

1 **METHODOLOGY**

2 **Quantitative evidence synthesis: a practical guide on meta-analysis, meta-regression, and**
3 **publication bias tests for environmental sciences**

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13 Short title: a practical guide for quantitative synthesis

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17 **Abstract**

18 Meta-analysis is a quantitative way of synthesizing results from multiple studies to obtain reliable
19 evidence of an intervention or phenomenon. Indeed, an increasing number of meta-analyses are
20 conducted in environmental sciences, and resulting meta-analytic evidence is often used in
21 environmental policies and decision-making. We conducted a survey of recent meta-analyses in
22 environmental sciences and found poor standards of current meta-analytic practice and reporting.
23 Only ~40% of the 73 reviewed meta-analyses reported heterogeneity (variation among effect sizes
24 beyond sampling error), and publication bias was assessed in less than half. Furthermore, although
25 almost all the meta-analyses had multiple effect sizes originating from the same studies, non-
26 independence among effect sizes was considered in only half of the meta-analyses. To improve the
27 implementation of meta-analysis in environmental sciences, we here outline practical guidance for
28 conducting a meta-analysis in environmental sciences. We describe the key concepts of effect size
29 statistics and meta-analysis, and detail procedures for fitting multilevel meta-analysis and meta-
30 regression models and performing associated publication bias tests. We demonstrate a clear need for
31 environmental scientists to embrace multilevel meta-analytic models, which explicitly model
32 dependence among effect sizes, rather than the commonly used random-effects models. Further, we
33 discuss how reporting and visual presentations of meta-analytic results can be much improved by
34 following reporting guidelines such as PRISMA-EcoEvo (Preferred Reporting Items for Systematic
35 Reviews and Meta-Analyses for Ecology and Evolutionary Biology). This paper, along with the
36 accompanying online tutorial ([link](#)), serves as a practical guide on conducting a complete set of
37 meta-analytic procedures (i.e., meta-analysis, heterogeneity quantification, meta-regression,
38 publication bias tests and sensitivity analysis) and also as a gateway to more advanced, yet
39 appropriate, methods.

40 **KEYWORDS**

41 Hierarchical models, robust variance estimation, spatial dependency, variance-covariance matrix,
42 meta-analysis of variance, missing data, network meta-analysis, multivariate meta-analysis

43 **Background**

44 Evidence synthesis is an essential part of science. The method of systematic review provides the
45 most trusted and unbiased way to achieve the synthesis of evidence [1-3]. Systematic reviews often
46 include a quantitative summary of studies on the topic of interest, referred to as a meta-analysis (for
47 discussion on the definitions of ‘meta-analysis’, see [4]). The term meta-analysis can also mean a
48 set of statistical techniques for quantitative data synthesis. The methodologies of the meta-analysis
49 were initially developed and applied in medical and social sciences. However, meta-analytic
50 methods are now used in many other fields, including environmental sciences [5-7]. In
51 environmental sciences, the outcomes of meta-analyses (within systematic reviews) have been used
52 to inform environmental and related policies (see [8]). Therefore, the reliability of meta-analytic
53 results in environmental sciences is important beyond mere academic interests; indeed, incorrect
54 results could lead to ineffective or sometimes harmful environmental policies [8].

55
56 As in medical and social sciences, environmental scientists frequently use traditional meta-analytic
57 models, namely fixed-effect and random-effects models [9, 10]. However, we contend that such
58 models in their original formulation are no longer useful and are often incorrectly used, leading to
59 unreliable estimates and their errors. This is mainly because the traditional models assume
60 independence among effect sizes, but almost all primary research papers include more than one
61 effect size, and this non-independence is often not considered (e.g., [11-13]). Furthermore, previous
62 reviews of published meta-analyses in environmental sciences (hereafter, ‘environmental meta-
63 analyses’) have demonstrated that less than half report or investigate heterogeneity (inconsistency)
64 among effect sizes [14-16]. Many environmental meta-analyses also do not present any sensitivity
65 analysis, for example, for publication bias (i.e., statistically significant effects being more likely to
66 be published, making collated data unreliable; [17, 18]). These issues might have arisen for several
67 reasons, for example, because of no clear conduct guideline for statistical part of meta-analyses in
68 environmental sciences and rapid developments in meta-analytic methods. Taken together, the field

69 urgently requires a practical guide to implement correct meta-analyses and associated procedures
70 (e.g., heterogeneity analysis, meta-regression, and publication bias tests; cf. [19]).

71

72 To assist environmental scientists conducting meta-analyses, the aims of this paper are five-fold.

73 First, we provide an overview of the processes involved in a meta-analysis while introducing some
74 key concepts. Second, after introducing the main types of effect size (statistics), we mathematically
75 describe the two commonly used traditional meta-analytic models, demonstrate their futility, and
76 introduce a practical, multilevel meta-analytic model for environmental sciences that appropriately
77 handles non-independence among effect sizes. Third, we show how to quantify heterogeneity (i.e.,
78 consistencies among effect sizes and/or studies) using this model, and then and explain such
79 heterogeneity using meta-regression. Fourth, we show how to test for publication bias in a meta-
80 analysis and describe other common types of sensitivity analysis. Fifth, we cover other technical
81 issues relevant to environmental sciences (e.g., scale and phylogenetic dependence) as well as some
82 advanced meta-analytic techniques. In addition, these five aims (sections) are interspersed with two
83 more sections, named ‘Notes’ on: 1) visualisation and interpretation and 2) reporting and archiving.
84 Some of these sections are accompanied by results from a survey of 73 environmental meta-
85 analyses published between 2019 and 2021; survey results depict current practices and highlight
86 associated problems (for the method of the survey, see Supporting Information). Importantly, we
87 provide easy-to-follow implementations of much of what is described below, using the *R* package,
88 *metafor* [20] and other *R* packages at the webpage ([https://itchyshin.github.io/Meta-](https://itchyshin.github.io/Meta-analysis_tutorial/)
89 [analysis_tutorial/](https://itchyshin.github.io/Meta-analysis_tutorial/)), which also connects the reader to the wealth of online information on meta-
90 analysis (see also [21]).

91

92 **Overview with key concepts**

93 Statistically speaking, we have three general objectives when conducting a *meta-analysis* [12]: 1)
94 estimating *an overall mean*, 2) quantifying consistency (*heterogeneity*) between studies, and 3)

95 explaining the heterogeneity (see Table 1 for the definitions of the terms in *italic*). A notable feature
96 of a meta-analysis is that an overall mean is estimated by taking the *sampling variance* of each
97 *effect size* into account: a study (effect size) with a low sampling variance (usually based on a larger
98 sample size) is assigned more weight in estimating an overall mean than one with a high sampling
99 variance (usually based on a smaller sample size). However, an overall mean estimate itself is often
100 not informative because one can get the same overall mean estimates in different ways. For
101 example, we may get an overall estimate of zero if all studies have zero effects with no
102 heterogeneity. In contrast, we might also obtain a zero mean across studies that have highly variable
103 effects (e.g., ranging from strongly positive to strongly negative), signifying high heterogeneity.
104 Therefore, quantifying indicators of heterogeneity is an essential part of a meta-analysis, necessary
105 for interpreting the overall mean appropriately. Once we observe non-zero heterogeneity among
106 effect sizes, then, our job is to explain this variation by running *meta-regression* models, and, at the
107 same time, quantify how much variation is accounted for (often quantified as R^2). In addition, it is
108 important to conduct an extra set of analyses, often referred to as *publication bias tests*, which are a
109 type of *sensitivity analysis* [11], to check the robustness of meta-analytic results.

110 **Choosing an effect size statistic**

111 In this section, we introduce different kinds of ‘effect size statistics’ or ‘effect statistics’. In the
112 literature, the term ‘effect size’ is typically used to refer to the magnitude or strength of an effect of
113 interest or its biological interpretation (e.g., environmental significance). Effect sizes can be
114 quantified using a range of statistics (for details, see [22]). In our survey of environmental meta-
115 analyses, the two most commonly used effect size statistics are: the logarithm of response ratio,
116 $\ln RR$ ([23]; also known as the ratio of means; [24]) and standardized mean difference, SMD (often
117 referred to as Hedges’ g or Cohen’s d [25, 26]). These are followed by proportion (%) and Fisher’s
118 z -transformation of correlation, or Zr . These four effect statistics nearly fit into the three categories,
119 which are named: 1) single-group statistics (a statistical summary form one group; e.g., proportion),
120 2) comparative statistics (comparing statistics between two groups e.g., SMD and $\ln RR$), and 3)

121 association statistics (relationships between two variables; e.g., Zr). Table 2 summarizes effect
122 statistics which are common or potentially useful for environmental scientists. Some of the readers
123 may be surprised that ‘mean’ can be an effect size for a meta-analysis, although once one realises
124 proportion is a type of mean, this makes sense (e.g., the mean concentration values of a certain
125 pollutant can be meta-analysed across studies). Also, this example nicely illustrates that any
126 statistics with sampling variance can become an ‘effect size’. The main reason why SMD, $\ln RR$, Zr ,
127 or proportion are popular effect statistics is that they are unitless, while a meta-analysis of mean, or
128 mean difference, can only be conducted when all effect sizes have the same unit (e.g., cm, kg).

129

130 Table 2 also includes effect statistics that are likely to be unfamiliar to environmental scientists;
131 these are effect sizes that characterise differences in the observed variability between samples, (i.e.,
132 $\ln SD$, $\ln CV$, $\ln VR$ and $\ln CVR$; [27, 28]) rather than central tendencies (averages). These
133 dispersion-based effect statistics can provide us with extra insights along with average-based effect
134 statistics. Although the literature survey showed none of these were used in our sample, these effect
135 sizes have been used in many fields, including agriculture (e.g., [29]), ecology (e.g., [30]),
136 evolutionary biology (e.g., [31]), psychology (e.g., [32]), education (e.g., [33]), psychiatry (e.g.,
137 [34]), neurosciences (e.g., [35]), and more. Perhaps, it is not difficult to think of an environmental
138 intervention that can affect not only mean but also variance of a group of individuals or plots.
139 Indeed, per unit yield, organic agriculture has a lower temporal stability compared to conventional
140 agriculture, although the former promotes greater biodiversity [29]. Also, environmental stressors
141 such as pesticides and eutrophication are likely to increase variability in biological systems because
142 stress accentuates individual differences in environmental responses (e.g., [36, 37]). Such ideas are
143 yet to be tested meta-analytically (cf. [38, 39]).

