- 1 Descriptive inference using large, unrepresentative nonprobability samples: An
- 2 introduction for ecologists
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## 8 Abstract

- 9 Biodiversity monitoring usually involves drawing inferences about some variable of interest
- 10 across a defined landscape from observations made at a sample of locations within that
- 11 landscape. If the variable of interest differs between sampled and non-sampled locations, and
- 12 no mitigating action is taken, then the sample is unrepresentative and inferences drawn from
- 13 it will be biased. It is possible to adjust unrepresentative samples so that they more closely
- 14 resemble the wider landscape in terms of "auxiliary variables". A good auxiliary variable is a
- 15 common cause of sample inclusion and the variable of interest, and if it explains an
- appreciable portion of the variance in both, then inferences drawn from the adjusted sample
- 17 will be closer to the truth. We applied six types of survey sample adjustment—subsampling,
- 18 quasi-randomisation, poststratification, superpopulation modelling, a "doubly robust"
- 19 procedure, and multilevel regression and poststratification—to a simple two-part biodiversity 20 monitoring problem. The first part was to estimate mean occupancy of the plant *Calluna*
- monitoring problem. The first part was to estimate mean occupancy of the plant *Calluna vulgaris* in Great Britain in two time-periods (1987-1999 and 2010-2019); the second was to
- estimate the difference between the two (i.e. the trend). We estimated the means and trend
- using large, but (originally) unrepresentative, samples from a citizen science dataset.
- 24 Compared to the unadjusted estimates, the means and trends estimated using most adjustment
- 25 methods were more accurate, although standard uncertainty intervals generally did not cover
- the true values. Completely unbiased inference is not possible from an unrepresentative
- 27 sample without knowing and having data on all relevant auxiliary variables. Adjustments can
- reduce the bias if auxiliary variables are available and selected carefully, but the potential for
- 29 residual bias should be acknowledged and reported.

# 30 Introduction

- 31 As the data revolution gathers pace, it is not surprising to see "big data" being used to
- 32 monitor biodiversity. Examples include observations submitted to mobile phone apps by
- amateur naturalists (Johnston et al., 2022) and digitised specimens from museums and
- 34 herbaria (Nelson & Ellis, 2019). Such data become bigger still when combined in data
- 35 aggregators such as the Global Biodiversity Information Facility (GBIF;
- 36 https://www.gbif.org/) or metadatabases such as PREDICTS (Hudson et al., 2014).
- 37 Unfortunately, quantity of data does not necessarily imply quality of insight.
- 38 Monitoring biodiversity is typically a matter of descriptive statistical inference. It is
- inferential in that the goal is to infer something about a target population from a sample of
- 40 that population (Boyd, Powney, et al., 2023). The population might comprise, say, all areal
- 41 units across some landscape ("sites"), in which case the sample would be a subset of those
- 42 sites. The inference is descriptive in that the aim is to describe (rather than explain) a variable
- 43 of interest in the population. A common example is the proportion of sites occupied by some
- 44 species (Bowler et al., 2021; Outhwaite et al., 2020; Powney et al., 2019; Stroh et al., 2023;
- 45 van Strien & van Grunsven, 2023), but there are many others.

- 46 Of more importance than the size of a sample for descriptive inference is whether it is
- 47 representative of the population about which inferences are to be drawn (Meng, 2018). In a
- 48 representative sample, the distribution of the variable of interest is similar to its distribution
- 49 in the population (Bethlehem et al., 2008). An equivalent definition is that there is little to no
- 50 correlation between inclusion in the sample and the variable of interest—the "data defect
- correlation", or ddc (Meng, 2018). Intuitively, statistics derived from a representative sample,
- 52 such as means and proportions, will be similar to their population equivalents.
- 53 Unfortunately, ddc's are likely to be appreciable in big biodiversity datasets. For one,
- 54 naturalists preferentially visit and collect data at sites where they are likely to see species that
- interest them (Bowler et al., 2022; Forister et al., 2023). Where those species' abundances or
- 56 distributions are the variables of analytic interest, preferential sampling naturally results in a
- 57 positive ddc (McClure & Rolek, 2023). On the other hand, naturalists might be constrained to
- 58 visiting and collecting data in, say, built up areas, which are easier to access than remote
- 59 locations (Geldmann et al., 2016; Hughes et al., 2020; Mandeville et al., 2022). Built-up areas
- 60 generally have low quality habitat, meaning that species are less likely to occupy them in
- 61 large numbers and that the ddc might be negative.
- 62 Inferences from unrepresentative samples, with appreciable ddc's, are likely to be misleading.
- 63 Imagine a researcher who wants to estimate the average abundance of some species across a
- 64 landscape. An obvious (but naïve) approach would be to calculate its mean abundance across
- 65 sampled sites and assume that this is similar to its average abundance across the wider
- 66 landscape. However, if the locations at which the species is most abundant were
- 67 preferentially sampled, then the sample-based estimate of its mean abundance will be
- upwardly biased. To use the analogy of Forister et al. (2023), sampled locations would be life
- 69 rafts; non-sampled locations would be the sinking ship.
- 70 It is simple to counteract the biasing effect of the ddc if the probability that each site was
- included in the sample is known; that is, if a *probability sample* is available. In this case,
- more weight can be placed on the data from sites that were less likely to be included. The
- effect of this type of weighting is easiest to explain heuristically: the sample is augmented
- with "copies" of the data from sites that were less likely to be sampled, effectively bringing
- sample inclusion probabilities across sites to parity. Two variables cannot be correlated if one
- 76 of them is constant, which means there can be no correlation between the weighted sample
- 77 inclusion probabilities and the variable of interest across sites. It follows that the ddc, which
- is the correlation between actual (weighted) sample inclusion and the variable of interest, is
- zero in expectation (Meng, 2022), and the sample can be considered representative (Lohr,
  2022). Weighting of this type is known as "design-based" inference, because the inclusion
- probabilities are a feature of the sampling design.
- 82 Design-based inference is not applicable for the types of big biodiversity datasets we consider
- 83 here, because they were not collected according to a probabilistic sampling design. We do not
- 84 know the probabilities that sites were visited by the collectors of specimens now held in
- 85 museums and on GBIF. Nor do we know the probabilities that citizen scientists visited and
- 86 collected data at each site across most landscapes. Matters are simpler when using data from 87 structured monitoring schemes, which often sim for a probability security (a particular)
- 87 structured monitoring schemes, which often aim for a probability sample (e.g PoMS). 88 However, incomplete untake of sites that were selected for inclusion (Decent et al. 2015)
- However, incomplete uptake of sites that were selected for inclusion (Pescott et al., 2015,
  2019) means that, in practice, these samples too are non-probabilistic. [Incomplete uptake in
- biodiversity monitoring is analogous to the issue of non-response in survey sampling (e.g.
- 91 Bethlehem et al., 2008).] Where sample inclusion probabilities are not known, an alternative
- 92 to design-based inference is needed.

