

1 Indirect genetic effects should make group size more evolvable than 2 expected

3

4 David N. Fisher

5 School of Biological Sciences, University of Aberdeen, King's College, Aberdeen, AB243FX

6 david.fisher@abdn.ac.uk

7

8 Abstract

9 Group size is an important trait for many ecological and evolutionary processes. However, it is not a
10 trait possessed by individuals but by social groups, and as many genomes contribute to group size
11 understanding its genetic underpinnings and so predicting its evolution is a conceptual challenge.
12 Here I suggest how group size can be modelled as a joint phenotype of multiple individuals, and so
13 how models for evolution accounting for indirect genetic effects are essential for understanding the
14 genetic variance of group size. This approach makes it clear that 1) group size should have a larger
15 genetic variance than initially expected as indirect genetic effects always contribute exactly as much
16 as direct genetic effects and 2) the response to selection of group size should be faster than
17 expected as the correlation between direct and indirect effects is always at the maximum positive
18 limit of 1. Group size should therefore show relatively rapid evolved increases and decrease, the
19 consequences of which and evidence for I discuss.

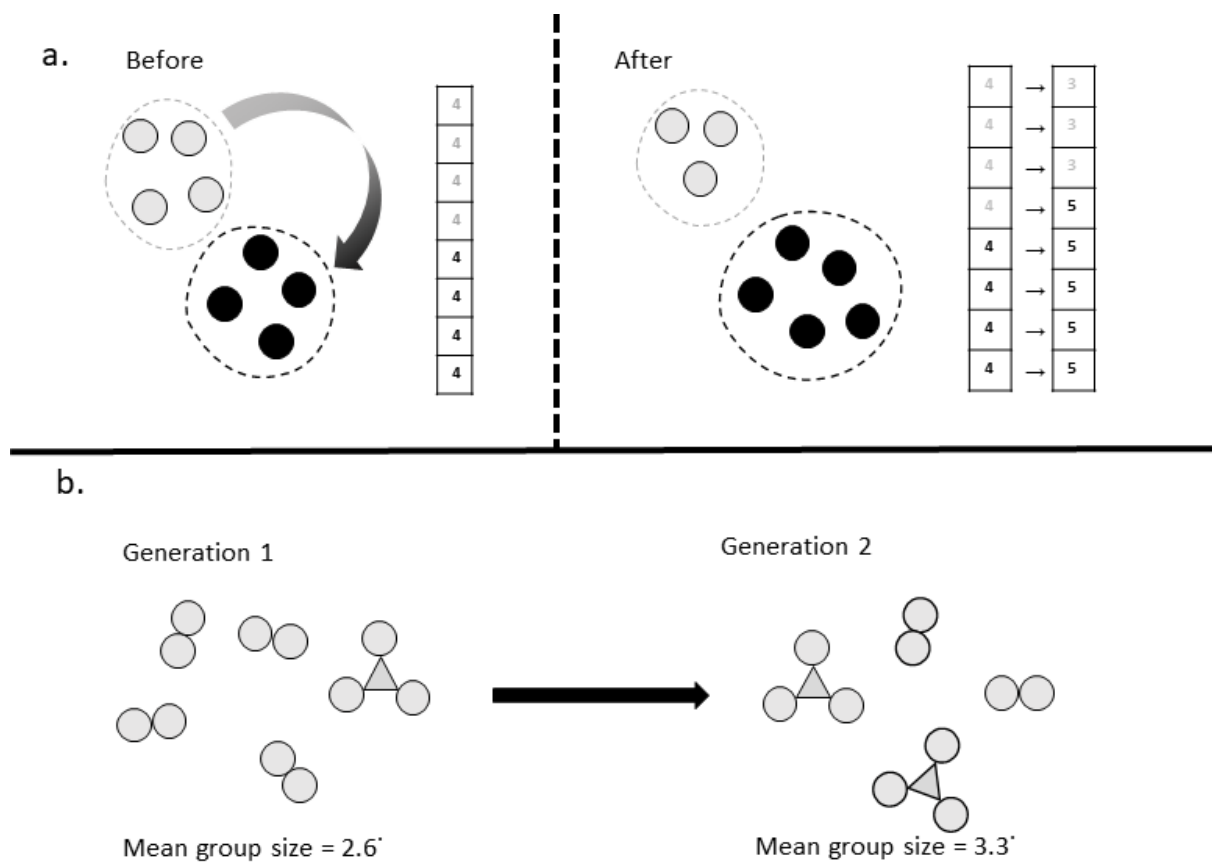
20 **Key words:** evolvability, group size, indirect genetic effects, joint phenotypes

21

22 Introduction

23 Understanding the evolution of traits that are jointly contributed to by multiple different organisms
24 and genomes is difficult (Queller, 2014). For example, group size represents how many organisms
25 are acting together within a limited space at a given time. Types of groups include shoals of fish and
26 flocks of birds moving cohesively, offspring and their parent(s) associating prior to dispersal, and
27 even long-term bonds in a monogamous pair can be thought of as groups of two individuals. Group
28 size is an important trait as it impacts various ecological and evolutionary processes that are density
29 dependent (e.g., sexual selection; Kokko & Rankin, 2006; McDonald, 2023). However, group size is
30 not the property of one individual, and so its evolution cannot be modelled in the way we might