144 **Choosing a meta-analytic model**

145 **Two traditional models & a proposed practical model**

146 The fixed-effect model, which should probably be more correctly referred to as the ‘common-
147 effect’ model, can be written as [9, 10, 40]:

$$148 \quad z_j = \beta_0 + m_j, \quad (1)$$

$$149 \quad m_j \sim N(0, v_j),$$

150 where the intercept, β_0 is the overall mean, z_j (the response/dependent variable) is the effect size
151 from the j th study ($j = 1, 2, \dots, N_{study}$; in this model, N_{study} = the number of studies = the number of
152 effect sizes), m_j is the effect of the j th sampling variance (v_j), which is normally distributed with the
153 mean of 0 and the ‘study-specific’ sampling variance, v_j (see also Figure 1A). The overall mean is
154 basically the same as a weighted average with the weights, $w_j = 1/v_j$. An important assumption of
155 meta-analysis is that sampling variance is known (note that we can usually estimate sampling
156 variance correctly and unbiasedly, using formulas; Table 2; but see section ‘Scale dependence’). As
157 you may see from this formulation, the fixed-effect model assumes that the only source of variation
158 in effect sizes (z_j) is the effect due to sampling variance (whose main determinant is the sample size,
159 n ; Table 2).

160

161 Similarly, the random-effects model can be expressed as:

$$162 \quad z_j = \beta_0 + u_j + m_j, \quad (2)$$

$$163 \quad u_j \sim N(0, \tau^2), \& \ m_j \sim N(0, v_j),$$

164 where u_j is the j th study effect (or ‘paper effect’, as we here equate ‘study’ with ‘paper’), which is
165 normally distributed with the mean of 0 and the between-study variance, τ^2 , and other notations are
166 the same as in Equation 1 (Figure 1B). Here, the overall mean is the weighted average with weights
167 $w_j = 1/(\tau^2 + v_j^2)$. The model assumes each study has its specific mean, $b_0 + u_j$, and

168 (in)consistencies among studies (effect sizes) are indicated by τ^2 . When τ^2 is 0 (or not different
 169 from 0), the random-effects model simplifies to the fixed-effect model (cf. Equations 1 & 2). Given
 170 no studies in environmental sciences are conducted in the same manner or even at exactly the same
 171 place and time, we should expect different studies to have different means. Therefore, in almost all
 172 cases in the environmental sciences, the random-effects model is a more ‘realistic’ model [9, 10,
 173 40]. Accordingly, most environmental meta-analyses (68.5%; 50 out of 73 studies) in our survey
 174 used the random-effects model, while only 2.7% (2 of 73 studies) used the fixed-effect model.

175

176 **Multilevel meta-analytic models**

177 Although we have introduced the random-effects model as being more realistic than the fixed-effect
 178 model (Equation 2), we argue that the random-effects model is rather limited and impractical for the
 179 environmental sciences. This is because random-effects models, like fixed-effect models, assume all
 180 effect sizes (z_j) to be independent. However, when multiple effect sizes are obtained from a study
 181 (paper), these effect sizes are dependent (for more details, see the next section on non-
 182 independence). Indeed, our survey showed that in almost all datasets used in environmental meta-
 183 analyses, this type of non-independence among effect sizes occurred (97.3%; 71 out of 73 studies,
 184 with two studies being unclear, so effectively 100%). Therefore, we propose the simplest and most
 185 practical meta-analytic model for environmental sciences as [13, 40] (see also [41, 42]):

$$186 \quad z_i = \beta_0 + u_{j[i]} + e_i + m_i, \quad (3)$$

$$187 \quad u_j \sim N(0, \tau^2), \quad e_i \sim N(0, \sigma^2), \quad \& \quad m_i \sim N(0, v_i)$$

188 where we explicitly recognize that $N_{effect} (i = 1, 2, \dots, N_{effect}) > N_{study} (j = 1, 2, \dots, N_{study})$ and,
 189 therefore, we now have the study effect (between-study effect), $u_{j[i]}$ (for the j th study and i th effect
 190 size) and effect-size level (within-study) effect, e_i (for the i th effect size), with the between-study
 191 variance, τ^2 , and with-study variance, σ^2 , respectively, and other notations are the same as above.
 192 We note that this model (Equation 3) is an extension of the random-effects model (Equation 2), and

193 we refer to it as the multilevel/hierarchical model (used in 7 out of 73 studies: 9.6%; note that
194 Equation 3 is also known as a three-level meta-analytic model; Figure 1C). Also, environmental
195 scientists who are familiar with (generalised) linear mixed-models may recognize u_j (the study
196 effect) as the effect of a random factor which is associated with a variance component, i.e., τ^2 [43];
197 also, e_i and m_i can be seen as parts of random factors, associated with σ^2 and v_i (the former is
198 comparable to the residuals, while the latter is something special for a meta-analysis).
199 It seems that many researchers are aware of the issue of non-independence so that they often use
200 average effect sizes per study (paper) or choose one effect size (at least 28.8%, 21 out of 73
201 environmental meta-analyses). However, as we discussed elsewhere [13, 40], such averaging or
202 selection of one effect size per study dramatically reduces our ability to investigate environmental
203 drivers of variation among effect sizes [13]. Therefore, we strongly support the use of the multilevel
204 model. Nevertheless, this proposed multilevel model, formulated as Equation 3 does not usually
205 deal with the issue of non-independence completely, which we elaborate on in the next section.

206 **Non-independence among effect sizes and among sampling errors**

207 When you have multiple effect sizes from a study (paper), there are two broad types and three cases
208 of non-independence (cf. [11, 12]): 1) effect sizes are calculated from different cohorts of
209 individuals (or groups of plots) within a study (Figure 2A, referred to as ‘shared study identity’),
210 and 2) effects sizes are calculated from the same cohort of individuals (or group of plots; Figure 2B,
211 referred to as ‘shared measurements’) or *partially* from the same individuals and plots, more
212 concretely, sharing individuals and plots from the control group (Figure 2C, referred to as ‘shared
213 control group’). The first type of non-independence induces dependence among effect sizes, but not
214 among sampling variances, and the second type leads to non-independence among sampling
215 variances. Many datasets, if not almost all, will have a combination of these three cases (or even are
216 more complex, see the section ‘Complex non-independence’). Failing to deal with these non-
217 independences will inflate Type 1 error (note that the overall estimate, b_0 is unlikely to be biased,
218 but standard error of b_0 , $se(b_0)$, will be underestimated; note that this is also true for all other

219 regression coefficients, e.g., b_1 ; see Table 1). The multilevel model (as in Equation 3) only takes
 220 care of cases of non-independence that are due to the shared study identity but neither shared
 221 measurements nor shared control group.

222

223 There are two practical ways to deal with non-independence among sampling variances. The first
 224 method is that we explicitly model such dependence using a variance-covariance (VCV) matrix
 225 (used in 6 out of 73 studies: 8.2%). Imagine a simple scenario with a dataset of three effect sizes
 226 from two studies where two effects sizes from the first study are calculated (partially) using the
 227 same cohort of individuals (Figure 2B); in such a case, the sampling variance effect, m_i , as in
 228 Equation 3, should be written as:

229

$$m_i \sim N(0, \mathbf{M})$$

230

$$\mathbf{M} = \begin{bmatrix} v_{1[1]} & \rho\sqrt{v_{1[1]}v_{1[2]}} & 0 \\ \rho\sqrt{v_{1[2]}v_{1[1]}} & v_{1[2]} & 0 \\ 0 & 0 & v_{2[3]} \end{bmatrix}, \quad (4)$$

231 where \mathbf{M} is the VCV matrix showing the sampling variances, $v_{1[1]}$ (study 1 & effect size 1), $v_{1[2]}$
 232 (study 1 & effect size 2), and $v_{2[3]}$ (study 2 & effect size 3) in its diagonal, and sampling
 233 covariance, $\rho\sqrt{v_{1[1]}v_{1[2]}} = \rho\sqrt{v_{1[2]}v_{1[1]}}$ in its off-diagonal elements, where ρ is a correlation
 234 between two sampling variances due to shared samples (individuals/plots). Once this VCV matrix is
 235 incorporated into the multilevel model (Equation 3), all the types of non-independence, as in Figure
 236 2, are taken care of. Table 3 shows formulas for the sampling variance and covariance of the four
 237 common effect sizes (SDM, lnRR, proportion and Zr). For comparative effect statistics (Table 2),
 238 exact covariances can be calculated under the case of ‘shared control group’ (see [44, 45]). But this
 239 is not feasible for most circumstances because we usually do not know what ρ should be. Some
 240 have suggested to fix this value at 0.5 (e.g., [11]) or 0.8 (e.g., [46]); the latter is a more conservative
 241 assumption. Or one can run both and use one for the main analysis and the other for sensitivity
 242 analysis (for more, see the section ‘Conducting sensitivity analysis & critical appraisal’).

243

244 The second method overcomes this very issue of unknown ρ by approximating average dependence
245 among sampling variance (and effect sizes) from the data and incorporating such dependence to
246 estimate standard errors (only used in 1 out of 73 studies). This method is known as ‘robust
247 variance estimation’, RVE, and the original estimator was proposed by Hedges and colleagues in
248 2010 [47]. Meta-analysis using RVE is relatively new, and this method has been applied to
249 multilevel meta-analytic models only recently [48]. Note that the random-effects model (Equation
250 2) and RVE could correctly model both types of non-independence. However, we do not
251 recommend the use of RVE with Equation 2 because, as we will later show, estimating σ^2 as well
252 as τ^2 will constitute the important part of understanding and gaining more insights from one’s data.
253 We do not yet have a definite recommendation on which method to use to account for non-
254 independence among sampling errors (using the VCV matrix or RVE). This is because no
255 simulation work in the context of multilevel meta-analysis has been done so far, using multilevel
256 meta-analyses [13, 48]. For now, one could use both VCV matrices and RVE in the same model
257 [48] (see also [21]).