- 93 Most approaches to inference from nonprobability samples involve *estimating* the inclusion
- probabilities. A relatively simple example is poststratification, where the observations (for
- each site) are split into strata based on covariates, and sites in strata that are underrepresented
- 96 in the population (based on the population totals of the covariates) are given more weight  $(1/1)^{1/2}$
- 97 (Valliant et al., 2018). Using covariates to estimate sample inclusion probabilities is
- 98 equivalent to adjusting the samples in such a way that the distributions of those covariates in 99 the sample more closely resemble their distributions in the population (i.e. across all sites in
- 100 the wider landscape). If the covariates affect *both* the variable of interest and sample
- 101 inclusion, then inferences drawn from the adjusted sample will be closer to the truth than
- 102 those from the original (naïve) sample. In the context of inference from nonprobability
- 103 samples, covariates affecting both sample inclusion and the variable of interest, which are not
- 104 of direct analytic interest themselves, are known as "auxiliary variables" (Thoemmes &
- 105 Mohan, 2015; Thoemmes & Rose, 2014).
- 106 Before going further, it is important to note that most approaches to inference from
- 107 nonprobability samples rest on the bold assumption that the variable of interest is
- 108 independent of sample inclusion after accounting for the auxiliary variables (Bailey, 2022);
- 109 that is, non-sampled sites are "Missing At Random" (MAR; Rubin, 1976). If the MAR
- assumption holds, then unbiased inference is possible. In reality, the MAR assumption is
- 111 likely to be violated, because data are not available on all relevant auxiliary variables, so the
- best we can hope for is a reduction in bias relative to naïve inferences drawn from the
- 113 unadjusted sample.
- 114 Use of sample adjustments in biodiversity monitoring is variable. It is common for
- 115 monitoring schemes to weight samples in such a way that the relative frequencies of habitats
- or geographic areas in the sample are similar to those in the population (Gregory et al., 2005;
- 117 Van Swaay et al., 2002, 2008; Weiser et al., 2020). But it is also common to see samples
- treated as though they are representative despite clear evidence to the contrary. For example,
- 119 Vellend et al. (2013) and Dornelas et al. (2014) purported to document globally
- representative time trends in species richness, but Gonzalez et al. (2016) showed that their
- samples were highly unrepresentative with respect drivers of biodiversity change and species richness itself (See Boyd, Boymey, et al. (2022) for a review of this debate and others like it.)
- richness itself. (See Boyd, Powney, et al. (2023) for a review of this debate and others like it.)
  We suspect that many of those who do not deal with issues of sample representativeness are
- not familiar with the gravity of the problem or the relevant theory and adjustment methods.
- 125 In this paper, we introduce six approaches to descriptive inference using unrepresentative
- nonprobability samples and demonstrate how they relate to each other (conceptually and
- 127 mathematically). We apply each approach to a simple two-part biodiversity monitoring
- problem. The first part is to estimate mean occupancy of the plant *C. vulgaris* across 1 km
- 129 grid squares in Britain in two time-periods; the second is to estimate the difference between
- 130 the two (i.e. the time trend). *Calluna vulgaris* is an attractive case study because we have
- 131 good estimates of its true geographic distribution in both periods from satellite (amongst
- 132 other sources). The approaches to inference that we demonstrate are subsampling, quasi-
- randomisation (Elliott and Valliant, 2017), poststratification (Little, 1993), superpopulation
   modelling (Valliant, 2009), a "doubly robust" estimator (Chen et al., 2020), and Multilevel
- modelling (Valliant, 2009), a "doubly robust" estimator (Chen et al., 2020), and Multilevel
   Regression and Poststratification (MRP; Gelman, 2007; Gelman and Little, 1997). Each can
- be (MRP more loosely than the rest) interpreted as an attempt to weight the sample in such a
- 137 way that it more closely resembles the population, in the hope that this results in more
- accurate descriptive inferences. We demonstrate the effects of each approach on the
- distributions of auxiliary variables in the sample, as well as on the resulting estimates of
- 140 mean occupancy in each period and the time trend between the two. Applying the adjustment

- 141 methods to a real-world example reveals challenges that ecologists are likely to face, and we
- 142 discuss these in detail.