31 model the trait of an individual such as body mass e.g., by quantifying the narrow-sense heritability
 32 and measuring selection on it. Multiple, potentially 1000s, of individuals contribute to group size,
 33 with each individual contributing a small and equal amount to the overall size of the group. Further,
 34 individuals impact both their own group size and the group size of others when they join and leave
 35 groups. For instance, consider two groups of four. If one individual leaves one group and joins
 36 another, it changes its own group size from four to five, increases the group size of its four new
 37 groupmates from four to five, and decreases the group size of its old groupmates from four to three
 38 (Fig. 1a). An individual's underlying sociability therefore impacts both the group sizes it experiences
 39 and those of others in the population. Understanding the genetic variation underpinning the trait at
 40 the population level, and so being able to predict the evolutionary change of the sizes of animal
 41 groups, therefore represents an important but difficult task (see also: Radersma, 2020 for a similar
 42 problem for social network phenotypes).



43
 44 **Figure 1.** a. Plastic changes in group membership affect many individuals in the population, not
 45 just the focal individual. In “Before”, we have two groups of four, coloured in grey and black. One
 46 of the grey individuals moves into the black group, changing colour as it does, giving the “After”
 47 situation. This single movement changes the group size of every individual in the two groups,
 48 demonstrating how individuals affect each other's group sizes. b. Evolved changes in sociability

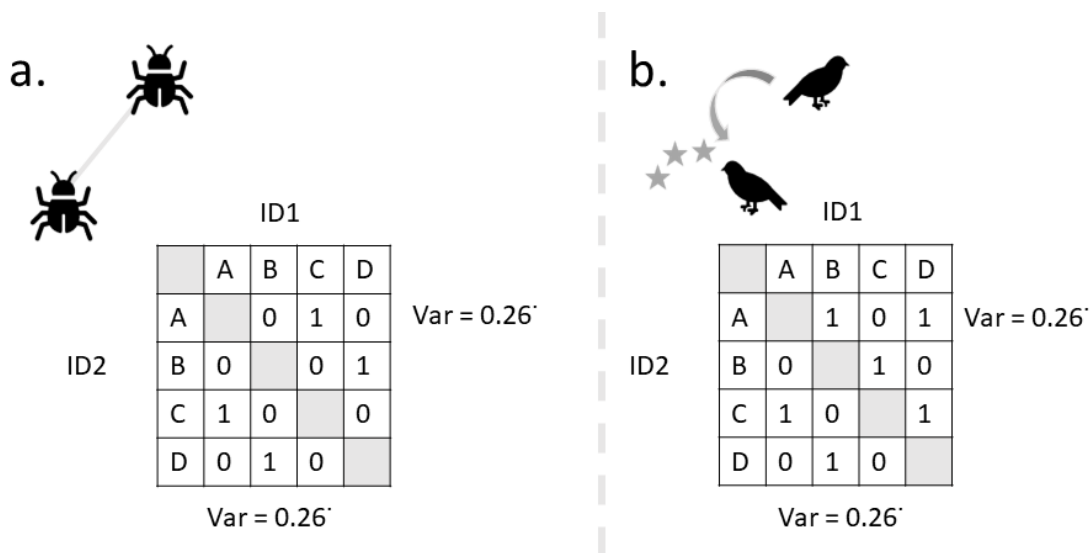
49 can lead to a rapid evolved change in mean group size. In Generation 1 there is a single sociable
50 individual (the triangle) who associates with three others, while the remaining eight unsociable
51 individuals associate in pairs, giving a mean group size of 2.6'. In Generation 2, one of the
52 unsociable individuals has been replaced by a sociable individual, meaning there are now two
53 groups of four and two pairs, and a mean group size of 3.3'; a rapid evolved increase. These two
54 examples show how small changes in sociability can lead to large changes in group sizes.

55

56 One approach is to consider group memberships at each time point that a population is surveyed.
57 This assumes that groups can be strictly defined at a given moment in time or for a set period and
58 does not apply to fleeting or ephemeral associations. For each possible pair of individuals in the
59 population, the individuals are either in the same group as each other or not (hereafter "paired or
60 not", named distinctly to distinguish from the general concept of being in groups of any size). Being
61 paired or not at a given point in time is therefore a binary trait under control of two individuals (even
62 when overall groups are larger than two, paired or not always refers to two individuals). Note that
63 we are not considering individual's preferences for particular others here, just their general
64 tendency to be with other individuals in the most general sense. We expect that an individual's
65 tendency to be paired or not will be influenced by its underlying sociability or gregariousness
66 (Gartland *et al.*, 2022), a latent trait we cannot directly observe but through how often an individual
67 is paired with others. Additionally, what is key is that, unlike traits that are completely under the
68 control of the focal individual (such as eye colour), the phenotypic and genetic variance of traits
69 influenced by two (or more) individuals, such as being paired or not, has both direct sources,
70 stemming from the focal individual, but also indirect sources, stemming from the partner. In the
71 case of being paired or not, an individual's trait will be influenced by both its own sociability (and
72 genetic variance for that) and the sociability of its partner (and the genetic variance for that; note
73 that the designation of focal and partner is arbitrary). In fact, in this formulation both individuals
74 contribute exactly equally to the trait of being paired or not, and therefore the variance attributable
75 to focal and partner individuals is identical.

