Assessing species interactions using integrated predator-prey models

Matthieu Paquet and Frédéric Barraquand

Institute of Mathematics of Bordeaux,

University of Bordeaux, CNRS, Bordeaux INP, Talence, France

Abstract

Inferring the strength of species interactions from demographic data is a challenging task. The Integrated Population Modelling (IPM) approach, bringing together population counts, capture-recapture, and individual-level fecundity data into a unified model framework, has been extended from single species to the community level. This allows to specify IPMs for multiple species with interactions specified as links between vital rates and stage-specific densities. However, there is no evaluation of such models when interactions are actually absent—while any interaction inference method runs the risk of producing false positives. We investigate here whether multispecies IPMs could output interactions where there are in fact none, building on an existing predator-prey IPM. We show that interspecific density-dependence estimates are centered on zero when simulated to be zero, and therefore their estimation is unbiased. Their coverage probability, quantifying how many times credible intervals include zero, is also satisfactory. We further confirm that adding random temporal variation to multispecies density-dependent link functions does not alter these results. An update of the observation model additionally shows that the data requirements of the model could have been a little underestimated, as convergence is difficult to reach for previously considered data scenarios. This study therefore reaffirms the potential of multispecies IPMs to infer correctly how biotic interactions influence demography, although it also shows that the data requirements of such models might have to be revised upwards.

Keywords: Integrated Population Model; data assimilation; species interactions; predation; density-dependence.

Correspondence to matthieu.paquet@outlook.com, frederic.barraquand@u-bordeaux.fr

1 Introduction

As dynamic population models with interactions between species are data-hungry, with S^2 interaction parameters for S species, ecological statistics searches for improved ways to infer such population-level interaction strengths. A recently developed technique consists in combining data sources in multispecies Integrated Populations Models (IPMs) including those interspecific interactions (Péron & Koons, 2012; Barraquand & Gimenez, 2019; Quéroué *et al.*, 2021). Because Integrated Population Models (IPMs, Besbeas *et al.*, 2002) combine data on demographic rates (e.g., capture recapture, breeding data) with data on population size (typically from counts), they allow: (a) estimating both demographic rates and population size (and hence their inter-dependencies) in a joint analysis, (b) a improved precision in parameter estimates, compared to separate analyses of component datasets, since the information contained in several datasets combine into estimated parameters (e.g., count data and capture recapture data both contain information on survival rates), and in some cases (c) to estimate parameters for which there is no dedicated data stream, that can only be estimated through inverse estimation of a demographic model (Kéry & Schaub, 2011; Abadi *et al.*, 2010). This last property is particularly useful to estimate population-level species interactions strengths, since population-level interactions are indirectly inferred. Although inverse estimation can in theory be performed using a single data source such as population counts, such inverse estimation is a difficult task fraught with identifiability issues. Asking whether multispecies IPMs performed better than classical inverse estimation from count data alone, Barraquand & Gimenez (2019) have shown that better estimates of interaction parameters could be obtained by combining data sources. Additionally, Quéroué *et al.* (2021) have revealed which interactions were strong enough to be detected in an empirical bird predator-prey system, where bottom-up demographic linkages from prey to predator were found but top-down links were not, in spite of known predation and probable impacts on prey dynamics—top-down effects were likely too weak to be detected.

In these multispecies IPM studies estimating interspecific interactions, between-species linkages have always been considered to be present in the simulations or in the underlying reality (based on background knowledge). Other choices are possible: some multispecies IPMs do not assume interspecific interactions to be present a priori (Lahoz-Monfort *et al.*, 2017), but they do not estimate them either and focus instead on environmental effects. However, multispecies IPMs with interspecific interactions could also be used in situations where it is not clear whether population-level

interactions between species are possible. This is all the more true that interactions are specified as links between vital rates and stage-specific densities, and while some of these relationships may be known a priori, others may not. The issue was raised but not tackled by Barraquand & Gimenez (2019): a natural follow-up is therefore to ask what happens whenever we try to estimate interactions that are actually absent, to make sure that multispecies IPMs do not yield false positives.

Let us note that when estimating or predicting interspecific interactions in general—not just with multispecies IPMs—whether methods could output false positives is a key concern (e.g., with multivariate autoregressive models, Barraquand *et al.* 2021; dynamic bayesian networks, Sander *et al.* 2017; or other machine learning tools, Strydom *et al.* 2021). The fact that all interaction inference methods run the risk of creating false positives of interspecific interactions at exaggerated rates only reinforces the need to evaluate it in multispecies IPMs.

An additional concern is temporal stochasticity in the functions linking vital rates of a given stage of species i to the densities of another stage of species j. In the simulation-based study of Barraquand & Gimenez (2019), it was assumed that such stochasticity was absent, while empirical studies (Péron & Koons, 2012; Quéroué *et al.*, 2021) assumed its presence in order to partition variation in vital rates due to species densities vs other factors changing over time. We therefore still need to understand whether theoretical performances hold in this more empirically realistic context, where environmental factors can perturb demographic rates, and those are not solely deterministic functions of species densities.

To sum up, we follow-up here on the multispecies IPM study of Barraquand & Gimenez (2019) by asking whether (1) inter-species interactions are truly estimated to be zero when species have in fact independent dynamics and (2) how species interaction strengths estimates can be affected by the absence and presence of environmental stochasticity (random year effects on demographic rates).

2 Methods

2.1 General description of the multispecies IPM

We used the same predator-prey model structure and parameter values as Barraquand & Gimenez (2019). The deterministic skeleton can be described as a density-dependent matrix population model

$$\mathbf{n}_{t+1} = \mathbf{A}(\mathbf{n}_t)\mathbf{n}_t. \tag{1}$$

Eq. 1 describes in discrete-time the dynamics of abundances of two species and two stages per species, with projection matrix

$$\mathbf{A}(\mathbf{n}_t) = \begin{pmatrix} 0 & \frac{1}{2} f_{V,t}\left(n^A_{V,t}\right) \phi^J_{V,t}\left(n^A_{P,t}\right) & 0 & 0 \\ \phi^A_{V,t} & \phi^A_{V,t} & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} f_{P,t}\left(n^J_{V,t}\right) \phi^J_{P,t}\left(n^A_{P,t}\right) \\ 0 & 0 & \phi^A_{P,t} & \phi^A_{P,t} \end{pmatrix}$$

and abundance vector

$$\mathbf{n}_t = \begin{pmatrix} n^J_{V,t} \\ n^A_{V,t} \\ n^J_{P,t} \\ n^A_{P,t} \end{pmatrix}$$

where $n^J_{V,t}, n^A_{V,t}, n^J_{P,t}$ and $n^A_{P,t}$ are respectively the abundances of juvenile prey (denoted V as 'victim'), adult prey, juvenile predators and adult predators, at time t. The fecundities $f_{V,t}, f_{P,t}$ are the expected number of juvenile prey and predator produced by an adult prey and predator, respectively. Survival probabilities between t and $t+1$ are denoted with ϕ, so that $\phi^J_{V,t}, \phi^A_{V,t}, \phi^J_{P,t}$ and $\phi^A_{P,t}$ are the survival probabilities of the juvenile prey, adult prey, juvenile predator and adult predator.

2.1.1 Count data

To simulate and account for demographic stochasticity, we modelled yearly (st)age specific abundances $\mathbf{n}_t$ using Binomial and Poisson distributions as in Barraquand & Gimenez (2019) eqs. (2)–(5).

Regarding the observation process for count data, the 2019 model assumed a negligible observation error ($\sigma^2 = 10^{-5}$). The reason was that in absence of replicated counts at each time unit, observation error variance is notoriously difficult to disentangle from process error variance (Knape, 2008; Auger-Méthé *et al.*, 2016). While in some cases it could be possible to remove observation error altogether, because total population sizes of each species (summed numbers of juveniles and adults) are the observed count variables (as in most IPMs), they need to appear in the model as drawn from some probability distribution—they need to be a stochastic node in the MCMC representation. It was therefore decided to keep the formulation of the model in its state-space version, but forcing it to observe true population size almost with certainty (negligible process error variance). However, we uncovered in the present work that stage-specific abundances could not be estimated properly.

Because correctly reproducing stage-specific abundances when fitting a stage-structured model is desirable, and that there is in most wildlife surveys some measure of observation error on counts, we assumed in the present article a non-negligible, positive observation error variance. As we do not have replicated counts at any given time, we do not attempt to estimate observation error variance, and assume that it is known and classically set on the logarithmic scale (i.e., the coefficient of variation of observed population size is constant). For predator counts (denoted P) we have:

$$y_{P,t}|\mathbf{n}_t \sim \mathcal{LN}\left(\log(n^J_{P,t} + n^A_{P,t}), \sigma^2_{obs}\right) \tag{2}$$

And similarly for prey counts :

$$y_{V,t}|\mathbf{n}_t \sim \mathcal{LN}\left(\log(n^J_{V,t} + n^A_{V,t}), \sigma^2_{obs}\right) \tag{3}$$

with $\mathcal{LN}$ the log-Normal distribution and its associated variance on the log-scale $\sigma^2_{obs} = 0.1$.

2.1.2 Survival data

To increase computational efficiency (particularly true for the scenarios with more individuals captured and a shorter time series) compared to the 2019 model, we simulated and fitted the capture-mark-recapture data in the m-array format, using a multinomial likelihood (e.g., Burnham, 1987). The data is in the form of a $(T-1) \times T$ matrix $\mathbf{M} = (m_{t,j})$, with $m_{t,j} = 0,\ \forall j < t$, where T is the total number of years of capture recapture history. $m_{t,t}$ is the number of individuals first marked as young at time t that were re-sighted the following year, and the last column $m_{t,T}$ is the number of individuals first marked at time t that were never re sighted. We then have:

$$\mathbf{m}_{t,\bullet} = (m_{t,t}, m_{t,t+1}, \ldots, m_{t,T}) \sim \text{Multinomial}\left(N_t, (\theta_{t,t}, \ldots, \theta_{t,T})\right) \tag{4}$$

with N_t the number of individuals first marked as young at time t.

Diagonal elements of the $\boldsymbol{\theta}$ matrix write

$$\theta_{t,t} = \phi^J_t p$$

and for $t < j < T$

$$\theta_{t,j} = \phi_t^J \prod_{k=t+1}^{j} \phi_k^A (1-p)^{j-t} p.$$

The last element pertains to individuals never recaptured

$$\theta_{t,T} = 1 - \sum_{k=t}^{T-1} \theta_{t,k}.$$

Parameters ϕ_t^J and ϕ_t^A are respectively the first year and adult survival probabilities from year t to year $t+1$ (for the species considered), and p the recapture (or re-sighting) probability set as constant among years and age classes.

Similarly, we also simulated and fitted m-array data of individuals first marked as adults $\mathbf{M}_a = (m_{t,j}^{(a)})$ for which the above mentioned equations are identical to the exception that ϕ^J is replaced by ϕ^A.

2.1.3 Fecundity data

Fecundity was modelled using a Poisson regression:

$$F_t \sim \text{Poisson}(f_t R_t) \tag{5}$$

with F_t the total number of offspring counted, R_t the number of surveyed broods/litters, and f_t the expected fecundity per adult each year t.