## 143 Methods

### 144 **True distribution of** *Calluna vulgaris*

145 We approximated the true distribution of the dwarf shrub vascular plant *Calluna vulgaris* 

- 146 (Heather) in two time periods: 1987–1999 and 2010–2019. For the first period, we used the
- 147 1990 UKCEH land cover map (Rowland et al., 2020); for the second, we used the 2018
- version (Morton et al., 2022). The land cover maps are derived from satellite, which means
- that they provide information for every 1 km grid square. From these maps, we identified 1
- km grid squares (British National Grid, EPSG:27700) with >0% heather or heather grassland
- 151 cover. To these, we added 1 km squares in which *C. vulgaris* was recorded in each time
- 152 period by the Botanical Society of Britain and Ireland (BSBI). The time periods considered 153 cover the main periods of recording for two national distribution atlases, which involved a
- 153 cover the main periods of recording for two national distribution atlases, which involved 154 concerted effort by volunteers (citizen scientists) to document vascular plants across the
- 155 United Kingdom (Preston, C.D., Pearman, D.A. & Dines, 2002; Stroh et al., 2023).
- 156 Acknowledging that some 1 km squares may have been erroneously classed as having some
- 157 heather or heather grassland coverage by the land cover maps, we removed any 1 km squares
- that fell within 10 km grid squares in which *C. vulgaris* had not been recorded by the BSBI in
- the period 1950–2019. Given that this period includes recording for three national
- 160 distribution atlases (the two cited above plus Perring & Walters, 1962), we assume that the
- 161 union of all 10 km occurrences within this period encompasses all known populations
- 162 irrespective of finer scale changes. Figure 1 maps the resulting estimates of the true 1 km
- 163 distributions of *C. vulgaris* in both time-periods.

164



166 Figure 1. Left column: the distribution of *Calluna vulgaris* in both time-periods. Green

167 squares are occupied and grey squares are not.  $\bar{y}_N$  is mean occupancy or, equivalently, the

168 proportion of squares occupied. The ddc's are the correlations between sample inclusion (1 if

169 the square is in the sample and 0 otherwise) and occupancy. Right column: the nonprobability

170 1 km samples for each time-period. Purple squares were sampled and grey squares were not.

n is the number of squares sampled. We assume that *C. vulgaris* was recorded in all sampled

172 grid squares that it occupied in the relevant time-period. The true trend is the difference

between population means, and the sample trend is the difference between sample means (i.e.

174 mean occupancy across purple squares).

## 175 Sample data on *Calluna vulgaris* occupancy

176 The 1 km samples for both time periods ("Sampled squares in Fig. 1) encompass any vascular

- 177 plant data for which the date of collection is known (i.e. the record is resolved to the day),
- 178 either at the 1 km scale or finer, collected by the BSBI for the national distribution atlases of
- 179 Preston et al. (2002) and Stroh et al. (2023). Having been collected by volunteers, the data
- 180 come under the banner of citizen science.

### 181 Auxiliary data

- 182 We used two auxiliary variables for which data are available for all 1 km grid squares in
- 183 Great Britain: the proportion of each 1 km grid square that falls within some form of
- 184 protected area (including everything from SSSI's to local nature reserves; UNEP-WCMC &
- 185 IUCN, 2020) and the average elevation of each 1 km square (Intermap, 2009). New protected
- areas are designated periodically, so we used the set that were designated prior to 1987 for
- 187 the first time-period and prior to 2010 for the second (i.e. the beginning of each period). We

- suspect that 1 km squares with more protected area coverage are more likely to be visited by
- 189 naturalists (Girardello et al., 2019) and, because protected areas tend to have higher quality
- habitat, are also more likely to be occupied by *C. vulgaris*. Likewise, elevation should affect
- both sample inclusion and *C. vulgaris* occupancy. Sites at higher elevations are harder to
- access on account of their relatively harsh terrain and remoteness, and elevation is a known 102
- 193 predictor of *C. vulgaris* occupancy (Stroh et al., 2023).
- 194 One of the adjustment methods that we describe below, quasi-randomisation, requires
- additional covariates (we use the term "covariate" to distinguish these from the auxiliary
- 196 variables as defined earlier). The method involves the estimation of sample inclusion
- 197 probabilities for every 1 km grid square in Britain. This is a matter of prediction rather than
- inference, because we know whether each 1 km square was sampled (i.e. there is no missing
- data), so it was sensible to use a wider range of covariates. See Table 1 in Boyd, Stewart, et
- al. (2023) for a list of the additional covariates used in this model.