76 For a population of size k at a given point in time, it is instructive to represent the paired status as a
77 binary and symmetrical matrix \mathbf{K} of $k \times k$ dimensions, where cells i, j and j, i are coded as "1" if
78 individuals i and j are paired in the same group and coded as "0" if they are not (the diagonal itself is
79 left blank; Fig. 2a). Mean group size can be recovered from this matrix by $1 + \left[\frac{\sum \mathbf{K}}{k} \right]$, allowing
80 comparison between the paired or not phenotype and groups size, a more common summary of
81 population social structure. In Fig. 2a names of the columns indicate the (arbitrarily defined) focal,

82 while names of the rows indicate the (arbitrarily defined) partner. Note how the matrix in Fig. 2a is
 83 symmetrical; there is exactly the same pattern of 0s and 1s on either side of the diagonal. Therefore,
 84 the variances of direct and indirect effects for the trait of paired or not are identical. This can be
 85 extended to cases where we have data on the number of times two individuals are paired. If there
 86 are t observations, we have a symmetrical matrix K_t where valued terms replace the 1s. Mean group
 87 size in this case is recovered through $1 + [\frac{\sum K_t}{kt}]$. For both the binary and the valued cases, because
 88 an individual that is paired as a focal will also be paired as a partner, the correlation between a focal
 89 individual's scores and those of its partners must be exactly 1. The fact that we have exactly identical
 90 direct and indirect variances and a perfect, positive correlation between them has interesting
 91 consequences when we consider the evolutionary potential of the trait of paired or not, and
 92 therefore of group size.



93

94 **Figure 2.** a. When modelling group size using an indirect genetic effects model, individuals
 95 contribute both to their own values for being paired, and to the values of others. Their
 96 contributions as the focal (ID1) and partner (ID2) are identical, and so the variances are the same
 97 and their correlation is exactly 1. B. When modelling the outcome of dyadic contests for
 98 dominance in the same way, we see that individuals contribute to the outcome both as a focal
 99 and as a partner, but in this case their contributions are exactly opposite, and so, while the
 100 variances are equal, the correlation is exactly -1.

101

102 The evolutionary potential of a trait is defined by its additive genetic variance. Typically, we only
 103 consider the *direct* additive genetic variance, i.e., how the genes in a focal organism influence its
 104 own trait. However, when other individuals influence the trait value, then we must also account for

105 *indirect* additive genetic variance i.e., how the genes in others influence the trait value (Scott &
 106 Fuller, 1965; Griffing, 1967; Moore *et al.*, 1997). Indirect genetic effects can contribute substantial
 107 additional genetic variance to morphological, life history, physiological, and behavioural traits (Ellen
 108 *et al.*, 2014), and as I have argued above must contribute exactly as much to the total genetic
 109 variance of the trait of paired or not as direct genetic effects do. In essence, individuals with genetic
 110 variants that increase their sociability will join groups more often, and therefore will increase the
 111 group sizes of other individuals in the population. This greatly increases the evolutionary potential of
 112 the trait, as a small increase (decrease) in sociability across generations will increase (decrease) the
 113 frequency at which individuals join groups, altering the group size of large portions of the population
 114 (Fig. 1b).

115 To quantify the change in evolutionary potential brought about by indirect genetic effects, we can
 116 consider the total heritable variance in a trait with and without indirect genetic effects. The trait we
 117 are considering here is whether an individual is paired or not with each other individual in the
 118 population (giving $k(k - 1)$ measures), rather than mean group size or total number of individuals
 119 in the group. The total heritable variance ($\hat{\sigma}_H^2$) reflects the amount of variation of a trait in a
 120 population which is underpinned by genetic variation, rather than environmental or stochastic
 121 variation. $\hat{\sigma}_H^2$ in the absence and presence of indirect genetic effects is shown in eqs. 1 & 2
 122 respectively (Bijma, 2011). In eq. 1 it is simply equal to the direct additive genetic variance ($\sigma_{A_D}^2$).

123
$$\hat{\sigma}_H^2 = \sigma_{A_D}^2 \quad \text{eq. 1}$$

124 In eq. 2 (including indirect genetic effects) $\hat{\sigma}_H^2$ includes $\sigma_{A_D}^2$, the indirect additive genetic variance
 125 ($\sigma_{A_I}^2$), and twice the covariance between direct and indirect effects ($\sigma_{A_{DS}}$).

126
$$\hat{\sigma}_H^2 = \sigma_{A_D}^2 + 2 \sigma_{A_{DS}} + \sigma_{A_I}^2 \quad \text{eq. 2}$$

127 Note that this is the same calculation as for the more familiar maternal genetic effects model
 128 (Mousseau & Fox, 1998). Note also that in models where more than two individuals interact the
 129 number of interacting individuals (or the group size, n) minus one is included in the calculation
 130 (Bijma & Wade, 2008), but since we are modelling our phenotype as a product of only and always
 131 exactly two individuals interacting, $n-1$ always equals 1 and so does not affect the sum. What is clear
 132 in the case of being paired or not is that, as $\sigma_{A_{DS}}$ is guaranteed to be positive, eq. 2 will always be
 133 larger, and potentially much larger, than eq. 1. Therefore, being paired or not, and so group size, will
 134 have a larger total heritable variance than initially expected based on $\sigma_{A_D}^2$ alone and therefore could
 135 have substantial potential for evolution.