258 **Quantifying & explaining heterogeneity**

259 **Measuring consistencies with heterogeneity**

260 As mentioned earlier, quantifying heterogeneity among effect sizes is an essential component of any
261 meta-analysis. Yet, our survey showed only 28 out of 73 environmental meta-analyses (38.4%)
262 report at least one index of heterogeneity (e.g., τ^2 , Q , and I^2). Conventionally, the presence of
263 heterogeneity is tested by Cochrane’s Q test. However, Q (often denoted as Q_T or Q_{total}), and its
264 associated p value, are not particularly informative: the test doesn’t tell about the extent of
265 heterogeneity (e.g., [10]), only whether heterogeneity is zero or not (when $p < 0.05$). Therefore, for
266 environmental scientists, we recommend two common ways of quantifying heterogeneity from a
267 meta-analytic model: absolute heterogeneity measure (i.e., variance components, τ^2 and σ^2) and

268 relative heterogeneity measure (i.e., I^2 ; see also the section ‘Notes on visualisation and
 269 interpretation’ for another way of quantifying and visualising heterogeneity at the same time, using
 270 prediction intervals). We have already covered the absolute measure (Equations 2 & 3), so here we
 271 explain I^2 , which ranges from 0 to 1. The heterogeneity measure, I^2 , for the random-effect model
 272 (Equation 2) can be written as:

$$273 \quad I^2 = \frac{\tau^2}{\tau^2 + \bar{v}}, \quad (5)$$

$$274 \quad \bar{v} = \frac{(N_{effect} - 1) \sum_{j=1}^k (1/v_i)}{(\sum_{j=1}^k (1/v_i))^2 - \sum_{j=1}^k (1/v_i)^2}, \quad (6)$$

275 where \bar{v} is referred to as the typical sampling variance (originally this is called ‘within-study’
 276 variance, as in Equation 2, and note that in this formulation, within-study effect and the effect of
 277 sampling error is confounded; see [49, 50]; see also [51]) and the other notations are as above. As
 278 you can see from Equation 5, we can interpret I^2 as relative variance due to differences between
 279 studies, or not due to sampling variance.

280

281 By seeing I^2 as a type of interclass correlation (also known as repeatability, [52]), we can generalize
 282 I^2 to multilevel models. In the case of Equation 3 ([40, 53]; see also [42]), we have:

$$283 \quad I_{total}^2 = \frac{\tau^2 + \sigma^2}{\tau^2 + \sigma^2 + \bar{v}}. \quad (7)$$

284 Because we can have two more I^2 , Equation 7 is denoted as I_{total}^2 ; these other two are I_{study}^2 and
 285 I_{effect}^2 , respectively:

$$286 \quad I_{study}^2 = \frac{\tau^2}{\tau^2 + \sigma^2 + \bar{v}}, \quad (8)$$

$$287 \quad I_{effect}^2 = \frac{\sigma^2}{\tau^2 + \sigma^2 + \bar{v}}. \quad (9)$$

288 I_{total}^2 represents variance due to differences both between and within studies or not due to
 289 differences in sampling variance, while I_{study}^2 is variance due to differences between studies, and
 290 I_{effect}^2 is variance due to differences within studies (Figure 3A). Once heterogeneity is quantified
 291 (note almost all data will have non-zero heterogeneity and an earlier meta-meta-analysis suggests in
 292 ecology, we have, on average, I^2 close to 90%, [53]), it is time to fit a meta-regression model to
 293 explain the heterogeneity. Notably, the magnitude of I_{study}^2 (or τ^2) and I_{effect}^2 (or σ^2) can already
 294 inform you which predictor variable (usually referred to as ‘moderator’) is likely to be important,
 295 which we explain in the next section.

296 **Explaining variance with meta-regression**

297 We can extend the multilevel model (Equation 3) to a meta-regression model with one moderator
 298 (also known as predictor, independent, explanatory variable, or fixed factor), as below:

$$299 \quad z_i = \beta_0 + \beta_1 x_{1j[i]} + u_{j[i]} + e_i + m_i, \quad (10)$$

300 where β_1 is a slope of the moderator (x_1), $x_{1j[i]}$ denotes the value of x_1 , corresponding to the j th
 301 study (and the i th effect sizes). Equation 10 (meta-regression) is comparable to the simplest
 302 regression with the intercept (β_0) and slope (β_1). Notably, $x_{1j[i]}$ differs between studies and,
 303 therefore, it will mainly explain the variance component, τ^2 (which relates to I_{study}^2). On the other
 304 hand, if noted like x_{1i} , this moderator would vary within studies or at the level of effect sizes,
 305 therefore, explaining σ^2 (relating to I_{effect}^2). Therefore, when τ^2 (I_{study}^2), or σ^2 (I_{effect}^2), is close to
 306 zero, there will be little point fitting a moderator(s) at the level of studies, or effect sizes,
 307 respectively.

308

309 As in multiple regression, we can have multiple (multi-moderator) meta-regression, which can be
 310 written as:

$$311 \quad z_i = \beta_0 + \sum_{h=1}^q \beta_h x_{h[i]} + u_{j[i]} + e_i + m_i, \quad (11)$$

312 where $\sum_{h=1}^q \beta_h x_{h[i]}$ denotes the sum of all the moderator effects, with q being the number of slopes
313 (starting with $h = 1$). We note that q is not necessarily the number of moderators. This is because
314 when we have a categorical moderator, which is common, with more than two levels (e.g., method
315 A, B & C), the fixed effect part of the formula is $\beta_0 + \beta_1 x_1 + \beta_2 x_2$, where x_1 and x_2 is what is
316 known as ‘dummy’ variables, which code whether the i th effect size belongs to, for example,
317 method B or C, with β_1 and β_2 being contrasts between A and B and between A and C, respectively
318 (for more explanations of dummy variables, see our webpage; also see [54, 55]). Traditionally,
319 researchers conduct separate meta-analyses per different groups (known as ‘sub-group analysis’),
320 but we prefer a meta-regression approach with a categorical variable, which is statistically more
321 powerful [40]. Also, importantly, what can be used as a moderator(s) is very flexible, including, for
322 example, individual/plot characteristics (e.g., age, location), environmental factors (e.g.,
323 temperature), methodological differences between studies (e.g., randomization), and bibliometric
324 information (e.g., publication year; see more in the section ‘Checking for publication bias and
325 robustness’). Note that moderators should be decided *priori*, meaning one’s meta-analysis plan and
326 design should include a list of moderators to be considered.

327
328 As with meta-analysis, the Q -test (Q_m or $Q_{moderator}$) is often used to test the significance of a
329 moderator(s). To complement this test, we can also quantify variance explained by a moderator(s)
330 using R^2 . We can define R^2 using Equation 11 as:

$$331 \quad R^2 = \frac{f^2}{f^2 + \tau^2 + \sigma^2}, \quad (12)$$

$$332 \quad f^2 = \text{Var} \left(\sum_{h=1}^q \beta_h x_{h[i]} \right), \quad (13)$$

333 where R^2 is known as marginal R^2 (*sensu* [56, 57]; cf. [58]), f^2 is the variance due to a
334 moderator(s), and $(f^2 + \tau^2 + \sigma^2)$ here equals to $(\tau^2 + \sigma^2)$ in Equation 7, as f^2 ‘absorbs’ variance
335 from τ^2 and/or σ^2 . We can compare the similarities and differences in Figure 3B where we denote a

336 part of f^2 originating from τ^2 as f_{study}^2 while σ^2 as f_{effect}^2 . In a multiple meta-regression model,
337 we often want to find a model with the ‘best’ or an adequate set of predictors (i.e., moderators). R^2
338 can potentially help such a model selection process. Yet, methods based on information criteria
339 (such as AIC) may be preferable. Although model selection based on the information criteria is
340 beyond the scope of the paper, we refer the reader to relevant articles (e.g., [59, 60]), and we show
341 an example of this procedure in our online tutorial ([link](#)).

342 **Notes on visualisation and interpretation**

343 Visualization and interpretation of results is an essential part of a meta-analysis [61, 62].
344 Traditionally, a forest plot is used to display the values and 95% of confidence intervals (CIs) for
345 each effect size. and the overall effect and its 95% CI (denoted as a diamond, as shown in Figure
346 4A). More recently, adding a 95% prediction interval (PI) to the overall estimate has been strongly
347 recommended because 95% PIs show a predicted range of values in which an effect size from a new
348 study would fall, assuming there is no sampling error [63]. Here, we think that examining the
349 formulas for 95% CIs and PIs for the overall mean (from Equation 3) is illuminating:

$$350 \quad 95\%CI = \beta_0 \pm t_{df[\alpha=0.05]} \cdot se(\beta_0), \quad (14)$$

$$351 \quad 95\%PI = \beta_0 \pm t_{df[\alpha=0.05]} \sqrt{se^2(\beta_0) + \tau^2 + \sigma^2}, \quad (15)$$

352 where $t_{df[\alpha=0.05]}$ denotes the t value with the degree of freedom, df , at 97.5 percentile (or $\alpha =$
353 0.05) and other notations are as above. In a meta-analysis, it has been conventional to use z value
354 1.96 instead of $t_{df[\alpha=0.05]}$, but simulation studies have shown the use of t value over z value reduces
355 Type 1 errors under many scenarios and, therefore, is recommended (e.g., [13, 64]). Also, it is
356 interesting to note that by plotting 95% PIs, we can visualize heterogeneity as Equation 15 includes
357 τ^2 and σ^2 .