# 201 Estimating the per-period population mean

- 202 The first step in our biodiversity monitoring problem is to estimate mean occupancy of *C*.
- 203 vulgaris in each time-period. Although not usually written this way, it is helpful for what
- 204 comes later to re-express the population mean as a weighted sum

$$\overline{y}_N = \frac{1}{N} \sum_{i=1}^N y_i = \sum_{i=1}^N \frac{y_i}{N} = \sum_{i=1}^N \frac{y_i w_i}{\sum_N w_i},$$
 equation 1

where y is occupancy (1 = occupied and 0 = unoccupied), N is the population size, i indexes

- 1 km grid squares and  $w_i = 1/N$  (N is the same in both time-periods). The denominator in
- the rightmost expression might seem unnecessary, because it equals one. We have retained it
- to illustrate the similarity between this expression and the sample-based estimators below,
- which have a similar form but whose sampling weights w do not necessarily sum to one. (We
- 211 use the term "estimator" to describe a rule for estimating some quantity from a sample; here,
- that quantity is the population mean.) For notational simplicity, we do not index the time-
- 213 period, and the reader should remember that  $\bar{y}_N$  is time-period specific. In practice, y is not
- known for all *i* in the population, so sample-based estimators of  $\bar{y}_N$  are needed.

### 215 The design-based estimator

- 216 The design-based estimator of the population mean, which is applicable only where a
- 217 probability sample of some sort is available (Lohr, 2022), has a similar form to eq. 1

$$\overline{y}_{db} = \sum_{i=1}^{n} \frac{y_i w_i}{\sum_n w_i}.$$

equation 2

- 218 The differences are that the sums are over the sample size n rather than N and that the
- weights  $w_i$  are not necessarily constant. Rather, the weight for unit *i*,  $w_i$ , is equal to the reciprocal of the probability that it was included in the sample =  $1/p_i$ .
- 221 Sample inclusion probabilities are, by definition, not known for nonprobability samples, so
- alternative estimators are required. We present six such estimators below, three of which-
- quasi-randomisation, poststratification and superpopulation modelling-are explicit attempts
- to come up with a set of weights  $w_i$  that produce a reasonable estimate of  $\overline{y}_N$  under eq. 2. The
- other three—a "doubly robust" estimator, subsampling and MRP—are not, but they are
- 226 conceptually similar.

## 227 Estimators for nonprobability samples

228 The following estimators are used in survey sampling to estimate population means from

nonprobability samples. More detail on each can be found in Valliant et al. (2018), Lumley

230 (2010) and Lohr (2022). See supplementary material 1 for an R Markdown document

containing the code to implement each of the adjustment methods.

## 232 Naïve sample mean

- 233 Where sample inclusion probabilities are unavailable, a simple option is to assume that  $w_i =$
- 1/n for all *i*. In this case, eq. 2 gives the (naïve) sample mean. As the weights are constant,
- the sample mean does not adjust for differences in *y* between the sampled and non-sampled
- 236 population units. It is nevertheless widely used in biodiversity monitoring.

## 237 Quasi-randomisation

- 238 An alternative approach is to imagine that the nonprobability sample was selected
- 239 probabilistically and to estimate the implied inclusion probabilities. Any binary model and
- 240 covariates can be used. Once inclusion probabilities  $p_i$  have been estimated, the weights  $w_i =$
- 241  $1/p_i$  (as in the design-based estimator). In our example, we used random forests and several
- 242 covariates (including the auxiliaries) to estimate pseudo-inclusion probabilities. More
- 243 complex appraoches are possible and have been used to map species distributions (Johnston
- et al., 2020).

## 245 Poststratification

- Another approach to estimating sampling weights is poststratification. Poststratification
- requires categorical auxiliary data, so continuous variables must be discretized prior to
- analysis (Valliant, 2020). The auxiliary variables are crossed (think contingency tables) to
- create poststrata. Each poststratum *j* has a sample size  $n_j$  and population size  $N_j$ . The
- sampling weight  $w_i$  for population unit *i* in poststratum *j* is given by  $N_j/n_j$ .
- In our example, we split elevation into ten categories using its deciles (i.e. cut points at the
- 10th and 20th percentiles, etc.). This did not make sense for the variables denoting the
- 253 proportion of each grid square that falls within a protected area, because most squares took
- the value one or zero. We split this variables into two categories, 0 and >0, i.e. whether or not
- there is some protected land in the grid square. Discretization gave  $10 \times 2 = 20$  poststrata.
- 256 It is sensible to discretize the auxiliary variables in such a way that the variable of interest
- 257 varies among categories. Otherwise, the adjustment from poststratifying will be minor (or
- 258 unnecessary!). Fig. 2 shows that mean occupancy of *C. vulgaris* in the samples differs
- appreciably among levels of the auxiliary variables.



Figure 2. Mean occupancy of *Calluna vulgaris* for each level of the auxiliary variables in

each time-period. The auxiliary variables were originally on a continuous scale, but we

discretized them to enable poststratification. See the main text for details.

### 264 Superpopulation modelling

Superpopulation modelling is conceptually different to the adjustment methods described above. The premise is that there exists some model that describes the variable of interest in the population. If this model can be recovered from the sampled outcome variable y and the auxiliary data, it can be used to predict the variable of interest in non-sampled units. Given a prediction for each non-sampled i, it is then simple to estimate the population mean.

270 A general (i.e. multiple) linear regression model of *y* has the form

$$E_M(y_i) = \mathbf{x}_i^T \boldsymbol{\beta},$$
 equation 3

271 where the subscript *M* indicates that the expectation (mean) is with respect to the model,  $x_i$  is

272 the vector of auxiliary variables for unit *i*, the superscript *T* indicates that the vector  $\mathbf{x}_i$  has

been transposed (to a row vector) and  $\beta$  is a column vector of parameters. A prediction of y

274 for unit *i* is

$$\hat{y}_i = x_i^T \hat{\beta}.$$
 equation 4

275 The accent on  $\beta$  indicates that it is an estimate (the least squares estimate in this case). If  $\bar{s}$  is

the set of non-sampled population units, the superpopulation model prediction of thepopulation mean is

$$\bar{y}_{sp} = \frac{\sum_{i \in s} y + \sum_{i \in \bar{s}} \hat{y}}{N}.$$
 equation 5

That is, it is the sum of the known outcome values in the sample and those predicted by the model for the remainder of the population divided by the population total.