2.2 Alternative scenarios and parameter values

2.2.1 Density dependence and random temporal variation on demographic rates

Intra- and inter-species density dependence of survival rates $\phi_{i,t}^j$ (with $i \in \{V, P\}$ and $j \in \{J, A\}$) and fecundities $f_{i,t}$ were modelled on the logit and log scale, respectively, as in Barraquand &

Gimenez (2019). We initially used the same equations as the 2019 model, which are:

$$\text{logit}(\phi^J_{P,t}) = \alpha_1 + \alpha_2 n^A_{P,t} \tag{6}$$

$$\text{logit}(\phi^J_{V,t}) = \alpha_3 + \alpha_4 n^A_{P,t} \tag{7}$$

$$\text{logit}(\phi^A_{P,t}) = \alpha_{\phi^A_P} \tag{8}$$

$$\text{logit}(\phi^A_{V,t}) = \alpha_{\phi^A_V} \tag{9}$$

$$\log(f_{P,t}) = \alpha_5 + \alpha_6 n^J_{V,t} \tag{10}$$

$$\log(f_{V,t}) = \alpha_7 + \alpha_8 n^A_{V,t} \tag{11}$$

(see associated results in Supplementary Information Table S1 and Figures S5 to S8).

However, to limit posterior correlation between intercept and slope parameters and improve their estimation, we centered the abundances in the density dependent functions. While centering is typically done and most efficient on mean values, mean abundances varied here from a simulation to the next due to stochasticity. Therefore, intercept parameter values would have to be redefined for each simulation to maintain equivalent mean demographic rate values and asymptotic stage specific abundance equilibria for all simulation. To avoid these complications, we centered by subtracting the corresponding fixed point equilibria estimated in Barraquand & Gimenez (2019) as $\overset{*}{n}{}^A_P = 21$, $\overset{*}{n}{}^J_V = 101$ and $\overset{*}{n}{}^A_V = 152$. The new α intercept parameters obey the following centered formulas:

$$\text{logit}(\phi^J_{P,t}) = \alpha_1 + \alpha_2 (n^A_{P,t} - \overset{*}{n}{}^A_P) \tag{12}$$

$$\text{logit}(\phi^J_{V,t}) = \alpha_3 + \alpha_4 (n^A_{P,t} - \overset{*}{n}{}^A_P) \tag{13}$$

$$\text{logit}(\phi^A_{P,t}) = \alpha_{\phi^A_P} \tag{14}$$

$$\text{logit}(\phi^A_{V,t}) = \alpha_{\phi^A_V} \tag{15}$$

$$\log(f_{P,t}) = \alpha_5 + \alpha_6 (n^J_{V,t} - \overset{*}{n}{}^J_V) \tag{16}$$

$$\log(f_{V,t}) = \alpha_7 + \alpha_8 (n^A_{V,t} - \overset{*}{n}{}^A_V). \tag{17}$$

To maintain equivalent dynamics to parameter set 1 of the 2019 model, we calculated the intercepts α_1, α_3, α_5 and α_7 as their original values plus the original slope multiplied by the estimated fixed point equilibrium of the n responsible for density dependence. For example, we now use whenever simulating $\alpha_3 = 0.5 - 0.025 \times 21 = -0.025$ and $\alpha_5 = 0 + 0.004 \times 101 = 0.404$ (Table 1).

In addition, we introduced scenarios with inter-annual random variation in the intercepts of density-dependent links, such that

$$\text{logit}(\phi^J_{P,t}) = \alpha_1 + \alpha_2(n^A_{P,t} - \overset{*}{n}{}^A_P) + \sigma_{\phi^J_P}\epsilon_{\phi^J_P} \tag{18}$$

$$\text{logit}(\phi^J_{V,t}) = \alpha_3 + \alpha_4(n^A_{P,t} - \overset{*}{n}{}^A_P) + \sigma_{\phi^J_V}\epsilon_{\phi^J_V} \tag{19}$$

$$\text{logit}(\phi^A_{P,t}) = \alpha_{\phi^A_P} + \sigma_{\phi^A_P}\epsilon_{\phi^A_P} \tag{20}$$

$$\text{logit}(\phi^A_{V,t}) = \alpha_{\phi^A_V} + \sigma_{\phi^A_V}\epsilon_{\phi^A_P} \tag{21}$$

with $\boldsymbol{\epsilon} \sim \mathcal{N}(0,1)$ i.i.d. and

$$\log(f_{P,t}) \sim \mathcal{N}(\alpha_5 + \alpha_6(n^J_{V,t} - \overset{*}{n}{}^J_V), \sigma^2_{f_P}) \tag{22}$$

$$\log(f_{V,t}) \sim \mathcal{N}(\alpha_7 + \alpha_8(n^A_{V,t} - \overset{*}{n}{}^A_V), \sigma^2_{f_V}). \tag{23}$$

Although mathematically identical, we used a parameterisation of the form $\mu + \epsilon\sigma,\ \epsilon \sim \mathcal{N}(0,\sigma^2)$ (sometimes called non-centered) for survival estimates and a centered parameterisation ($\mathcal{N}(\mu,\sigma^2)$) for fecundity estimates as it was found to be optimal for the mixing of the MCMC chains. As we were primarily interested in the ability of multispecies IPMs to estimate species interactions when these were in fact absent, inter species density dependence parameter values for α_2 and α_4 were either set to zero for the simulations, or at the same value as in Barraquand & Gimenez (2019). Parameter values used to simulate data and their interpretation can be found in Table 1.

2.2.2 Initial values and monitoring setup

For all simulation scenarios we used the initial population size vector

$$\begin{pmatrix} n^J_{V,1} \\ n^A_{V,1} \\ n^J_{P,1} \\ n^A_{P,1} \end{pmatrix} = \begin{pmatrix} 100 \\ 100 \\ 20 \\ 20 \end{pmatrix}$$

and the yearly number of monitored prey and predator broods/litters respectively $R^V_t = 50$ and $R^P_t = 20$. For consistency with Barraquand & Gimenez (2019), all scenarios were crossed with two alternative population monitoring duration and number of marked juveniles: either 100 juveniles

Table 1: Model parameters with their values. Values of α_4 and α_6 in the scenarios with true presence of species interactions are presented in brackets. Temporal standard deviations (SD) are only present in the scenarios with random temporal variation. For interpretation, note that α_i and temporal SD parameters are within exponential functions. For instance, $\alpha_5 = 0.404$ corresponds to a mean fecundity of $e^{0.404} \approx 1.5$.

Parameter	Value	Interpretation
α_1	0.29	juvenile predator survival – intercept
α_2	-0.01	juvenile predator survival – slope
α_3	-0.025	juvenile prey survival – intercept
α_4	**0** (-0.025)	juvenile prey survival – slope – inter species density dependence
α_5	0.404	predator fecundity – intercept
α_6	**0** (0.004)	predator fecundity – slope – inter species density dependence
α_7	1.24	prey fecundity – intercept
α_8	-0.005	prey fecundity – slope
p	0.7	recapture probability
$\alpha_{\phi_P^A}$	logit(0.7)	adult predator survival – intercept
$\alpha_{\phi_V^A}$	logit(0.6)	adult prey survival – intercept
σ^2_{obs}	0.1	observation error
σ_{f_P}	0.1	temporal SD of predator fecundity
σ_{f_V}	0.1	temporal SD of prey fecundity
$\sigma_{\phi_P^J}$	0.1	temporal SD of juvenile predator survival
$\sigma_{\phi_P^A}$	0.1	temporal SD deviation of adult predator survival
$\sigma_{\phi_V^J}$	0.1	temporal SD deviation of juvenile prey survival
$\sigma_{\phi_V^A}$	0.1	temporal SD deviation of adult prey survival

are marked each year for $T = 10$ years, or 20 juveniles are marked each year for $T = 30$ years, for both species. However, due to the inclusion of non-negligible observation error in the counts, our model faces convergence/practical identifiability issues for 29–56% of simulated data-sets at these sample sizes (Figures S5 to S8). Therefore, we focus mostly in the present work on a new scenario for which 100 juveniles are marked each year (we assume only juveniles are marked) for 30 years. Results using the previous monitoring setups (and the non centered density-dependencies) are presented in the Supplementary Information B.

We consider two alternative situations without interspecific interactions, i.e., with or without random temporal noise. To compare model performances in the no-interactions setting to cases with interspecific interactions, we also simulated and fitted data in presence of species interactions using the same α_i values as Barraquand & Gimenez (2019) under the four above-mentioned scenarios (i.e., with/without interactions $\times$ with/without stochasticity on interactions; see Supplementary Table 2 and Figures S1 and S3). For each of these four combinations of parameter sets, we simulated 100 datasets using the Nimble package (de Valpine *et al.*, 2017, 2022, version 0.12.2) in R (R Core Team, 2022, version 4.2.1).

2.3 Priors specification and model fitting

Multispecies IPMs were implemented in a Bayesian framework, hence the need to specify priors. When fitting the models to simulated data, we used $\mathcal{N}(100, 10)$ and $\mathcal{N}(20, 10)$ priors for the initial stage-specific prey and predator population sizes (truncated to be positive). These priors also differed from Barraquand & Gimenez (2019) where they were all set to $\mathcal{N}(25, 10^{-5})$.

Priors for standard deviations were chosen as $\sigma \sim \text{Exp}(1)$, which corresponds to priors with maximum entropy on the log and logit scales (e.g., McElreath, 2020). Prior probabilities of recapture were drawn as $p \sim \text{Unif}(0, 1)$ and vital rate/interaction parameters were given weakly informative priors $\alpha_k \sim \mathcal{N}(0, 1)$ $(k \in 1, ..., 8)$.

Data were both simulated and fitted using the Nimble R package (R Core Team, 2022; de Valpine *et al.*, 2017, 2022, version 0.12.2). To improve their mixing and minimize their posterior correlations, intercepts, slopes and temporal SD were block sampled using automated factor slice samplers (Tibbits *et al.*, 2014; Ponisio *et al.*, 2020). For each simulated dataset, we fitted the same multispecies IPM that was used to generate the data (e.g., no random temporal noise estimated on data without temporal noise), except in that species interactions were estimated even in absence of such interactions. Two MCMC chains were run for 40000 iterations and we sampled the last 20000

iterations every 20^{th} iteration leading to 2000 posterior samples saved per dataset. Real parameter values were used as initial values to minimise time to convergence (see Appendix Section C for an evaluation of the influence of initial values on parameter estimation). We assess convergence and mixing of the chains for all α_i by calculating the potential scale reduction factor ($\hat{R}$, Brooks & Gelman 1998; Gelman & Rubin 1992) and effective sample size ($n_{eff.}$)using the "gelman.diag()" and the "effectiveSize()" functions of the *coda* package (Plummer *et al.*, 2006, version 0.19-4). We only used outputs from models for which all α_i had $\hat{R} < 1.1$ and $n_{eff.} > 50$, that is, 96/100 models for the scenario without random temporal variation and 73/100 models for the scenario with random temporal variation. The computer code is provided at `https://github.com/MatthieuPaquet/multi_species`.