136 Further, when predicting the response to selection, the covariance between direct and indirect
137 genetic effects can radically alter our estimates (Moore *et al.*, 1997). The response to selection
138 (change in mean phenotype across a single generation; $\Delta\bar{P}$) in the absence of indirect genetic effects
139 is given in *eq. 3*; it is simply the product of the selection gradient (β) and the direct additive genetic
140 variance (Muir, 2005; Bijma & Wade, 2008):

$$141 \quad \Delta\bar{P} = \beta\sigma_{A_D}^2 \quad \text{eq. 3}$$

142 Meanwhile, the response to selection in the presence of indirect genetic effects includes the direct
143 indirect genetic covariance:

$$144 \quad \Delta\bar{P} = \beta[\sigma_{A_D}^2 + \sigma_{A_{DS}}]$$

145 Positive values of $\sigma_{A_{DS}}$ greatly enhance the response to selection, speeding evolution, while negative
146 values can reduce, remove, or even reverse the response to selection (Bijma *et al.*, 2007; Bijma &
147 Wade, 2008), potentially causing evolutionary change to move in the opposite direction to selection
148 (Fisher & Pruitt, 2019). In the case of being paired or not, as I have argued above, we must have a
149 strong (the strongest possible) positive covariance between direct and indirect genetic effects.
150 Individuals with genes that predispose them to join others and so make groups larger also cause
151 other individuals to be with others and so be in larger groups (or be in a group at all). Therefore,
152 group size has a larger evolutionary potential than initially expected, as both direct and indirect
153 genetic effects must contribute to its total genetic variation, and evolutionary responses will be
154 especially rapid as these direct and indirect effects are also perfectly positively correlated.

155 Interestingly, this is the exact inverse situation to that of another trait expressed jointly: outcomes in
156 dyadic contests for dominance. In the case of dyadic contests, each contest must have one winner
157 and one loser. These outcomes are therefore perfectly *negatively* correlated, as if the focal
158 individual wins its partner always loses, and vice versa. As Wilson *et al.* (2011) have highlighted, the
159 indirect genetic variance for outcomes in dyadic contests must equal the direct genetic variance (as
160 designation of focal and partner is again arbitrary and so both contribute equally to the outcome).
161 Further, the direct-indirect genetic correlation must be -1, as individuals with genes that predispose
162 them to win contests cause other individuals to lose contests. Another way of thinking about this is
163 to consider the matrix in Fig 2b, which shows the outcomes of dyadic contests in a population. This
164 matrix is asymmetrical; if there is a “1” in a cell in the top right half, there is a “0” in the
165 corresponding cell on the opposite side of the diagonal in the bottom left half, and vice versa. The
166 consequences for the predicted evolution of average dyadic contest outcome are stark: evolutionary
167 change in the trait mean becomes *impossible* as predicted increases through direct effects are
168 always exactly cancelled out by changes in the opposite direct in indirect effects (this appeals to our

169 common sense, half of all in the individuals participating in dyadic contests must lose [trait value of
170 0], while half win [trait value 1], and so the mean trait value can never differ from 0.5, and so should
171 never be able to evolve; Wilson *et al.*, 2011).

172 The cases of paired or not and the outcomes of dyadic contests are exact mirrors of each other; in
173 both cases the direct genetic variance must equal the indirect genetic variance, and for both we
174 expect perfect correlations between direct and indirect genetic effects. However, for paired or not
175 this is a perfect positive correlation (Fig. 2a), while for outcomes of dyadic contests it is perfectly
176 negative (Fig. 2b). Therefore, while for dyadic contest outcome we never expect evolution, for
177 paired or not (and so group size) we expect relatively rapid evolutionary changes (which could be
178 increases or decreases in mean group size).

179 While the result for paired or not might seem esoteric, it is actually quite intuitive. If an individual
180 starts off alone, and then joins a group (of size n), they increase not only their own group size (from
181 1 to $n + 1$) but also the group size of all those already in the group (from n to $n + 1$). If this initially
182 lone individual and the group they join are the only animals in the population, this means the mean
183 group size in the population goes from $(1 + n*n)/(n + 1)$ to $n + 1$, a rapid increase at the population
184 level given only one individual changed its behaviour (if n was 30 this is an increase from 29.06 to
185 31). If we imagine the same process, but instead of plastic change within a generation, evolved
186 change across generations, it is easy to see how rapid changes in group size can occur (see also Fig.
187 1). Even small increases in sociability will give a rapid increase in mean group size as not only are the
188 more sociable individuals in larger groups, but even those with the same underlying tendency to be
189 sociable as the previous generation have a higher mean group size, as they are more often being
190 joined by the more sociable individuals (Fig. 1b). This is true independently of the conceptual
191 framework used to understand it; my use of indirect genetic effects is merely a tool to make
192 accurate predictions about change across generations. It might seem more straightforward to
193 measure sociability directly, and to estimate its heritability and selection on it, but sociability is a
194 latent trait that can only be inferred from observations of individuals interacting with others, and so
195 it always needs untangling from indirect effects. When we observe individuals forming groups, the
196 phenotypes we are observing are inherently a product of at least two genomes, a phenomenon
197 evolutionary the models incorporating indirect genetic effects I highlight here are specifically
198 designed to account for (see also: Queller, 2014).