A feature of  $\bar{y}_{sp}$  is that it can be expressed in the same form as the design-based estimator in

- eq. 2, with the weights  $w_i$  being a function of the auxiliary variables in sampled and non-
- sampled population units (Elliott & Valliant, 2017). (Code to verify this numerically is
- available at https://github.com/robboyd/selectionBiasEffects/tree/master/R.) Like the other

- 284 adjustment models, then, the superpopulation estimator is an approach to estimating the
- sampling weights  $w_i$ . 285
- Linear regression might seem like an unusual choice of model for a binary outcome 286
- (occupancy), but we felt that it was the best option here. One reason is that the implied model 287
- 288 is actually linear for an estimator with the form of eq. 2 (Valliant, 2020). Most important,
- however, is that the use of a linear model enables the estimation of sampling weights 289
- (Valliant et al., 2018; supplementary material 1; 290
- 291 https://github.com/robboyd/biasAdjustments). This is helpful, because those weights can be
- used to show the effects of superpopulation modelling on the distributions of the auxiliary 292
- variables in the sample (see "Evaluating the effects of the adjustments" below). Alternative 293
- 294 models can be used where weights are not required (e.g. Wu and Sitter, 2001). In our 295 example superpopulation model, we used the auxiliary variables as predictors.

#### Doubly robust estimator 296

- The doubly robust estimator combines the superpopulation model and the sample inclusion 297
- 298 model from the quasi-randomisation procedure in such a way that if either is correct, and the
- 299 sample size is large, then the estimate of the population mean unbiased (Valliant, 2020). It
- has the general form (Wu, 2022) 300

$$\bar{y}_{dr} = \frac{1}{N} \sum_{i \in S} \frac{r_i}{p_i} + \frac{1}{N} \sum_{i=1}^N \hat{y}_i, \qquad \text{equation } 6$$

- where  $r_i = y_i \hat{y}_i$  (i.e. the residuals of superpopulation model). The second term on the right 301
- is the superpopulation model prediction of  $\overline{Y}_N$ . If the superpopulation model is correctly specified, then it is an unbiased estimate of  $\overline{Y}_N$ . However, if the superpopulation model is 302
- 303
- misspecified, then the second term needs to be corrected, which is where the first term comes 304 in. If the quasi-randomisation sample inclusion model is correctly specified, the first term 305
- 306 corrects the second by adding the residuals of the superpopulation model divided by the
- (correctly) estimated pseudo inclusion probabilities. This is sufficient to produce an unbiased 307
- estimate of  $\overline{Y}_N$  even where the superpopulation model is wrong. Where the superpopulation 308
- model is correct, the first term is 0, because  $r_i = 0$ . Where neither model is correct,  $\overline{y}_{dr}$  is a 309
- biased estimator of  $\overline{Y}_N$ . See Chen et al. (2020), who combined probability and nonprobability 310
- samples, for a similar approach. 311

#### Subsampling 312

- Perhaps more familiar to ecologists than the above approaches is subsampling (Beck et al., 313
- 314 2014; Steen et al., 2020). The idea is to create a representative "miniature" of the population
- out of the sample (Meng, 2022) and to calculate the quantity of interest (mean occupancy) 315
- 316 from this subsample. Subsampling trades sample size for representativeness.
- Our approach was to draw stratified random samples of size N/10 = 22,958 with 317
- 318 replacement from the original samples. We used the same strata as described above (under
- Poststratification). The decision to set n = N/10 was somewhat arbitrary, but changing the 319
- subsample size makes little difference to the point estimates of the population means 320
- 321 (although they become more precise with increasing subsample size; supplementary material
- 1). The subsample mean is the estimator of the population mean. 322

#### Multilevel regression and poststratification (MRP) 323

- 324 MRP is an extension of poststratification and a variation of superpopulation modelling
- (Gelman, 2007; Gelman & Little, 1997; Valliant et al., 2018). A hierarchical model is used to 325
- estimate mean occupancy in each poststratum. The advantage of using a hierarchical model is 326
- 327 that cells with few or no data borrow information from cells with more data (i.e. partial

- 328 pooling or shrinkage is exploited). The population mean is the weighted mean of the stratum 329 means, where the weights are equal to the proportion of the population in each stratum.
- 330 Our hierarchical model is a binomial GLM with a logit link function, a fixed intercept and
- random intercepts for the auxiliary variables and their interaction (see <u>https://mc-</u>
- 332 <u>stan.org/rstanarm/articles/mrp.html</u> for a similar formulation). We fitted the model in a
- Bayesian framework using 5 Markov Chain Monte Carlo (MCMC) chains, each with 1000
- iterations. This was sufficient to achieve convergence on all parameters in both time-periods.

