

1 Interspecific spatial associations as a facet of biodiversity, 2 and a review of approaches to measure them

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15 1 Abstract

16 Interspecific spatial associations (ISA), which include co-occurrences, segregations, or attractions
17 among two or more species, have been an under-represented topic in biodiversity science and in large-
18 scale assessments of biodiversity change in the anthropocene. Also, ISA has not been perceived as a
19 facet of biodiversity on par with beta diversity or species richness. This is likely because it is unclear
20 what makes ISA useful in a biodiversity context, little is known about the theoretical connections
21 between ISA and other biodiversity facets, and there is a confusing variety of approaches to
22 measuring ISA. Here we address these three issues. First, we argue that ISA is an important facet of
23 biological diversity since it not only reflects species interactions, but it also provides a benchmark for
24 validation of ecological theories, and it can be explored for potentially predictive macroecological
25 patterns. Second, we review links of ISA to other classical biodiversity facets, namely to alpha, beta,
26 and gamma diversity, and species accumulation curves, showing that they mostly fail to reflect
27 changes/variation in ISA, with the exception of average pair-wise beta diversity. Third, we review the
28 metrics that are designed to reflect ISA. These are spatially implicit indices of association for both
29 binary and abundance data, community variograms, and summary functions such as bivariate pair
30 correlation functions for point patterns. We test and compare some of these approaches on empirical
31 and simulated data. We provide specific recommendations for how to use these approaches in
32 biodiversity science and macroecology. Our main conclusion is that measuring of ISA must evolve to
33 embrace spatially explicit, i.e. distance dependent, approaches.

34 **Keywords:** C-score, point process, interspecific, intraspecific, conspecific, heterospecific, spatial
35 scale, grain, semivariogram, geostatistics

36

37 “... there is no absolutely general measure of the degree of dependence”

38 (Cramér 1924, quoted by Goodman and Kruskal 1979, quoted by Hubálek 1982)

39 **2 Introduction**

40 Organisms are rarely distributed randomly in space. Instead, they aggregate or segregate as a result of
 41 spatial distribution of resources, barriers, environments, and/or by interactions with other organisms.
 42 Such non-random spatial aggregation and segregation occurs both among individuals within a single
 43 species and among species; we call the former the *conspecific spatial aggregation* (CSA), and the
 44 latter the *interspecific spatial association* (ISA) (Fig. 1, Appendix S1). Patterns of CSA are indicative
 45 of ecological niches, interactions among individuals of the same species, or dispersal limitations
 46 (Table 1). CSA also underpins concepts such as species endemism, beta diversity, and rarity (Table
 47 1), and there is a substantial literature on these connections (Fig. S1). In contrast, ISA indicates
 48 overlap of niches among species, as well as interspecific interactions and interaction networks (Table
 49 1), which underpins community assembly, coexistence theory, and ecosystem functioning. ISA is also
 50 foundational to classifications of communities to habitats, coenoses, or biomes (Hoekstra et al. 2004).
 51 Thus, both CSA and ISA can be seen as both useful and fundamental components or “facets” of
 52 biodiversity, if biodiversity is broadly defined as “variation of life at all levels of biological
 53 organization” (Gaston and Spicer 2009).

54 Perhaps surprisingly, ISA has been underrepresented relative to CSA in the study of macroecological
 55 and biogeographic patterns of biodiversity in space and time [with notable exceptions (Gotelli et al.
 56 2010, Lyons et al. 2016, Tóth et al. 2019), and ISA has been missing in recent high-profile studies of
 57 the ongoing biodiversity change (Millenium Ecosystem Assessment 2005, WWF International 2012,
 58 Newbold et al. 2015, Blowes et al. 2019). To demonstrate this gap, we scanned Clarivate Web of
 59 Science (Fig. S1), finding that literature on biodiversity has most often focused on quantities at sites
 60 (i.e. species richness, functional and phylogenetic diversity, extinctions, invasions, relative
 61 abundances), or quantified similarity among sites (i.e. beta diversity, turnover, nestedness, species-
 62 area relationships; Fig. S1), which are also intimately connected with CSA (Storch et al. 2008). In
 63 contrast, terms associated specifically with ISA received an order of magnitude less attention
 64 measured by the total number of published papers per year (Fig. S1), although ISA analyses require
 65 exactly the same data as analysis of beta diversity. So the lack of attention cannot be explained by a
 66 lack of data.

67 Clearly, although ISA is an important component of biodiversity (Table 1, next section), it has not
 68 been perceived as such by biodiversity scientists. We propose three reasons for this: First, it may be
 69 unclear what makes ISA important or useful when studying biodiversity. Second, little is known about
 70 the theoretical connections, or their lack, between patterns of ISA and other biodiversity patterns (e.g.
 71 those of richness or beta diversity). Third, it is unclear how biodiversity scientists should actually
 72 measure ISA, given the plethora of approaches.

73 In this paper, we aim to address each of these three issues. In the first part, we summarize why ISA is
 74 an important facet of biodiversity that deserves to be quantified alongside the other facets such as beta
 75 diversity or species-area relationships. We then outline the theoretical links between ISA and some
 76 fundamental facets of biodiversity, focusing particularly on species richness, beta diversity and
 77 species-area relationships. Finally, we review the current methods to measure ISA. We sort the
 78 methods according to the types of data that ecologists are likely to encounter, and we compare the
 79 methods on empirical datasets and on simulated pairs of species with known ISA. Based on our
 80 review and the simulations, we offer guidelines to select the appropriate approach to analyzing ISA
 81 based on the question of interest and particular type of data at hand. We hope our results will
 82 stimulate the study of ISA and promote its use in biodiversity assessments alongside more traditional
 83 measures.

84 **3 Why ISA matters for biodiversity**

85 Why, in the context of biodiversity, should we consider ISA patterns in space and time? The best-
86 known reason for analyzing patterns of inter-specific spatial associations and co-occurrences is that
87 they may give hints on biotic interactions and interaction networks among species (Gotelli et al. 2010,
88 Harris 2016, Morueta-Holme et al. 2016, Thurman et al. 2019), which is among the biggest topics of
89 biodiversity science (Fig. S1, Proulx et al. 2005, Newman 2006, Bascompte and Jordano 2017). The
90 traditional approach is to conduct null model randomizations of the presence-absence matrices
91 (Connor and Simberloff 1979, Gotelli 2000), whereas more recent approaches statistically partition
92 ISA due to shared environmental requirements and dispersal limitations from ISA caused by the
93 interactions, for example by joint species distribution modelling (JSDM, Warton et al. 2015,
94 Ovaskainen et al. 2017, Zurell et al. 2018), by looking at ISA within environmentally homogeneous
95 environment with no dispersal barriers (e.g. Tóth et al. 2019), or by making an assumption about the
96 spatial scale of biotic interactions vs. environmental variables, which enables to separate these two in
97 a null model (e.g. Wiegand et al. 2012). The latter is practical since it requires no data on
98 environmental conditions.

99 Other reasons for measuring ISA, which we cover below, are less appreciated. First, the problem of
100 inferring biotic interactions from co-occurrences can also be meaningfully reversed. Instead of asking
101 “How important are biotic interactions in a given system?” we can ask “What drives the observed
102 patterns of ISA?” Or more specifically: “To what extent can we explain the observed ISA by
103 environmental conditions, dispersal limitations, and/or biotic interactions?” This approach broadens
104 the focus to all of the processes that potentially generate the observed ISA (Table 1). It is also a
105 challenge for biogeography and macroecology, where explaining gradients of various facets of
106 diversity has dominated the field for decades, yet patterns of co-occurrence have been largely
107 overlooked (Fig. S1), in spite of some remarkable exceptions (Blois et al. 2014, Weinstein et al. 2017,
108 D’Amen et al. 2018).

109 Second, ISA and its patterns are useful even without mechanistic underpinning, because patterns are
110 useful as summary statistics for predictions and forecasts, based on inductive logic, as opposed to the
111 causal one. Examples of such predictive biodiversity patterns that proved to be useful are species-area
112 relationships with their utility to predict extinctions due to habitat loss (Keil et al. 2015) or the use of
113 richness-environment correlations for making spatial interpolations and predictions of diversity
114 patterns (Algar et al. 2009). There is a similar value in documenting generality of empirical patterns
115 of ISA in both time and space, since they can enable us to predict ISA in data-deficient locations, or
116 its change under anthropogenic environmental change.

117 We thus argue that ISA can be understood as a summary statistic capturing a unique state of nature,
118 on a par with other popular quantities such as species richness or beta diversity. Simply reporting how
119 these summary statistics vary geographically, or in time, repeatedly proved to be among the most
120 powerful starting stimuli in the field, generating countless explanatory and testable hypotheses. An
121 example is the very existence of latitudinal and altitudinal diversity patterns, which have fascinated
122 ecologists for centuries. The recently uncovered temporal patterns of biodiversity proved to be
123 similarly stimulating -- an example is the zero net change of local species richness coupled with
124 decrease in beta diversity (Dornelas et al. 2014, Tóth et al. 2019, Blowes et al. 2019) and with
125 decrease of global gamma diversity (Barnosky et al. 2011). Similar approach has recently gained
126 traction in the co-occurrence field. For example, Lyons et al. (2016) hypothesize that observed
127 changes in ISA patterns might be indicative of the impact of human expansion and agriculture on
128 assembly of communities. Likewise, Tóth et al. (2019) isolate the footprint of biotic interactions via

129 ISA patterns, without direct interaction data.

130 Third, ISA can provide new explicanda for major ecological theories (McGill 2010, Currie 2019).
 131 This could be an addition to patterns which are correlated with CSA, but uncorrelated with ISA, for
 132 example the species-area relationships (Plotkin et al. 2000, Storch 2016) (see next section). For
 133 example, it has been demonstrated that neutral theory (Hubbell 2001) or the maximum entropy theory
 134 (Harte 2011) both reproduce realistic species-area relationships, but it is unknown if they predict
 135 patterns of ISA [but see Bell (2005)]. The ability to explain patterns of ISA can thus be a new panna
 136 cotta for validating theories.

137 The last reason for why biodiversity science should re-focus on ISA is that some of the simple
 138 measures of biodiversity, such as average species richness or rarefaction, are insensitive to ISA, as we
 139 will show in the next section. Any biodiversity assessment that relies only on these simple measures
 140 runs into a risk of missing variation, or temporal change, of ISA. This also emphasizes the need for
 141 metrics designed to specifically quantify ISA.

142 **4 ISA vs other biodiversity metrics**

143 In order to study ISA in the context of biodiversity, one should be aware of how it relates to other
 144 biodiversity metrics and patterns. As mentioned above, this may be critical in any comprehensive
 145 biodiversity assessment that aims to capture as many independent facets of biodiversity as possible.
 146 Apart from that, the other facets may interfere with our ability to capture ISA, or inversely, ISA may
 147 interfere with our ability to measure other facets, which may necessitate statistically accounting for
 148 the confounding effects. Below we focus on what we see as the simplest and most fundamental
 149 metrics, namely alpha, beta, and gamma diversity, species-area relationships, and species
 150 accumulation curves.

151 **4.1 ISA vs alpha diversity**

152 Here we show that local species richness at any single given site is potentially sensitive to changes in
 153 ISA, while mean local richness (alpha diversity) is insensitive to changes in ISA.

154 Let α_j be local species richness at a site j , where $j \in 1:n$, and where n is the total number of sites
 155 within a given spatial domain. Let O_i be the number of occupied sites (i.e. occupancy) by species i ,
 156 where $i \in 1:\gamma$, and where γ is the total number of species (i.e. gamma diversity) present at all sites
 157 together. When we manipulate ISA in the system, values of α_j change as a result - for example, in
 158 Figure 2a, a change from interspecific segregation to aggregation results in corresponding changes in
 159 each site's α_j (one site gains species and two sites loose species).

160 Let us now consider $\bar{\alpha}$, the alpha diversity averaged across all sites, which can also be calculated as
 161 the sum of prevalences O_i/n (Šizling and Storch 2004), i.e. as:

$$162 \bar{\alpha} = \frac{\sum_{j=1}^n \alpha_j}{n} = \sum_{i=1}^{\gamma} \frac{O_i}{n} \quad (1)$$

163 Again consider the scenario in Figure 2a in which there was a shift in the ISA from segregated to

164 aggregated, given that O_i , n and γ remained constant, $\bar{\alpha}$ will not be affected by the change in ISA. In
 165 other words, when species in a given spatial domain segregate or move close to each other, it has no
 166 effect on average local species richness. Hence, an empirical assessment of biodiversity which
 167 summarizes net change of $\bar{\alpha}$ over many locations may be blind to changes of ISA, unless it also
 168 assess patterns that are sensitive to ISA, for example pairwise beta diversity. Further, this insensitivity
 169 of $\bar{\alpha}$ propagates to species-area relationships and to species accumulation curves diversity, as we
 170 show later.

171 4.2 ISA vs gamma diversity

172 From a purely geometrical perspective, simply rearranging mutual positions (ISA) of species within a
 173 given spatial domain has no effect on total number of species γ in the domain (given that n is
 174 constant). A more interesting question is what happens when the effect is reversed, i.e. how ISA
 175 changes when γ increases or decreases. This has biological implications, since γ limits the magnitude
 176 of ISA within a given domain, which can also limit biotic interactions. It also has methodological
 177 implications, since variation in γ across spatial domains can hinder direct comparisons of ISA within
 178 these domains, which may require statistical treatment (Ulrich et al. 2018). Several propositions about
 179 the relationship between ISA and γ have been made and some of them have been empirically tested.

180 The first has been summarized by McGill (2010): the richer the metacommunities, the weaker the
 181 associations will appear on average, despite the presence of some strong associations (Paine 1988,
 182 Wootton 1997, McGill 2010). This can be seen by considering that the total number of possible
 183 pairwise associations in the domain is $\gamma(\gamma - 1)/2$. If every species is significantly spatially associated
 184 with k species in a symmetric fashion, then the total number of significant spatial associations in the
 185 domain is $(\gamma k)/2$. Thus, for any given $k < (\gamma - 1)$, the total number of all possible pairwise
 186 associations increases faster with γ than the number of actually significant associations.

187 The second proposition operates on relative abundances: If the total area and density of individuals
 188 are constant, but there is an increase of the total richness γ , then the average per-species abundance
 189 must decrease, which will reduce the likelihood of detecting inter-specific co-occurrences in
 190 communities (Hubbell and Foster 1986, Lieberman and Lieberman 2007, Wiegand et al. 2007b,
 191 Volkov et al. 2009, Wiegand et al. 2012, Rajala et al. 2019). This only concerns the observed co-
 192 occurrences, and the effect should disappear after the observed spatial associations are contrasted with
 193 those predicted from a null model that is constrained by the observed γ and n .

194 The third proposition exposes the mathematical constraint on the possible values of *negative*
 195 associations in a species-by-species association matrix (Brown et al. 2004). Simply put, if species A
 196 and B have strong negative association (represented by negative correlation, covariance, or other
 197 index), then it is mathematically impossible for a third species C to have strong negative association
 198 with both A and B. This is because the association matrix is positive semidefinite (Brown et al. 2004).
 199 Fox (2012) also showed that, under the assumption that all species have the same negative correlation
 200 with each other (e.g. due to competition-induced compensatory dynamics), the minimum possible
 201 value of the correlation approaches 0 as we increase species richness. Thus, on average, the more
 202 competing species are added to the metacommunity, the weaker their observed average negative
 203 association gets.

204 The fourth proposition, which is biological rather than statistical in nature, suggests that communities
 205 with more species may only be stable if the interactions get weaker on average, as found by May

206 (1972) in an analysis of the stability of Lotka-Volterra type multispecies models. Stone (2016) found
 207 in a generalization of the analysis that stability and feasibility under increasing species richness
 208 requires a strong reduction in the mean and standard deviation of the value of the interspecific
 209 competition coefficients.

210 Based on all of these arguments, we should expect the overall ISA to weaken as γ increases. Indeed,
 211 Wiegand et al. (2012) found that species associations were significantly weaker in rich forest
 212 communities compared to species poor ones, even after the null-expected associations were taken into
 213 account. However, it is unclear if this occurred for the purely statistical reasons provided in
 214 proposition 1-3, and thus it may be desirable to account for them if ISA is compared across systems
 215 with different γ . Ulrich et al. (2018) provide null models to account for the effect of varying γ in
 216 spatially implicit binary co-occurrence species-by-site matrices, suggesting a randomization
 217 procedure that preserves both column and row total of the species-by-site matrix. We are unaware of
 218 similar procedures that account for the statistical effect of γ on ISA in abundance-based matrices, or
 219 in spatially explicit data. Finally, we also note that there may be limits in the ability of the null models
 220 to control for these effects (Ulrich et al. 2017).