3 Results

Overall, the estimation of density dependence curves did not show any sign of bias for interspecific density dependence (either absent, Figures 1 and 3 or present, Figures S1 and S3) and intraspecific density dependence. This was true without and with temporal stochasticity (Figures 1 to 4).

This absence of bias extends to the alternative data designs with smaller sample sizes considered in Barraquand & Gimenez (2019) (shown in Supplementary Information in Figures S5 to S8). Estimated α_i parameters also did not show sign of bias in any scenario (Tables S1 and 2).

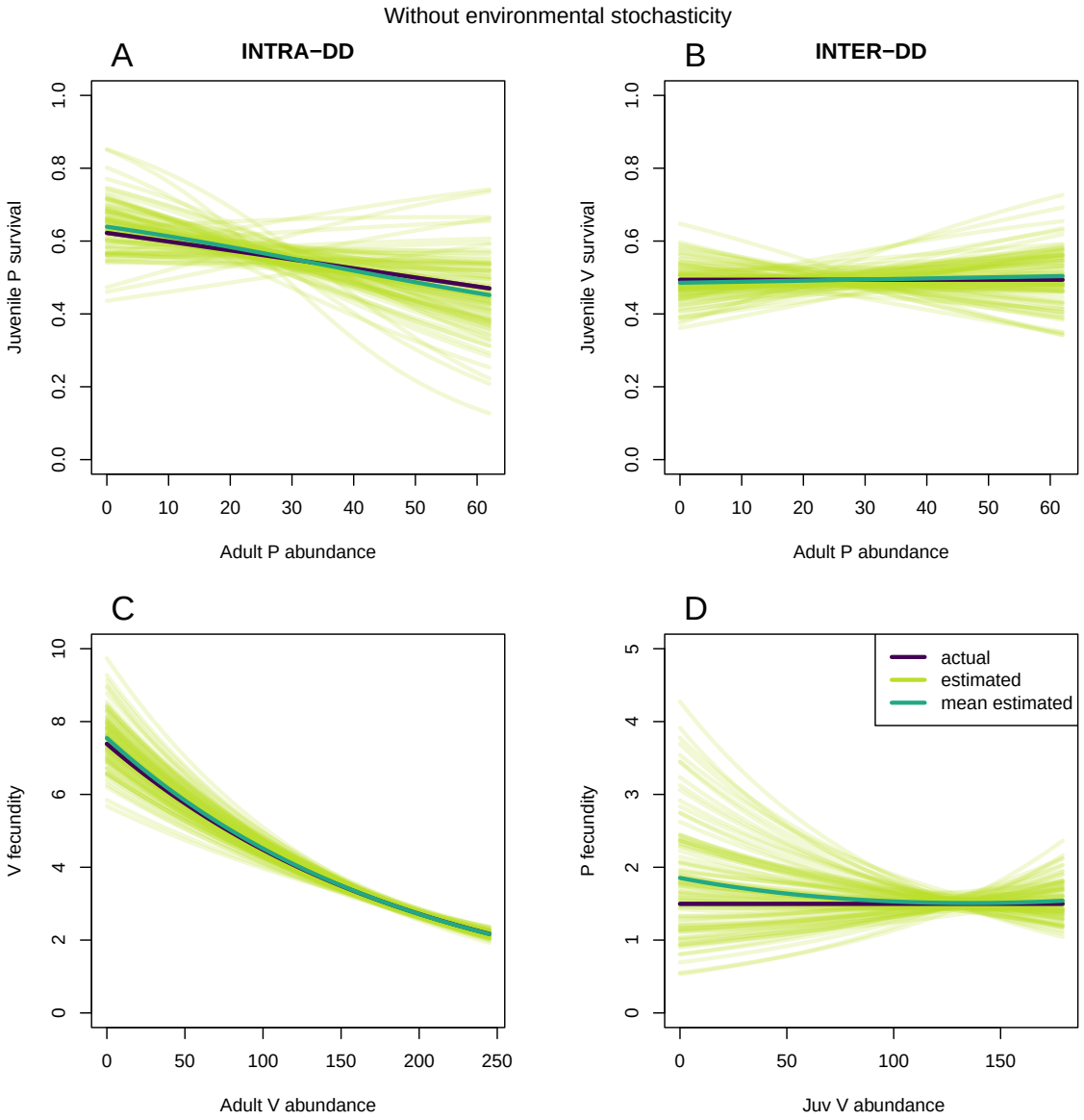

Figure 1: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario without random time variation. Purple: simulated relationships, light green: posterior mean relationships for the 96 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships. True inter species density-dependencies (right panels) were set to be absent.

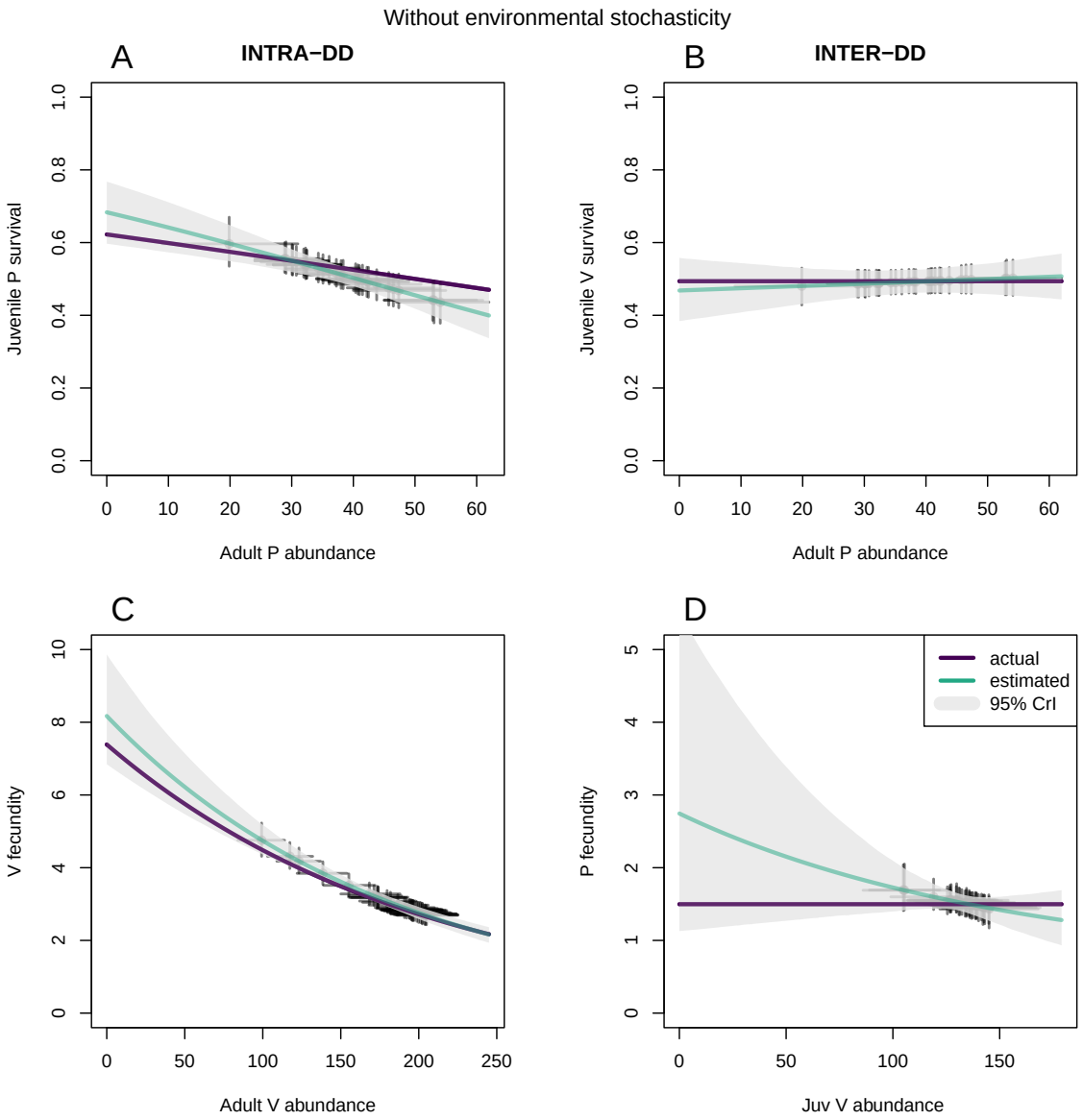

Figure 2: Example of posterior mean (blue-green line) and 95% Credible Intervals (grey polygons) of density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities estimated by one of the 100 models run in the scenario without random time variation. Purple lines indicate the simulated (true) relationships. Points represent estimated mean demographic parameter each year plotted against estimated yearly abundance values and vertical and horizontal error bars their respective 95% Credible Intervals.

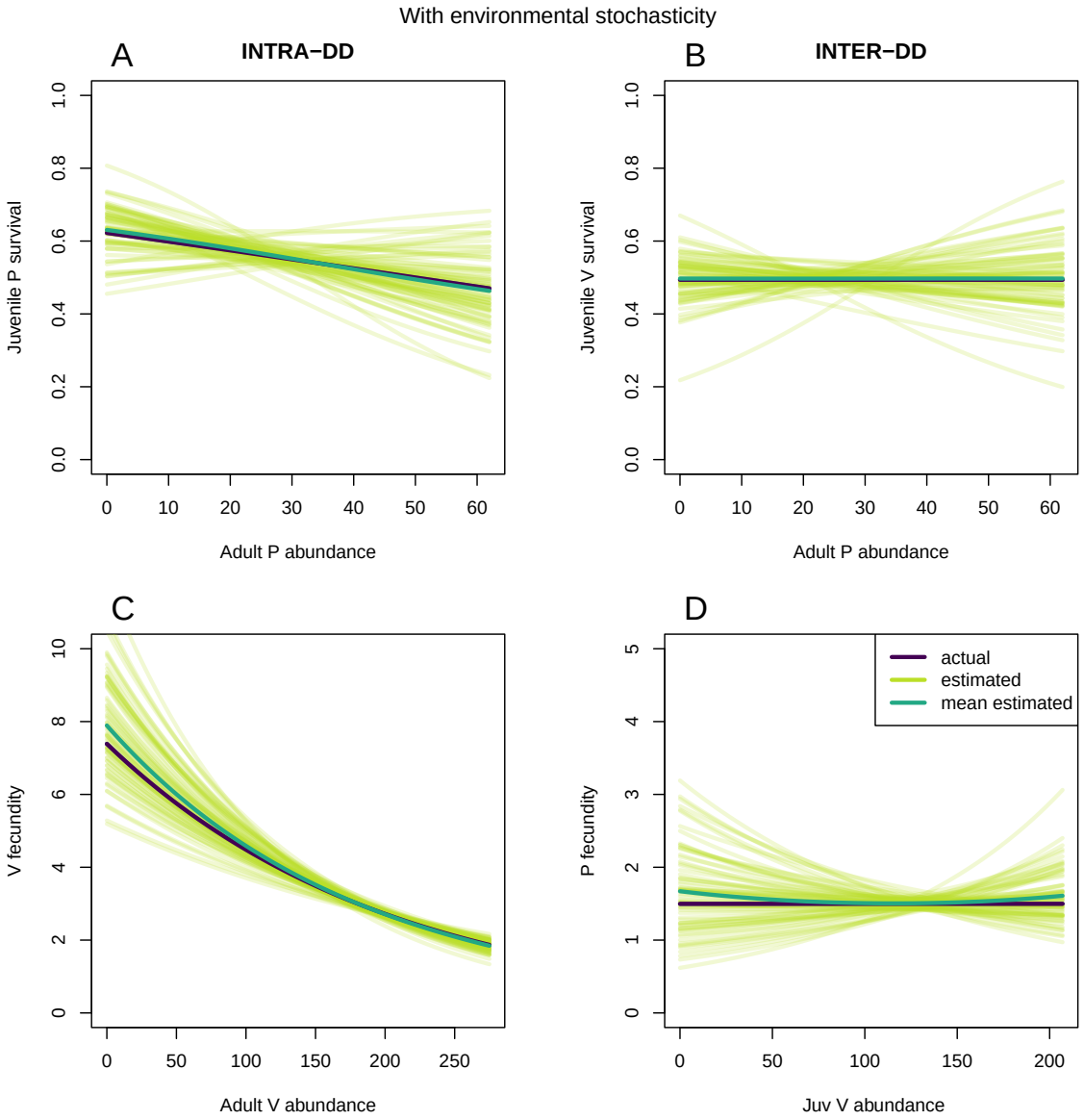

Figure 3: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with random time variation. Purple: simulated relationships, light green: posterior mean relationships for the 73 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships. True inter species density-dependencies (right panels) were set to be absent.