## 335 Confidence intervals

- 336 We present 95% confidence/credible intervals for all estimates of mean occupancy (credible
- 337 intervals for MRP, which we implemented in a Bayesian framework). For most methods—
- 338 superpopulation modelling, quasi-randomisation, subsampling and the doubly robust
- 339 estimator—we constructed bootstrap confidence intervals. Resampling the original data with
- replacement, we created 1000 bootstrap samples, from which we obtained a distribution of
- estimates from each method and calculated percentile intervals. For MRP, we extracted
- 342 credible intervals from the posterior distributions of mean occupancy. We used the 343 confidence intervals provided by the *survey* package (Lumley, 2010) for the poststratified and
- confidence intervals provided by the survey package (Lunney, 2010) for the posisiratiled and
- naïve (i.e. unadjusted) estimates.

## 345 Estimating the trend in mean occupancy

- Having estimated mean occupancy in each time-period, the next step was to estimate the
- 347 difference between the two =  $\bar{y}_2 \bar{y}_1$  (i.e. the trend). We constructed a confidence interval
- 348 for the trend estimated using each method in one of two ways depending on whether the
- 349 method produced one estimate or a distribution. The methods that produced a distribution of
- $\bar{y}_2 \bar{y}_1$  include those that we bootstrapped and MRP, which we fitted in a Bayesian framework (meaning we have a posterior distribution). For these methods, we extracted
- 351 framework (meaning we have a posterior distribution). For these methods, we extracted 352 percentile confidence intervals (95%) from the distributions of estimated trends. For the
- others, poststratification and the naïve estimator (the sample mean), we used the normal
- approximation of the 95% confidence interval, given by  $\pm 1.96 \times$  the standard errors, where
- the standard errors are  $\sqrt{var(\bar{y}_2) + var(\bar{y}_1)}$  (Gelman, 2007).

## 356 **Evaluating the effects of the adjustments**

- 357 We used relative frequency plots (Cf. Makela et al., 2014) to assess whether the adjustments
- brought the distributions of the auxiliary variables in the samples closer to their distributions
- in the population. The first step was to split each auxiliary variable into fifty bins of equal width an angle its many The relative frequency of grid equation (the i'a) in each bin h is
- 360 width spanning its range. The relative frequency of grid squares (the *i*'s) in each bin k is 261 N = (N + i) + i = 1 is the number of grid squares in each bin k in the nonvelocitien and N is the
- $N_{i,k}/N$ , where  $N_{i,k}$  is the number of grid squares in each bin k in the population and N is the population size (we use k to index the bins to distinguish them from the strata described
- earlier). Similarly, the relative frequency of sampled grid squares in each k is  $n_{i,k}/n$ , where
- $n_{i,k}$  is the number of sampled grid squares in bin k and n is the total sample size. In the
- adjusted samples, the equivalent relative frequency is  $\frac{\sum_{i \in k} w_i}{\sum_{i \in k} w_i}$  (slightly different for
- 266 subsampling; see below). We compared the original and adjusted samples' deviations from
- 367 the population using the Mean Absolute Error (MAE) of the relative frequencies across all k.
- 368 If the MAE from the adjusted sample is smaller than the original sample, then the adjustment
- brought the distribution of the auxiliary variable closer to its population distribution.
- 370 We were not able to produce adjusted relative frequency plots based on the doubly robust
- 371 estimator or MRP. The problem was that could not estimate reasonable sampling weights
- from either method, which are needed to adjust the relative frequencies of the auxiliaries.
- 373 Whilst it has been shown how to derive unit-level sampling weights where the MRP

- multilevel model is linear (Gelman, 2007), no formula has yet been derived for the case of the
- binomial GLM (Valliant et al., 2018). As for the doubly robust estimator, Valliant (2020)
- 376 showed how to derive "model-assisted" weights. Unfortunately, in our case, many of the
- 377 model-assisted weights were very large and negative. The extreme weights appear to be
- 378 caused by the pattern of residuals from the superpopulation model (recalling that we used a 379 linear regression despite the fact that occupancy is binary), but it is beyond the scope of this
- paper to definitively diagnose the problem. There is no obvious way to derive weights from
- the subsampling estimator either. However, for this estimator, the adjusted relative
- 382 frequencies of the auxiliaries are simply their distributions in the subsamples so are simple to
- 383 obtain.
- 384 Assessing whether the estimates of mean occupancy in each period and the trend were
- improved by each adjustment method was simpler. We measured the difference between the
- point estimates of mean occupancy and the truth using the absolute error =  $|\bar{y}_N \bar{y}_{est}|$ , where
- 387  $\bar{y}_{est}$  is the estimate. For the trends, whose signs are of interest, we simply used the
- 388 differences between the estimates and the truth. We also assessed whether the
- 389 confidence/credible intervals produced by each method covered the true means and trend. We
- 390 did not consider the power to detect the trend—that is, whether the methods' uncertainty
- 391 intervals span zero at some percentile—because many biodiversity applications are
- 392 descriptive-inferential rather than decision-theoretic.

# 393 **Results**

# 394 Per-period sample representativeness and estimated mean occupancy

- 395 The samples are large but somewhat unrepresentative (Fig. 1). Forty-three percent of grid
- squares were sampled in period one, and the ddc is -0.115; in period two, 62% of grid squares
- were sampled, and the ddc is -0.057. A consequence of these ddc's is that the naive sample
- means underestimate the population means, especially in period one where the magnitude of  $\frac{1}{2}$
- the ddc is greater (Fig. 3).
- 400 With the exception of the doubly robust estimate in period two, the estimates of mean
- 401 occupancy from all adjustment methods in both time-periods had lower absolute errors than

402 the naïve sample mean (Fig. 3; mean absolute errors are provided in supplementary material

- 403 2). The confidence intervals for the poststratified, subsample and quasi-randomisation
- 404 estimates covered the true population mean in period one. In period two, no method's
- 405 confidence/credible interval covered the population mean.