358

359 A ‘forest’ plot can become quickly illegible as the number of studies (effect sizes) becomes large,
360 so other methods of visualizing the distribution of effect sizes have been suggested. Some suggested
361 to present a ‘caterpillar’ plot, which is a version of the forest plot, instead (Figure 4B; e.g., [65]).
362 We here recommend an ‘orchard’ plot, as it is can present results across different groups (or a result
363 of meta-regression with a categorical variable), as shown in Figure 4C [65]. For visualization of a
364 continuous variable, we suggest what is called a ‘bubble’ plot, shown in Figure 4D. Visualization
365 not only helps us interpret meta-analytic results, but can also help to identify something we may not
366 see from statistical results, such as influential data points and outliers that could threaten the
367 robustness of our results.

368 **Checking for publication bias and robustness**

369 **Detecting and correcting for publication bias**

370 Checking for and adjusting for any publication bias is necessary to ensure the validity of meta-
371 analytic inferences [66]. However, our survey showed almost half of the environmental meta-
372 analyses (46.6%; 34 out of 73 studies) neither tested for nor corrected for publication bias (cf. [14-
373 16]). The most popular methods used were: 1) graphical tests using funnel plots (26 studies;
374 35.6%), 2) regression-based tests such as Egger regression (18 studies; 24.7%), 3) Fail-safe number
375 tests (12 studies; 16.4%), and 4) trim-and-fill tests (10 studies; 13.7%). We recently showed that
376 these methods are unsuitable for datasets with non-independent effect sizes, with the exception of
377 funnel plots [67] (for an example of funnel plots, see Figure 5A). This is because these methods
378 cannot deal with non-independence in the same way as the fixed-effect and random-effects models.
379 Here, we only introduce a two-step method for multilevel models that can both detect and correct
380 for publication bias [67] (originally proposed by [68, 69]), more specifically, the “small study
381 effect” where an effect size value from a small-sample-sized study can be much larger in magnitude
382 than a ‘true’ effect [70, 71]. This method is a simple extension of Egger’s regression [72], which
383 can be easily implemented by using Equation 10:

384
$$z_i = \beta_0 + \beta_1 \sqrt{\frac{1}{\tilde{n}_i}} + u_{j[i]} + e_i + m_i, \quad (16)$$

385
$$z_i = \beta_0 + \beta_1 \left(\frac{1}{\tilde{n}_i}\right) + u_{j[i]} + e_i + m_i, \quad (17)$$

386 Where \tilde{n}_i is known as effective sample size; for Zr and proportion it is just n_i , and for SMD and
 387 lnRR, it is $n_{iC}n_{iT}/(n_{iC} + n_{iT})$, as in Table 2. When β_1 is significant, we conclude there exists a
 388 small-study effect (in terms of a funnel plot, this is equivalent to significant funnel asymmetry).
 389 Then, we fit Equation 17 and then, we look at the intercept β_0 , which will be a bias-corrected
 390 overall estimate (note that β_0 in Equation 16 provides less accurate estimates when non-zero overall
 391 effects exist [68, 69]; Figure 5B). An intuitive explanation of why β_0 (Equation 17) is the bias-
 392 corrected estimate is that the intercept represents $1/\tilde{n}_i = 0$ (or $\tilde{n}_i = \infty$); in other words, β_0 is the
 393 estimate of the overall effect when we have a very large (infinite) sample size.

394
 395 Conveniently, this proposed framework can be extended to test for another type of publication bias,
 396 known as time-lag bias, or the decline effect, where effect sizes tend to get closer to zero over time,
 397 as larger or statistically significant effects are published more quickly than smaller or non-
 398 statistically significant effects [73, 74]. Again, a decline effect can be statistically tested by adding
 399 year to Equation 3:

400
$$z_i = \beta_0 + \beta_1 c(\text{year}_{j[i]}) + u_{j[i]} + e_i + m_i, \quad (18)$$

401 where $c(\text{year}_{j[i]})$ is the mean-centred publication year of a particular study (study j and effect size
 402 i); this centring makes the intercept β_0 meaningful, representing the overall effect estimate at the
 403 mean value of publication years (see [55]). When the slope is significantly different from 0, we
 404 deem that we have a decline effect (or time-lag bias; Figure 5C).

405
 406 However, there may be some confounding moderators, which need to be modelled together. Indeed,
 407 Egger's regression (Equations 16 & 17) is known to detect the funnel asymmetry when there is little

408 heterogeneity; this means that we need to model $\sqrt{1/\tilde{n}_i}$ with other moderators that account for
409 heterogeneity. Given this, we probably should use a multiple meta-regression model, as below:

$$410 \quad z_i = \beta_0 + \beta_1 \sqrt{\frac{1}{\tilde{n}_i}} + \beta_2 c(\text{year}_{j[i]}) + \sum_{h=3}^q \beta_h x_{h[i]} + u_{j[i]} + e_i + m_i, \quad (19)$$

411 where $\sum_{h=3}^q \beta_h x_{h[i]}$ is the sum of the other moderator effects apart from the small-study effect and
412 decline effect, and other notations are as above (for more details see [67]). We need to carefully
413 consider which moderators should go into Equation 19 (e.g., fitting all moderators or using an AIC-
414 based model selection method; see [59, 60]). Of relevance, when running complex models, some
415 model parameters cannot be estimated well, or they are not ‘identifiable’ [75]. This is especially so
416 for variance components (random-effect part) rather than regression coefficients (fixed-effect part).
417 Therefore, it is advisable to check whether model parameters are all identifiable, which can be
418 checked using the *profile* function in *metafor* (for an example, see our tutorial webpage).

419 **Conducting sensitivity analysis & critical appraisal**

420 Sensitivity analysis explores the robustness of meta-analytic results by running a different set of
421 analyses from the original analysis, and comparing the results (note that some consider publication
422 bias tests a part of sensitivity analysis; [11]). For example, we might be interested in assessing how
423 robust results are to the presence of influential studies, to the choice of method for addressing non-
424 independence, or weighting effect sizes. Unfortunately, in our survey, only 37% of environmental
425 meta-analyses (27 out of 73) conducted sensitivity analysis. There are two general and interrelated
426 ways to conduct sensitivity analyses [60, 76, 77]. The first one is to take out influential studies (e.g.,
427 outliers) and re-run meta-analytic and meta-regression models. We can also systematically take
428 each effect size out and run a series of meta-analytic models to see whether any resulting overall
429 effect estimates are different from others; this method is known as ‘leave-one-out’, which is
430 considered less subjective and thus recommended.

431

432 The second way of approaching sensitivity analysis is known as subset analysis, where a certain
433 group of effect sizes (studies) will be excluded to re-run the models without this group of effect
434 sizes. For example, one may want to run analysis without studies which did not randomize samples.
435 Yet, as mentioned earlier, we recommend using meta-regression (Equation 13) with a categorical
436 variable of randomization status ('randomized' or 'not randomized'), to statistically test for an
437 influence of moderators. It is important to note that such tests for risk of bias (or study quality) can
438 be considered as a way of quantitatively evaluating the importance of study features that were noted
439 at the stage of critical appraisal, which is essential part of any systematic review (see [11, 78]). In
440 other words, we can use meta-regression or subset analysis to quantitatively conduct critical appraisal
441 using (study-level) moderators that code, for example, blinding, randomization, and selective
442 reporting. Despite the importance of critical appraisal ([78]), only 4 of 73 environmental meta-
443 analyses (5.6%) in our survey assessed the risk of bias in each study included in a meta-analysis
444 (i.e., evaluating a primary study in terms of the internal validity of study design and reporting). We
445 emphasize that critically appraising each paper or checking them for risk of bias is an extremely
446 important topic. Also, critical appraisal is not restricted to quantitative synthesis. Therefore, we do
447 not cover any further in this paper (see more for [79, 80])

448 **Notes on transparent reporting & open archiving**

449 For environmental systematic reviews and maps, there are reporting guidelines called RepOrting
450 standards for Systematic Evidence Syntheses in environmental research, ROSES [81] and synthesis
451 assessment checklist, the Collaboration for Environmental Evidence Synthesis Appraisal Tool
452 (CEESAT; [82]). However, these guidelines are somewhat limited in terms of reporting quantitative
453 synthesis because they cover only a few core items. These two guidelines are complemented by the
454 Preferred Reporting Items for Systematic Reviews and Meta-Analyses for Ecology and
455 Evolutionary Biology (PRISMA-EcoEvo; [83]; cf. [84, 85]), which provides an extended set of
456 reporting items covering what we have described above. Items 20-24 from PRISMA-EcoEvo are
457 most relevant: these items outline what should be reported in the Methods section: i) sample sizes

458 and study characteristics, ii) meta-analysis, iii) heterogeneity, iv) meta-regression and v) outcomes
459 of publication bias and sensitivity analysis (see Table 4). Our survey, as well as earlier surveys,
460 suggest there is a large room for improvement in the current practice ([14-16]). Incidentally, the
461 orchard plot is well aligned with Item 20, as this plot type shows both the number of effect sizes and
462 studies for different groups (Figure 4C). Further, our survey of environmental meta-analyses
463 highlighted the poor standards of data openness (with 24 studies sharing data: 32.9%) and code
464 sharing (7 studies: 29.2%). Environmental scientists must archive their data as well as their analysis
465 code in accordance with the FAIR principles (Findable, Accessible, Interoperable, and Reusable;
466 [86]) using dedicated depositories such as Dryad, FigShare, Open Science Framework (OSF),
467 Zenodo or others (cf. [87, 88]), preferably not on the publisher's webpage (as paywall may block
468 access). However, archiving itself is not enough; data requires metadata (detailed descriptions) and
469 the code needs to also be FAIR [89, 90].