199

200 Consequences of the higher evolvability of group size

201 The primary consequence of the increased total heritable variance in group size is that we expect to
202 see relatively rapid increases (decreases) across generations in mean group size when selection
203 favours (disfavours) larger groups. Note that the initial genetic variation in being paired or not may
204 still be quite small, especially if environmental variation strongly influences grouping, and so the
205 total heritable variation in group size may not be large in the absolute sense, but it should always be
206 larger than that expected from direct genetic effects alone. Group size is commonly linked to fitness,
207 as it can provide protection for predators and access to mates and other resources, but also be
208 associated with increased food competition and exposure to disease. Variation in group size may
209 therefore often be linked to variation in fitness, and so individual sociability may be under selection
210 in a range of systems (Snyder-Mackler *et al.*, 2020; Gartland *et al.*, 2022; selection on group size is
211 discussed more below). Given we now expect a higher degree of genetic variation in group size,
212 evolved changes should be common, albeit I have no general expectations about a direction (i.e., I
213 do not expect animals to be typically evolving to live in larger or smaller groups). In the presence of
214 consistent directional selection, we expect group sizes to rapidly evolve in line with selection (*eq. 4*).
215 Even if selection was weak and highly variable in direction, we would still expect relatively rapid
216 changes in group size across generations as there is large amounts of genetic variation, but these will
217 be both increases and decreases, and so mean group sizes should be highly variable around a mean
218 value over evolutionary time. However, as noted above, the trait of paired or not could have
219 exceptionally low direct genetic variance if the tendency to be paired is strongly influenced by
220 environmental effects such as current resource availability or predation risk. In this case, even the
221 addition of indirect effects may not raise the total heritable variance to a particularly high level,
222 keeping the rate of evolutionary change low. Directly estimating the direct and indirect genetic
223 variance in the tendency to be in pairs in wild populations is key for understanding the trait's
224 evolutionary potential, and therefore the evolutionary potential of group size.

225 A high variability of group size over evolutionary timescales would mean that other ecological and
226 evolutionary processes that depend on group size should also be highly variable. For instance, the
227 spread of an infection through a population can depend on the typical group size, if transmission is
228 fast within groups and not between them (Nunn *et al.*, 2015). Fewer, larger groups will then allow a
229 faster spread than many small groups. If group sizes are variable across generations, then the speed
230 of disease spread, or indeed any processes that is influenced by group size, will also be highly
231 variable. This high degree of variability means that making predictions for timescales encompassing
232 multiple generations will be difficult.

233 In the presence of direct selection for larger groups, we would expect to see a rapid increase in
234 group size. For short-lived species such as some insects, multiple generations can occur in a year or
235 even season, and so evolved changes in group size might be observably on those timescales. We
236 already are aware that large aggregations of pest insects such as desert locust (*Schistocerca*
237 *gregaria*) can appear seemingly from nowhere, with plastic changes in aggregative behaviour
238 assumed to be behind this (Uvarov, 1921; recently reviewed in: Simpson, 2022). However, evolved
239 changes in sociability and therefore group size might also contribute if selection for larger groups
240 emerged, given that those changes could be very rapid. The importance of evolved changes for
241 outbreaks in desert locust is likely limited due to their generation times (although changes in social
242 behaviour across generations do appear possible; Roessingh *et al.*, 1993) but in short-lived species
243 such as *Drosophila spp.* the importance of evolved changes is more plausible (Behrman *et al.*, 2018).

244 The evolution of group size as discussed here may also apply to the evolution of multicellularity. In a
245 population of unicellular organisms, a mutant cell that adheres to or joins other individuals forms a
246 multicellular aggregation not just for itself, but for the other individual(s) it has joined (Fig. 1b).
247 Change in mean phenotype (the number of cells grouped together) could then change relatively
248 quickly as more “sociable” cells (such as those *Saccharomyces cerevisiae* that express flocculin
249 proteins that bind cells together; Belpaire *et al.*, 2022) would lead to many cells being involved in
250 multicellular aggregations, whether the other cells have an innate tendency to group or not. Further
251 work on facultatively multicellular organisms such as *S. cerevisiae* under artificial selection for “floc”
252 formation (Fisher & Regenberg, 2019) could test whether the evolution of multicellularity is faster
253 than that expected based on direct genetic variance for production of flocculin proteins alone.