- 407 Figure 3. Naive (i.e. unadjusted) and adjusted sample-based estimates of mean occupancy in
- 408 each time-period. The shaded regions are 95% confidence/credible intervals (see the main
- 409 text for information on we constructed these for each method). The large black circles are the
- 410 true population means in each time-period.

### 411 Estimated trend in mean occupancy

- 412 Estimates of the trend in mean occupancy from all adjustment methods were more accurate
- than the difference in sample means (i.e. the naïve estimate; Fig. 4). However, no method's
- 414 point estimate came close to the true trend of -0.047, and their confidence/credible intervals
- 415 did not cover it.



416

417 Figure 4. Trends in mean occupancy between periods one and two produced by the estimator

418 from each adjustment method, in addition to the naive sample estimate. Error bars delimit

419 95% confidence/credible intervals. The solid vertical black line denotes the true population

420 trend (-0.047).

# 421 **Distributions of auxiliary variables**

422 As measured using Mean Absolute Errors (MAEs), the adjustment methods were generally

423 very good at bringing the distributions of the auxiliaries in the samples closer to those in the

424 population. Fig 5 shows the sample and population distributions of elevation, but the MAEs

425 for this and the proportion of each grid square that falls within a protected area can be found

426 in supplementary material 2.



Figure 5. Sample, population and weighted sample distributions of the auxiliary variable road

429 length (Table 1) in periods one and two.

### 430 Discussion

We applied six approaches to descriptive inference from nonprobability samples to a simple
biodiversity monitoring problem: the estimation of mean occupancy of the plant *C. vulgaris*

in two time-periods and the trend between the two. The methods generally worked well in the

434 sense that they brought the distributions of auxiliary variables in the samples closer to their

435 distributions in the population (all 1 km grid squares in Britain). Successful redistribution of

the auxiliaries translated into improvements of the estimates of mean occupancy in both time-

437 periods and the trend between the two. Importantly, however, no method was completely

438 unbiased, and their uncertainty intervals did not cover the true values of occupancy in the 439 second period or the trend. An abatement rather than an elimination of bias is probably the

best outcome that can be expected, because most adjustment methods rest on the untenable

- 441 assumption that non-sampled locations are "Missing At Random" (MAR); that is, the
- 442 variable of interest is completely independent of sample inclusion given the auxiliary
- 443 variables.

Unlike most practical situations, we were able to test the MAR assumption, because we know 444 the true distribution of C. vulgaris in Britain. In the first time-period, the partial correlation 445 446 between sample inclusion and occupancy, conditional on elevation and protected area 447 coverage, is -0.018; in period two, it is 0.035 (supplementary material 1). These "adjusted" ddc's are lower in magnitude than the original ddc's, -0.115 and -0.058, which means that 448 accounting for elevation and protected area coverage increased the representativeness of the 449 samples (recalling that a smaller ddc means a more representative sample). That is not to say 450 that the samples became *fully* representative, which would be the case in expectation in a 451 452 MAR scenario. The usual yardstick for a representative sample is the simple random sample, whose ddc is of the order  $N^{-1/2}$  (Meng, 2018). In our example,  $N^{-1/2} = 2.2^{-6}$ , which is 453 several orders of magnitude smaller than the "adjusted" ddc's. This goes to show that without 454 a truly miniscule ddc, which would only be induced (in expectation) where the MAR 455 456 assumption holds or under random sampling, sample means as estimators of population means will be appreciably biased (especially where N is large). 457