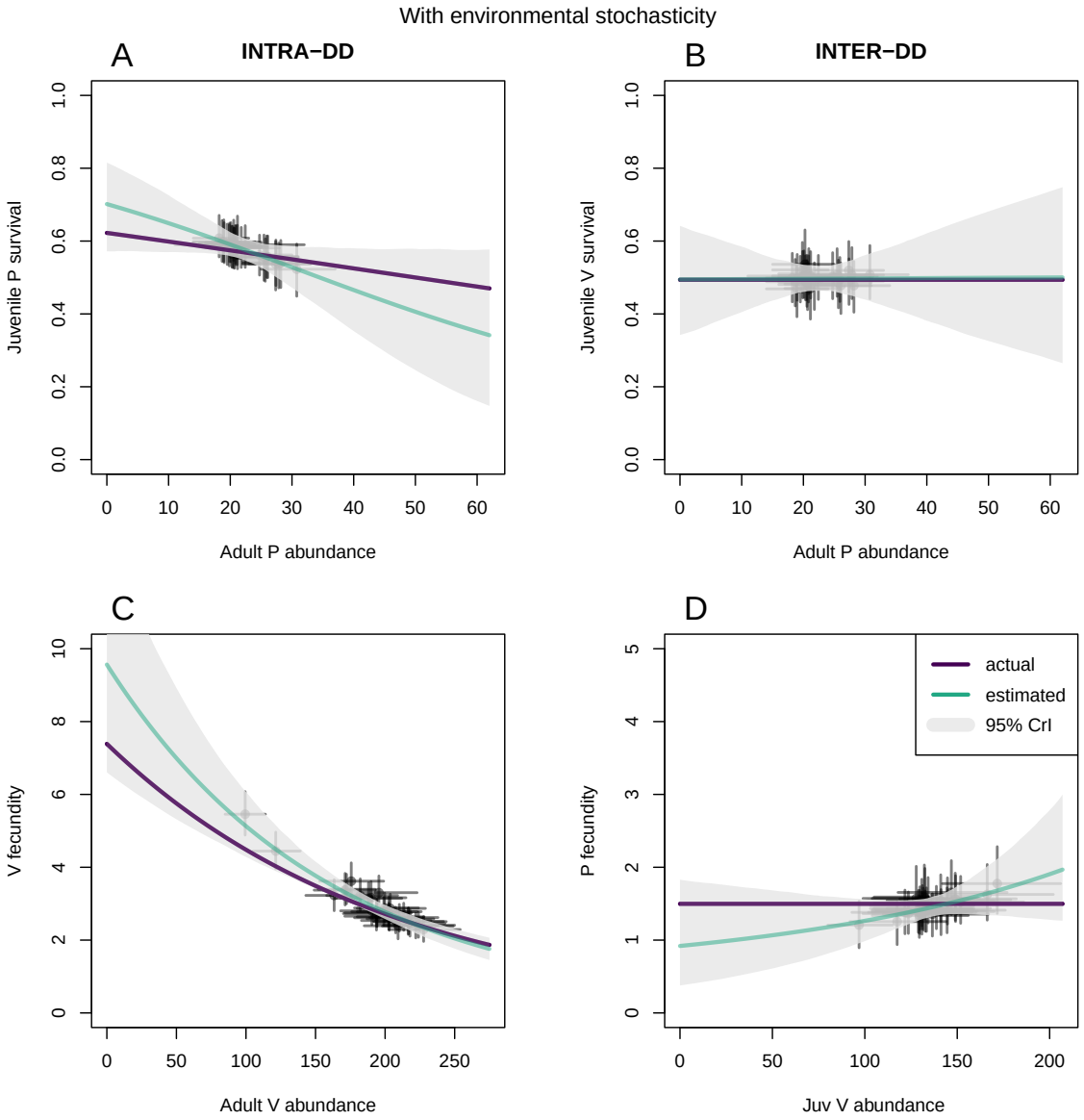

Figure 4: Example of posterior mean (blue-green line) and 95% Credible Intervals (grey polygons) of density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities estimated by one of the 100 models run in the scenario with random time variation. Purple lines indicate the simulated (true) relationships. Points represent estimated mean demographic parameter each year plotted against estimated yearly abundance values and vertical and horizontal error bars their respective 95% Credible Intervals.

We did not detect more false positive species interactions than expected by chance when investigating the coverage probability of the species interaction parameters at 95% (i.e., the proportion of simulations where 95% CrI of estimated parameter includes the true parameter value). In the scenario with 100 juveniles marked each year for 30 years and no interspecific density dependence nor temporal random variation, this probability was 0.96 for α_4 and 0.94 for α_6 (cf Table 2, see Figure 2 for an example of estimated mean and pointwise 95% CrI density dependent curves).

Coverage probabilities were also satisfactory when interspecific interactions were simulated to be nonzero (0.96 and 0.98). Species interactions parameters were still estimable with no noticeable bias in the presence of random time variation (Figures 3 and 4), in which case the coverage probabilities of the species interaction parameters α_4 and α_6 at 95% were both 0.96 in absence of interspecific interactions (Table 2). In the presence of interspecific interactions, coverage values were similar. Moreover, the addition of random time variation did not noticeably alter the precision of the species interaction parameters, both in absence and presence of species interactions (Figure S3, Table 2).

Table 2: Summary table of parameter estimates. Value refers to the true values used to simulate the data and values of the interspecific density dependent parameters are highlighted in bold. Estimate (95% quantiles) are the mean and the 95% quantiles of the posterior mean estimates. Coverage 95% is the proportion of 95% Credible Intervals that included the true parameter values.

Scenario	Param.	Value	Estimate (95% quantiles)	Coverage 95%
30 years	α_1	0.29	0.327 (0.139; 0.585)	0.89
100 ind. marked/year	α_2	-0.01	-0.013 (-0.041; 0.012)	0.89
No temporal noise	α_3	-0.025	-0.033 (-0.197; 0.141)	0.97
No interspecies DD	α_4	**0**	0.001 (-0.015; 0.016)	0.96
	α_5	0.404	0.414 (0.217; 0.601)	0.95
	α_6	**0**	-0.000 (-0.006; 0.006)	0.94
	α_7	1.24	1.242 (1.194; 1.292)	0.96
	α_8	-0.005	-0.005 (-0.006; -0.004)	0.95
30 years	α_1	0.29	0.314 (0.110; 0.527)	0.95
100 ind. marked/year	α_2	-0.01	-0.012 (-0.031; 0.011)	0.96
Temporal noise	α_3	-0.025	-0.013 (-0.209; 0.172)	0.93
No interspecies DD	α_4	**0**	0.000 (-0.018; 0.022)	0.96
	α_5	0.404	0.401 (0.223; 0.561)	0.93
	α_6	**0**	0.000 (-0.004; 0.006)	0.96
	α_7	1.24	1.246 (1.160; 1.316)	0.92
	α_8	-0.005	-0.005 (-0.007; -0.004)	0.96
30 years	α_1	0.29	0.325 (0.179; 0.552)	0.94
100 ind. marked/year	α_2	-0.01	-0.012 (-0.033; 0.002)	0.96
No temporal noise	α_3	-0.025	-0.009 (-0.175; 0.180)	0.95
Interspecies DD	α_4	**-0.025**	-0.026 (-0.043; -0.010)	0.96
	α_5	0.404	0.403 (0.285; 0.556)	0.95
	α_6	**0.004**	0.004 (-0.002; 0.008)	0.98
	α_7	1.24	1.243 (1.191; 1.296)	0.90
	α_8	-0.005	-0.005 (-0.007; -0.004)	0.92
30 years	α_1	0.29	0.334 (0.149; 0.536)	0.97
100 ind. marked/year	α_2	-0.01	-0.015 (-0.029; 0.005)	0.96
Temporal noise	α_3	-0.025	-0.017 (-0.218; 0.174)	0.95
Interspecies DD	α_4	**-0.025**	-0.025 (-0.044; -0.009)	1
	α_5	0.404	0.404 (0.282; 0.537)	0.92
	α_6	**0.004**	0.004 (-0.001; 0.008)	0.96
	α_7	1.24	1.234 (1.164; 1.311)	0.91
	α_8	-0.005	-0.005 (-0.007; -0.003)	0.88

4 Discussion

Building on the multispecies integrated predator-prey model of Barraquand & Gimenez (2019), we investigated here whether multispecies IPMs could output interactions where there are in fact none. We did so by modelling functions relating vital rates to stage-specific species densities, whose slope parameters are used to model species interactions. We found that when those slopes were simulated as zero, the estimates were centered on zero and therefore unbiased. There was also a good coverage probability of interaction parameters (close to 0.95 for 95% CrIs). We also found that adding noise to these multispecies density-dependent link functions did not alter these results (although parameter estimation was less often possible in this case, see discussion below). This confirms that multispecies IPMs are a promising way to estimate species interactions, and in particular, that they could be used to infer whether two species interact or not when such information is missing.