470 **Other relevant and advanced issues**

471 **Scale dependence**

472 The issue of scale dependence is a unique yet widespread problem in environmental sciences (see
473 [7, 91]); our literature survey indicated three quarters of the environmental meta-analyses (56 out of
474 73 studies) have inferences that are potentially vulnerable to scale-dependence [92]. For example,
475 studies that set out to compare group means in biodiversity measures, such as species richness, can
476 vary as a function of the scale (size) of the sampling unit. When the unit of replication is a plot (not
477 an individual animal or plant), the aerial size of a plot (e.g., 100 cm² or 1 km²) will affect both the
478 precision and accuracy of effect size estimates (e.g., lnRR and SMD). In general, a study with larger
479 plots might have more accurately estimated species richness differences, but less precisely than a
480 study with smaller plots and greater replication. Lower replication means that our sampling variance
481 estimates are likely to be misestimated, and the study with larger plots will generally have less
482 weight than the study with smaller plots, due to a higher sampling variance. Inaccurate variance

483 estimates in little-replicated ecological studies are known to cause an accumulating bias in
484 precision-weighted meta-analysis, requiring correction [93]. To assess the potential for scale-
485 dependence, it is recommended that analysts test for possible for covariation among plot size,
486 replication, variances, and effect sizes [91]. If detected, analysts should use an effect size statistic
487 that is less sensitive to scale dependence (lnRR), and could use the size of a plot as a moderator in
488 meta-regression and consider, or we could run an unweighted model ([7]; note that only 12%, 9 out
489 of 73 studies, accounted sampling area in some way).

490 **Missing data**

491 In many fields, meta-analytic data almost always encompass missing values see [94-96]. Broadly,
492 we have two types of missing data in meta-analyses [97, 98]: 1) missing data in standard deviations
493 or sample sizes, associated with means, preventing effect size calculations (Table 2), and 2) missing
494 data in moderators. There are several solutions for both types. The best, and first to try, should be
495 contacting the authors. If this fails, we can potentially ‘impute’ missing data. Single imputation
496 methods using the strong correlation between standard deviation and mean values (known as mean-
497 variance relationship) are available, although single imputation can lead to Type I error [94, 95]
498 (see also [93]) because we do not model the uncertainty of imputation itself. Contrastingly, multiple
499 imputation, which creates multiple versions of imputed datasets, incorporates such uncertainty.
500 Indeed, multiple imputation is a preferred and proven solution for missing data in effect sizes and
501 moderators [97, 98]. Yet, correct implementation can be challenging (see [98]). What we require
502 now is an automated pipeline of merging meta-analysis and multiple imputation, which accounts for
503 imputation uncertainty, although it may be challenging for complex meta-analytic models.
504 Fortunately, however, for lnRR, there is a series of new methods that can perform better than the
505 conventional method and which can deal with missing SDs [99]; note that these methods do not
506 deal with missing moderators. Therefore, where applicable, we recommend these new methods,
507 until an easy-to-implement multiple imputation workflow arrives.

508 **Complex non-independence**

509 Above, we have only dealt with the model that include study identities as a clustering/grouping
510 (random) factor. However, many datasets are more complex, with potentially more clustering
511 variables in addition to the study (paper) identity. It is certainly possible that an environmental
512 meta-analysis contains data from multiple species. Such a situation creates an interesting
513 dependence among effect sizes from different species, known as phylogenetic relatedness, where
514 closely related species are more likely to be similar in effect sizes compared to distantly related
515 ones (e.g., mice *vs.* rats and mice *vs.* sparrows). Our multilevel model framework is flexible and can
516 accommodate phylogenetic relatedness. A phylogenetic multilevel meta-analytic model can be
517 written as [40, 100, 101]:

$$518 \quad z_i = \beta_0 + a_{k[i]} + s_{k[i]} + u_{j[i]} + e_i + m_i, \quad (20)$$

$$519 \quad a_k \sim N(0, \omega^2 \mathbf{A}), \quad s_k \sim N(0, \gamma^2), \quad u_j \sim N(0, \tau^2), \quad e_i \sim N(0, \sigma^2), \quad \& \quad m_i \sim N(0, v_i),$$

520 where $a_{k[i]}$ is the phylogenetic (species) effect for the k th species (effect size i ; $N_{effect} (i = 1, 2, \dots,$
521 $N_{effect}) > N_{study} (j = 1, 2, \dots, N_{study}) > N_{species} (k = 1, 2, \dots, N_{species}))$, normally distributed with $\omega^2 \mathbf{A}$
522 where is the phylogenetic variance and \mathbf{A} is a correlation matrix coding how close each species are
523 to each other and ω^2 is the phylogenetic variance, $s_{k[i]}$ is the non-phylogenetic (species) effect for
524 the k th species (effect size i), normally distributed with the variance of γ^2 (the non-phylogenetic
525 variance), and other notations are as above. It is important to realize that \mathbf{A} explicitly models
526 relatedness among species, and we do need to provide this correlation matrix, using a distance
527 relationship usually derived from a molecular-based phylogenetic tree (for more details, see [40,
528 100, 101]). Some may think that the non-phylogenetic term ($s_{k[i]}$) is unnecessary or redundant
529 because $s_{k[i]}$ and the phylogenetic term ($a_{k[i]}$) are both modelling variance at the species level.
530 However, a simulation recently demonstrated that failing to have the non-phylogenetic term ($s_{k[i]}$)
531 will often inflate the phylogenetic variance ω^2 , leading to an incorrect conclusion that there is a
532 strong phylogenetic signal (as shown in [101]). The non-phylogenetic variance (γ^2) arises from, for

533 example, ecological similarities among species (herbivores *vs.* carnivores or arboreal *vs.* ground-
534 living) not phylogeny [40].

535

536 Like phylogenetic relatedness, effect sizes arising from closer geographical locations are likely to
537 be more correlated [102]. Statistically, spatial correlation can be also modelled in a manner
538 analogous to phylogenetic relatedness (i.e., rather than a phylogenetic correlation matrix, **A**, we fit a
539 spatial correlation matrix). For example, Maire and colleagues [103] used a meta-analytic model
540 with spatial autocorrelation to investigate the temporal trends of fish communities in the network of
541 rivers in France. We note that a similar argument can be made for temporal correlation, but in many
542 cases, temporal correlation could be dealt with, albeit less accurately, as a special case of ‘shared
543 measurements’, as in Figure 2. An important idea to take away is that one can model different, if
544 not all, types of non-independence as a random factor(s) in a multilevel model.

545 **Advanced techniques**

546 Here we touch upon five advanced meta-analytic techniques with potential utility for environmental
547 sciences, providing relevant references so that interested readers can obtain more information on
548 these advanced topics. The first one is the meta-analysis of magnitudes, or absolute values (effect
549 sizes), where researchers may be interested in deviations from 0, rather than the directionality of the
550 effect [104]. For example, Cohen and colleagues [105] investigated absolute values of phenological
551 responses, as they were concerned with the magnitudes of changes in phenology rather than
552 directionality.

553

554 The second method is the meta-analysis of interaction where our focus is on synthesizing the
555 interaction effect of, usually, 2 × 2 factorial design (e.g., the effect of two simultaneous
556 environmental stressors; [44, 106, 107]). Recently, Siviter and colleagues [108] showed that
557 agrochemicals interact synergistically (i.e., non-additively) to increase the mortality of bees; that is,

558 two agrochemicals together caused more mortality than the sum of mortalities of each chemical
559 (i.e., additive effect).

560

561 Third, network meta-analysis has been heavily used in medical sciences; network meta-analysis
562 usually compares different treatments in relation to placebo and ranks these treatments in terms of
563 effectiveness [109]. The very first ‘environmental’ network meta-analysis, as far as we know,
564 investigated the effectiveness of ecosystem services among different land types [110].

565

566 Fourth, a multivariate meta-analysis is where one can model two or more different types of effect
567 sizes with the estimation of pair-wise correlations between different effect sizes. The benefit of such
568 an approach is known as the ‘borrowing of strength’, where the error of fixed effects (moderators;
569 e.g., b_0 and b_1) can be reduced when different types of effect sizes are correlated (i.e., $se(b_0)$ and
570 $se(b_1)$ can be smaller [111]) For example, it is possible for $\ln RR$ (differences in mean) and $\ln VR$
571 (differences in SDs) to be modelled together (cf. [112]).

572

573 Fifth, as with network meta-analysis, there has been a surge in the use of ‘individual participants
574 data’, called ‘IPD meta-analysis’, in medical sciences [113, 114]. The idea of IPD meta-analysis is
575 simple – rather than using summary statistics reported in papers (sample means and variances), we
576 directly use raw data from all studies. We can either model raw data using one complex multilevel
577 (hierarchical) model (one-step method) or calculate statistics for each study and use a meta-analysis
578 (two-step method; note that both methods will usually give the same results). Study-level random
579 effects can be incorporated to allow the response variable of interest to vary among studies, and
580 overall effects correspond to fixed, population-level estimates. The use of IPD or ‘full-data
581 analyses’ has also surged in ecology, aided by open-science policies that encourage the archival of
582 raw data alongside articles, and initiatives that synthesise raw data (e.g., PREDICTS [115],
583 BioTime [116]). In health disciplines, such meta-analyses are considered the ‘gold standard’ [117],

584 owing to their potential for resolving issues regarding study-specific designs and confounding
585 variation, and it is unclear whether and how they might resolve issues such as scale dependence in
586 environmental meta-analyses [91, 118].

587 **Conclusions**

588 In this article, we have attempted to describe the most practical ways to conduct quantitative
589 synthesis, including meta-analysis, meta-regression, and publication bias tests. In addition, we have
590 shown that there is much to be improved in terms of meta-analytic practice and reporting via a
591 survey of 73 recent environmental meta-analyses. Such improvements are urgently required,
592 especially given the potentially influence that environmental meta-analyses can have for policies
593 and decision making [8]. So often, meta-analysts have called for better reporting of primary
594 research (e.g., [119, 120]), and now this is the time to raise the standards of reporting in meta-
595 analyses. We hope our contribution will help to catalyse a turning point for better practice in
596 quantitative synthesis in environmental sciences. We remind the reader most of what is described is
597 implemented in the *R* environment at our tutorial webpage and researchers can readily use the
598 proposed models and techniques ([link](#)). Finally, meta-analytic techniques are always developing
599 and improving. It is certainly possible that in the future, our proposed models and related methods
600 will become dated, just as the traditional fixed-effect and random-effects models already are.
601 Therefore, we must endeavour to be open-minded to new ways of doing quantitative research
602 synthesis in environmental sciences.