254

255 Selection on group size

256 While this article is focused on the total heritable variation in group size, when considering the
257 evolution of this trait we must also consider selection on group size, and how that depends on the
258 type of genetic variation available. For species that form groups, we often expect the relationship
259 between group size and fitness to be humped, such that fitness for individuals within a group
260 increases with increasing group size up to an optimum, and then declines (Sibly, 1983). The shape of
261 this relationship might be due to initial benefits such as detection of predators with increased group
262 sizes, and but increased costs of group size after a point such as risk of transmission of diseases at
263 especially high group sizes. In standard models for phenotypic selection, this could be captured
264 through the use of linear and quadratic selection gradients, where we would expect a positive linear
265 gradient and a negative quadratic one (Phillips & Arnold, 1989). Note that for group size to have

266 fitness consequences the associations need to be more than simply ephemeral co-locations in space
267 and time, which fits within my general definition of groups given above.

268 As group co-membership is a joint phenotype, it is partly under control of both current
269 group members and those other individuals who may be alone or in other groups who wish to join
270 another group. This means there can be a conflict of interest (in terms of fitness outcome) for
271 individuals joining an existing group (Giraldeau & Caraco, 1993; Higashi & Yamamura, 1993). If a
272 group is at the optimum size, additional individuals joining would imply fitness costs for the current
273 group members, as they are now in a group larger than the optimum. In contrast, from the
274 perspective of the joining individual, their fitness is likely to be increased by joining, as they
275 transition from being alone into a group that will give them higher fitness, even if it is above the
276 optimum group size (Sibly, 1983). The resolution of this conflict depends on both who controls group
277 membership (current group members or joining individuals) and the relatedness between
278 interacting individuals (Giraldeau & Caraco, 1993; Higashi & Yamamura, 1993). The fact that joining
279 individuals can reduce the fitness of current group members indicates that a form of negative social
280 selection is acting on group membership, when the trait of one individual reduces the fitness of
281 others (Wolf *et al.*, 1999), which could lead to mean fitness in the population being below the
282 maximum possible (“maladaptation”; McGlothlin & Fisher, 2021). Further, social selection interacts
283 with indirect genetic effects (which we expect to be ubiquitous for group co-membership) to
284 influence the phenotypic response to selection (along with relatedness; Bijma & Wade, 2008). As we
285 now always expect a positive correlation between direct and indirect effects, the additional effect of
286 indirect genetic effects should be to accelerate the response to selection, in whichever direction the
287 combination of relatedness and direct and social selection suggests (Bijma & Wade, 2008; see also:
288 McGlothlin *et al.*, 2014).

289 Finally, a note on group-level (or among-group) selection gradients (Goodnight *et al.*, 1992;
290 Okasha, 2004a). Within a single observation, all individuals within a group have the same group size.
291 Therefore, at this temporal scale there can be no within-group selection gradient for this trait, and
292 all selection must manifest itself at the among-group level (if taking a Price covariance approach,
293 partitioned to the among-group covariance rather than the within-group covariance; Okasha,
294 2004b). Across multiple observations, individuals can be part of many groups, and so fitness due to
295 group size can vary both within and among groups. This would imply that selection can indeed act at
296 multiple levels. Care therefore should be taken when estimating and interpreting selection
297 gradients; understanding what they mean both in isolation and what can be inferred from the
298 combination of within- and among-group selection (Goodnight *et al.*, 1992).

299

300 Evidence for the evolvability of group size

301 Above I have outlined that we expect group size to be highly evolvable, given that there should be
302 genetic variance from indirect and well as direct sources in the tendency to be paired with other
303 individuals, and the covariance between these will always be positive. Is there any empirical
304 evidence that allows us to evaluate whether this is the case or not? The one case study I am aware
305 of indicated that sociability does indeed have genetic variance, and responds to selection, but we
306 cannot evaluate whether it is at the pace expected. Scott *et al.* have determined that sociability is
307 heritable in both male ($h^2 = 0.24$) and female ($h^2 = 0.21$) fruit flies *Drosophila melanogaster* (Scott *et al.*
308 *et al.*, 2018), and that it increases (decrease) in response to artificial selection for higher (lower)
309 sociability (Scott *et al.*, 2022). In their study, sociability was measured by allowing arenas containing
310 16 flies to form groups (Scott *et al.*, 2022), and so was analogous to being paired or not and also
311 mean group size; the formulation of grouping using in the current article. Scott and colleagues have
312 therefore effectively assessed whether mean group size responds to artificial selection. They found it
313 did, with an increase of 40% in females and 54% in males over 25 generations. Scott *et al.* (2022)
314 performed within-group selection, taking the four most (or least for the down-selection lines)
315 sociable flies in each of 12 groups for males and females per generation. This mode of selection does
316 not take advantage of any genetic variation among groups (Muir, 2005; Muir *et al.*, 2013), and so it is
317 not clear whether the observed response is faster or slower than that expected by the narrow sense
318 heritabilities found in their earlier work, and therefore if it is as fast as that predicted by the model
319 of evolution accounting for indirect genetic effects I present here. Nevertheless, this study does at
320 least show that group size responds to artificial selection, and so must possess some genetic
321 variance. Further work would need to select for the most sociable across all individuals within a
322 population, not just within each group, and measure the increase of group size across generations,
323 in order to test the prediction that the evolution of group size should be especially rapid.