221 4.3 ISA vs beta diversity

222 Here we show how ISA is conceptually related to another important biodiversity facet: beta diversity.
 223 We also show how one particularly popular matrix-wise measure of beta diversity, Whittaker's index,
 224 is insensitive to ISA, while pairwise indices of beta diversity are sensitive to ISA (Fig. 2), although
 225 we still lack the exact mathematical theory for this. We show that spatially explicit point pattern
 226 analysis may offer the right toolbox to build such a theory.

227 There is a fundamental connection between ISA and beta diversity, i.e. the differentiation of species
 228 composition in space. The connection is best illustrated on a spatially implicit site-by-species
 229 community matrix Y . In short, ISA is the association among *species* (Simberloff and Connor 1979,
 230 Hubálek 1982, Bell 2005, Legendre and Legendre 2012), whereas beta diversity is the dissimilarity
 231 among *sites*. In this simplified case, both ISA and beta diversity are calculated using exactly the same
 232 data and indices (Tables 2, 3); the only difference between them is whether they are applied to the
 233 rows ("R-mode" of Legendre & Legendre 2012) or columns of Y ("Q-mode"). In other words, any
 234 index of beta diversity that is normally applied to sites can be applied to species and can be
 235 meaningfully interpreted as an index of ISA, and vice versa (Legendre and Legendre 2012, Arita
 236 2017). For example, Araújo and Rozenfeld (2013) define a "co-occurrence score" as the "ratio of the
 237 number of geographical cells where species A and B co-occur to the total number of occupied cells".
 238 Although not stated, this is equivalent to the classic Jaccard index. Thus, the list of measures that have
 239 been typically used to measure ISA (Tables 2 and 3) can be expanded with e.g. Jaccard or Sørensen-
 240 type indices (Arita 2017). Inversely, the list of commonly used measures of beta diversity can be
 241 expanded by some typical ISA indices; for instance the C_{forbes} (Table 2) could find its niche in the beta
 242 diversity research, since it explicitly quantifies the deviation of the observed ISA (or beta diversity)
 243 from the ISA (or beta diversity) expected under random distribution of incidences (Forbes 1907).

244 However, little has been written about the actual relationship between beta diversity and ISA within a
 245 given spatial domain. There is insufficient theory and empirical evaluation showing exactly how ISA
 246 and beta diversity are related, and what the limits and constraints of the relationship are. The one
 247 simple exception is Whittaker's beta diversity when expressed as $\gamma/\bar{\alpha}$, which is insensitive to ISA
 248 (Fig. 2 and next section), given that the extent of the spatial domain remains constant. Some useful

connections between ISA and beta diversity are given by Arita (2017), who showed that both ISA and beta diversity are linked to the fill of binary community matrix, from which it follows that pairwise metrics of beta diversity should somehow be correlated with ISA, although not perfectly (Fig. 2). Also, Šizling et al. (2011) and McGlenn and Hurlbert (2012) give a potential clue by showing the relationship between average pairwise Jaccard beta diversity and the Whittaker index is modulated by the occupancy frequency distribution [see also McGeoch and Gaston (2002)]. This reasoning could perhaps be extended to provide a link between pairwise beta diversity and ISA.

In contrast to the spatially implicit indices for binary and abundance data, the connection between ISA and beta diversity is well known in analyses of point patterns (Wiegand and Moloney 2014) which do not operate with discrete sites, but rather with continuously varying areas for which position and species identity of every single individual is known. The ISA-beta connection can be demonstrated in the spatially-explicit version of Simpson's index $\beta(r)$ (Shimatani 2001, Wiegand and Moloney 2014 section 3.1.5.1), and this is something that could potentially inspire development of theory for other data types. Unlike the traditional spatially implicit version of the Simpson's index (Simpson 1949) (i.e., the probability that two randomly selected individuals are heterospecifics), which is a measure of diversity, $\beta(r)$ is a measure of beta diversity, since it captures dissimilarity over a given distance (Shimatani 2001) (i.e., the probability that two randomly selected individuals distance r apart are heterospecifics). The index is defined as:

$$\beta(r) = \sum_{i=1}^y \sum_{j=1}^y f_i f_j \frac{g_{ij}(r)}{g(r)} \delta_{ij} = 1 - \sum_{m=1}^y \frac{f_m^2 g_{mm}(r)}{g(r)} \quad (2)$$

Note the two alternative but equivalent definitions. In the first definition in eq. 2, f_i and f_j are the relative abundances of species i and j , $g_{ij}(r)$ is the bivariate pair correlation function describing the spatially explicit ISA and $g(r)$ is the pair correlation function of all individuals together (see following sections). The $\delta_{ij}(r) = 1$ if $i \neq j$ and $\delta_{ij}(r) = 0$ if $i = j$. As expected, if there are no spatial patterns of ISA, i.e. when $g_{ij}(r) = 1$, we obtain the non-spatial Simpson index, and depending on the abundances and ISA of the different species, beta diversity will be larger or smaller than this point of reference. The second definition in eq. 2 operates purely with con-specific aggregation (CSA), measured by within-species pair correlation function $g_{mm}(r)$. We can see that the spatially explicit $\beta(r)$ depends on the balance between the ISA and CSA, whose overall effect sums up to 1.

We thus conclude that point pattern analysis, through $\beta(r)$, offers a comprehensive framework that can link abundances, CSA, ISA, gamma diversity and alpha diversity, each with an exactly defined and mathematically tractable metrics. Not only does it stress the importance of making all of the diversity facets spatially explicit, but it also potentially offers a roadmap for future unification of the concepts in the field of macroecology that deals with plot-, grid-, or sample-based spatially implicit data on abundances or incidences.

4.4 ISA vs species-area relationships and species-accumulation curves

Here we demonstrate that species-area relationships and rarefaction curves are insensitive to ISA. We have stated that $\bar{\alpha}$ and γ in a given domain are insensitive to ISA, given that spatial extent or a study remains constant. These are the two components of Whittaker's index of beta diversity (Whittaker 1960), which is $\gamma/\bar{\alpha}$, and so Whittaker's index is insensitive to ISA. It means that nested species-area relationships (SAR), which are a generalization of the Whittaker index over a continuous range of $\bar{\alpha}$

289 and γ (Crist and Veech 2006) must also be insensitive to ISA (Fig. 2). However, this only holds when
 290 $\bar{\alpha}$ is considered in the nested SAR (Storch 2016); we are unaware of any study that investigates this
 291 for other types of SAR [e.g. island SAR (Scheiner 2003)].

292 When every individual's spatial position and identity is known, then the theory of point pattern
 293 analysis also makes it clear that there is no direct link between ISA and SAR. The relevant equation is
 294 (Shimatani and Kubota 2004):

$$295 \quad S(r) = \sum_{i=1}^{\gamma} H_i(r), \quad (3)$$

296 where $S(r)$ is number of species present within r from an arbitrarily chosen “test” location, H_i is the
 297 spherical contact distribution function for species i , which is the probability that the first neighbor of
 298 species i is distance r away from the test location. $S(r)$ becomes a species-area curve when r is
 299 converted to πr^2 . Importantly, the H_i is insensitive to ISA, since it is only based on the locations of
 300 species i . We note that point pattern analysis also has a scaling curve that is sensitive to ISA: the
 301 individual species-area relationship [ISAR (Wiegand et al. 2007a)] which always focuses on a focal
 302 species f :

$$303 \quad IS(r) = \sum_{i=1}^{\gamma} D_{fi}(r), \quad (4)$$

304 where $D_{fi}(r)$ is the bivariate nearest neighbor distribution function, and $IS(r)$ is the probability that a
 305 point of species i is distance r away from an average point of focal species f . Again, r can be
 306 converted to area as πr^2 .

307 Finally, we turn to species-accumulation curves, from which the classical examples are the spatially
 308 implicit individual-based and sample-based rarefaction curves (Gotelli and Colwell 2001), and their
 309 spatially-explicit versions (McGlenn et al. 2019). In the former, individuals or samples are
 310 accumulated randomly, irrespectively to their spatial position, which effectively breaks any pattern of
 311 both CSA or ISA, making the spatially implicit curves indeed insensitive to ISA. In the latter spatially
 312 explicit case, samples (plots) are accumulated by nearest neighbors, which makes these curves closely
 313 related to SARs, which we have shown to be sensitive to CSA, but insensitive to ISA. This is in line
 314 with the core idea of partitioning of rarefaction curves to their components (McGlenn et al. 2019),
 315 which are the regional species-abundance distribution, density of individuals, and con-specific
 316 aggregation, but not ISA.

317 **4.5 ISA vs biodiversity - summary**

318 To summarize this section, we have shown that although there are biodiversity facets that reflect ISA,
 319 such as pairwise between-site beta diversity, there are also many which ignore ISA. Specifically, these
 320 are the average local species richness $\bar{\alpha}$, the regional gamma diversity γ , their ratio $\gamma/\bar{\alpha}$, and species
 321 accumulation curves including species-area relationships and rarefaction curves. The insensitivity of
 322 these measures to ISA has two important practical implications: First, when the research focus is only
 323 species richness, con-specific aggregation, and their spatial scaling, then there is no need to worry that
 324 ISA confounds these facets. Second, for the same reason, studies that aim to describe the multi-
 325 faceted nature of biodiversity need to consider additional approaches designed specifically to capture
 326 ISA. Below we offer an overview of these approaches.

327 5 Approaches to measuring ISA

328 Methods capturing aspects of ISA have emerged from several schools of thought based on different
 329 data types (Fig. 3). The first school uses non-spatial information on presence/absence (or abundance)
 330 of species in different sites and has focused on tests of hypotheses related to assembly of ecological
 331 communities (Cody and Diamond 1979) by comparing the observed patterns of ISA with simulations
 332 of null models (Gotelli and Graves 1996, Ulrich and Gotelli 2010, Sanderson and Pimm 2015). The
 333 second school has been more descriptive, identifying typical groups of species that can be observed
 334 together, a typical goal in phytocoenology (Braun-Blanquet 1964). This has seen much of its
 335 development in continental Europe (Komárek 2017), particularly in geobotany, and it relies on
 336 methods such as ordinations and cluster analysis (ter Braak 1987, Šmilauer and Lepš 2014). The third
 337 school comes from the field of geostatistics (Cressie 2010) and uses additionally the spatial position
 338 of the sites, offering extensions of variograms that show how covariance between two species changes
 339 with spatial distance (Wagner 2003). The fourth school, requiring the most detailed data on exact
 340 spatial position of every individual, and offering the richest inference, is the analysis of point patterns
 341 (Wiegand and Moloney 2014). While each of these schools of thought have generated numerous
 342 conceptually diverse measures of ISA, there has been little cross-fertilization. Below we provide an
 343 overview of the main approaches.

344 5.1 Spatially implicit approaches to ISA

345 We begin with measures of ISA designed for one of the most common types of data in biodiversity
 346 science, the *community matrix* Y , which describes the distribution of γ species (rows) over n sites
 347 (columns). Each element y_{ij} of matrix Y contains either binary incidence or some measure of
 348 abundance, and $i \in 1:\gamma$ and $j \in 1:n$. We follow (Gotelli 2000) by setting rows as species and columns
 349 as sites, but others may prefer to reverse these. Since a community matrix Y contains no information
 350 on the spatial location of the sites, we use the term *spatially implicit* for all measures of ISA that only
 351 use Y .

352 To date, nearly 100 indices applicable to Y have been proposed to capture ISA in binary co-
 353 occurrence data (Hubálek 1982, Rajagopalan and Robb 2005, Legendre and Legendre 2012, Ulrich
 354 and Gotelli 2013, Arita 2017) and for abundance data (Legendre and Legendre 2012, Legendre and
 355 De Cáceres 2013), although only a dozen have been widely used in ecology. Some of the pairwise
 356 indices, such as C-score or togetherness (Table 2) were developed specifically to capture ISA, others
 357 were adopted from the literature on beta diversity (Hubálek 1982, Legendre and Legendre 2012, Arita
 358 2017). Guidelines on the selection of appropriate indices exist based on theoretical properties and
 359 performance on empirical data (Hubálek 1982, Koleff et al. 2003, Legendre and Legendre 2012,
 360 Legendre and De Cáceres 2013), as well as on arguments of comparability between current and
 361 historical analyses (Hubálek 1982). In Tables 2 and 3, we give examples of some widely used and/or
 362 sufficiently unique indices. Most of the indices are available through R packages *vegan* (Oksanen et
 363 al. 2019), *EcoSimR* (Gotelli et al. 2015), *bipartite* (Dormann et al. 2008), and *betapart* (Baselga and
 364 Orme 2012).

365 5.1.1 Pairwise associations in binary data

366 The conceptually simplest approach is to look at associations between binary occurrences of two
 367 species, either focusing at a specific pair of interest, or as a species-by-species association matrix (Z)

368 of all possible pairwise associations. Table 2 lists some of the typical pairwise binary examples that
 369 have been widely used, or that represent a unique approach to capturing ISA. Pairwise indices for
 370 binary data (Table 2) are based on four different quantities that result from the community matrix: the
 371 number of sites occupied uniquely by species 1 (c) and species 2 (b), the number of sites where both
 372 species co-occur (a), the number of sites where none occurs (d), and $n = a + b + c + d$. The classical and
 373 widely used C-score ($C_{seg} = bc$), for example, gives the number of pairs of sites with a “checkerboard”
 374 (i.e., one hosts species 1, the other species 2). Inversely, togetherness ($C_{tog} = ad$), gives the number of
 375 pairs of sites with no species and those with both species. The Jaccard index then gives the proportion
 376 of sites occupied by both species among all occupied sites ($C_{jacc} = a / (a + b + c)$).

377 5.1.2 Pairwise associations in abundance data

378 Table 3 lists some commonly used indices for pair-wise ISA in abundance data. The first family
 379 includes indices of covariance and correlation, both parametric and non-parametric (i.e. CA_{cor} and
 380 CA_{rho}), applied on either raw or transformed abundance data. The typical transformations are
 381 logarithmic, Hellinger (avoids the double zero problem), or square root transformation; are all aimed
 382 at removing the strong leverage of extremely common or rare species on correlations (Legendre and
 383 Legendre 2012). Another family includes indices that are extensions of the incidence-based similarity
 384 measures, and example is Růžička similarity CA_{ruz} , which is one of the abundance-based versions of
 385 Jaccard’s index for binary data (Legendre and De Cáceres 2013).

386 5.1.3 Higher-order and matrix-wise associations

387 When the aim is to quantify the overall magnitude of ISA in the entire matrix Y in a single number,
 388 one option is to simply use the mean or median of the species-by-species association matrix Z .
 389 However, focusing only on pairwise comparisons ignores interactions of higher order [i.e. interactions
 390 between 3 or more species (Harris 2016)]. Although not widely deployed, methods have been
 391 proposed that capture the magnitude of species associations across multiple orders. For example,
 392 Baselga (2017) and Arita (2017) both present their variants of the classical similarity measures for
 393 incidence data and abundance data that, in theory, capture N-wise species associations when applied
 394 to the rows of Y . The problem with these indices is their sensitivity to double zeroes and it is still
 395 unclear how common are the higher-order associations [a.k.a. motifs (Milo 2002)] in the real world;
 396 accordingly, this approach to similarity measures has already attracted criticism (Marion et al. 2017).
 397 Tables 2 and 3 list some matrix-wise metrics that have been popular.

398 5.1.4 Single species’ contribution to overall ISA

399 Legendre and De Cáceres (2013) proposed an index of contribution of a single locality to the overall
 400 beta diversity in Y . The same index can be calculated for rows instead of columns of Y , thus
 401 becoming a measure of species contribution to overall association; however, we are unaware of a
 402 study that employs such an approach to species-wise ISA.