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607 **Author contributions**

608 SN was commissioned to write this article, so that he assembled a team of co-authors. SN discussed
609 the idea with YY, ELM, RS and ML, and all of them contributed to the design of this review. ML
610 led the survey working with YY and ELM, while YY led the creation of the accompanying
611 webpage working with RS. SN supervised all aspects of this work and wrote the first draft, which
612 was commented on, edited, and therefore, significantly improved by the other co-authors.

613 **Conflict of interest**

614 The author reported no conflict of interest

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621

622 **Figure legends**

623

624 **Fig. 1** Visualisation of the three statistical models of meta-analysis: A) a fixed-effect model (1-
625 level), B) a random-effects model (2-level), and C) a multilevel model (3-level; see the text for what
626 symbols mean).

627

628 **Fig. 2** Visualisation of the three types of non-independence among effect sizes: 1) due to shared
629 study identities (effect sizes from the same study may be similar in values), 2) due to shared
630 measurements (effect sizes come from the same group of individuals/plots but are based on

631 different types of measurements), and 3) due to shared control (effect sizes are calculated using the
632 same control group and multiple treatment groups; see the text for more details).

633
634 **Fig. 3** Visualisation of variation (heterogeneity) partitioned into different variance components: A)
635 quantifying different types of I^2 from a multilevel model (3-level; see Fig. 1C) and B) variance
636 explained, R^2 , by moderators. Note that different levels of variances would be explained, depending
637 on which level a moderator belongs to (study level and effect-size level).

638
639 **Fig. 4** Different types of plots useful for a meta-analysis using data from Midolo et al. [121]: A) a
640 typical forest plot with the overall mean shown as a diamond at the bottom (20 effect sizes from 20
641 studies are used), B) a caterpillar plot (100 effect sizes from 24 studies are used), C) an orchard plot
642 of categorical moderator with seven levels (all effect sizes are used), and D) a bubble plot of a
643 continuous moderator. Note that the first two only show confidence intervals, while the latter two
644 also show prediction intervals (see the text for more details).

645
646 **Fig. 5** Different types of plots for publication bias tests: A) a funnel plot using model residuals,
647 showing a funnel (white) that shows the region of statistical non-significance (30 effect sizes from
648 30 studies are used), B) a bubble plot visualising a multilevel meta-regression that tests for the
649 small study effect (note that the slope was non-significant: $\beta = 0.120$, 95%CI = [-0.095, 0.334]; all
650 effect sizes are used), and C) a bubble plot visualising a multilevel meta-regression that tests for the
651 decline effect (the slope was non-significant: $\beta = 0.003$, 95%CI = [-0.002, 0.008]).

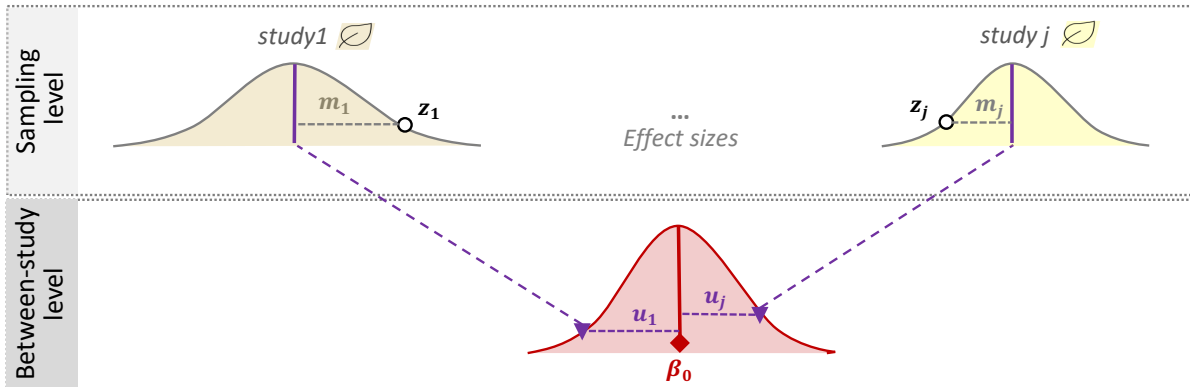
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654 Fig 1
 655

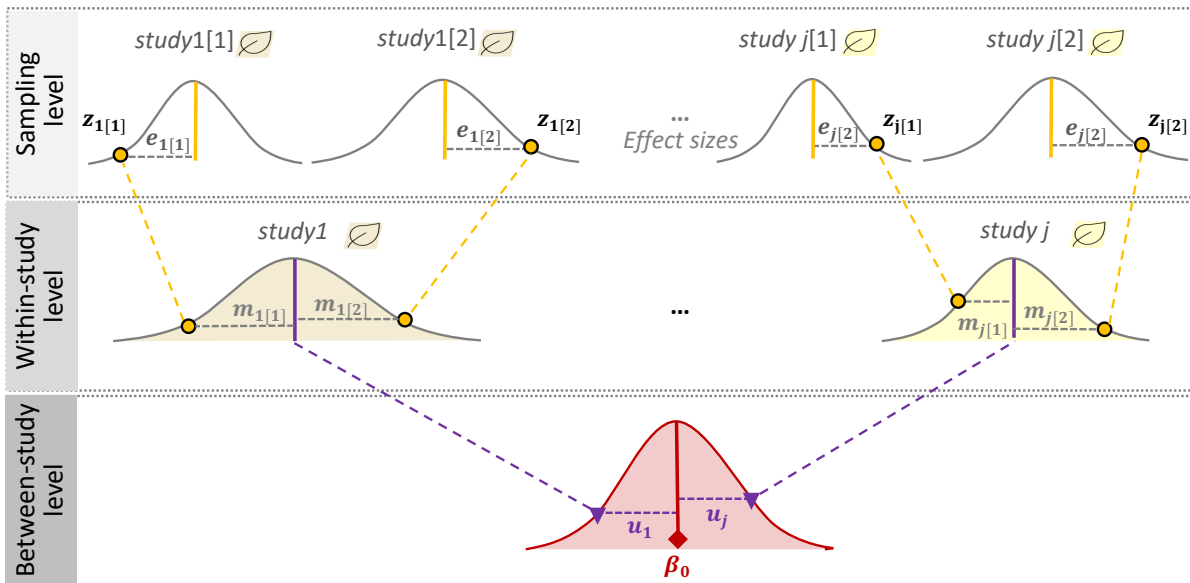
A Fixed-effect model: $z_j = \beta_0 + m_j$



B Random-effects model: $z_j = \beta_0 + u_j + m_j$

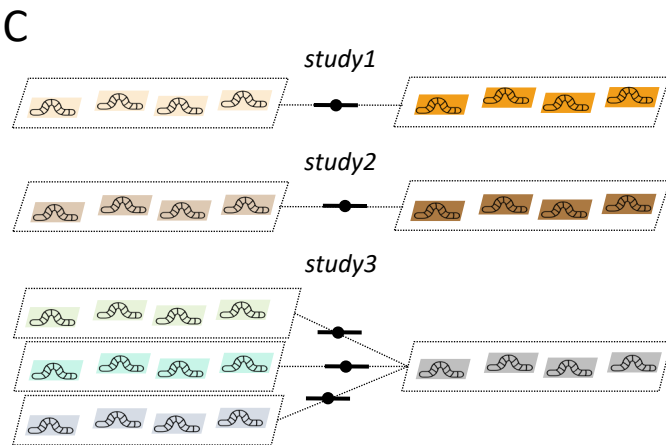
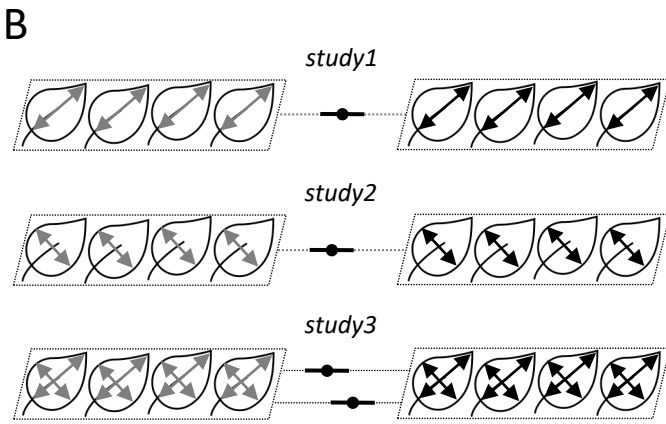
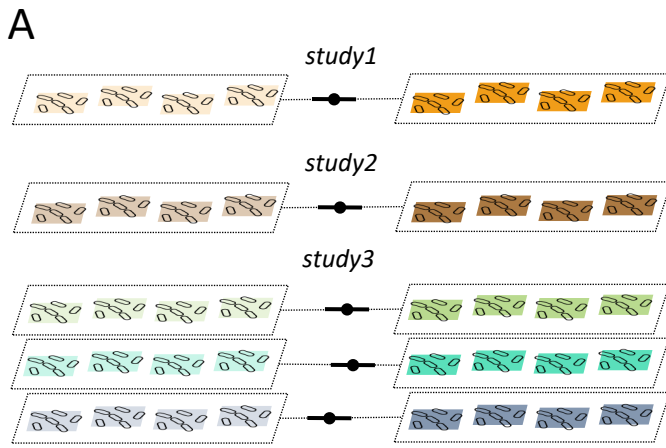