324

325 Indirect effects on sociability itself

326 A final consideration is that an individual's sociability itself may be influenced by indirect genetic
327 effects. An individual's decision to join or leave groups may be influenced by the traits of the other
328 individuals already in those groups. If those traits are partly genetically determined, then there will
329 be indirect genetic effects on sociability (Fisher, 2023). Therefore, an individual's *willingness* to join a
330 group will be influenced by the genes of others (Fisher, 2023), but also its *realised* group size will be
331 influenced by the genes of others (this article). The overall heritability of group size may therefore

332 be influenced by direct genetic effects for sociability (individuals' have an underlying preference to
333 be with others that is partly genetically determined), indirect genetic effects for sociability (an
334 individual's preference to be with others depends on their traits and therefore also their genes), and
335 indirect genetic effects for group size (the sociability of others, and therefore their genes, influences
336 the realised group size of an individual), plus the covariances among these components. Predicting
337 the outcome of this is complicated, but parallels may be drawn with models for the heritability of
338 social phenotypes in social networks using latent variables representing the tendency to be social
339 and the contribution to social associations (Radersma, 2020).

340

341 Conclusions

342 In summary, I have suggested that the evolution of group size can be understood using an indirect
343 genetic effects model. This model predicts that group size should have a relatively large genetic
344 variance and so should respond surprisingly rapidly to selection. This high evolvability will increase
345 the variability in demographic, ecological, and evolutionary processes that depend on group size.
346 Testing whether this prediction is true or not is the next step.

347

348 Acknowledgements

349 I am grateful to Alastair Wilson and Ben Jarrett for comments and suggestions on an earlier draft,
350 and to the two anonymous reviewers whose critique improved the initial submission. I have no
351 conflicts of interest.

352

353 References

- 354 Behrman, E.L., Howick, V.M., Kapun, M., Staubach, F., Bergland, A.O., Petrov, D.A., *et al.* 2018. Rapid
355 seasonal evolution in innate immunity of wild *Drosophila melanogaster*. *Proceedings of the*
356 *Royal Society B: Biological Sciences* **285**: 20172599. Royal Society.
- 357 Belpaire, T.E.R., Pešek, J., Lories, B., Verstrepen, K.J., Steenackers, H.P., Ramon, H., *et al.* 2022.
358 Permissive aggregative group formation favors coexistence between cooperators and
359 defectors in yeast. *ISME J* **16**: 2305–2312. Nature Publishing Group.
- 360 Bijma, P. 2011. A general definition of the heritable variation that determines the potential of a
361 population to evolve. *Genetics* **189**: 1347–1359.
- 362 Bijma, P., Muir, W.M. & Van Arendonk, J.A.M. 2007. Multilevel selection 1: Quantitative genetics of
363 inheritance and response to selection. *Genetics* **175**: 277–88.
- 364 Bijma, P. & Wade, M.J. 2008. The joint effects of kin, multilevel selection and indirect genetic effects
365 on response to genetic selection. *Journal of Evolutionary Biology* **21**: 1175–88.

- 366 Ellen, E.D., Rodenburg, T.B., Albers, G.A.A., Bolhuis, J.E., Camerlink, I., Duijvesteijn, N., *et al.* 2014.
 367 The prospects of selection for social genetic effects to improve welfare and productivity in
 368 livestock. *Frontiers in genetics* **5**: 377. Frontiers Research Foundation.
- 369 Fisher, D.N. 2023. Direct and indirect phenotypic effects on sociability indicate potential to evolve. *J*
 370 *of Evolutionary Biology* **36**: 209–220.
- 371 Fisher, D.N. & Pruitt, J.N. 2019. Opposite responses to selection and where to find them. *Journal of*
 372 *Evolutionary Biology* **32**: 505–518. John Wiley & Sons, Ltd (10.1111).
- 373 Fisher, R.M. & Regenberg, B. 2019. Multicellular group formation in *Saccharomyces cerevisiae*.
 374 *Proceedings of the Royal Society B: Biological Sciences* **286**: 20191098. Royal Society.
- 375 Gartland, L.A., Firth, J.A., Laskowski, K.L., Jeanson, R. & Ioannou, C.C. 2022. Sociability as a
 376 personality trait in animals: methods, causes and consequences. *Biological Reviews* **97**: 802–
 377 816. John Wiley & Sons, Ltd.
- 378 Giraldeau, L.-A. & Caraco, T. 1993. Genetic relatedness and group size in an aggregation economy.
 379 *Evol Ecol* **7**: 429–438.
- 380 Goodnight, C.J., Schwartz, J.M. & Stevens, L. 1992. Contextual analysis of models of group selection,
 381 soft selection, hard selection, and the evolution of altruism. *The American Naturalist* **140**:
 382 743–761.
- 383 Griffing, B. 1967. Selection in reference to biological groups. I. Individual and group selection applied
 384 to populations of unordered groups. *Australian journal of biological sciences* **20**: 127–39.
- 385 Higashi, M. & Yamamura, N. 1993. What Determines Animal Group Size? Insider-Outsider Conflict
 386 and Its Resolution. *The American Naturalist* **142**: 553–563.
- 387 Kokko, H. & Rankin, D.J. 2006. Lonely hearts or sex in the city? Density-dependent effects in mating
 388 systems. *Philosophical Transactions of the Royal Society B: Biological Sciences* **361**: 319–334.
- 389 McDonald, G.C. 2023. The impact of small groups on pre- and postcopulatory sexual selection in
 390 polyandrous populations. *Ecology and Evolution* **13**: e10057.
- 391 McGlothlin, J.W. & Fisher, D.N. 2021. Social Selection and the Evolution of Maladaptation. *Journal of*
 392 *Heredity*, doi: 10.1093/JHERED/ESAB061. Oxford University Press (OUP).
- 393 McGlothlin, J.W., Wolf, J.B., Brodie, E.D. & Moore, A.J. 2014. Quantitative genetic versions of
 394 Hamilton's rule with empirical applications. *Philosophical transactions of the Royal Society of*
 395 *London. Series B, Biological sciences* **369**: 20130358.
- 396 Moore, A.J., Brodie, E.D.I. & Wolf, J.B. 1997. Interacting phenotypes and the evolutionary process: I.
 397 Direct and indirect genetic effects of social interactions. *Evolution* **51**: 1352–1362.
- 398 Mousseau, T.A. & Fox, C.W. 1998. The adaptive significance of maternal effects. *Trends in Ecology &*
 399 *Evolution* **13**: 403–407.
- 400 Muir, W.M. 2005. Incorporation of competitive effects in forest tree or animal breeding programs.
 401 *Genetics* **170**: 1247–1259.