An important additional outcome of our study pertains to the sample size needed to be able to estimate intra and interspecific interactions, which is likely higher than previously anticipated. By adding observation error on count data ($\sigma^2_{obs} = 0.1$ on the log scale) to allow for identifiability of stage-specific abundances, we had to increase the sample size of the capture-mark-recapture dataset used in Barraquand & Gimenez (2019) up to 100 prey individuals and 100 predator individuals newly marked every years for 30 years, in order to reach practical identifiability of the density dependence parameters and satisfactory convergence of the MCMC chains for a large majority of the datasets (i.e., 98/100). Estimation was still unbiased with the data designs considered in Barraquand & Gimenez (2019) but failing for a number of datasets. When adding unexplained environmental stochasticity (i.e., random time variation on the link functions), the proportion of converging MCMC chains went down to 73/100 datasets, which means that density dependence parameters could be satisfactorily estimated for about three quarters of the datasets. These proportions were highly similar when interspecific interactions were present (i.e., 97/100 and 74/100 respectively). This raises the question of how common such large datasets are for (suspected) predator-prey population pairs. That being said, parameter estimation was still possible with smaller sample sizes in many cases (i.e., 44/100 datasets in the worse case studied, Figure S8), and the only predator-prey IPM using real data so far used 22 years of capture recapture histories for 318 predators and 1210 prey individuals (i.e., c.a. 14 and 55 individuals per year respectively).

In field population studies, additional types of data available are likely to improve estimation of species interactions and we give three examples below. First, when age classes can be determined

during the count observation process, including such information explicitly in the model (see e.g., Weegman *et al.*, 2016; Paquet *et al.*, 2019) will increase identifiability and/or precision of survival parameters and age specific abundances, and therefore will likely improve the estimation of density dependence parameters as well. This stage-specific abundance information may also allow, in some cases where counts are provided with little error, to remove the observation process, which we cannot do in our current model formulation because the observed population size sums adult and juvenile densities, and this sum has to arise from a probability distribution (Equations (2) and (3)). Second, integrating dead recovery data of prey is likely to give extra information on the strength of predator-prey interactions. Dead recoveries are classically implemented in capture-mark-recovery models (Seber, 1972; North & Morgan, 1979) which in some cases can be combined with CMR data (Barker, 1999) and counts (Reynolds *et al.*, 2009). Since the probability to find a dead prey is likely affected by predation rates in the population (e.g., in some systems prey eaten will not be recovered, in others dead recoveries may present signs of predation), taking the predation process into account in the dead recoveries data-generation mechanism could improve the estimation of the strength of predator-prey interactions. Finally, the spatial structure of the data should contain additional information that may help to estimate parameters. The extension to spatially explicit IPMs (Chandler & Clark, 2014; Zhao, 2020) for interacting populations represents a promising way forward for the estimation of species interactions.

Although our results are encouraging, the efficiency of multispecies IPMs in estimating species interactions may also depend on the parameter set, and thus on the ecological features of the populations studied. For example, the parameters considered here correspond well to vertebrate predator-prey systems with a stable equilibrium in absence of environmental perturbations. Faster life histories, different stage or age structure, and multiple factors contributing to altering the quantity of information encapsulated in the various data streams may alter the sample sizes required for efficient inferences. When applying these models to new systems with different life history parameters and density-dependent structures, simulated datasets with plausible ecological features for the empirical system considered (and similar data designs), will help confirm that parameter values can be recovered without bias and with sufficient precision. Tools such as JAGS (Plummer *et al.*, 2003) or Nimble (de Valpine *et al.*, 2017) make it particularly handy to both simulate and fit data with complex dynamic models.

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Supplementary Information

A Results from the scenarios in presence of species interactions

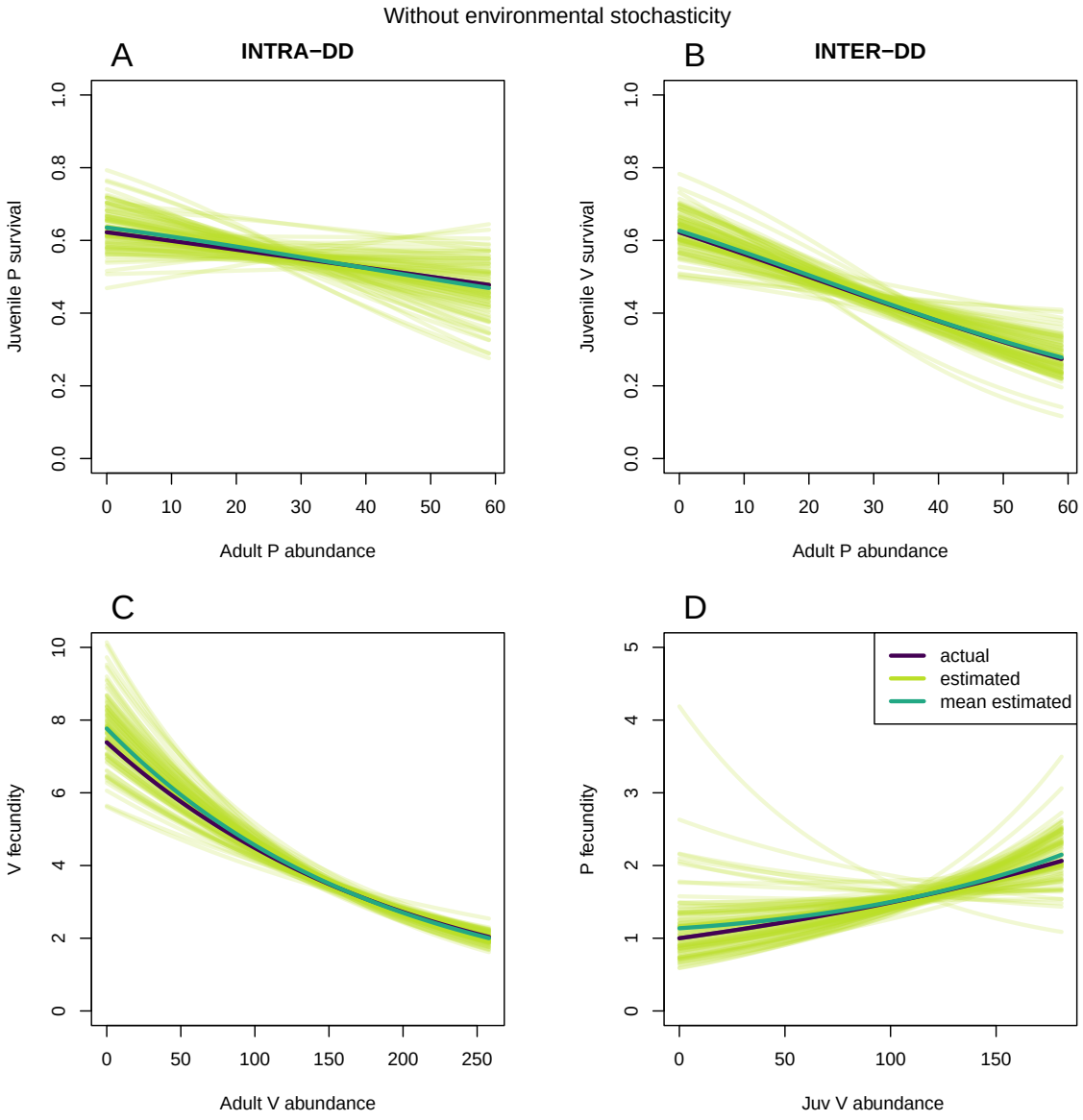

Figure S1: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario without random time variation in presence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 97 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

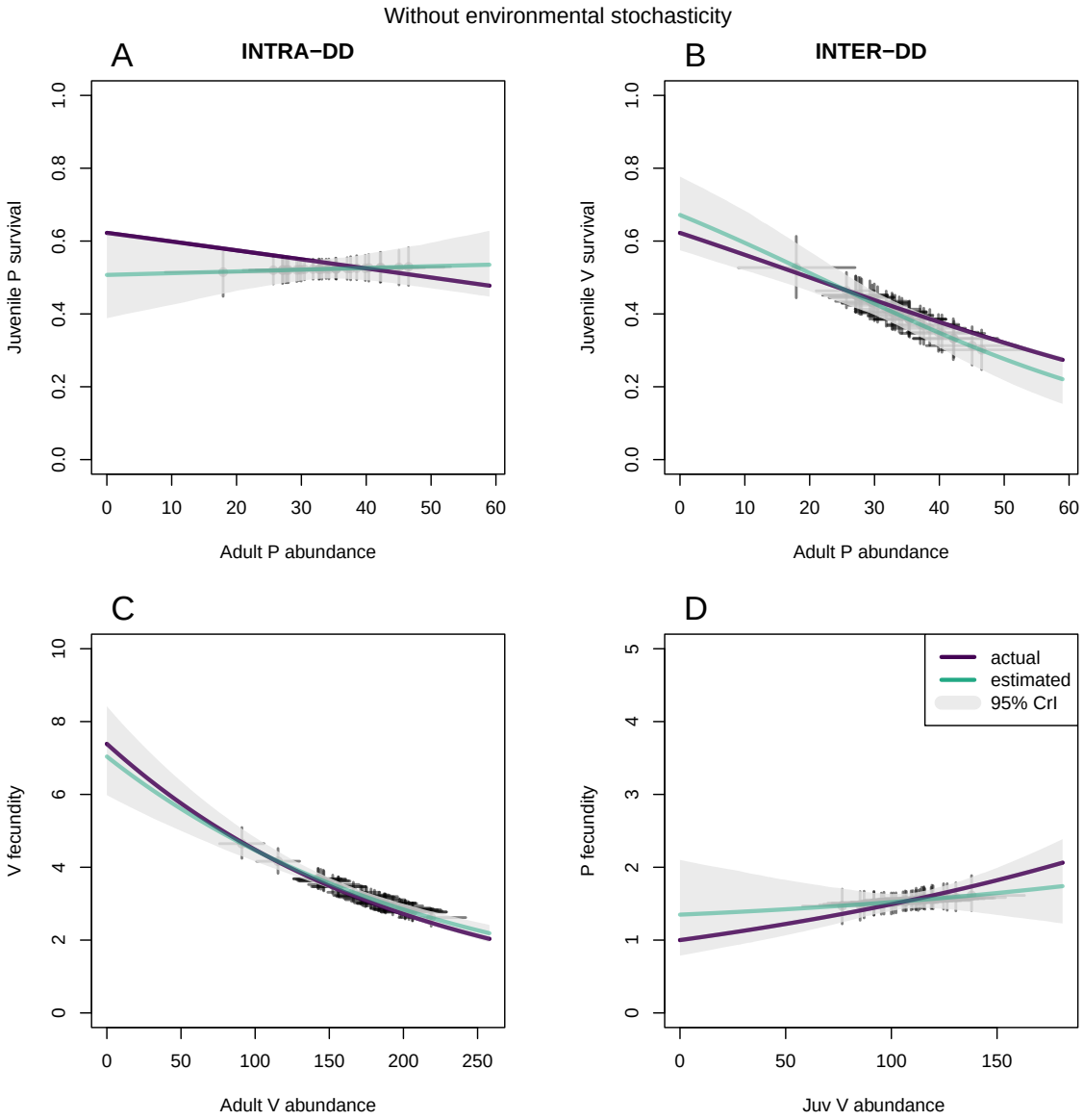

Figure S2: Example of posterior mean (blue-green line) and 95% Credible Intervals (grey polygons) of density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities estimated by one of the 100 models run in the scenario without random time variation in presence of true inter species density-dependencies. Purple lines indicate the simulated (true) relationships. Points represent estimated mean demographic parameter each year plotted against estimated yearly abundance values and vertical and horizontal error bars their respective 95% Credible Intervals.