- 458 It might seem wise to include as many potential auxiliaries as possible to reduce the chance
- 459 of missing a genuine one. For example, Collins et al. (2001) advocated for including all
- 460 variables exceeding some prescribed correlation with sample inclusion and the variable of
- 461 interest. This strategy can be a dangerous one, however. Thoemmes & Rose (2014) show that
- 462 including correlates of sample inclusion and the variable of interest, rather than theoretically463 justifiable causes, can increase the bias in estimates of population means (also see Thoemmes
- 464 & Mohan, 2015). Indeed, in a previous version of this manuscript (Boyd, Stewart, et al.,
- 465 2023), we took a more inclusive approach to the selection of auxiliary variables, and our
- 466 estimates of *C. vulgaris* occupancy in period two were generally more biased than the naïve
- 467 estimate from the unadjusted sample.
- Identifying appropriate auxiliary variables is likely to be the most challenging part of
   adjusting samples in biodiversity monitoring. In many situations, causes of the variable of
- 409 adjusting samples in biodiversity monitoring. In many situations, causes of the variable of470 interest and sample inclusion are not known. Taxon and dataset experts might be able to
- identify potential auxiliary variables, but it is unlikely that they can identify them all (which
- 471 identify potential auxiliary variables, but it is unifierly that they can identify them an ( 472 would be needed to satisfy the MAR assumption). The experts might also erroneously
- 472 would be needed to satisfy the WAR assumption). The experts high also enoneously473 identify auxiliary variables that are not suitable, in which case adjusting for those variables
- 475 identify auxiliary variables that are not suitable, in which case adjusting for those variables
   474 might do more harm than good (Thoemmes & Rose, 2014). Even if experts were able to
- 474 inight do more narm than good (Thoenines & Rose, 2014). Even if experts were able to 475 correctly identify all relevant auxiliaries, those variables might not be reflected in available
- 475 data. Transparency regarding availability and choice of auxiliary variables should be an
- 477 important component of reporting for all biodiversity monitoring.
- 478 Acknowledging that variables of interest in biodiversity monitoring are likely to be dependent on sample inclusion even after controlling for the available auxiliaries, it might be worth 479 480 considering adjustment methods that forgo the MAR assumption. For example, Tchetgen Tchetgen & Wirth (2017) showed it is possible to recover a true population regression model 481 (and therefore the population mean) by incorporating "instrumental variables". They define 482 instrumental variables as those that are predictive of sample inclusion, independent of the 483 variable of interest and independent of "selection bias" (the latter defined as the mean of the 484 variable of interest in the sample minus the mean of the variable of interest in non-sampled 485 population units). We screened three additional variables-the proportion of each grid square 486 that is accessible to the public, the density of postcodes in each grid square and its nearest 487 neighbours, and the length of major roads in each grid square and its nearest neighbours-to 488 see if they satisfied these three assumptions, but none did (supplementary material 1). In 489 490 practical situations, where the variable of interest is not known for non-sampled population
- 491 units, testing these assumptions would be challenging.
- 492 Whilst we are confident that the availability of data on auxiliary variables was the limiting 493 factor in our example, it is possible that improvements to the adjustment methods themselves could have improved matters. Where sampling weights are not of interest, for example, it 494 might be sensible to use a binomial generalised linear model, rather than a general linear 495 496 regression, for the superpopulation model (Wu & Sitter, 2001). The multilevel modelling component of MRP exploits partial pooling, so we could have used more finely resolved 497 strata on the basis that estimates for sparse strata (with low sample sizes) would be shrunk 498 499 towards those from strata with more data. The question is whether fine-tuning the adjustment 500 methods is likely to result in large improvements in accuracy. As Mercer et al., (2018), writing in the context of adjusting survey samples, put it, "[t]he right variables make a big 501 difference for accuracy. Complex statistical methods, not so much." The fact that most 502 503 adjustment methods performed almost similarly in our example is further evidence that the
- 504 choice of auxiliary variables matters more than the specifics of the adjustment method.

505 Given that the methods performed similarly in terms of accuracy, it would be sensible to

- 506 consider those that are quickest to run. As we implemented it, MRP took by far the longest to
- run of all the methods—about ten hours per time-period on a computer cluster. Bootstrapping
- to estimate confidence intervals meant that other methods, too, were quite expensive to run.
- 509 This was particularly true for the quasi-randomisation and doubly robust procedures, both of 510 which involved repeatedly fitting the sample inclusion model—itself a time consuming
- 511 process. The remainder of the methods—superpopulation modelling, subsampling and
- 512 poststratification—took a negligible amount of time to run.
- 513 Although we have only considered one species and dataset, previous studies (in other
- disciplines) shed light on the factors that affect the accuracy of inference from nonprobability
- samples more generally. Omitting genuine auxiliary variables in the adjustment process is
- 516 more problematic where those variables explain larger proportions of the variance in the 517 variable of interest and sample inclusion (Collins et al., 2001). Equally, inclusion of certain
- 517 variable of interest and sample inclusion (Collins et al., 2001). Equally, inclusion of certain 518 variables that are not appropriate auxiliaries becomes more problematic where they explain
- 519 larger proportions of the variance in the variable of interest and sample inclusion (Thoemmes
- 520 & Rose, 2014). In practice, we do not know the strengths of the effects potential auxiliaries
- 521 on the variable of interest and sample inclusion, or whether they have effects at all, but it is
- 522 clear that the selection of auxiliary variables will be a critical component of adjusting samples
- 523 in biodiversity monitoring.
- 524 Given the importance of selecting appropriate auxiliary variables, we propose the following
- 525 general strategy for analysts intending to draw inferences about biodiversity change from
- 526 geographically unrepresentative nonprobability samples. The first step should be to consult
- taxon and dataset experts, who might be able to identify relevant auxiliary variables. Where
   possible, consulting multiple experts to capture their uncertainty about what affects sample
- inclusion and the variable of interest would be desirable. If data are available on these
- 530 variables, then their distributions in the sample and population should be compared to assess
- 531 whether the data are representative with respect to that variable. Several tools are available to
- perform such comparisons (Boyd et al., 2021; Ruete, 2015). The next step should be to adjust
- the sample based on the relevant auxiliaries and to draw inferences from the adjusted
- samples. Like others (e.g. Mercer et al., 2018), we found that it is of little consequence which
- adjustment method is used, so it is sensible to pick one that is quick to run. Rather than
- assuming the adjustment worked perfectly, it is important to acknowledge and report the
- 537 potential for residual bias. As we have shown, traditional uncertainty intervals are not 538 guaranteed (or even likely) to cover the true population parameters of interest unless all
- relevant auxiliaries are known and reflected in available data (Meng, 2018). Where there is
- doubt about the relevant auxiliary variables, a safer strategy is to assess the risk of bias
- qualitatively and to ensure it is reflected in the way that findings are reported (Boyd et al.,
- 542 2022; Meineke & Daru, 2021; Pescott et al., 2022).
- 543

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