- 402 Muir, W.M., Bijma, P. & Schinckel, A. 2013. Multilevel selection with kin and non-kin groups,
403 experimental results with japanese quail (*Coturnix japonica*). *Evolution* **67**: 1598–1606.
- 404 Nunn, C.L., Jordán, F., McCabe, C.M., Verdolin, J.L. & Fewell, J.H. 2015. Infectious disease and group
405 size: more than just a numbers game. *Philosophical transactions of the Royal Society of*
406 *London. Series B, Biological sciences* **370**: 20140111-.
- 407 Okasha, S. 2004a. Multilevel selection and the partitioning of covariance: A comparison of three
408 approaches. *Evolution* **58**: 486–494. Blackwell Publishing Ltd.
- 409 Okasha, S. 2004b. Multi-Level Selection, covariance and contextual analysis. *The British Journal for*
410 *the Philosophy of Science* **55**: 481–504. Oxford University Press.
- 411 Phillips, P.C. & Arnold, S.J. 1989. Visualizing multivariate selection. *Evolution* **43**: 1209–1222. Wiley.
- 412 Queller, D.C. 2014. Joint phenotypes, evolutionary conflict and the fundamental theorem of natural
413 selection. *Philosophical Transactions of the Royal Society B: Biological Sciences* **369**:
414 20130423–20130423.
- 415 Radersma, R. 2020. Estimating heritability of social phenotypes from social networks. *Methods in*
416 *Ecology and Evolution* 2041–210X.13499. John Wiley & Sons, Ltd.
- 417 Roessingh, P., Simpson, S.J. & James, S. 1993. Analysis of phase-related changes in behaviour of
418 desert locust nymphs. *Proceedings of the Royal Society B: Biological Sciences* **252**: 43–49.
- 419 Scott, A.M., Dworkin, I. & Dukas, R. 2022. Evolution of sociability by artificial selection. *Evolution* **76**:
420 541–553. John Wiley & Sons, Ltd.
- 421 Scott, A.M., Dworkin, I. & Dukas, R. 2018. Sociability in Fruit Flies: Genetic Variation, Heritability and
422 Plasticity. *Behavior Genetics* **48**: 247–258.
- 423 Scott, J.P. & Fuller, J.L. 1965. *Genetics and the social behavior of the dog*. University of Chicago Press,
424 Chicago.
- 425 Sibly, R.M. 1983. Optimal group size is unstable. *Animal Behaviour* **31**: 947–948. Elsevier Science,
426 Netherlands.
- 427 Simpson, S.J. 2022. A journey towards an integrated understanding of behavioural phase change in
428 locusts. *Journal of Insect Physiology* **138**.
- 429 Snyder-Mackler, N., Burger, J.R., Gaydosh, L., Belsky, D.W., Noppert, G.A., Campos, F.A., *et al.* 2020.
430 Social determinants of health and survival in humans and other animals. *Science* **368**.
431 American Association for the Advancement of Science.
- 432 Uvarov, B.P. 1921. A revision of the genus *Locusta*, L. (= *Pachytylus*, Fieb.), with a new theory as to
433 the periodicity and migrations of locusts. *Bulletin of Entomological Research* **12**: 135–163.
- 434 Wilson, Alastair.J., Morrissey, M.B., Adams, M.J., Walling, C.A., Guinness, F.E., Pemberton, J.M., *et al.*
435 2011. Indirect genetics effects and evolutionary constraint: An analysis of social dominance
436 in red deer, *Cervus elaphus*. *Journal of Evolutionary Biology* **24**: 772–783. Blackwell
437 Publishing Ltd.

438 Wolf, J.B., Brodie III, E.D. & Moore, A.J. 1999. Interacting Phenotypes and the Evolutionary Process.
439 II. Selection Resulting from Social Interactions. *The American Naturalist* **153**: 254–266.
440