co-locations in space  
268 and time, which fits within my general definition of groups given above.

269 As group co-membership is a joint phenotype, it is partly under control of both current  
270 group members and those other individuals who may be alone or in other groups who wish to join  
271 another group. This means there can be a conflict of interest (in terms of fitness outcome) for  
272 individuals joining an existing group (Giraldeau & Caraco, 1993; Higashi & Yamamura, 1993). If a  
273 group is at the optimum size, additional individuals joining would imply fitness costs for the current  
274 group members, as they are now in a group larger than the optimum. In contrast, from the  
275 perspective of the joining individual, their fitness is likely to be increased by joining, as they  
276 transition from being alone into a group that will give them higher fitness, even if it is above the  
277 optimum group size (Sibly, 1983). The resolution of this conflict depends on both who controls group  
278 membership (current group members or joining individuals) and the relatedness between  
279 interacting individuals (Giraldeau & Caraco, 1993; Higashi & Yamamura, 1993). The fact that joining  
280 individuals can reduce the fitness of current group members indicates that a form of negative social  
281 selection is acting on group membership, when the trait of one individual reduces the fitness of  
282 others (Wolf *et al.*, 1999), which could lead to mean fitness in the population being below the  
283 maximum possible (“maladaptation”; McGlothlin & Fisher, 2021). Further, social selection interacts  
284 with indirect genetic effects (which we expect to be ubiquitous for group co-membership) to  
285 influence the phenotypic response to selection (along with relatedness; Bijma & Wade, 2008). As we  
286 now always expect a positive correlation between direct and indirect effects, the additional effect of  
287 indirect genetic effects should be to accelerate the response to selection, in whichever direction the  
288 combination of relatedness and direct and social selection suggests (Bijma & Wade, 2008; see also:  
289 McGlothlin *et al.*, 2014).

290 Finally, a note on group-level (or among-group) selection gradients (Goodnight *et al.*, 1992;  
291 Okasha, 2004a). Within a single observation, all individuals within a group have the same group size.  
292 Therefore, at this temporal scale there can be no within-group selection gradient for this trait, and  
293 all selection must manifest itself at the among-group level (if taking a Price covariance approach,  
294 partitioned to the among-group covariance rather than the within-group covariance; Okasha,  
295 2004b). Across multiple observations, individuals can be part of many groups, and so fitness due to  
296 group size can vary both within and among groups. This would imply that selection can indeed act at  
297 multiple levels. Care therefore should be taken when estimating and interpreting selection  
298 gradients; understanding what they mean both in isolation and what can be inferred from the  
299 combination of within- and among-group selection (Goodnight *et al.*, 1992).

300

### 301 Evidence for the evolvability of group size

302 Above I have outlined that we expect group size to be highly evolvable, given that there should be  
303 genetic variance from indirect and well as direct sources in the tendency to be paired with other  
304 individuals, and the covariance between these will always be positive. Is there any empirical  
305 evidence that allows us to evaluate whether this is the case or not? The one case study I am aware  
306 of indicated that sociability does indeed have genetic variance, and responds to selection, but we  
307 cannot evaluate whether it is at the pace expected. Scott *et al.* have determined that sociability is  
308 heritable in both male ( $h^2 = 0.24$ ) and female ( $h^2 = 0.21$ ) fruit flies *Drosophila melanogaster* (Scott *et al.*  
309 *et al.*, 2018), and that it increases (decrease) in response to artificial selection for higher (lower)  
310 sociability (Scott *et al.*, 2022). In their study, sociability was measured by allowing 16 flies in an arena  
311 to form groups (Scott *et al.*, 2022), and so was analogous to being paired or not and also mean group  
312 size; the formulation of grouping using in the current article. Scott and colleagues have therefore  
313 effectively assessed whether mean group size responds to artificial selection. They found it did, with  
314 an increase of 40% in females and 54% in males over 25 generations. Scott *et al.* (2022) performed  
315 within-group selection, taking the four most (or least for the down-selected lines) sociable flies in  
316 each of 12 groups, for both males and females, per generation. This mode of selection does not take  
317 advantage of any genetic variation among groups (Muir, 2005; Muir *et al.*, 2013), and so it is not  
318 clear whether the observed response is faster or slower than that expected by the narrow sense  
319 heritabilities found in their earlier work, and therefore if it is as fast as that predicted by the model  
320 of evolution accounting for indirect genetic effects I present here. Nevertheless, this study does at  
321 least show that group size responds to artificial selection, and so must possess some genetic  
322 variance. Further work would need to select for the most sociable animals across all individuals  
323 within a population, not just within each group, and measure the increase of group size across  
324 generations, in order to test the prediction that the evolution of group size should be relatively  
325 rapid.

326

### 327 Indirect effects on sociability itself

328 A final consideration is that an individual's sociability itself may be influenced by indirect genetic  
329 effects. An individual's decision to join or leave groups may be influenced by the traits of the other  
330 individuals already in those groups. If those traits are partly genetically determined, then there will  
331 be indirect genetic effects on sociability (Fisher, 2023). Therefore, an individual's *willingness* to join a  
332 group will be influenced by the genes of others (Fisher, 2023), but also its *realised* group size will be

333 influenced by the genes of others (this article). The overall heritability of group size may therefore  
334 be influenced by direct genetic effects for sociability (individuals' have an underlying preference to  
335 be with others that is partly genetically determined), indirect genetic effects for sociability (an  
336 individual's preference to be with others depends on their traits and therefore also their genes), and  
337 indirect genetic effects for group size (the sociability of others, and therefore their genes, influences  
338 the realised group size of an individual), plus the covariances among these components. Predicting  
339 the outcome of this is complicated, but parallels may be drawn with models for the heritability of  
340 social phenotypes in social networks using latent variables representing the tendency to be social  
341 and the contribution to social associations (Radersma, 2020).

342

### 343 Conclusions

344 In summary, I have suggested that the evolution of group size can be understood using an indirect  
345 genetic effects model. This model predicts that group size should have a relatively large genetic  
346 variance and so should respond surprisingly rapidly to selection. This high evolvability will increase  
347 the variability in demographic, ecological, and evolutionary processes that depend on group size.  
348 Testing whether this prediction is true or not is the next step.

349

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354

### 355 References

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