403 5.1.5 Statistical significance, null models, Z-scores

404 When measuring ISA, one may need to test statistical significance of the observed ISA metric. That
 405 is, to calculate the probability that the metric has been produced by chance only, given that there is no
 406 ISA -- this is the so called ‘null expectation’. The simplest test of significance of association in a two-
 407 species binary matrix is Fisher’s exact test (Arita 2016), which is identical to the randomization
 408 procedure of Veech (2013). However, when more than two species are involved, or when the data are

409 abundances rather than incidences, one needs to use a randomization procedure that aims to produce
 410 the expected distribution of a given ISA metric under the null expectation. For binary data these null
 411 models are covered by Gotelli (2000), and available through R package EcoSimR (Gotelli et al.
 412 2015), while Ulrich and Gotelli (2010) provide an extensive evaluation of the models for abundance
 413 data.

414 Apart from the calculation of statistical significance, one may also quantify the deviation of the
 415 observed metric from the null expectation, and use this deviation as a new metric of ISA. This idea
 416 underpins the C_{forbes} and C_{FETMP} metrics (Table 2), and the so-called Z-score (Gotelli and McCabe
 417 2002, Ulrich et al. 2009, Ulrich and Gotelli 2013), where the latter is defined as $(E_{raw} - E_{exp})/SD_{exp}$,
 418 and where E_{raw} is the ISA metric (e.g. from Table 2) calculated on observed data, E_{exp} is the null
 419 expectation of the index, and SD_{exp} is the standard deviation of the null expectation. The Z-score
 420 approach is also useful when comparing between systems which differ in the number of samples and
 421 species which can influence a raw estimate of ISA.

422 5.2 Spatially explicit approaches to ISA

423 Thus far, we have only considered spatially implicit metrics of ISA that ignore the spatial distances
 424 (lags) between samples, individuals, or species' geographic ranges. Yet this spatial structure can be of
 425 key significance, particularly when attempting to detect nonrandom associations. Consider the simple
 426 example in Figure 4 in which the same community matrix can be underlain by either between-species
 427 aggregation or segregation at fine spatial scales. Spatially implicit metrics of ISA reviewed thus far,
 428 conflate these two spatial community patterns, and thus miss part of the ISA.

429 In contrast, spatially explicit techniques directly acknowledge that ISA is intimately connected to
 430 spatial distance between sites or individuals. When spatial coordinates of sites or individuals are
 431 available, the general way to make the ISA spatially explicit is to only consider pairs of sites that are
 432 within a given distance interval when using any of the metrics from the previous section (Tables 2 and
 433 3), and then to examine a range of distances. This is also the idea behind community variograms
 434 (Wagner 2003) described below. A point pattern-based version of this, when the location and identity
 435 of each individual is known, is to use bivariate pair correlation functions which describe positive and
 436 negative ISA between individuals over continuous distance (Wiegand and Moloney 2014). In the
 437 following section, we describe principles of these two approaches, and refer to software
 438 implementations.

439 5.2.1 Community variograms

440 Community variograms, borrowed from geostatistics, use the species-by-site community matrix Y
 441 together with spatial coordinates of each site (Wagner 2003). A community variogram then expresses
 442 the species-by-species variance-covariance matrix $Z(r)$ as a function of spatial distance or lag r
 443 between two samples. Spatial lags can be binned to avoid interpreting distance lags with low sample
 444 size and thus high uncertainty in the estimate of covariance, and covariances should not be interpreted
 445 at lags larger than half the maximum extent (Wagner 2003, Wagner and Fortin 2005). The community
 446 variogram approach allows the following analyses:

- 447 • At each distance, one can examine the diagonal elements of $Z(r)$ for within-species variances
 448 (i.e. CSA), or the off diagonal elements which are the between-species covariances (an
 449 Euclidean measure of ISA, sensitive to double zeroes), allowing examination of how both of

450 these change with distance, and also the relative magnitude of CSA and ISA at a given
451 distance.

- 452 • At each distance, negative and positive between-species covariances can be summarized
453 separately, as a sum or average. This allows to assess the relative magnitude of positive
454 (attraction) and negative (repulsion) ISA at a given distance.

455 We note that covariance calculated on binary data is closely algebraically tied to the C_{seg} or C_{tog}
456 metrics and their scaled versions (Table 2), which summarize only negative or positive covariances
457 respectively. Another closely related metric is the ratio of total community variance to within-species
458 variance (i.e. C_{ratio} , Table 2), which should be 1 when species are independent. Similarly to
459 covariance, the C_{seg} , C_{tog} and C_{ratio} , as well as many of the other metrics from Tables 2 and 3, can be
460 made distance-dependent and used in the community variogram framework. We also note that
461 spatially implicit metrics are simply the weighted sum of spatially explicit metrics across all possible
462 spatial lags in which the weights are equivalent to the number of samples separated by a given lag.
463 Finally, the approach can easily be integrated into the joint species distribution models, as also
464 demonstrated by Ovaskainen et al. (2017).

465 To test for non-random patterns of spatial species covariance an appropriate null model is required.
466 The distance-dependent C_{ratio} is typically used with a trivial null model of $C_{ratio} = 1$ under species
467 independence which can be biased in a number of different ways (Palmer and van der Maarel 1995).
468 In particular, it can be biased by patterns of within-species clumping. Even if species are arranged
469 independently on a landscape if they have strong patterns of within-species clumping they will appear
470 to be spatially segregated at least up to the scale of the within-species clump size. Therefore, the most
471 common type of null model is one in which the within-species spatial clumping is held constant but
472 otherwise species are shuffled randomly (Palmer and van der Maarel 1995, Roxburgh and Chesson
473 1998). Two R packages that allow calculation of community variograms are spacemaker (Dray 2019)
474 with the function `variomultiv`, and package `vario` (<https://github.com/dmccglinn/vario>) with the
475 function `vario`.

476 Even though the idea of community variograms has been featured in prominent methodological
477 reviews (Dray et al. 2012), and elements of it occasionally appear in empirical analyses (Wagner et al.
478 2005, Seabloom et al. 2005, Kikvidze et al. 2005, Ovaskainen et al. 2017), we are unaware of its
479 direct use specifically for the purpose of estimating distance-dependent ISA. At the same time the
480 method is the closest thing to the truly spatially-explicit description of ISA for community matrices
481 with additional spatial coordinates, and we thus see potentially important applications.

482 5.2.2 Point pattern analysis

483 There is a suite of methods that capture various facets of ISA in data where exact position and species
484 identity of every single individual within a spatial domain is known. These data, known as point
485 patterns, are rich in detail, offering the most accurate and spatially explicit quantification of ISA, but
486 are also costly to get and thus rare, and they have limits when applied to mobile organisms.
487 Consequently, analyses of ISA based on point patterns are less common than analyses based on
488 community matrices. Here we focus on bivariate pair correlation functions and P-M classification
489 scheme (Wiegand et al. 2007b, Wiegand and Moloney 2014).

490 The bivariate pair correlation function $g_{12}(r)$ measures the association between two species 1 and 2 at
491 different spatial scales (Stoyan and Stoyan 1994, Wiegand et al. 2007b); it is the density of a second
492 species at distance r of the typical individual of a first species, normalized with the overall density of

493 the second species in the plot. Thus, positive association (attraction) occurs for $g_{12}(r) > 1$ (larger than
 494 expected neighborhood density) and negative association (segregation) for $g_{12}(r) < 1$ (smaller than
 495 expected neighborhood density). The $g_{12}(r)$ is particularly useful since it quantifies repulsion or
 496 attraction at each distance independently on other distances. Example studies that employ $g_{12}(r)$ are
 497 (Wiegand et al. 2007b, 2012, Wang et al. 2010). The popular K-function $K_{12}(r)$ is the cumulative
 498 version of $g_{12}(r)$. The Z-scores of the point pattern summary functions are also sometimes used
 499 (Velázquez et al. 2016); popular software to calculate $g_{12}(r)$ and $K_{12}(r)$ be are Programita (Wiegand
 500 and Moloney 2004, 2014), and R package spatstat (pcfcross function) (Baddeley et al. 2016).

501 *The P-M classification scheme* visualizes pairwise spatial association between species at a given
 502 spatial scale r , using the Z-score of the cumulative neighbourhood density $K_{12}(r)/\pi r^2$ as x-axis (M-
 503 axis) and the Z-score of the nearest neighbor distribution function $D_{12}(r)$ as y-axis (P-axis) (Getzin et
 504 al. 2014). Because $K_{12}(r)$ and $D_{12}(r)$ capture fundamentally different aspects of ISA, the scheme
 505 allows for four ISA association categories: independence, segregation, partial overlap, and mixing.
 506 The scheme is best used to compare the overall ISA structure e.g., among tropical forests at a given
 507 spatial scale. It can be calculated using the Programita software (Wiegand and Moloney 2004, 2014),
 508 and we also offer an R implementation at <https://github.com/petrkeil/spasm> that relies heavily on the
 509 spatstat package (Baddeley et al. 2016).

510 *Null models for point patterns.* A well developed toolbox, summarized by Wiegand and Moloney
 511 (2014), is available to those seeking to compare observed summary statistics [e.g. $g_{12}(r)$, $K_{12}(r)$,
 512 $D_{12}(r)$] with those expected under the null expectations of independence. These are based on breaking
 513 the association between species, while keeping all of the other properties of single-species point
 514 patterns intact. The simplest null model for independence is the toroidal shift where one entire pattern
 515 is displaced against the other by a random vector (and the points falling outside the plot are wrapped
 516 using torus geometry), with a more refined version based on pattern reconstruction (Wiegand et al.
 517 2013, Getzin et al. 2014). Depending on the question, other null models can be used as well. For
 518 example, a heterogeneous point process where the individuals of pattern 2 are displaced only to
 519 random location within distance r of their original location. Here we note that particularly the
 520 heterogeneous point process null models (also combined with pattern reconstruction) should be
 521 appealing to all those seeking to estimate biotic interaction from mere occurrence data; notably, this
 522 can be done without actually having the environmental data at hand, but by assuming that the spatial
 523 distance of biotic interactions is shorter than the distance of environmental autocorrelation (Wiegand
 524 et al. 2007b). Because in this null model points are displaced only within distance r of their original
 525 location they may land in a similar environments. Null models for point patterns are implemented in
 526 Programita software (Wiegand and Moloney 2004, 2014) and in the spatstat R package (Baddeley et
 527 al. 2016).

528 **6 Comparison of the approaches**

529 Here, we compare the performance of the approaches reviewed above when they are used on a
 530 common set of empirical and simulated communities. Our aim is to assess redundancy among the
 531 approaches, as well as their sensitivity to the common variables such as number of sites, number of
 532 species, magnitude of con-specific aggregation, or spatial grain. We are also interested in how well
 533 the different measures capture negative associations (i.e. segregation) as opposed to the positive
 534 associations (attraction) of ISA. Code and data for these analyses are at
 535 <https://github.com/petrkeil/spasm>.

536 6.1 Spatially implicit measures vs empirical data

537 Our goal in this first exercise was to calculate the common metrics of ISA for a set of real-world and
 538 spatially implicit species-by-site matrices, and to see how the metrics correlate with each other. We
 539 evaluated the metrics listed in Tables 2 and 3 using 290 empirical binary community matrices collated
 540 in (Atmar and Patterson 1995), and 186 empirical abundance matrices collated in (Ulrich and Gotelli
 541 2010). We excluded matrices with too little information to allow meaningful calculation of all of the
 542 indices, or which gave negative or positive infinity values of some of the metrics. For the pairwise
 543 metrics, we averaged them over the species-by-species association matrix Z to obtain a single number
 544 comparable with the matrix-wise measures. We subjected the metrics to principal components
 545 analysis (PCA), for which we transformed some of them to have an approximately normal
 546 distribution. We plotted the PCA as an ordination biplot, and we also plotted a graph representation of
 547 the correlation matrix of the measures (Fig. 5).

548 In both the incidence- and abundance-based spatially implicit indices we found clear differentiation
 549 along the PCA axes (Fig. 5a, b) and in the graph (Fig. 5c, d), reflecting the different aspects of ISA
 550 that they were designed to capture. In binary metrics, there is a clear cluster dissimilarity-based
 551 indices (C_{jacc} , C_{sor}), the Whittaker index (C_w), Alroy's index (C_{alroy}), as well as its closely related
 552 connectance (C_{conn}) (Fig. 5 a, c, Fig. S1). Two measures that explicitly measure departure from
 553 Poisson randomness (C_{FETmP} , C_{forbes}) grouped together. The classical C-score (C_{segSc}) and its
 554 counterpart, togetherness (C_{togSc}), the matching coefficient (C_{match}), the checkerboard score ($C_{checker}$),
 555 and number of unique combinations (C_{combo}) are to some degree unrelated to the rest of the metrics. In
 556 the abundance-based metrics, we found similar clustering of the dissimilarity-based ISA metrics
 557 (CA_{ruz} , CA_{brays} , CA_{chi} , CA_{hell}), while the correlation-based metrics (CA_{cor} , CA_{cor_hell} , CA_{tau}) formed another
 558 group.

559 Notably, among the incidence-based metrics only C_{combo} is strongly correlated with the total number of
 560 sites in a matrix (n), while only $C_{checker}$ correlated strongly with the total number of species (γ) (Fig.
 561 S2). Unsurprisingly, covariance-based measures (CA_{cov} , CA_{cov_hell}) grouped together with the total
 562 number of sites n . Among all the metrics several metrics are correlated with γ , but none of them
 563 strongly (Figure S2, S3).

564 6.2 Spatially implicit measures vs spatially explicit simulations

565 In the second exercise, we devised simulations with known magnitude of ISA between two species
 566 (Fig. 6, S4, Appendix S2). We aimed to illustrate how the different approaches are able to recover this
 567 simulated ISA. In contrast to spatially implicit simulations performed in other studies (Gotelli 2000,
 568 Ulrich and Gotelli 2010), we simulated the position of every individual within a bounded domain. In
 569 each simulation, we generated point patterns of two species, with a given magnitude of ISA between
 570 them, and with varying con-specific aggregation and number of individuals per species (see Appendix
 571 S2 for details). See Keil (2019) for an example use of the same simulation procedure.

572 We modelled ISA as dependent on spatial distance (Fig. 6b), and it was controlled by a single
 573 parameter called simply ISA, with negative values for segregation ($ISA < 0$), zero for independence
 574 ($ISA = 0$), and positive for attraction ($ISA > 0$) (Fig. 6). In order to calculate measures based on
 575 incidence or abundance, we converted the point patterns to grids of varying resolutions (grains).
 576 Across all simulations, we then measured performance of the metrics from Tables 2 and 3 as their
 577 Spearman correlation with the ISA parameter. We also examined how the performance was affected

578 by spatial grain and magnitude of conspecific spatial aggregation (CSA) (Fig. S6, S7). Detailed
 579 description of the simulations, and their analysis, is in Appendix S2, and complete code for the
 580 exercise is at <https://github.com/petrkeil/spasm>.

581 We found the best correlation with overall ISA, as well as correlation with both negative ISA
 582 (attraction) and negative ISA (repulsion), in Pearson's tetrachoric correlation (C_{pears}), Forbes index
 583 (C_{forbes}), and the mid-P variant of Fisher's Exact Test (C_{FETmp}) for binary data, and Spearman's
 584 correlation (CA_{rho}) and Hellinger distance (CA_{hell}) for abundance data (Fig. 7). The best overall
 585 Spearman correlations between the simulated ISA and its estimated measures were around 0.75 (Fig.
 586 7), an imperfection that we attribute to the inability of the spatially implicit measures to capture the
 587 distance-dependent part of ISA (Fig. 4, Fig. 6b). We found no clear indication that either abundance
 588 or incidence-based metrics performed best. We also found that measures based on correlation (C_{pears} ,
 589 CA_{rho} , CA_{cor} , CA_{cov}), or on deviation from an expected null association (C_{forbes} , C_{FETmp}) performed better
 590 in capturing ISA, while dissimilarity measures (C_{sor} , C_{jacc} , CA_{bray} , CA_{ruz}) performed worse. This is also
 591 in line with our supplementary analysis of Z-scores (Figs. S6 and S7). We found that refining the
 592 spatial grain of the analysis, and increasing the magnitude of CSA, had both mostly negative or no
 593 effect on the performance of the metrics (Figs. S6 and S7), although there were exceptions from the
 594 trend.