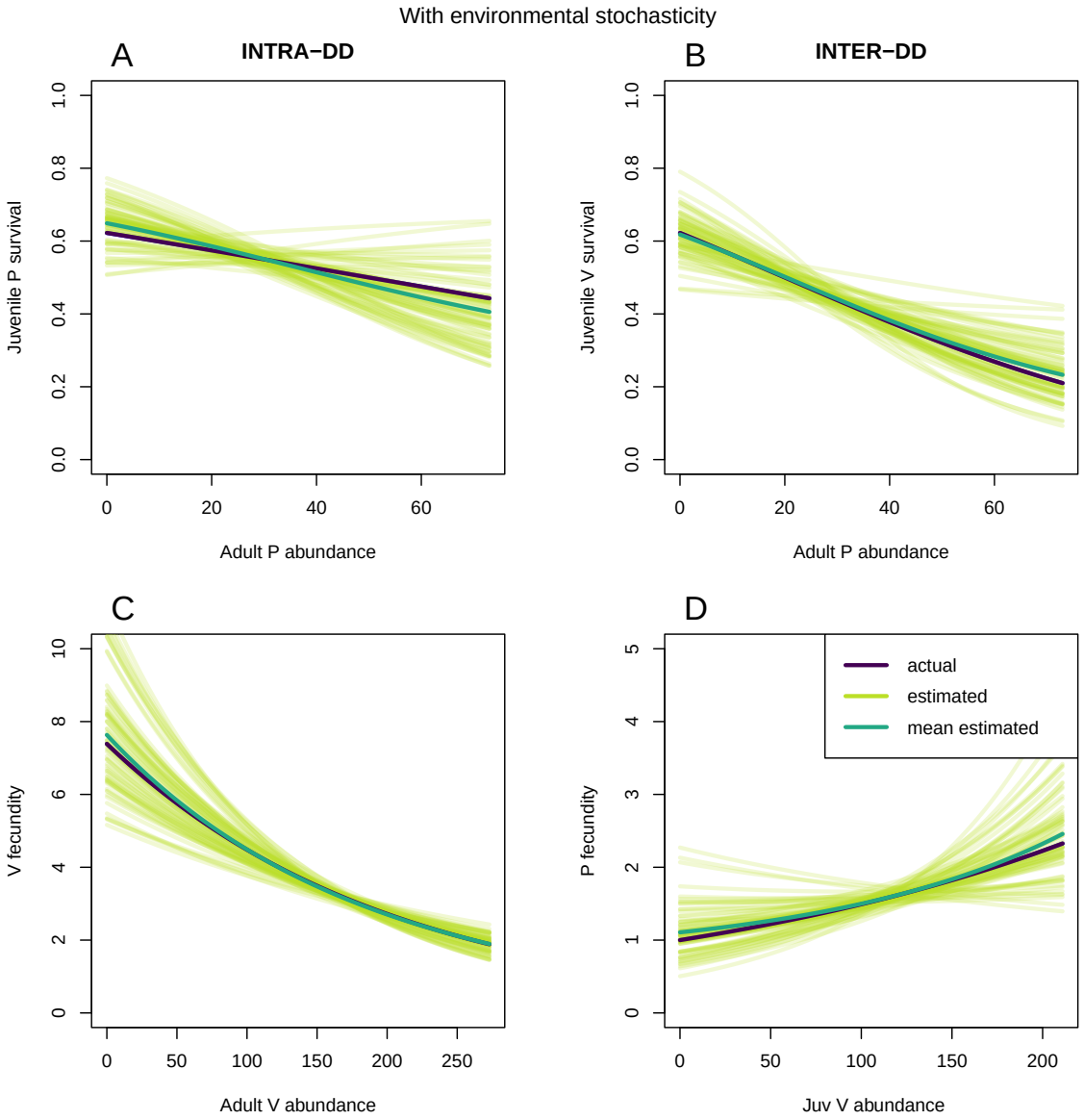

Figure S3: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with random time variation in presence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 74 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

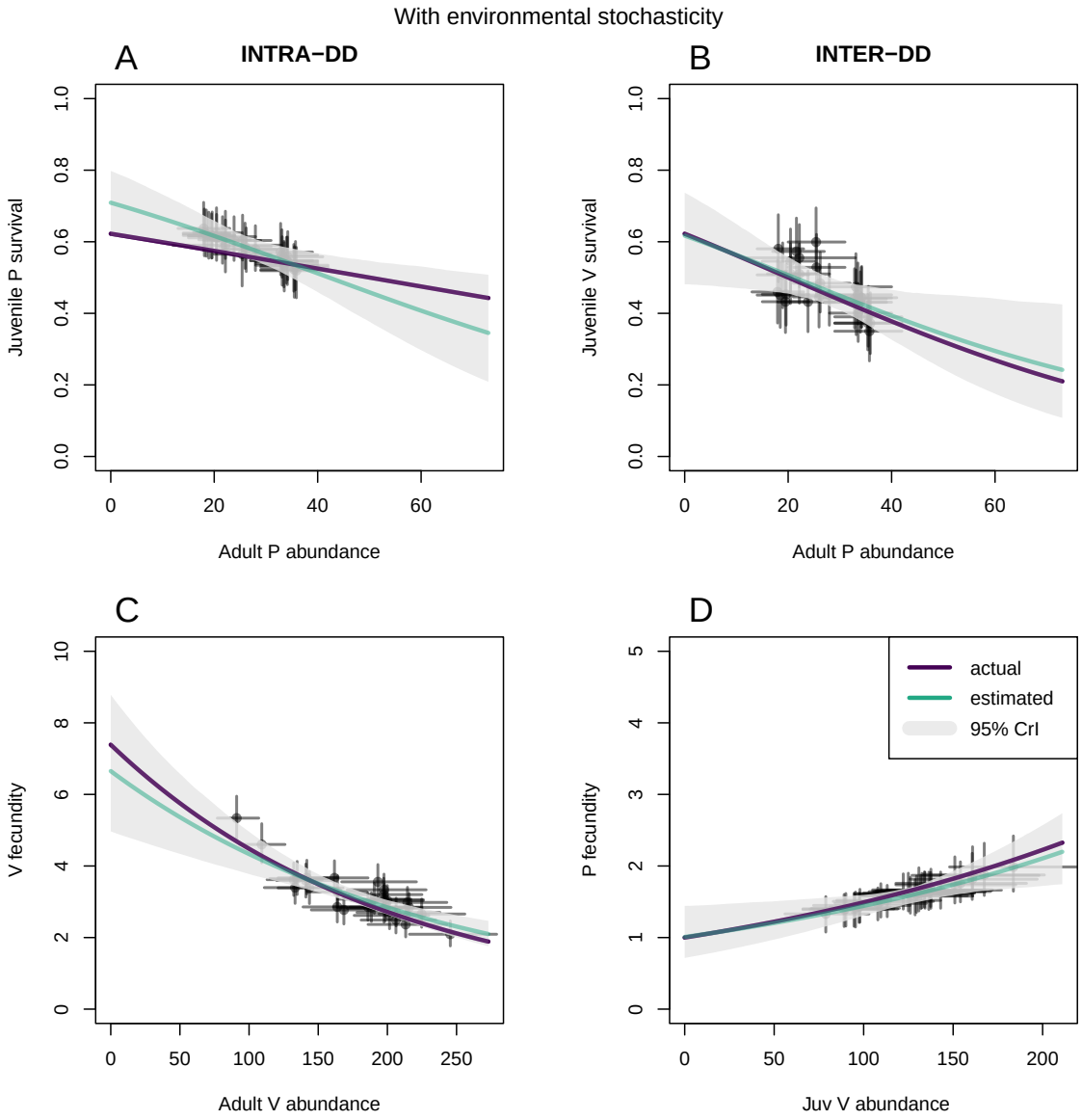

Figure S4: Example of posterior mean (blue-green line) and 95% Credible Intervals (grey polygons) of density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities estimated by one of the 100 models run in the scenario with random time variation in presence of true inter species density-dependencies. Purple lines indicate the simulated (true) relationships. Points represent estimated mean demographic parameter each year plotted against estimated yearly abundance values and vertical and horizontal error bars their respective 95% Credible Intervals.

B Results from the scenarios with 100 juveniles of each species marked each year for 10 years, and 20 juveniles of each species marked for 30 years, without centering abundances in the link functions

Table S1: Value refers to the true values used to simulate the data and values of the interspecific density dependent parameters are highlighted in bold. Estimate (95% quantiles) are the mean and the 95% quantiles of the posterior mean estimates. Coverage 95% is the proportion of 95% Credible Intervals that included the true parameter values.

Scenario	Param.	Value	Estimate (95% quantiles)	Coverage 95%
10 years	α_1	0.50	0.506 (-0.136; 1.422)	0.97
100 ind. marked/year	α_2	-0.01	-0.003 (-0.051; 0.018)	0.97
No temporal noise	α_3	-0.025	0.043 (-0.608; 0.684)	0.98
	α_4	0	-0.003 (-0.029; 0.023)	0.98
	α_5	0.404	0.304 (-0.491; 1.029)	0.95
	α_6	0	0.001 (-0.004; 0.007)	0.93
	α_7	2	1.995 (1.793; 2.204)	0.98
	α_8	-0.005	-0.005 (-0.007; -0.004)	0.98
10 years	α_1	0.5	0.287 (-0.178; 0.856)	1
100 ind. marked/year	α_2	-0.01	0.039 (-0.020; 0.488)	0.98
Temporal noise	α_3	-0.025	0.014 (-0.477; 0.615)	1
	α_4	0	-0.001 (-0.027; 0.020)	1
	α_5	0.404	0.330 (-0.208; 0.863)	1
	α_6	0	0.001 (-0.004; 0.005)	1
	α_7	2	1.958 (1.549; 2.293)	0.91
	α_8	-0.005	-0.005 (-0.007; -0.003)	0.93
30 years	α_1	0.5	0.636 (0.051; 1.366)	0.94
20 ind. marked/year	α_2	-0.01	-0.002 (-0.047; 0.032)	0.97
No temporal noise	α_3	-0.025	0.038 (-0.524; 0.483)	1
	α_4	0	-0.001 (-0.021; 0.018)	0.99
	α_5	0.404	0.312 (-0.502; 1.010)	0.92
	α_6	0	0.001 (-0.004; 0.007)	0.96
	α_7	2	2.00 (1.011; 2.194)	0.94
	α_8	-0.005	-0.005 (-0.006; -0.004)	96
30 years	α_1	0.5	0.577 (-0.008; 1.161)	0.98
20 ind. marked/year	α_2	-0.01	-0.015 (-0.043; 0.014)	1
Temporal noise	α_3	-0.025	-0.005 (-0.520; 0.363)	0.98
	α_4	0	-0.000 (-0.013; 0.016)	1
	α_5	0.404	0.336 (-0.466; 0.770)	0.98
	α_6	0	0.000 (-0.003; 0.006)	0.98
	α_7	2	1.975 (1.704; 2.264)	0.95
	α_8	-0.005	-0.005 (-0.007; -0.003)	0.95