C Multilevel model: $z_i = \beta_0 + u_j[i] + m_i + e_i$

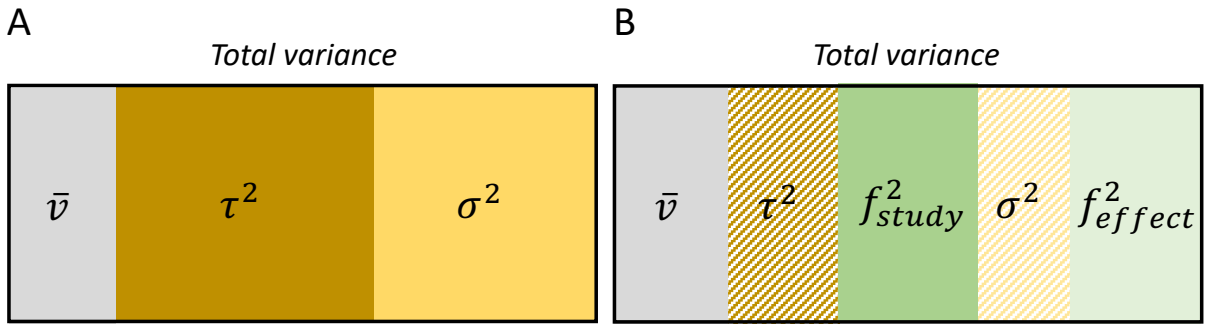


656
 657
 658

659 **Fig 2**
660



661
662



Quantifying heterogeneity: I^2

$$I^2_{total} = \frac{\tau^2 + \sigma^2}{\tau^2 + \sigma^2 + \bar{v}}$$

$$I^2_{study} = \frac{\tau^2}{\tau^2 + \sigma^2 + \bar{v}}$$

$$I^2_{effect} = \frac{\sigma^2}{\tau^2 + \sigma^2 + \bar{v}}$$

Legend

- \bar{v} Sampling variance
- τ^2 Between-study variance
- σ^2 Within-study variance

Explaining variance: R^2

$$R^2 = \frac{f^2}{f^2 + \tau^2 + \sigma^2}$$

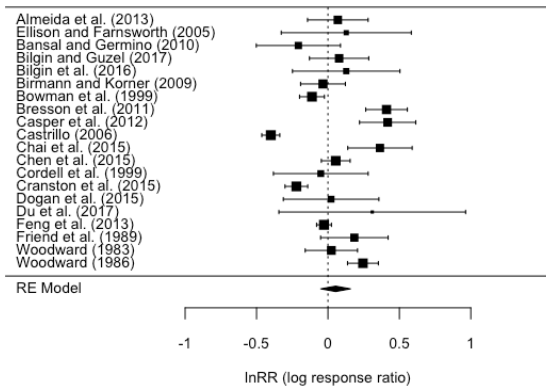
$$f^2 = f^2_{study} + f^2_{effect}$$

Legend

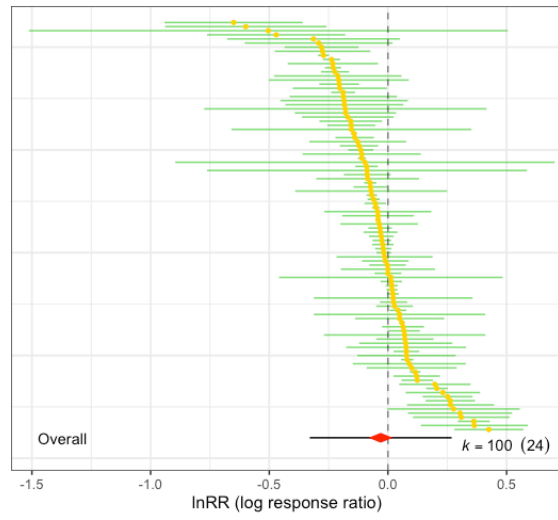
- \bar{v} Sampling variance
- τ^2 Unexplained τ^2 (study level)
- σ^2 Unexplained σ^2 (effect-size level)
- f^2 Explained variance
- f^2_{study} Explained variance (study level)
- f^2_{effect} Explained variance (effect-size level)

667 **Fig 4**
 668

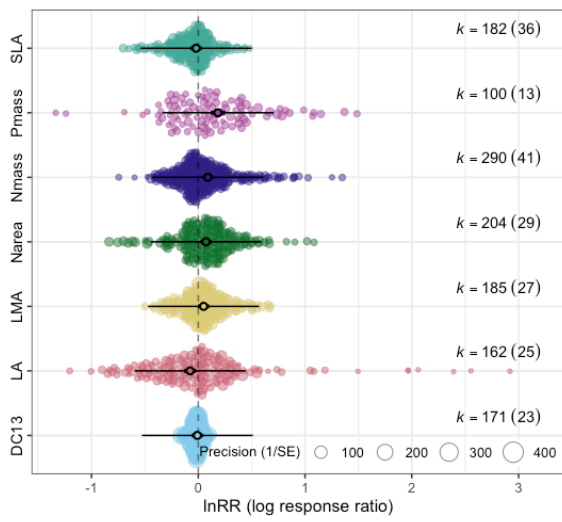
A



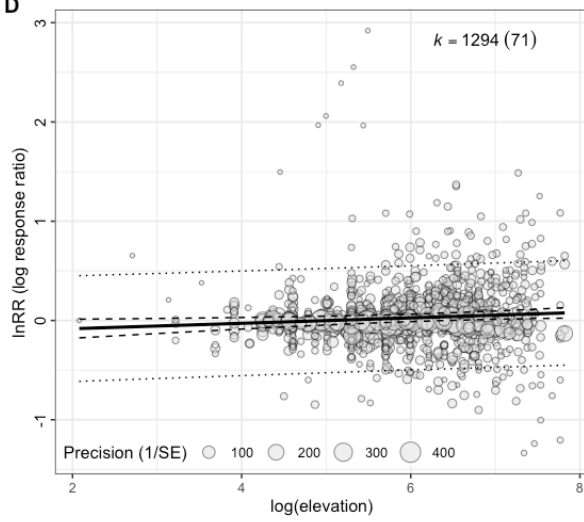
B



C



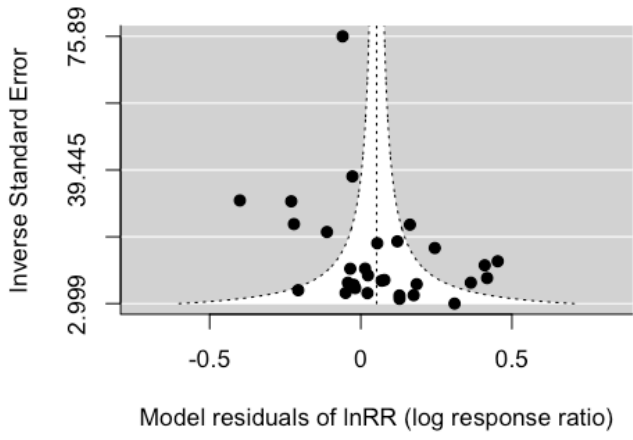
D



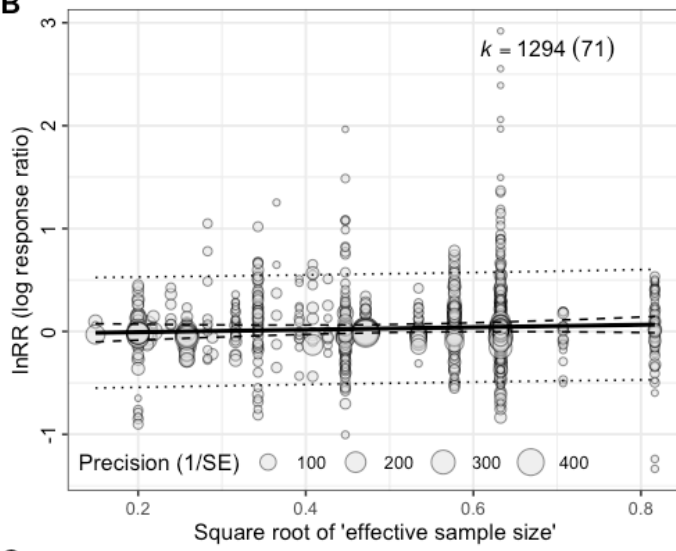
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672 **Fig 5**
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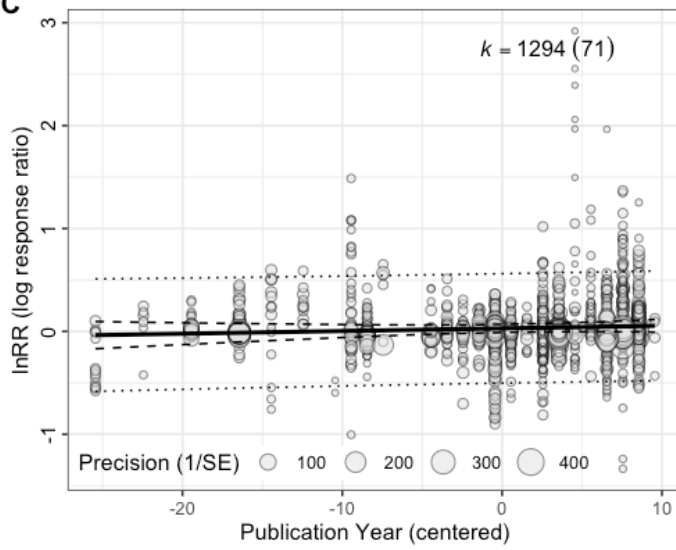
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678 **Tables**679 **Table 1 Definitions of key concepts and associated statistical parameters, which are used in formulas in the main text**

Term	Definition (with associated parameters, if any)
Effect size	A measurement of effect (usually state of a single group, comparison between groups, or association, see Table 2). In a meta-analytic model, it becomes the response variable (denoted as z_i in the formulas).
Sampling variance	A measure of uncertainty in effect size (denoted as v_i). Its inverse is often called ‘weight’ (the square-root of weight is ‘precision’, and the square root of sampling variance is ‘sampling standard error’).
Meta-analysis	A statistical method to aggregate effect sizes from studies on the same or similar topics, by assigning different weights basing on sampling variance of effect sizes. Strictly speaking, in a formal (weighted) meta-analysis, sampling variance needs to be incorporated and it is assumed to be known (Table 2).
Overall mean (effect)	An average effect size based on a meta-analytic model (denoted as β_0 and its standard errors $se(\beta_0)$).
Heterogeneity	An indicator of consistency among effect sizes, or an extent of variation around the overall effect (β_0); heterogeneity can be quantified by absolute measures, such as τ^2 , or relative measures, such as I^2 .