595 Importantly, we found that the spatially implicit metrics tended to saturate at extreme negative (ISA <
 596 10) association (Fig. S5), most likely because the community matrices are identical above these
 597 extreme ISA values (demonstrated in Fig. 4). Thus, most abundance-based metrics show weak overall
 598 correlation with repulsion (Fig. 7b), with the exception of the distance-based Ruzicka (CA_{ruz}) and
 599 percentage difference (CA_{bray}) indices. Finally, we found that when the metrics were averaged at a
 600 given spatial grain, they varied dramatically in their relationship with grain (Fig. S8), and this
 601 variation is difficult to interpret.

602 **6.3 Spatially explicit measures vs spatially explicit simulations**

603 Finally, we used the 2-species simulations to illustrate the idea of community variograms and pair
 604 correlation functions. Here, our goal was simply to show the potential of these methods, rather than to
 605 perform the same comprehensive evaluation as above, since these techniques do not measure ISA in a
 606 single number, but as a function of spatial distance r . Because of that, they have the potential to
 607 actually recover the shape of the entire probability density function $f_{sp2}(r)$ from Figure 6b. For the
 608 spatially explicit techniques, we performed 9 simulations that correspond exactly to the panels of
 609 Figure 6a (the only difference is that we used 200 individuals per species). For the purpose of fitting
 610 the community variograms, we used a single grid resolution with 20 cells along each side of the
 611 simulated domain.

612 Community variograms (Fig. 8a) estimated the relationship between distance r and negative
 613 covariance in a way that matched the shape of the original $f_{sp2}(r)$ from Figure 6b. However, they had
 614 problem with accurately capturing the spatial pattern of attraction when there was a confounding
 615 effect of strong con-specific dispersion (CSA > 0.01), where the pattern was indistinguishable from
 616 independence. In contrast to community variograms, pair correlation functions more accurately
 617 estimated the distance-dependent ISA (compare Fig. 6b with Fig. 8a), i.e. the estimated relationship
 618 between distance and pair correlation function closely matches the shape of the original $f_{sp2}(r)$ from
 619 Figure 6b. Similarly to community variograms, there was a somewhat limited performance for
 620 attraction and high CSA values, but the problem is less severe. Overall, the point pattern-based

621 bivariate pair correlation functions provided the most complete picture of the “true” simulated ISA
622 pattern.

623 7 Discussion and recommendations

624 Based on the existing literature and our comparisons of the methods, we make several concrete
625 recommendations for capturing ISA in the context of biodiversity.

626 7.1 Best indices

627 There is a variety of indices that were designed to capture different aspects of ISA and some of them
628 may even be uncorrelated [see our results, but also Hubálek (1982)]. Thus, in empirical assessments,
629 we recommend not to rely on a single metric [as also recommended by Ulrich and Gotelli (2013)].
630 Overall, we suggest that the most promising indices for spatially implicit analyses are those that can
631 capture both negative and positive ISA. They should also offer the option to be eventually integrated
632 into, or compared with, spatially explicit analyses such as community variograms, it should be
633 possible to contrast them with indices of con-specific aggregation, and they should be applicable in
634 association matrices of parametric joint species distribution models. For abundance data these are
635 covariance (CA_{cov}) and Pearson correlation (CA_{cor}), coupled with a data transformation (e.g. Hellinger
636 or log) if appropriate. For incidence data these are the C-score (C_{seg} , C_{segSc}) and togetherness (C_{tog} ,
637 C_{togSc}) which capture the positive and negative ISA respectively and are mathematically linked to
638 covariance. We caution that that low C-score values do not indicate high togetherness, and vice versa.
639 Thus, both should be employed, unless only one direction of ISA is specifically of interest.

640 From the other indices for pairwise binary data, among the all-purpose metrics that capture both
641 repulsion and attraction, we recommend the mid-P index (C_{FETMP}), Forbes’s coefficient of association
642 (C_{forbes}), or Pearson’s tetrachoric correlation (C_{pears}); the latter is also (with reservations) recommended
643 by Hubálek (1982). Jaccard’s index (C_{jacc}) is a good alternative, since it captures both negative and
644 positive ISA, and it can easily be interpreted as proportional overlap, although it may not reflect the
645 overall ISA as accurately as the correlation-based indices. For pairwise abundance data, apart from
646 covariance- and correlation-based parametric indices, we advocate for the Spearman rank-rank
647 correlation (C_{rho}), since it requires no prior transformation, and it captures well both negative and
648 positive ISA.

649 Concerning the community-wide measures that quantify the magnitude of ISA for all species in a
650 single number, an obvious choice is to use summarized pairwise metrics, although one needs to
651 beware that some summarizations (e.g. averaging) blend repulsions and attractions. Perhaps the best
652 way to avoid this problem is to decompose the pairwise association matrix to positive vs negative
653 ISA, by separately summarizing positive vs negative covariances in abundance data (this is also the
654 approach used in community variograms), or by considering both togetherness and C-score in
655 incidence data. Finally, we advise caution when using indices such as Whittaker’s (C_w) or the related
656 connectance (C_{conn}) because of their problematic interpretation which conflates ISA with beta
657 diversity.

658 7.2 ISA is better spatially explicit

659 Our results highlight a serious limitation of spatially implicit indices of ISA: they fail to consider

660 spatial proximity of two species when they are already 100% spatially segregated (Fig. 4), a problem
 661 that will grow in severity as spatial resolution becomes finer. Ultimately, this problem will make the
 662 spatially implicit metrics meaningless at spatial grains that reach the size of an average individual, or
 663 when the data become point patterns. This partly explains why none of the examined spatially implicit
 664 metrics gave a perfect correlation with the simulated distance-dependent ISA, and why we observed
 665 the saturation of performance towards extreme values of ISA in our simulations (Fig. S5). This is a
 666 drawback of any analysis based purely on spatially implicit community matrices, even though the
 667 problem may be less severe at coarse spatial resolutions. We argue that there is only one way to
 668 address it systematically and conceptually: Whenever there is information on spatial position of the
 669 sites, indices of ISA are better considered as a function of spatial distance. Both the community
 670 variograms and point pattern analysis offer straightforward ways to do that.

671 Apart from being practical, going spatially explicit (when data permit) also makes ISA more
 672 biologically interpretable; after all, interspecific biotic interactions among individuals do happen over
 673 a certain distance. Thus, measuring ISA in a spatially explicit way can identify those distances over
 674 which the interactions matter. An added advantage of such an approach is that it also allows to
 675 separate ISA due to interactions vs environment, without the necessity of actually having the
 676 environmental data when it appears that fine-scale environmental heterogeneity is negligible
 677 (Wiegand et al. 2012).

678 One specific application in which ignoring spatial distance is likely to result in severe consequences is
 679 Joint Species Distribution Modeling, or JSDM (Warton et al. 2015, Ovaskainen et al. 2017, Zurell et
 680 al. 2018), where species-by-species covariances (or correlations) are estimated as model parameters,
 681 conditional on the species-environment relationships. We recommend that these covariance matrices
 682 also need to be conditional on spatial distance in order to avoid the saturation arising from strong ISA.
 683 One specific implementation of such an approach is offered through hierarchical parametric models of
 684 Ovaskainen et al. (2017).

685 **7.3 Spatial scale**

686 Most of the commonly studied facets of biodiversity depend on spatial scale. In the case of ISA, scale
 687 has been approached from two angles. The first focuses on ISA as a function of the average area of a
 688 site in a community matrix, which is equivalent to spatial resolution (grain) of a grid (Økland 1994,
 689 Hui 2009, Segurado et al. 2012, Araújo and Rozenfeld 2013, McNickle et al. 2018). These studies
 690 show that ISA is grain-dependent, but neither theory nor empirical observations predict a systematic
 691 direction of the grain dependence; ISA-area relationships can be increasing, decreasing, or hump-
 692 shaped. One thing that complicates consensus is the use of various metrics of ISA across studies. Our
 693 simulations (Fig. S8) show that selection of the ISA metric critically affects the grain dependency; for
 694 example, Z-scores of abundance-based metrics may have hump-shaped relationship with grain (e.g. Z-
 695 score of CA_{bray}), while raw binary dissimilarity may monotonically increase or decrease with grain
 696 (Fig. S8). This is something that the field needs to sort out before any empirical scaling of ISA is
 697 explored and interpreted.

698 The second approach to spatial scaling of ISA uses distance instead of grain in the form of community
 699 variograms or bivariate pair correlation functions (Wagner 2003, Wiegand and Moloney 2014). One
 700 advantage of this approach is its straightforward biological interpretation, particularly in the context
 701 of biotic interactions, since spatial distance is the ultimate condition for interactions (grain is only
 702 proximate). In other words, most ecologists will understand that species interact over a certain
 703 distance, but might be puzzled by the statement that they interact at a given grain.

Luckily, both the grain-based and distance-based approaches to the scaling of ISA can be combined in a single analysis [see Wiegand et al. (2012)]. Finally, point-pattern analysis has theory that links the area-based with the distance-based approaches to ISA (Wiegand and Moloney 2014). Future investigations of ISA should more explicitly embrace the issue of scale (both the grain and perhaps also extent) by focusing on the ISA-area relationships (Araújo and Rozenfeld 2013, McNickle et al. 2018), or by focusing on the spatially explicit approaches to ISA which handle scale more naturally than the spatially implicit ones.

7.4 Null models and Z-scores

Most of the literature on ISA emphasizes the importance of null models and null expectations, be it spatially implicit (Ulrich and Gotelli 2013) or explicit (Wiegand and Moloney 2014). The most common use of these is to get to statistical significance of the observed ISA, and to standardize the metrics so that they are comparable across different ecological situations or studies. In Figures S6 and S7, we show that transforming ISA indices to Z-scores makes them more robust against the confounding effects of conspecific aggregation or varying resolution, while (Ulrich et al. 2018) show that null models also account for the confounding effect of total species richness (γ). The same sentiment underlies Wiegand and Moloney's (2014) book: to analyze spatially explicit patterns of ISA, one has to contrast them against a null expectation of no ISA. However, one needs to bear in mind that when Z-scores and null models are used, they tend to converge to the same value, irrespective of the original meaning of the metric (Keil 2019); in a way, the meaning of the null model overrides the meaning of the index. Thus, when null models are deployed, we recommend that users know their ecological interpretation exactly.

Since null models often involve intense randomization algorithms, they may be computationally demanding, particularly when used in large-scale macroecological analyses of biodiversity. Luckily, there are analytical shortcuts for some of the approaches. For example, in spatially implicit methods, if computational efficiency is desirable, measures such as C_{FETMP} or C_{forbes} already have the deviation from the expected randomness implicit in their definition.

7.5 Measuring macroecological patterns of ISA

Finally, we return to the main point of this paper, which is the premise that patterns of ISA is an important standalone facet of biodiversity that is on par with macroecological classics such as species richness or beta diversity. We have demonstrated that ISA is at least partly independent of these other facets. Thus, in order to empirically document patterns of ISA, and their generality or variation over broad spatial and temporal scales, we need analytical approaches designed specifically to measure ISA with the kind of data available over broad scales. From all of the reviewed approaches, we see community variograms as the most useful, since:

(1) Community variograms are spatially explicit, thus they avoid the pitfalls of the spatially implicit indices mentioned above, offering rich biological interpretation.

(2) Community variograms are applicable to a wide range of data types, including systematic continental surveys such as the US North American Breeding Bird Survey, metacommunity data in databases such as PREDICTS, BioTime or CESTES (Newbold et al. 2015, Jeliaskov 2019, Blowes et al. 2019), regional gridded atlases such as the Atlas Florae Europaeae, and global grids such as the the IUCN red list data. In contrast, point pattern analysis has highly specific requirements on data format,

745 limiting its use to a small number of local plots with limited spatial extent.

746 (3) Calculation of community variograms is computationally feasible.

747 Given that there is an ever increasing availability of biodiversity data from large spatial extents (Jetz
748 et al. 2012), we see an exciting opportunity here for exploration of empirical macroecological patterns
749 of ISA, particularly through community variograms. Future work should examine how community
750 variograms change along macroecological gradients.

751 **8 Conclusions**

752 We have based this paper on the premise that inter-specific spatial associations (ISA) are an
753 underrepresented topic in biodiversity science and macroecology, and that this is an important
754 knowledge gap. We argued that there are several reasons for why ISA, and its spatio-temporal
755 patterns, are worth exploring. Apart from its connection to biotic interactions, ISA can also provide a
756 benchmark for judging different types of ecological theories, and it can serve as a summary statistic
757 capturing a unique property of nature. This is underscored by the fact that many of the biodiversity
758 statistics that have been monitored are insensitive to ISA.

759 We provide an overview of the main approaches to measure ISA, which we sorted into three main
760 schools of thought, based on the data that they use: spatially implicit indices, community variograms,
761 and bivariate pair correlation functions. Our main conclusion is that considering space, and
762 particularly spatial distance, is vital for the progress of the field, and for any broad-scale assessment
763 of patterns of ISA in geographic space and in time. In all, we hope that our overview of ISA, its
764 measures, and its utility provides a starting point for researchers interested in broadening the scope of
765 biodiversity facets that they study, as well as a new inspiration for those who have already studied
766 ISA. Among these, we turn to two kinds of researchers for whom our review seems particularly
767 relevant: The first are those working in the emerging field of joint species distribution models
768 (JSDM), where spatial distance has rarely been considered, and which still rely mostly on spatially
769 implicit covariances and correlations. Second, we would like to appeal to those dealing with
770 interaction networks and biodiversity-ecosystem function (BEF) issues. The critical role of spatial
771 distance and scale in ISA is something that they need to consider, and our review offers specific ways
772 how to approach that.

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777 **10 References**

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779 **Table 1** Brief summary of processes that generate CSA and ISA, biodiversity patterns that are linked
 780 to CSA and ISA, and the approaches to measure them.

	Conspecific spatial aggregation (CSA)	Interspecific spatial association (ISA)
What generates it?	species-specific dispersal limitations, <i>conspecific interactions</i> among individuals, interplay between <i>niche width</i> and spatial aggregation of environmental conditions	differences in dispersal limitations among species, <i>interspecific interactions</i> among individuals, interplay between <i>niche overlap</i> and aggregation of environmental conditions
Which biodiversity facets and patterns are sensitive to it?	beta diversity and its distance decay, species-area relationships (SAR), endemics-area relationships (EAR), occupancy-area relationships (OAR), altitudinal and latitudinal gradients of range size and endemism, spatial gradients of diversity	still mostly unclear
Broad approaches to measure it	beta diversity indices, local slope of SAR, EAR and OAR, species accumulation curves (MoB framework), mean range size, spatial Taylor's power law, spatial overdispersion	indices of association, community variograms, pair correlation functions, K-functions

782 **Table 2** Measures of ISA for binary community data. From more than 70 measures (Keil 2019) we
 783 have included those that have either been popular, recommended based on suitable properties, or that
 784 represent a distinct approach to ISA. Notation for pairwise measures for the pairwise comparison of
 785 two species: a is the number of sites where both species co-occur, c and b are numbers of sites
 786 occupied uniquely by each species respectively, d is the number of sites where none of the species
 787 occur, and n is the total number of sites, i.e. $a + b + c + d$. Other notation is explained directly in the
 788 table.