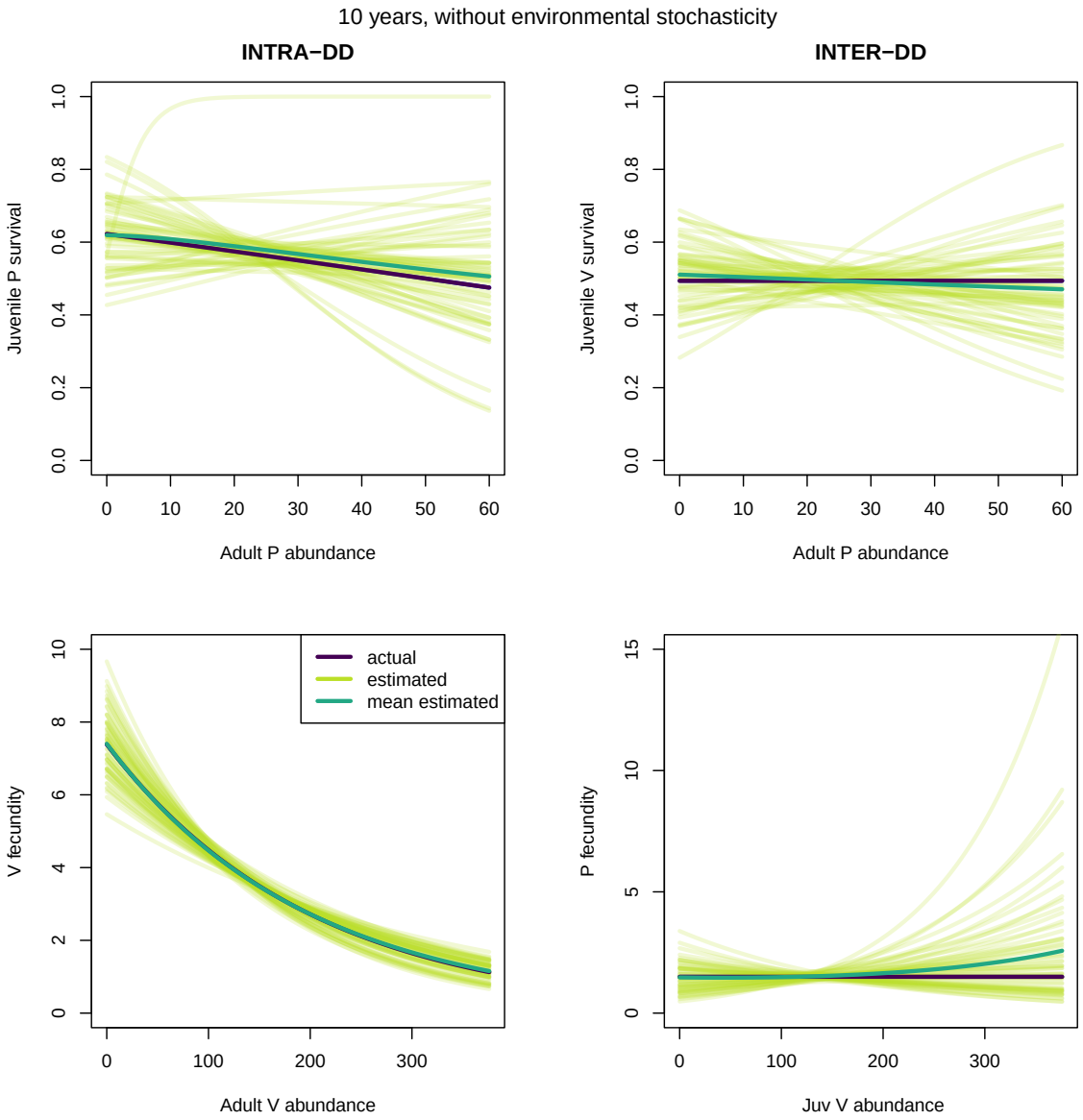

Figure S5: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with 100 juveniles per species marked each year for 10 years without random time variation in absence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 59 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

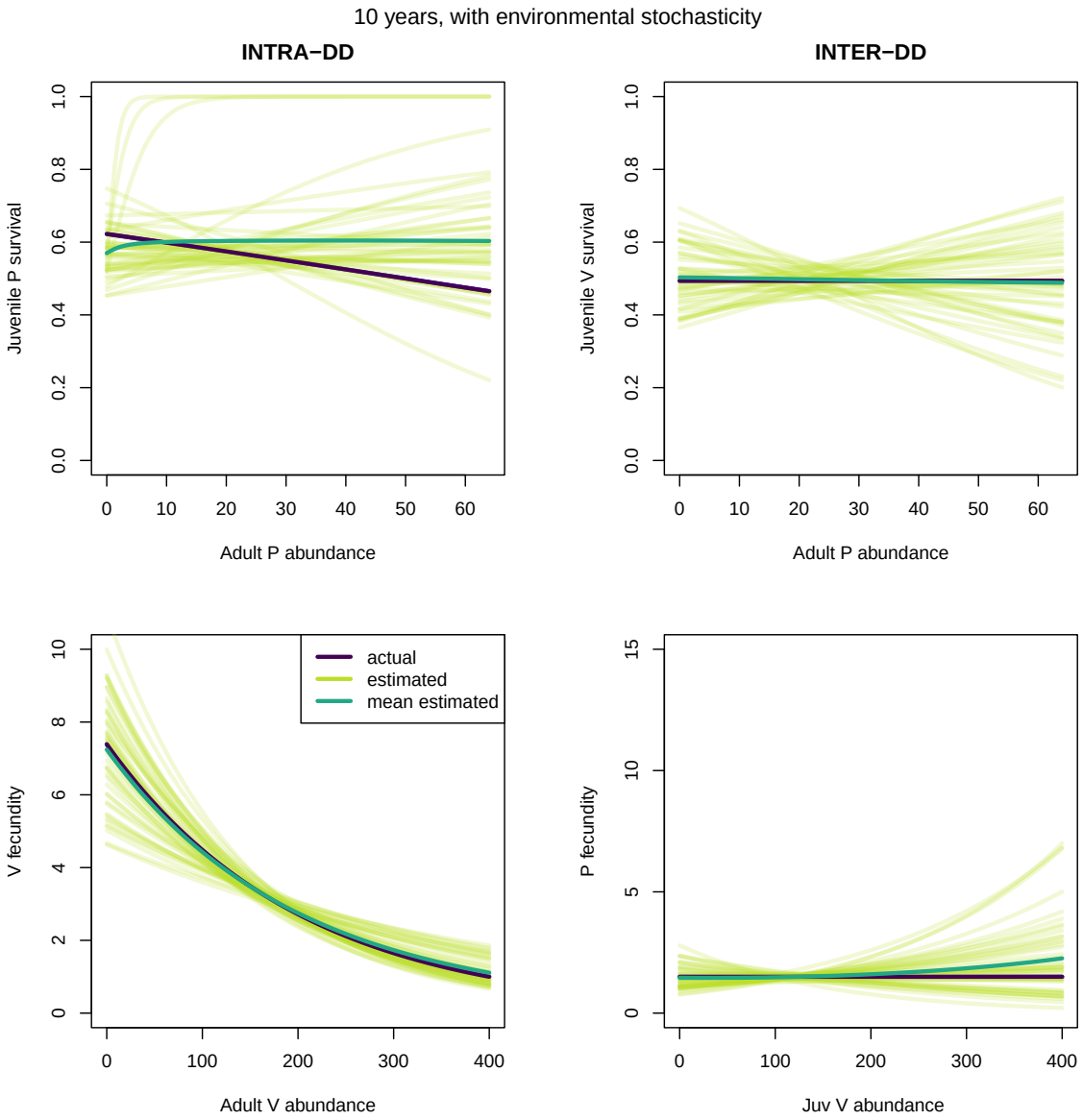

Figure S6: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with 100 juveniles per species marked each year for 10 years with random time variation in absence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 46 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

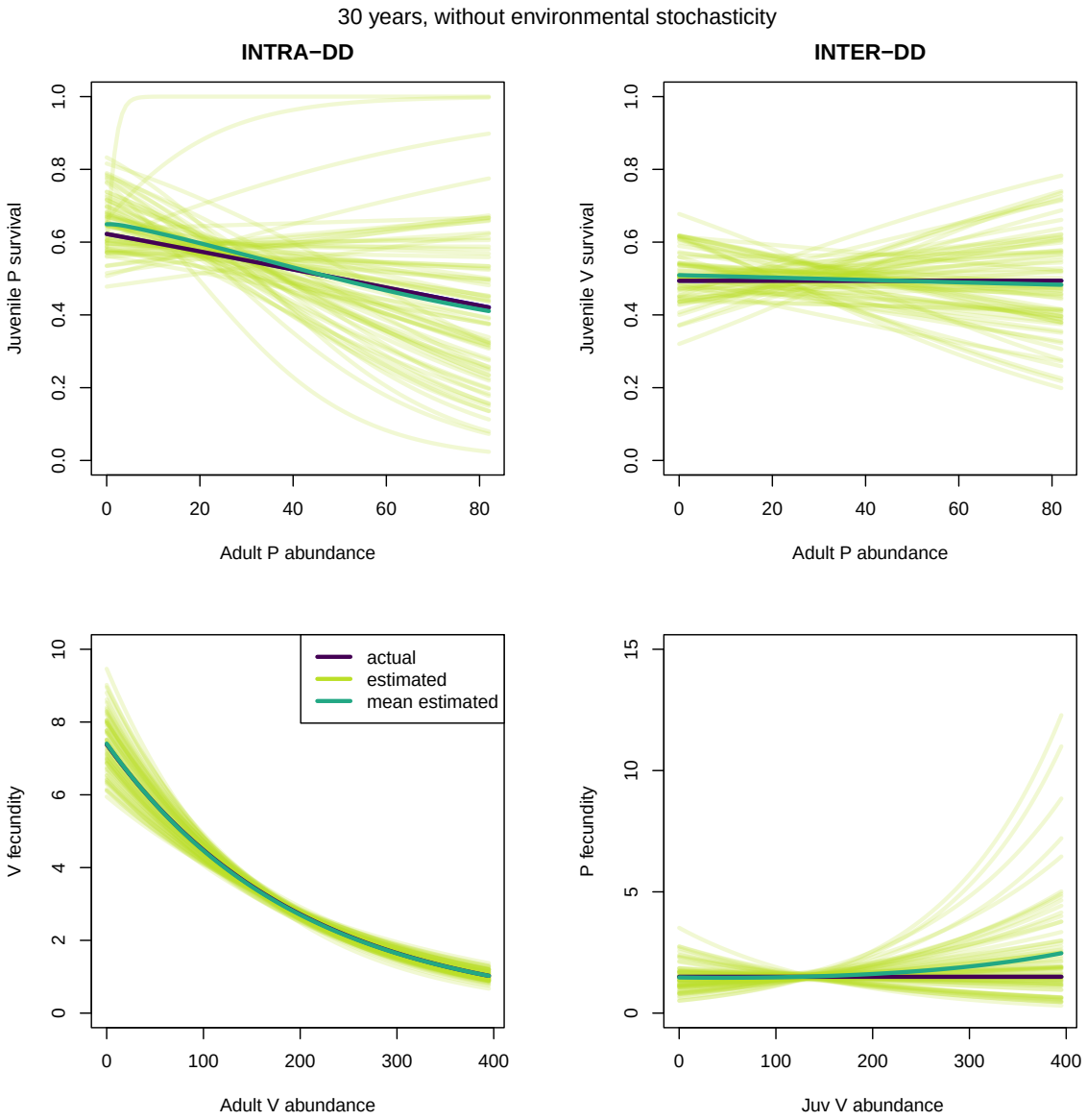

Figure S7: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with 20 juveniles per species marked each year for 30 years without random time variation in absence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 71 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