Meta-regression	A regression model which extends a meta-analytic model with a moderator(s), aiming to explain heterogeneity (quantified as R^2) and quantifying the effect of a moderator (denoted as, for example, β_1).
Publication bias tests	A set of statistical methodologies to detect and correct for publication bias, where a subset of results (positive findings) is more likely to be published and present in the meta-analytic dataset than otherwise.
Sensitivity analysis	A set of statistical analyses that checks the robustness of one's main analysis; if sensitivity analysis shows different results (qualitatively and/or quantitatively), then we must doubt the robustness of the main findings.

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681

682 **Table 2 Selected list of effect size statistics and their sampling variances, belonging to three types: 1) single-group effect, 2) comparative effect**
 683 **and 3) association effect**

Type	Statistic	Estimate	Sampling variance	Reference
Single group	Mean	\bar{x}_i	s_i^2/n_i	[122]
Single group	Proportion	$p_i = \frac{y_i}{n_i}$	$\frac{p_i(1-p_i)}{n_i} = \frac{y_i(n_i - y_i)}{n_i^3}$	[122]
Single group	Log standard deviation (lnSD)	$\ln s_i$	$\frac{1}{2(n_i - 1)}$	[27]
Single group	Log coefficient of variation (lnCV)	$\ln\left(\frac{s_i}{\bar{x}_i}\right)$	$\frac{s_i^2}{n_i \bar{x}_i^2} + \frac{1}{2(n_i - 1)}$	[27]
Comparative	Mean difference (MD)	$\bar{x}_{iT} - \bar{x}_{iC}$	$\frac{s_{iC}^2}{n_{iC}} + \frac{s_{iT}^2}{n_{iT}}$	[122]
Comparative	Standardised mean difference (SMD)	$d_i = \frac{\bar{x}_{iT} - \bar{x}_{iC}}{\sqrt{\frac{(n_{iC} - 1)s_{iC}^2 + (n_{iT} - 1)s_{iT}^2}{n_{iC} + n_{iT} - 2}}}$	$\frac{1}{n_{iC}} + \frac{1}{n_{iT}} + \frac{d_i^2}{2(n_{iC} + n_{iT})}$	[25]
Comparative	Risk (proportion) difference (RD)	$\frac{y_{iT}}{n_{iT}} - \frac{y_{iC}}{n_{iC}}$	$\frac{y_{iT}(n_{iT} - y_{iT})}{n_{iT}^3} + \frac{y_{iC}(n_{iC} - y_{iC})}{n_{iC}^3}$	[122]

Comparative	Log odds ratio (lnOR)	$\ln\left(\frac{y_{iT}}{n_{iT} - y_{iT}}\right) - \ln\left(\frac{y_{iC}}{n_{iC} - y_{iC}}\right)$	$\frac{1}{y_{iT}} + \frac{1}{n_{iT} - y_{iT}} + \frac{1}{y_{iC}} + \frac{1}{n_{iC} - y_{iC}}$	[122]
Comparative	Log response ratio (lnRR)	$\ln\left(\frac{\bar{x}_{iT}}{\bar{x}_{iC}}\right)$	$\frac{s_{iC}^2}{n_{iC}\bar{x}_{iC}^2} + \frac{s_{iT}^2}{n_{iT}\bar{x}_{iT}^2}$	[123]
Comparative	Log variability ratio (lnVR)	$\ln\left(\frac{S_{iT}}{S_{iC}}\right)$	$\frac{1}{2(n_{iC} - 1)} + \frac{1}{2(n_{iT} - 1)}$	[27]
Comparative	Log coefficient of variation ratio (lnCVR)	$\ln\left(\frac{S_{iT}}{\bar{x}_{iT}}\right) - \ln\left(\frac{S_{iC}}{\bar{x}_{iC}}\right)$	$\frac{s_{iC}^2}{n_{iC}\bar{x}_{iC}^2} + \frac{1}{2(n_{iC} - 1)} + \frac{s_{iT}^2}{n_{iT}\bar{x}_{iT}^2} + \frac{1}{2(n_{iT} - 1)}$	[27]
Association	Fisher's z-transformation of correlation, r (Zr)	$\frac{1}{2} \ln\left(\frac{1 + r_i}{1 - r_i}\right)$	$\frac{1}{n_i - 3}$	[122]

684 For the column 3rd and 4th, notations represent: \bar{x} (mean), s (standard deviation), n (sampling size), y (the number of events), the subscript T (treatment
685 group), the subscript C (control group) and the subscript i (the i th effect size or study). Note that better estimators may be found in the relevant
686 references; for example, SMD can be best estimated by multiplying by $\left(1 - \frac{3}{4(n_{iC} + n_{iT} - 2) - 1}\right)$, and see also [93].

687

688 **Table 3** Examples of dependence between two sampling variances (v_1 and v_2) and their covariance for four common effect size statistics

Statistic	Situation	Variances	Covariance
Proportion	Shared measurement	$v_1 = \frac{y_1(n_1 - y_1)}{n_1^3}$	$\rho \sqrt{\frac{y_1(n_1 - y_1)}{n_1^3} \frac{y_2(n_2 - y_2)}{n_2^3}}$
		$v_2 = \frac{y_2(n_2 - y_2)}{n_2^3}$	
Zr	Shared measurement	$v_1 = \frac{1}{2} \ln\left(\frac{1 + r_1}{1 - r_1}\right)$	$\rho \sqrt{\frac{1}{4} \ln\left(\frac{1 + r_1}{1 - r_1}\right) \ln\left(\frac{1 + r_2}{1 - r_2}\right)}$
		$v_2 = \frac{1}{2} \ln\left(\frac{1 + r_2}{1 - r_2}\right)$	
lnRR	Shared measurement	$v_1 = \frac{s_{1C}^2}{n_{1C} \bar{x}_{1C}^2} + \frac{s_{1T}^2}{n_{1T} \bar{x}_{1T}^2}$	$\rho \sqrt{\left(\frac{s_{1C}^2}{n_{1C} \bar{x}_{1C}^2} + \frac{s_{1T}^2}{n_{1T} \bar{x}_{1T}^2}\right) \left(\frac{s_{2C}^2}{n_{2C} \cdot \bar{x}_{2C}^2} + \frac{s_{2T}^2}{n_{2T} \cdot \bar{x}_{2T}^2}\right)}$
		$v_2 = \frac{s_{2C}^2}{n_{2C} \cdot \bar{x}_{2C}^2} + \frac{s_{2T}^2}{n_{2T} \cdot \bar{x}_{2T}^2}$	
	Shared control	$v_1 = \frac{s_{1C}^2}{n_{1C} \bar{x}_{1C}^2} + \frac{s_{1T}^2}{n_{1T} \bar{x}_{1T}^2}$	$\frac{s_{1C}^2}{n_{1C} \cdot \bar{x}_{1C}^2}$

$$v_2 = \frac{s_{1C}^2}{n_{1C} \cdot \bar{x}_{1C}^2} + \frac{s_{2T}^2}{n_{2T} \cdot \bar{x}_{2T}^2}$$

$$v_1 = \frac{1}{n_{1C}} + \frac{1}{n_{1T}} + \frac{d_1^2}{2(n_{1C} + n_{1T})}$$

SMD

Shared

measurement

$$v_2 = \frac{1}{n_{2C}} + \frac{1}{n_{2T}} + \frac{d_1^2}{2(n_{2C} + n_{2T})}$$

$$\rho \sqrt{\left(\frac{1}{n_{1C}} + \frac{1}{n_{1T}} + \frac{d_1^2}{2(n_{1C} + n_{1T})}\right) \left(\frac{1}{n_{2C}} + \frac{1}{n_{2T}} + \frac{d_2^2}{2(n_{2C} + n_{2T})}\right)}$$

$$v_1 = \frac{1}{n_{1C}} + \frac{1}{n_{1T}} + \frac{d_1^2}{2(n_{1C} + n_{1T} + n_{2T})}$$

Shared

control

$$v_2 = \frac{1}{n_{1C}} + \frac{1}{n_{2T}} + \frac{d_2^2}{2(n_{1C} + n_{1T} + n_{2T})}$$

$$\frac{1}{n_{1C}} + \frac{d_1 d_2}{2(n_{1C} + n_{1T} + n_{2T})}$$

689 For the 2nd column, see Figure 2. For the 3rd and 4th column, notations represent: the subscript 1C and 2C (control group for 1st and 2nd effect size,
690 respectively, but for shared control, 1C is used for both effect sizes, but 1C and 2C are the same cohort or set of plots), the subscript 1T and
691 2T(treatment group for the 1st and 2nd effect size, respectively; for shared groups, 1T and 2T represents different groups of individuals/plots whereas for
692 shared measurements, 1T and 2T are the same set of individuals/plots), and the other notations are as in Table 1 and the main text (see also [44, 45]).

693 **Table 4 Items relevant to reporting results for a meta-analysis from the Preferred Reporting Items for Systematic reviews and Meta-Analysis**
 694 **for Ecology and Evolutionary Biology (PRISMA-EcoEvo; [83])**

Item	Description
20: Sample sizes and study characteristics	“Report the number of studies and effect size for data included in meta-analyses and subsets of data included in meta-regressions. Provide a summary of key characteristics for reported outcomes (either in text or figures; e.g., one quarter of effect sizes reported for vertebrates and the rest invertebrates) and their limitations (e.g., collinearity and overlaps between moderators), including characteristics related to individual study quality (risk of bias).”
21: Meta-analysis	“Provide a quantitative synthesis of results across studies, including estimates for the main effect size, with confidence/credible intervals.”
22: Heterogeneity	“Report indicators of heterogeneity in the estimated effect (e.g. I^2 , τ^2 and other variance components).”
23: Meta-regression	“Provide estimates of meta-regression slopes (i.e. regression coefficients) for all variables that were assessed for their contribution to heterogeneity. Include confidence/credible intervals, and report interactions if they were included. Describe outcomes from model selection, if done (e.g. R^2 and AIC).”
24: Outcomes of publication bias and sensitivity analysis	“Provide results for the assessments of the risks of bias (e.g. Egger’s regression, funnel plots) and robustness of the review’s results (e.g. subgroup analyses, meta-regression of study quality, results from alternative methods of analysis, and temporal trends)”

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