Measure	Reference	Symbol	Formula or description	R code in
A) Pairwise				
C-score	(Stone and Roberts 1990)	C_{seg}	bc	bipartite::C.score EcoSimR::c_score vegan::designdist
Scaled C-score	(Ulrich and Gotelli 2013)	C_{segSc}	$\frac{bc}{n(n-1)/2}$	vegan::designdist
Togetherness	(Stone and Roberts 1992)	C_{tog}	ad	bipartite::togetherness vegan::designdist
Scaled togetherness	(Ulrich and Gotelli 2013)	C_{togSc}	$\frac{ad}{n(n-1)/2}$	vegan::designdist
Jaccard similarity	(Jaccard 1901)	C_{jacc}	$\frac{a}{a+b+c}$	betapart::betapart vegan::betadiver
Dice-Sorensen similarity	(Dice 1945, Sørensen 1948)	C_{sor}	$\frac{2a}{2a+b+c}$	betapart::beta.pair vegan::betadiver
Coefficient of association	(Forbes 1907)	C_{forbes}	$\frac{na}{(a+b)(a+c)}$	vegan::betadiver
Alroy's coefficient (a new take on C_{forbes})	(Alroy 2015)	C_{alroy}	$\frac{a(z+\sqrt{z})}{(a+b)(a+c)+a\sqrt{z}+\frac{bc}{2}}$ where $z=a+b+c$	vegan::designdist
Pearson tetrachoric correlation	(Pearson and Heron 1913)	C_{pears}	$\frac{ad-bc}{[(a+b)(c+d)(a+c)(b+d)]^{0.5}}$	vegan::designdist
Mid-P variant of Fisher's exact test	(Kallio et al. 2011, Tóth et al. 2019)	C_{FETmP}	$\left(\sum_{x_{min} \leq x \leq x_{max}} \frac{\binom{i}{x} \binom{n-i}{j-x}}{\binom{n}{j}} \right) - \frac{\binom{i}{a} \binom{n-i}{b}}{2 \binom{n}{j}}$ Where $i = a+b$, $j = a+c$, and x is the possible number of overlaps, with $x_{min} = \max(a-d, 0)$ and $x_{max} = \min(i, j)$. The symbol $'$ denotes the 'choose' operation.	https://github.com/anikobtoth/FCW
Matching coefficient	(Sokal and Michener 1958)	C_{match}	$\frac{a+d}{n}$	vegan::designdist
B) Matrix-wise				
Whittaker index	(Whittaker 1960, Arita 2017)	C_w	This is the fill of the Y matrix, which is $\frac{Y}{\bar{\alpha}} = \frac{n}{\bar{n}}$ where \bar{n} is the average number of occupied sites per species.	vegan::betadiver

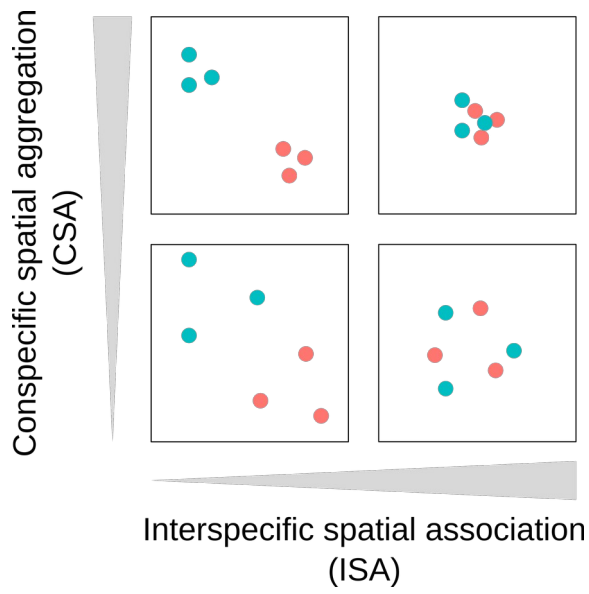
Variance ratio	(Schluter 1984)	C_{ratio}	$S_r^2 / \sum \sigma^2$, where S_r^2 is the variance of per-site species richness and σ^2 is the sum of per-species variances of incidences.	EcoSimR::v_ratio https://github.com/mcglinnlab/vario
Checker score	(Gotelli 2000)	$C_{checker}$	Number of species pairs forming perfect checkerboard distributions.	EcoSimR::checker
Number of unique species combinations	(Gotelli 2000)	C_{combo}	Number of species that always co-occur.	EcoSimR::species_combo
Network connectance	(Dormann et al. 2009)	C_{conn}	$F / \gamma n$, where F is the number of all co-occurrences	bipartite::networklevel

790 **Table 3** Select measures of ISA for abundance data. From the plethora of existing measures have
 791 included those that have been popular, recommended, or that represent a distinct approach to ISA.
 792 Specifically, we selected three correlation-based indices, two distance-based indices, two abundance-
 793 based variants of the binary indices, and two matrix-wise indices. x and y are the vectors of abundance
 794 of two species, \bar{x} and \bar{y} are their means, x_+ and y_+ are their sums, σ_x and σ_y are their
 795 standard deviations, x_i and y_i are abundances at site i , and n is the total number of sites.
 796

Measure	Reference	Symbol	Formula or description	Notes	R code in
A) Pairwise					
Covariance	(Legendre and Legendre 2012)	CA_{cov} , CA_{cov_hell}	$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$	With optional transformation (Hellinger, log, sqrt) of raw abundances.	stats::cov
Pearson correlation (scaled covariance)	(Legendre and Legendre 2012)	CA_{cor} , CA_{cor_hell}	$\frac{CA_{cov}(xy)}{\sigma_x \sigma_y}$	With optional transformation (Hellinger, log, sqrt) of raw abundances.	stats::cor
Spearman's Rho	(Legendre and Legendre 2012)	CA_{rho}	CA_{cor} between the rank values of x and y		stats::cor
Chi-squared distance	(Lebart and Fénelon 1971, Legendre and De Cáceres 2013)	CA_{chi}	$\sqrt{(x_+ + y_+) \sum_{i=1}^n \frac{1}{x_i + y_i} \left(\frac{x_i}{x_+} - \frac{y_i}{y_+} \right)^2}$		vegan::decostand with stats::dist
Hellinger distance	(Rao 1995, Legendre and De Cáceres 2013)	CA_{hell}	$\sqrt{\sum_{i=1}^n \left(\sqrt{\frac{x_i}{x_+}} - \sqrt{\frac{y_i}{y_+}} \right)^2}$		vegan::decostand with stats::dist
Percentage difference (former "Bray-Curtis" index)	(Odum 1950, Legendre and De Cáceres 2013)	CA_{bray}	$\frac{\sum_{i=1}^n x_i - y_i }{x_+ + y_+}$	One of the abundance-based variants of C_{sor} .	vegan::vegdist
Ruzicka similarity	(Růžička 1958, Oksanen et al. 2019)	CA_{ruz}	$\frac{2CA_{bray}}{1 + CA_{bray}}$	One of the abundance-based variants of C_{jacc} .	vegan::vegdist
B) Matrix-wise					
N-wise Ruzicka	(Baselga 2017)	CA_{ruzN}	Long formula, see Baselga (2017).	Multi-species version of CA_{ruz} .	betapart::beta.multi.abund
Variance ratio	(Ulrich and Gotelli 2010)	CA_{ratio}	The same principle as the binomial C_{ratio} .		

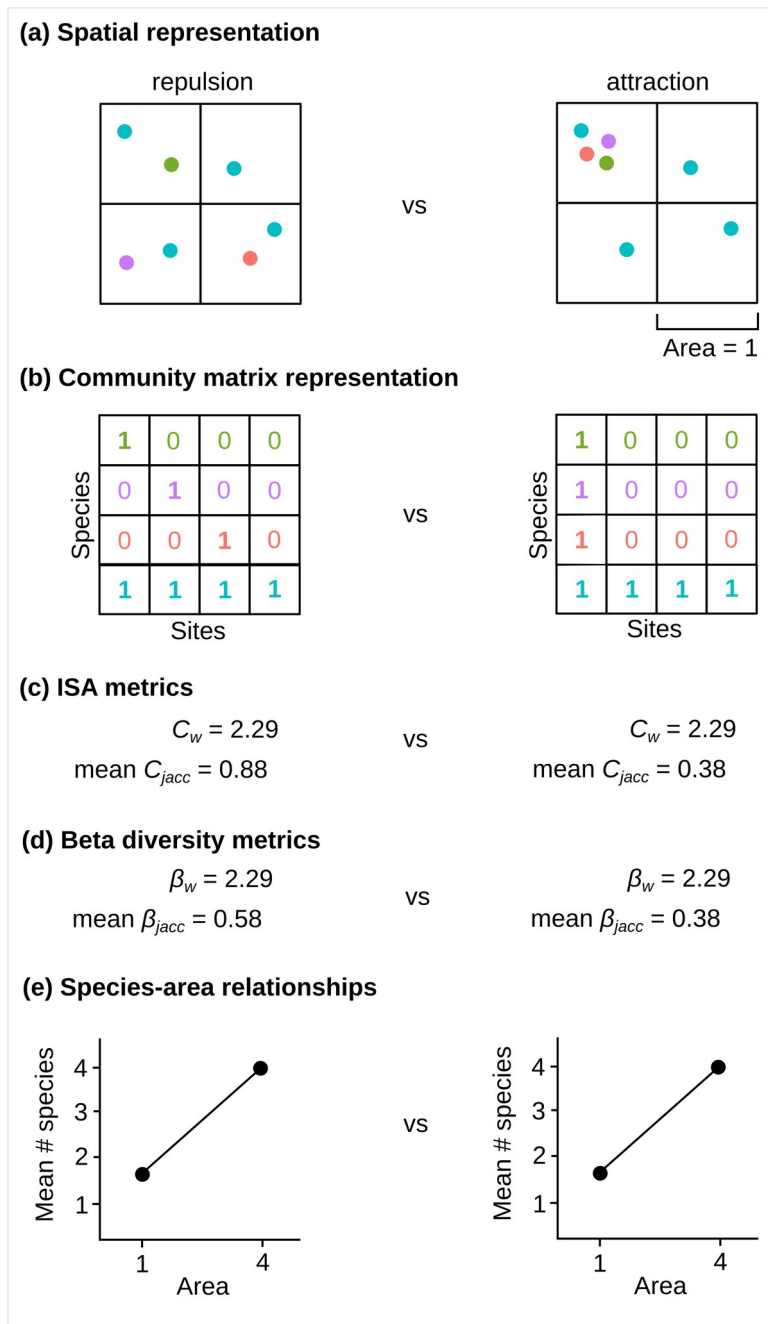
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802 **Figure 1** The difference between con-specific spatial association (CSA, vertical gradient) and inter-
803 specific association (ISA, horizontal gradient), where the latter is the subject of this paper. Points are
804 individuals, colours mark species.

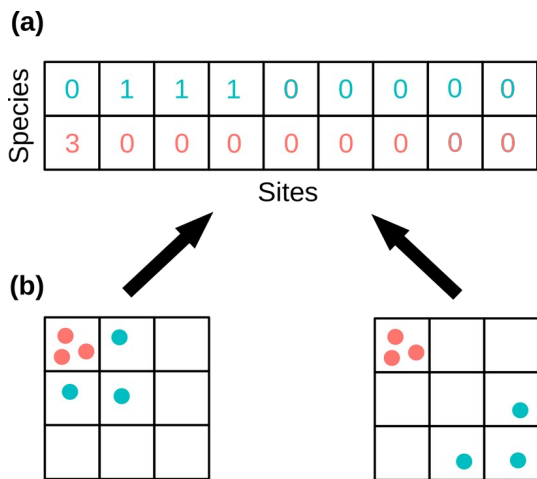


805 **Figure 2** Insensitivity of species-area relationships and Whittaker’s index to ISA. (a) Two
 806 communities consist of 4 square sites each, with 4 species (colours). The communities differ in the
 807 magnitude of pairwise ISA; species in the left one are segregated, those in the right one are attracted
 808 to each other. (b) These communities can be described by spatially implicit community matrices Y
 809 from which metrics of ISA (c) can be calculated. While the C_w metric remains constant in both
 810 communities, the mean pairwise C_{jacc} correctly reflects ISA. (d) The same logic applies when beta
 811 diversity measures such as β_w and β_{jacc} , where the former is simply a ratio of gamma diversity (total
 812 richness of a community) and mean alpha diversity (mean richness across sites), which is also the
 813 slope of slope of SAR, which remains constant even though ISA changes (e). Beware that β_w and C_w
 814 are the same thing (Arita 2017), which severely limits their interpretation as either beta diversity or
 815 ISA metric.

Schools of thought	Typical data	Example metrics	Visual representations	Software																								
<p>Assembly rules Coexistence theory Metacommunities Cody & Diamond (1975) Ulrich & Gotelli (2010)</p> <p>Phytocoenology Ordinations Braun-Blanquet (1964) ter Braak (1988)</p>	<p>Incidence matrix</p> <p>Sites</p> <table border="1"> <tr><td>Sp1</td><td>1</td><td>0</td><td>1</td></tr> <tr><td>Sp2</td><td>1</td><td>1</td><td>0</td></tr> <tr><td>Sp3</td><td>0</td><td>1</td><td>0</td></tr> </table> <p>Abundance matrix</p> <p>Sites</p> <table border="1"> <tr><td>Sp1</td><td>3</td><td>0</td><td>1</td></tr> <tr><td>Sp2</td><td>1</td><td>2</td><td>0</td></tr> <tr><td>Sp3</td><td>0</td><td>3</td><td>0</td></tr> </table>	Sp1	1	0	1	Sp2	1	1	0	Sp3	0	1	0	Sp1	3	0	1	Sp2	1	2	0	Sp3	0	3	0	<p>Species-wise (1 species) SCA metric</p> <p>Pair-wise metrics (2 species) Togetherness C_{tog} C-score C_{seg} Jaccard index C_{jacc} Covariance CA_{cov} Pearson correlation CA_{cor}</p> <p>Matrix-wise summary metrics (all species) Variance ratio C_{ratio} Connectance C_{conn} Mean pairwise metrics</p>	<p>Graph</p> <p>Ordination diagram, k-means clusters</p> <p>Corplot</p>	<p>Metrics: EcoSimR bipartite vegan spaa coocur</p> <p>Visuals: corrplot qgraph cluster ade4 vegan</p> <p>Signif. tests: EcoSimR</p>
Sp1	1	0	1																									
Sp2	1	1	0																									
Sp3	0	1	0																									
Sp1	3	0	1																									
Sp2	1	2	0																									
Sp3	0	3	0																									
<p>Geostatistics Wagner (2003)</p>	<p>Georeferenced Incidences at sites</p> <p>Georeferenced abundances at sites</p>	<p>Distance-dependent covariance, or other pairwise metrics</p>	<p>Community variogram</p>	<p>vario</p>																								
<p>Point pattern analysis Wiegand & Moloney (2014)</p>	<p>Fully mapped sites</p> <p>Fully mapped region</p>	<p>$D_{12}(r)$ $K_{12}(r)$ Bivariate Pair Correlation Function (PCF) P-M classification Species Mingling Index Mean Compositional Information $F(r)$</p>	<p>Bivariate PCF plot</p> <p>P-M classification plot</p>	<p>Programita spatstat</p>																								

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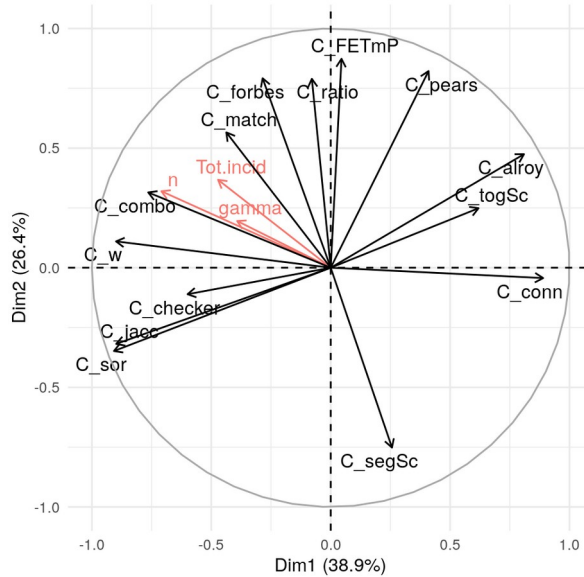
817 **Figure 3** Approaches to capturing inter-specific spatial association (ISA) among species, classified by
 818 the broad ecological schools of thought, together with typical data that are used in the approaches.
 819 Note that there is a gradient of the amount of information/detail in the data. With the exception of
 820 Programita, all the listed software consists of R packages.



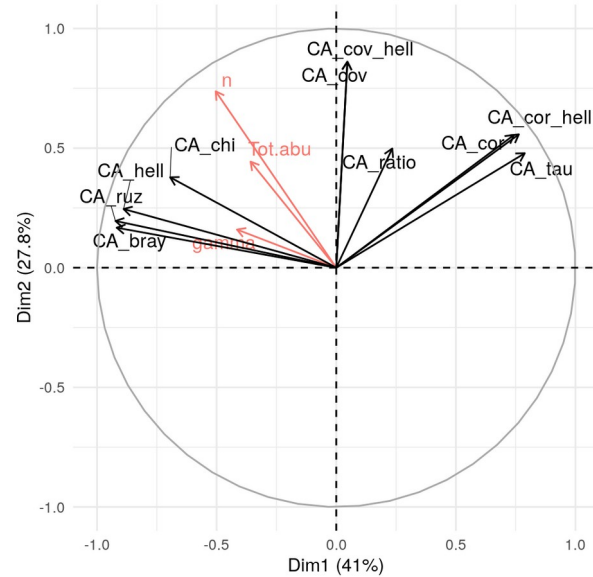
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822 **Figure 4** The fundamental importance of spatial distance in ISA. A single community matrix (a)
 823 reflects two different spatial arrangements of the community (b), each with a different magnitude of
 824 ISA - the two species in the left spatial matrix are more attracted, while on the right they are more
 825 segregated, yet this is not in any way reflected by the community matrix.