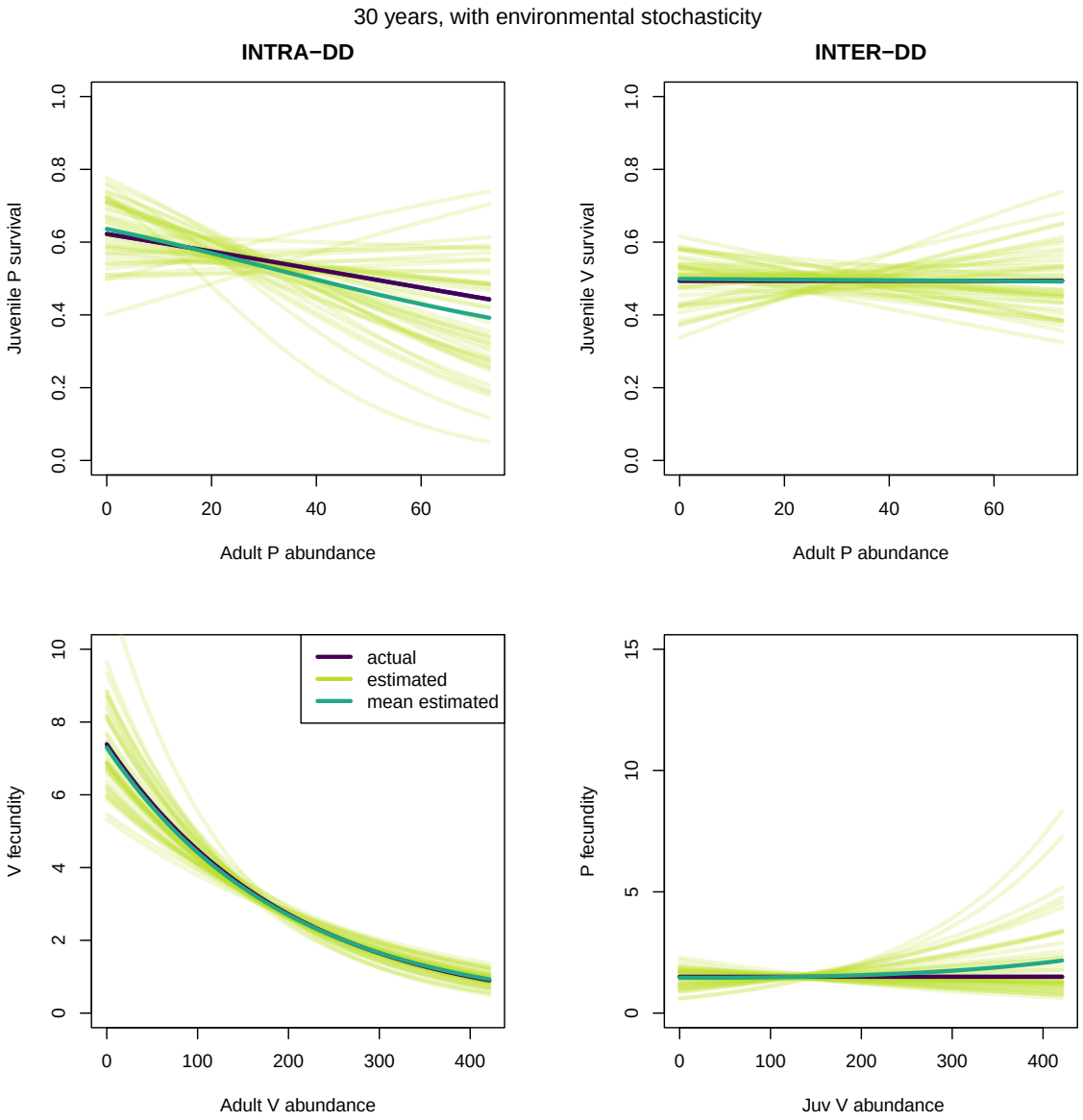

Figure S8: Density-dependencies for juvenile survival rates (**A** for predator and **B** for prey) as well as prey (**C**) and predator (**D**) fecundities in the scenario with 20 juveniles per species marked each year for 30 years with random time variation in absence of true inter species density-dependencies. Purple: simulated relationships, light green: posterior mean relationships for the 44 fitted models that appear to converge satisfactorily, dark green: average of the posterior mean relationships.

C Sensitivity of parameter estimation to the choice of initial values

To assess whether the accuracy of the estimation of density dependent parameters was conditioned by the fact that we used true parameter values as initial values, we also ran the MCMC using values that substantially deviated from the true value and expected posterior distributions. For this study, we used data (and the corresponding model) without temporal random noise and without true interspecific interactions. We chose one simulated dataset for which the true values of α_2, α_4, α_6 and α_8 fell well within the 95% credible intervals of the posterior samples when using the true value as initial value (see script https://github.com/MatthieuPaquet/multi_species/blob/main/script_initial_values.R for more details on the procedure). We then simulated 100 sets of initial values that deviated from the true values by 4 standard deviations estimated from the posterior samples when the true values were used as initial values (hereafter $SD_{\hat{\alpha_i}}$). For the parameters for which negative density dependence was expected, we simulated the 100 initial values as $\alpha_i^{init} \sim \mathcal{N}(\alpha_i - 4SD_{\hat{\alpha_i}}, SD_{\hat{\alpha_i}})$ whereas for α_8, which was a potentially positive prey $\rightarrow$ predator link (and would have been assumed positive in an empirical analysis), we used $\alpha_8^{init} \sim \mathcal{N}(\alpha_8 + 4SD_{\hat{\alpha_8}}, SD_{\hat{\alpha_8}})$. We used true parameter values as initial values for all other model parameters. Preliminary runs showed that convergence was reached very quickly (typically after a couple of iterations) with efficient mixing. We then ran 2 chains for 1200 iterations and discarded the first 200 as burn-in and did not use thinning. For comparison we also run 2 MCMC chains once, under the same settings, using the true values as initial values (see script https://github.com/MatthieuPaquet/multi_species/blob/main/script_MCMC_simulatedinitial_values_out_of_posterior.R). The results showed no sign of influence of the initial value chosen on the parameter estimates (Figure S9).

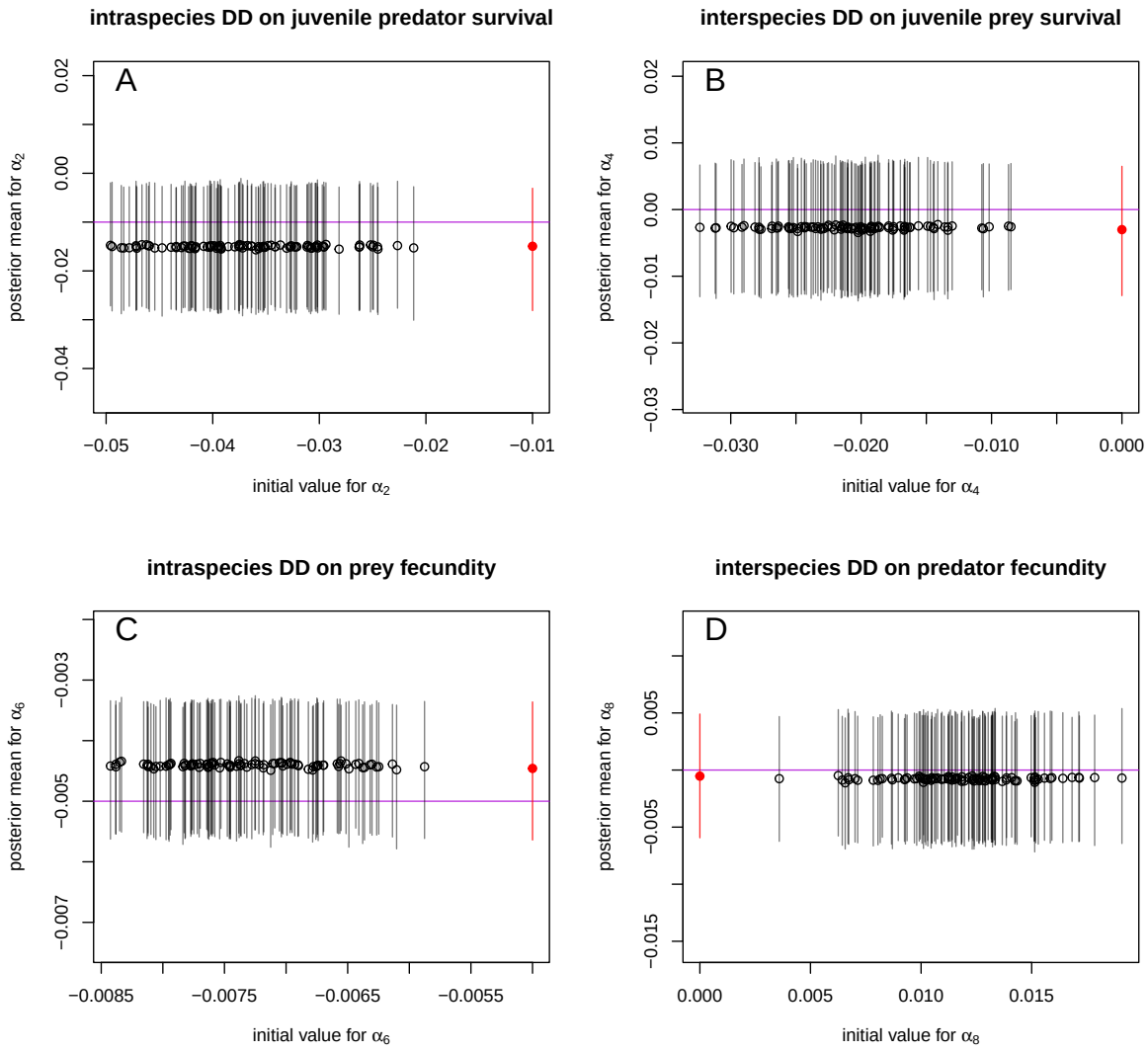

Figure S9: Estimation of density dependent parameter values (α_2 in panel **A**, α_4 in panel **B**, α_6 in panel **C** and α_8 in panel **D**) in relation to the initial values chosen to start the MCMC chains. Dots show the posterior means and vertical lines the 95% credible intervals. Purple horizontal lines highlight the value used to simulate the data. Red dots and intervals show the case where the true values are used as initial values.