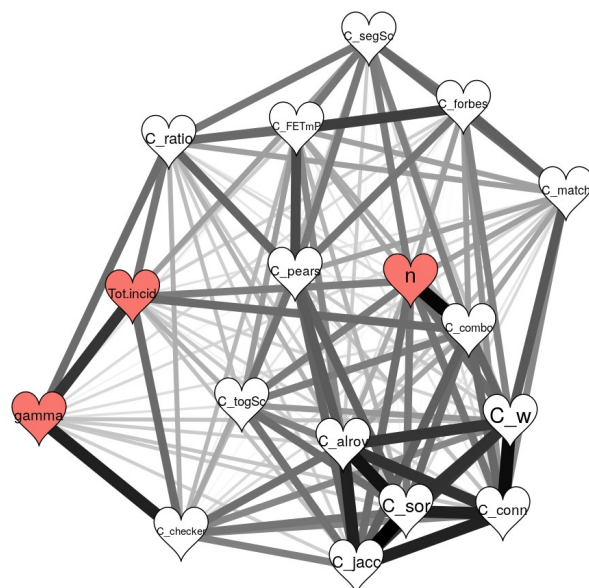
(a) Binary data - PCA



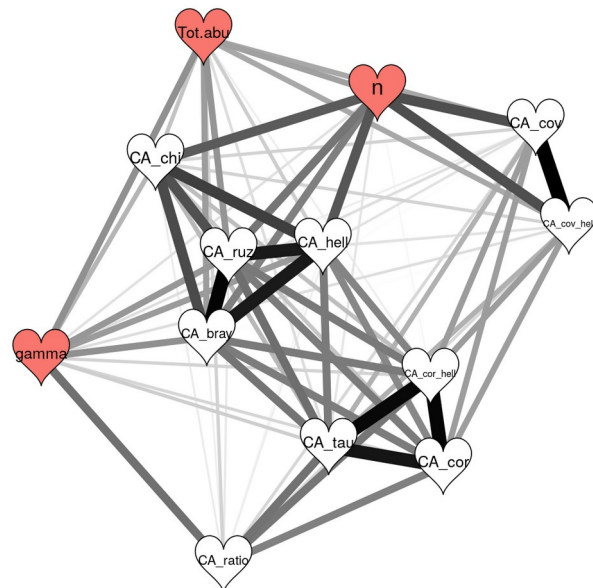
(b) Abundance data - PCA



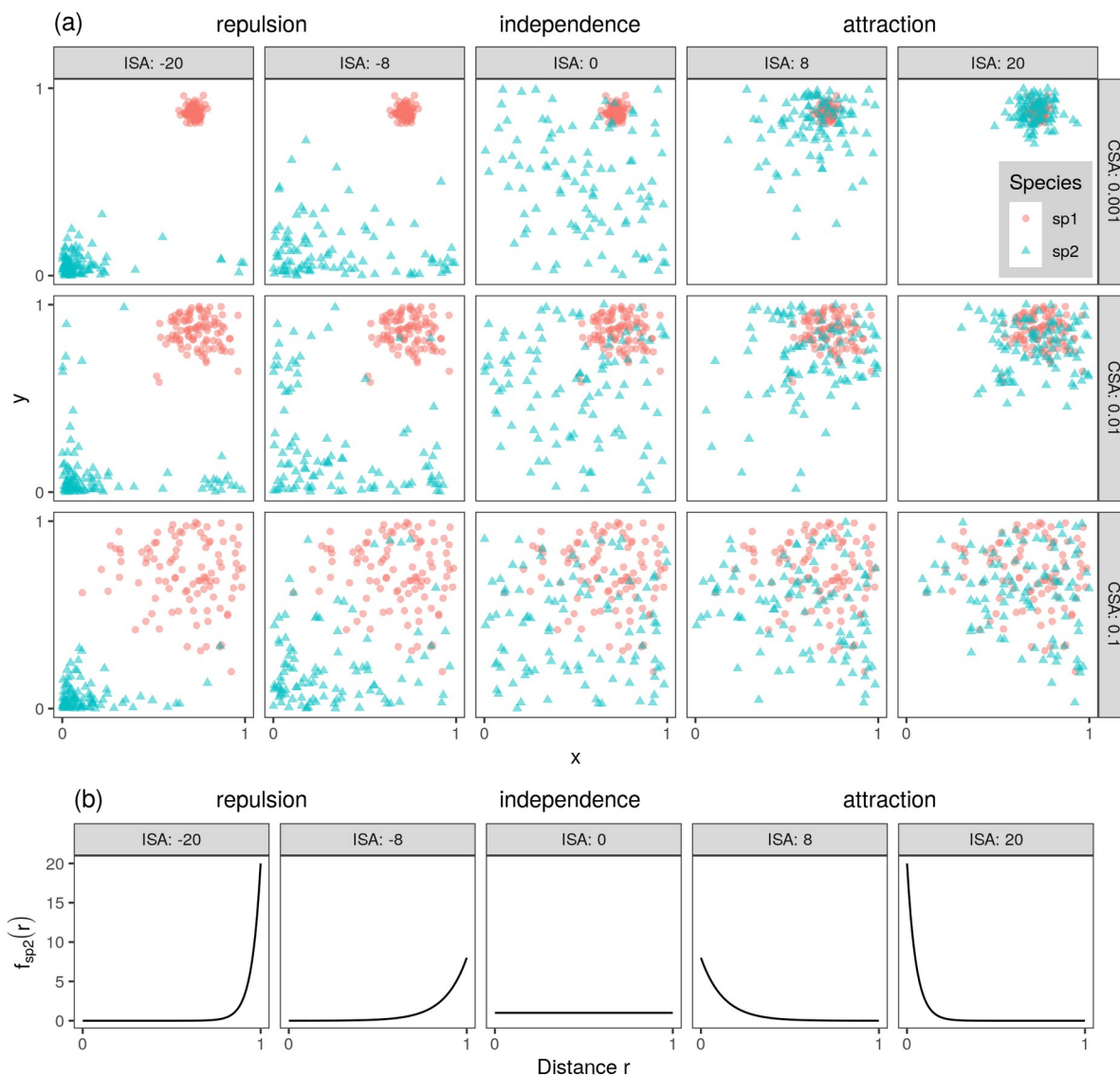
(c) Binary data - graph



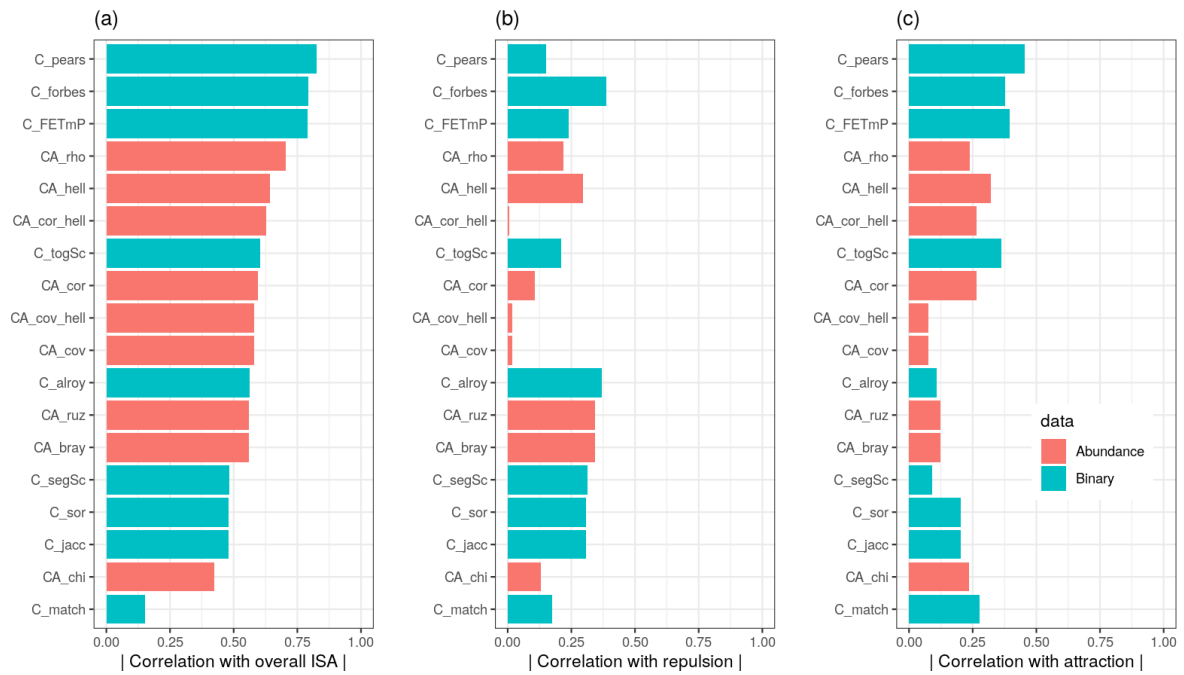
(d) Abundance data - graph



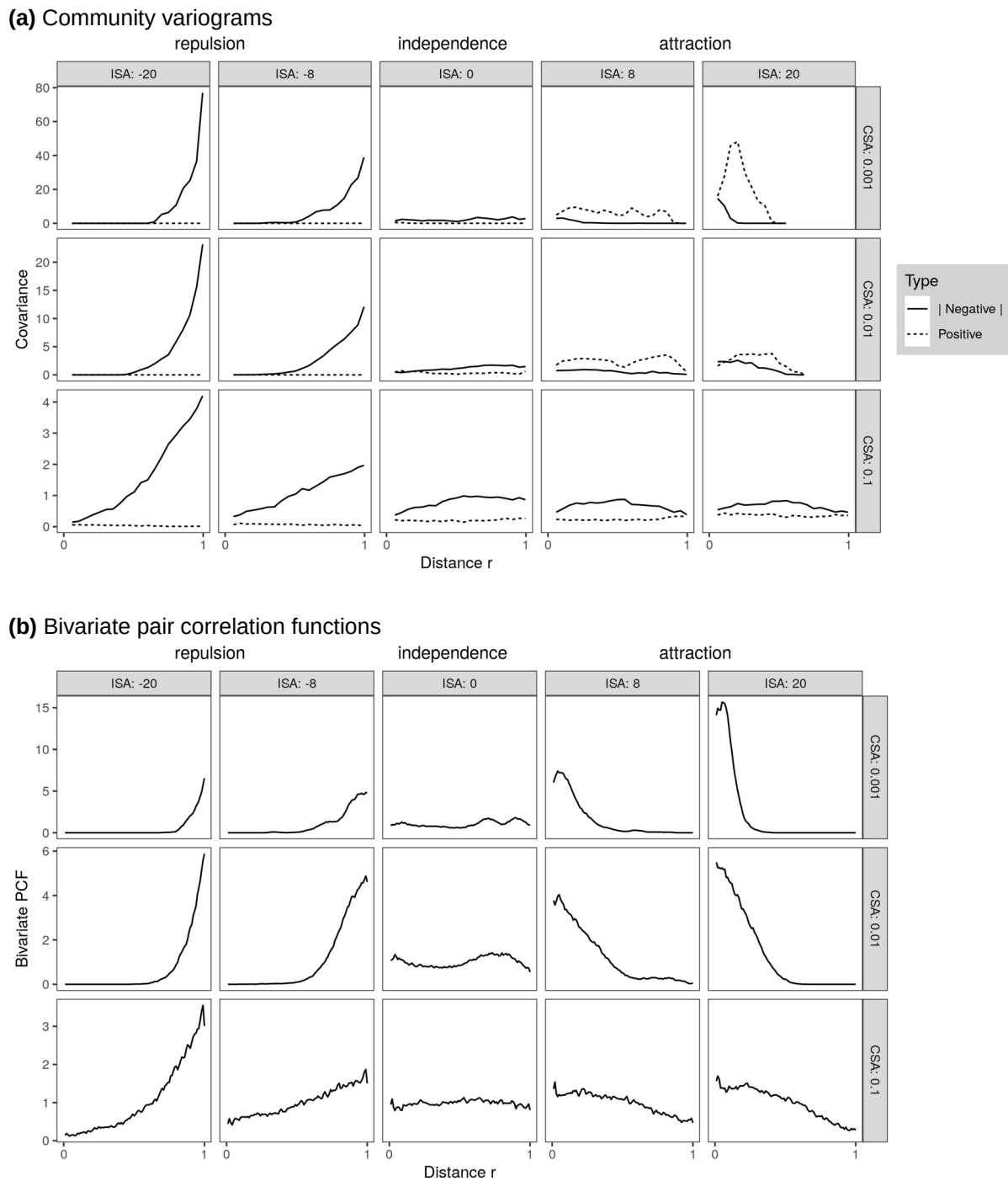
826 **Figure 5** Comparison of ISA metrics calculated on empirical community matrices of Atmar and
 827 Patterson (1995) and Ulrich and Gotelli (2010). Panels (a-b) use the binary measures from Table 2,
 828 and are based on binary (presence/absence) version of all matrices. Panels (c-d) use the abundance-
 829 based measures of Table 3, and use only the abundance matrices of Ulrich and Gotelli (2010). Panels
 830 (a-b) show first two axes of principal components analysis (PCA), panels (c-d) show a graph
 831 representations of correlation matrices between the metrics. Red indicates variables that are not ISA
 832 metrics.



833
 834 **Figure 6** (a) Simulated spatial distributions of individuals (points) of two species (sp1 and sp2) in a
 835 square domain under 3 levels of con-specific aggregation (CSA) of sp1 and 5 levels of inter-specific
 836 aggregation (ISA). (b) Truncated exponential probability density function [$f_{sp2}(r)$ (Keil 2014)]
 837 describes how likely is to observe an individual of sp2 at a given distance from any individual of sp1.
 838 This $f_{sp2}(r)$ is convenient since its shape depends on a single parameter (here called ISA) which
 839 represents various magnitudes of inter-specific repulsion (left) and attraction (right) and their
 840 relationship with distance. Similar figure was also used in Keil (2019).



841
 842 **Figure 7** Ability of pairwise spatially implicit metrics from Table 1 and 2 to recover the magnitude of
 843 ISA from spatially explicit simulations. Panel (a) shows overall correlation between the true ISA and
 844 the metric. Panels (b) and (c) show the correlation when only inter-specific repulsion is considered
 845 (ISA < 0) or when only positive attraction is considered (ISA > 0). Given are absolute values of
 846 Spearman correlation coefficient. Note that some metrics very well separate negative from positive
 847 associations (i.e. they have good correlation with overall ISA), but within these two categories they
 848 have weak correlation with the underlying ISA parameter, e.g. covariance-based measures (CA_{cov} ,
 849 CA_{cov_hell}). See Fig. S5 for details of these relationships.



850 **Figure 8.** Ability of two spatially explicit approaches to recover ISA patterns of the two species from
 851 Figure 4. (a) Community variograms calculated on abundance data obtained by aggregation of the
 852 point pattern in a 20 x 20 pixel grid. Also, 200 points were simulated for each species, instead of the
 853 100 points in Fig. 4. (b) Bivariate pair correlation function calculated directly from the point patterns.

Supplementary material

This is supplementary material for manuscript “*Interspecific spatial associations as a facet of biodiversity, and a review of approaches to measure them*” by Petr Keil, Thorsten Wiegand, Anikó B. Tóth, Daniel McGlenn, and Jonathan M. Chase.

Appendix S1 - Glossary

Several attempts have been made to clarify the terminology of spatial associations and resemblance in the sites vs. species context (Hubálek 1982, Legendre and Legendre 2012), but the consensus is not entirely clear and many of the offered definitions are author- or study-specific. Here we provide what we see as rough signal across the literature that we have reviewed:

- **Inter-specific** and **hetero-specific** are used synonymously for relationships among individuals of two or more species.
- **Intra-specific** and **con-specific** are used synonymously for relationships among individuals within a single species.
- **Association** is a general term that describes any of mutual arrangement of spatial positions of two or more species, irrespectively to its direction, range of values, or particular interpretation.
- **Resemblance** is more general than association. Legendre and Legendre (2012) use association for relationships among species, while resemblance is the more general term applicable to both beta diversity among sites and association among species.
- **Co-occurrence** can be used for an occurrence of two or more species at a given site, or it can be used for a magnitude of the observed inter-specific association. It is usually reserved for binary (presence/absence) data. Co-occurrences should not be confused with biotic interactions.
- **Similarity** (and its mathematical complement, **dissimilarity**) are measures of resemblance that always take values between 0 and 1, are not metric, but can be converted/re-scaled to metric distances.
- **Distances** are measures of resemblance that have a minimum at 0, but can have various upper bounds (including infinity), depending on the constraints of the space in which they are measured.
- **Correlation-based metrics of resemblance** are centered around 0 (no relationship), with values > 0 for positive relationship, and < 0 for negative relationship. They can be converted/re-scaled to take values between 0 and 1.
- **Repulsion or segregation vs attraction or aggregation.** These usually refer to negative vs positive spatial associations among species, but they are often also used for con-specific patterns. A typical example is aggregation, which is often used for spatial clumping among conspecific individuals.
- **Biotic interaction** or **inter-specific interaction** is an effect of individuals of one species on individuals of other species (it can also be mutual). Examples are predation, mutualism, parasitism, or competition. Interactions do influence interspecific spatial associations, but usually together with other factors.

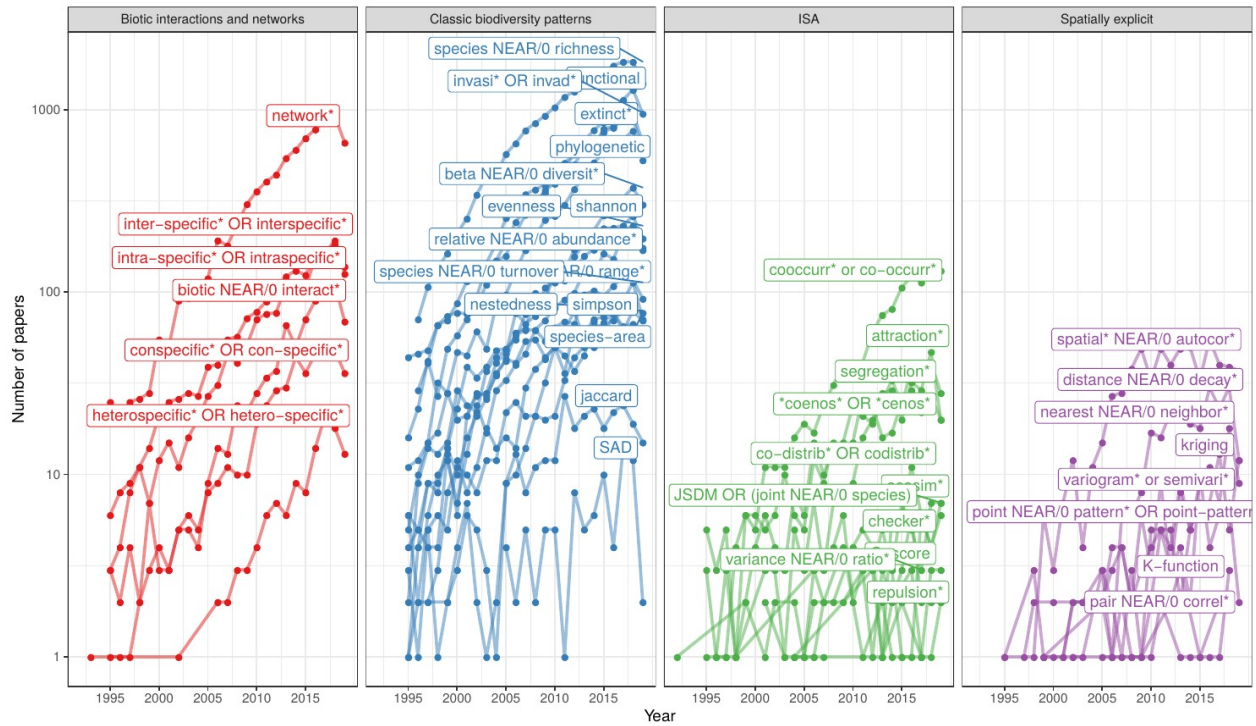


Figure S1 Temporal trends in sub-fields of biodiversity science. Y-axis shows the total number of papers published in a given year that are listed on Clarivate Web of Science, and that contain the search given term AND biodiversity. Note the \log_{10} scale of the y-axis. Left plot (red lines) shows terms related to general notion of association and interaction among species. Second to the left plot (blue lines) shows terms associated with classical biodiversity patterns in space and time. Second to the right plot (green lines) shows terms specifically related to ISA. Right plot (purple lines) shows terms related to spatially explicit aspects of biodiversity. The search was done on 19 Sep 2019. The data and code for this plot are available from the online repository at <https://github.com/petrkeil/spasm>.

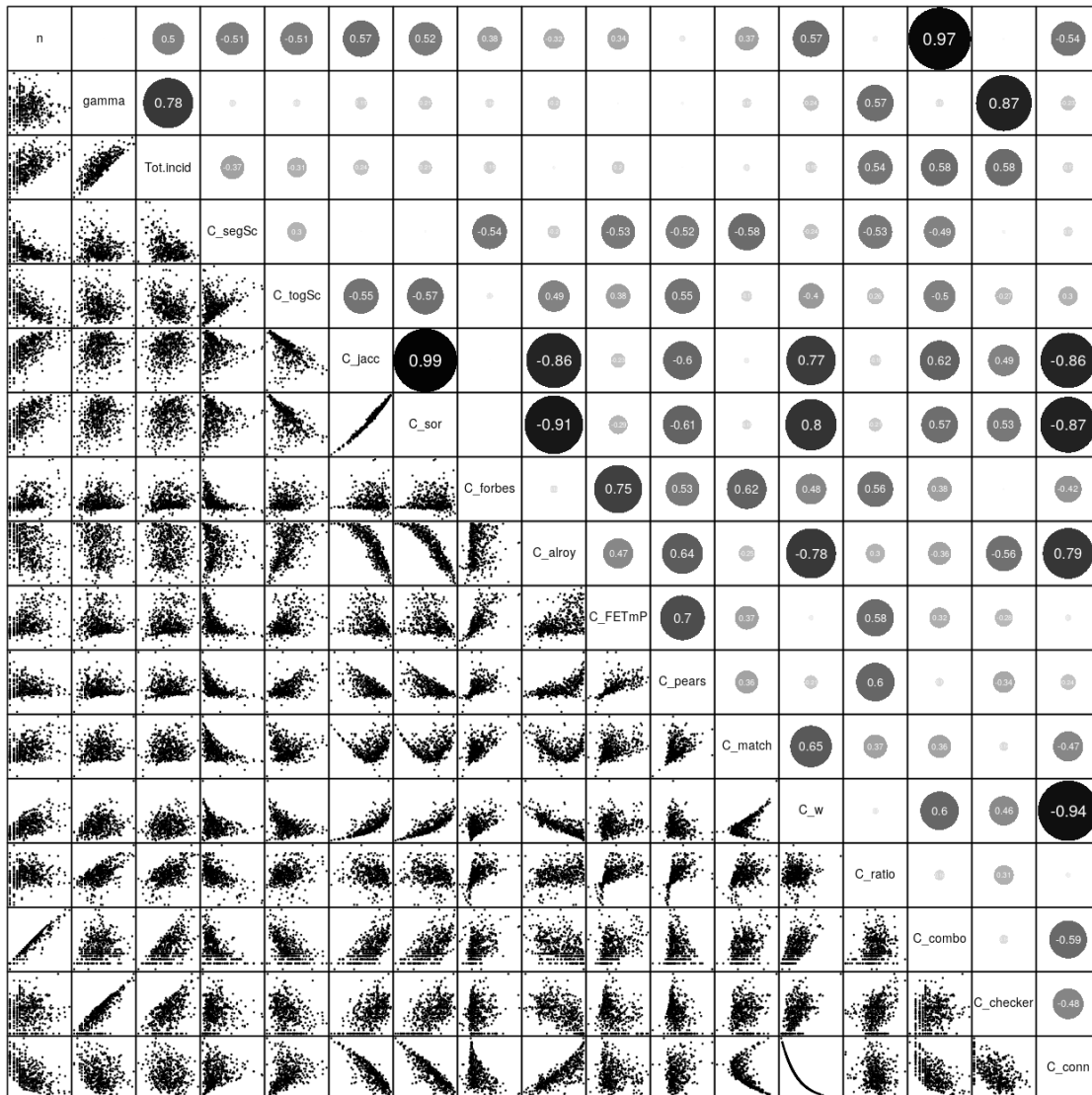


Figure S2 Correlations between ISA metrics for binary data from Table 2 applied to the empirical community matrices by Atmar and Patterson (1995) and Ulrich and Gotelli (2010). In case of the pairwise metrics, each point represents the mean value of the entire matrix. N , Gamma, and Tot.incid are numbers of sites, species, and incidences (i.e. matrix fill) respectively. C_{forbes} , C_w , C_{combo} , C_{ratio} , n , gamma, and Tot.incid were log-transformed. C_{segSc} , C_{togSc} , $C_{checker}$, were $\log(x+1)$ transformed. Numbers in the upper triangular section are Pearson correlations, with size and grey intensity proportional to the magnitude of the correlation.

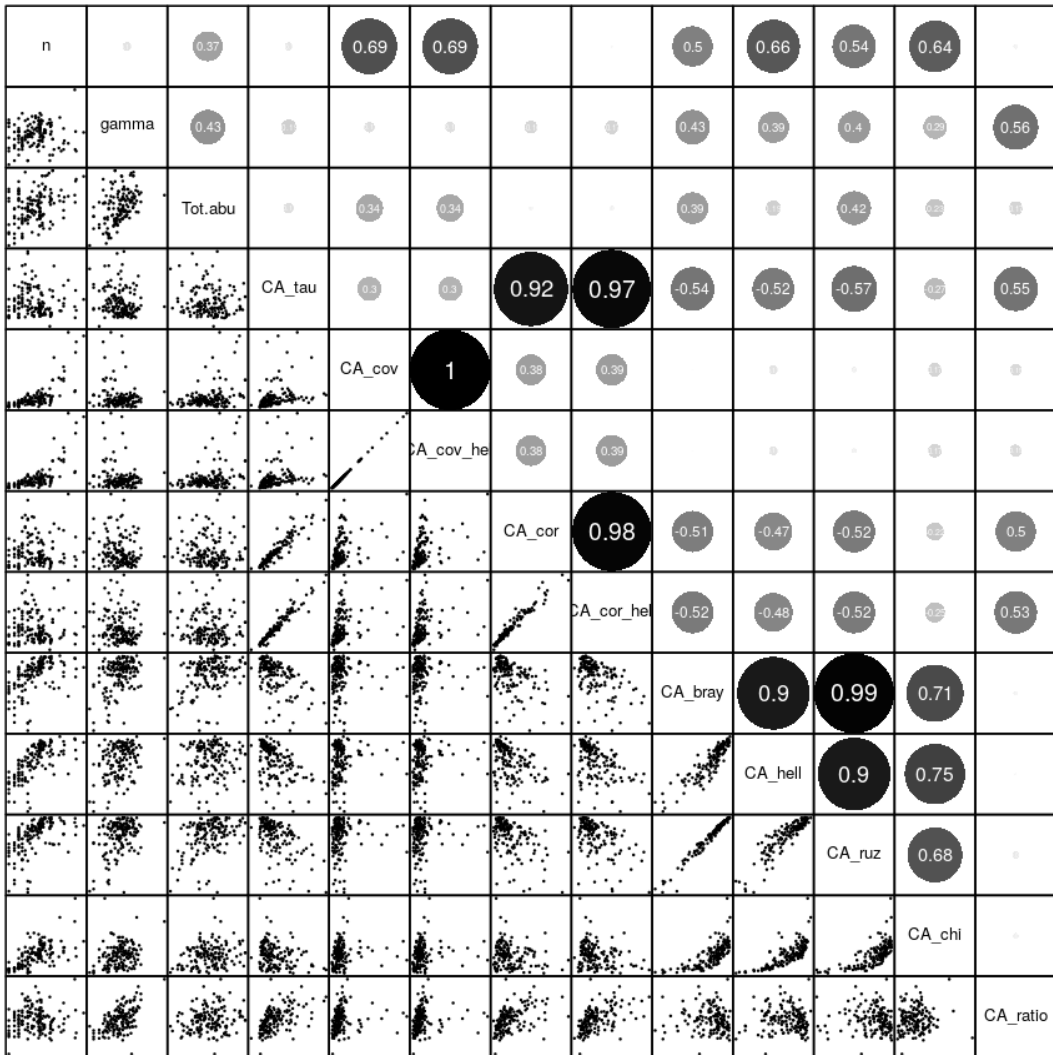


Figure S3 Correlations between ISA metrics for abundance data from Table 2 applied to the empirical community matrices by Ulrich and Gotelli (2010). In case of the pairwise metrics, each point represents a mean value of the entire matrix. n , γ , and Tot.abu are numbers of sites, species, and the total number of individuals in the entire community matrix respectively. CA_{ratio} , CA_{cov} , CA_{cov_hell} , n , γ , and Tot.abu were log-transformed. Numbers in the upper triangular section are Pearson correlations, with size and grey intensity proportional to the magnitude of the correlation.

Appendix S2 - Exact simulation procedure

Why only pairs? We refrained from simulating spatially explicit spatial association between more than two species, since the simulated patterns would need to achieve specified spatial association between each pair of species simultaneously, as well as the decay (or increase) of each of these associations with distance. Although the most recent advances in multivariate geostatistics may enable this (Genton and Kleiber 2015), these methods are still young, not widely available, and are computationally challenging to simulate cross-covariance structures of more than 3 layers (species). Further, there is the limit on the magnitude of negative associations in multi-species matrices (Brown et al. 2004) which would prevent us from exploring scenarios with strong negative ISA. As a result, we only evaluated pairwise measures of ISA. For each ISA metric we measured its correlation with the ISA parameter across all simulation setting.

Simulations. We simulated spatially explicit distributions of two species, sp1 and sp2 with abundances N_1 and N_2 respectively, as two point patterns in a square domain with side of 1 (Fig. 6a in the main text). One simulation proceeded as follows:

- (Fig. S4a) We chose a random point with coordinates μ_x and μ_y within the domain, with uniform probability density across the domain; this point was the center of distribution of sp1.
- (Fig. S4b) We created 2-dimensional probability density of points of sp1 as a bivariate normal distribution $f_{sp1}(\mu, \Sigma)$, where Σ is the covariance matrix with marginal variances $\sigma_x = \sigma_y = CSA$ and with covariance $\sigma_{xy} = 0$. μ is the vector of coordinates μ_x and μ_y .
- (Fig. S4c) We drew N_1 points from that probability density surface. These are individuals of species 1.
- (Fig. S4d) For every location in the domain we calculated its distance r from the nearest point of sp1.
- (Fig. S4e) We transformed r using a truncated exponential function (Keil 2014)

$$f_{sp2}(r) = \frac{\alpha e^{\alpha r}}{e^{\alpha b} - e^{\alpha a}} \text{ where } r \in [a, b], \text{ where } a=0 \text{ and } b=1, \text{ but these truncation points can be set}$$

to any value depending on the size of the domain. We use the negative value of parameter α as the strength of interspecific association ($ISA = -\alpha$), with $ISA < 0$ being segregation, $ISA = 0$ for independence, and $ISA > 0$ being positive attraction between species.

- (Fig. 4b) We drew N_2 points from from the $f_{sp2}(r)$. These are individuals of species 2.

We repeated this procedure for each combination of the following parameter values:

$CSA \in \{0.001, 0.01, 0.1\}$, $N_1 \in \{10, 100, 1000, 10000\}$, $N_2 \in \{10, 100, 1000, 10000\}$, and for

$ISA \in \{-20, -17.5, -15, \dots, 0, \dots, 15, 17.5, 20\}$, which we then aggregated to square spatial grids with

$\{32, 16, 8, 4\}$ grid cells along each side. Thus, the value of 32 represents the finest (smallest) grain, and

4 the coarsest (largest) grain. Altogether, this produced 3264 simulated pairs of species, each represented

by either a point pattern or a grid, and we further converted to 3264 community matrices Y , with either abundance or incidence values, and with known exact spatial position of each grid cell.

Analysis of the simulations. For each of the simulated community matrices Y (each with 2 species) we calculated the pair-wise incidence-based ISA measures from Table 2, and the abundance-based measures from Table 3. In some of the measures we also tested their Z-score variant, calculated as $(E_{raw} - E_{exp})/SD_{exp}$, where E_{raw} is the ISA metric (from Tables 2 and 3) calculated on observed data, E_{exp} is the null expectation of the index, and SD_{exp} is the standard deviation of the null expectation calculated over a set of community matrices obtained by 200 randomizations of Y . The randomizations were as follows: For the incidence matrices, we took the total number of incidences of each species, randomly assigned each of the incidence to a new site with uniform probabilities for each site, which corresponds to the “sim2” algorithm of EcoSimR package (Gotelli et al. 2015). For the abundance-based measures we randomly re-assigned each individual to a new site with uniform probability. Thus, in both algorithms, incidences or individuals are reshuffled only within each row of Y , irrespectively to the matrix column totals. In case of the abundance data, we also tried to run the simulations with the IT algorithm of Ulrich and Gotelli (2010), but the results were similar. To evaluate performance of each metric, we calculated its Spearman’s Rho (rank-rank correlation) with the ISA parameter across all 4,080 simulations. All functions and scripts for the simulations and their analysis are provided at <https://github.com/petrkeil/spasm>.

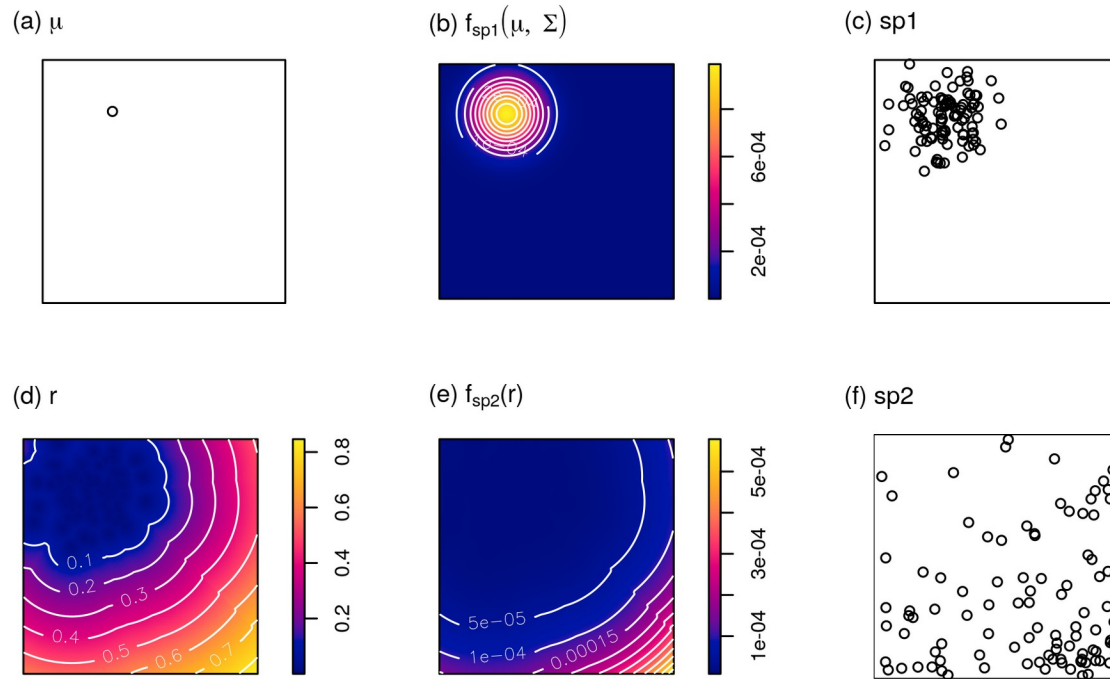


Figure S4 Simulation of two point patterns of two species, sp1 and sp2. The procedure is described in the main text. Briefly, point pattern of sp1 is simulated as a point process with bivariate normal probability density $f_{sp1}(\mu, \Sigma)$ with zero covariance and marginal variances describing the con-specific aggregation (CSA) of sp1. Point pattern of sp2 is then simulated as a point process with $f_{sp2}(r)$ describing the magnitude of ISA, where r is distance to the nearest point of sp1. This figure was also used in Keil (2019).

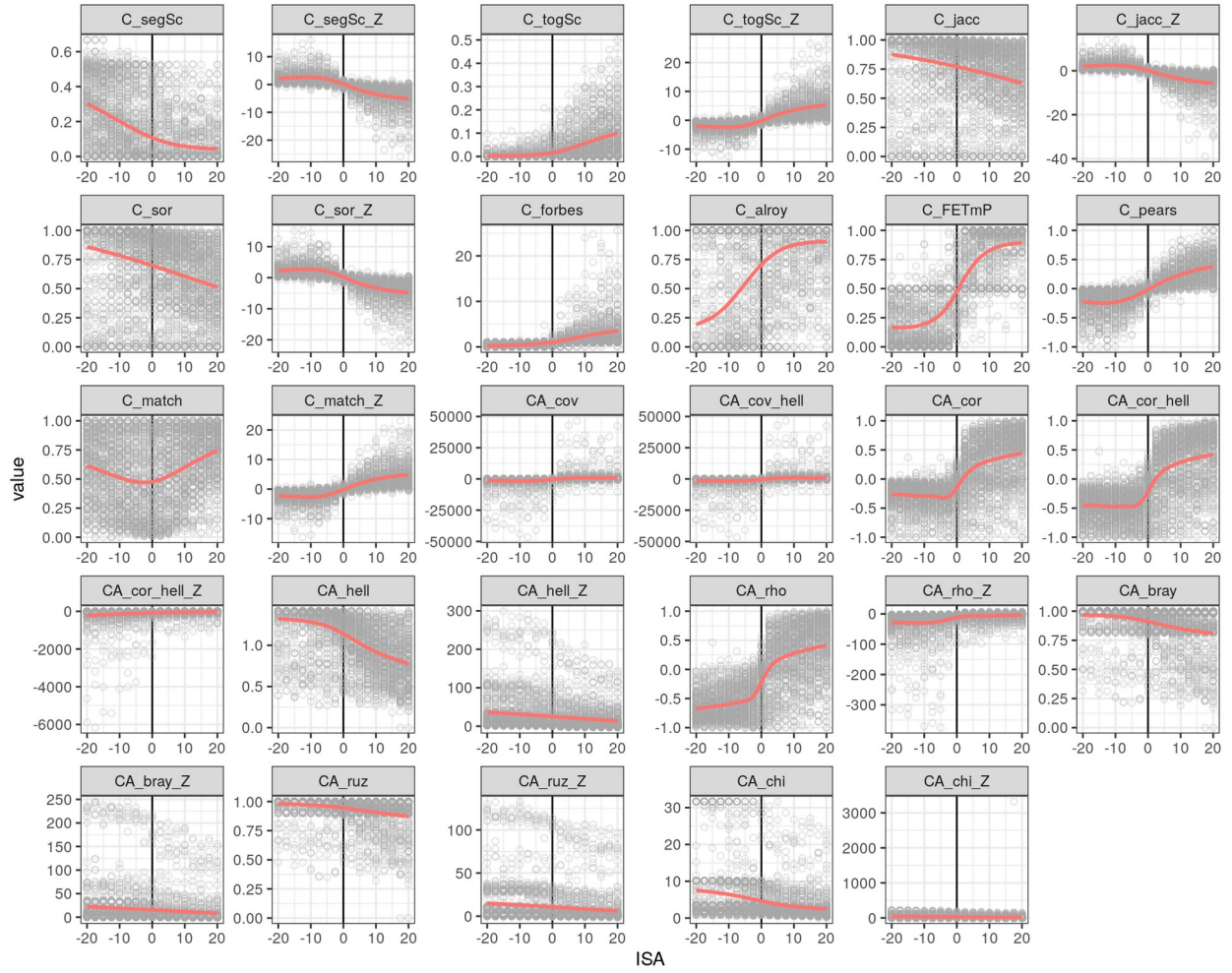


Figure S5 Relationships between the magnitude of ISA in artificial 2-species point pattern communities, and indices (measures) of ISA. These plots are the basis for Figure 7 in the main text.

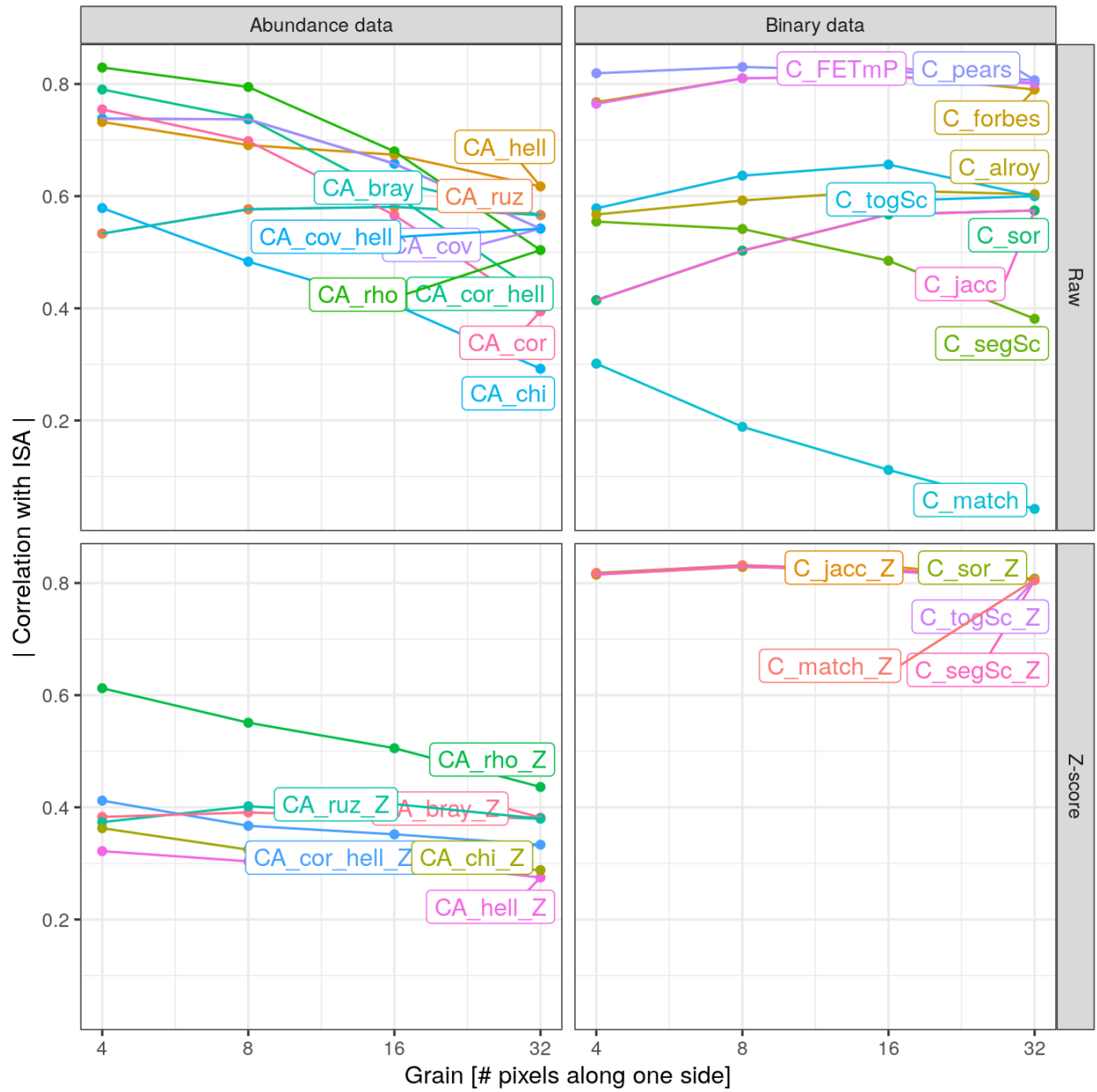


Figure S6 Relationship between the performance of ISA metrics and spatial grain that was used to aggregate point patterns. The performance is the absolute value of Spearman correlation between parameter ISA and the metric.

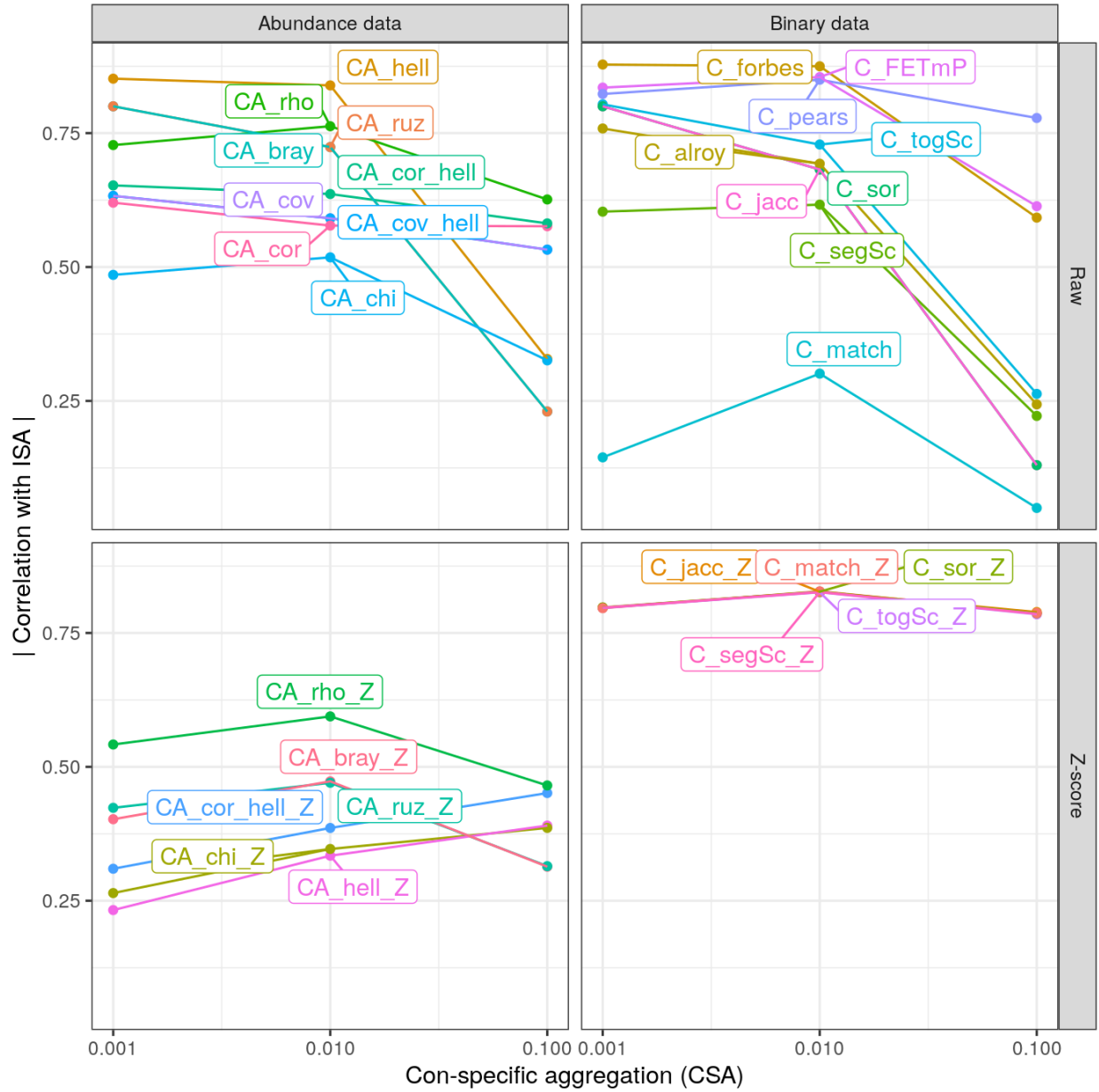


Figure S7 Relationship between the performance of ISA metrics and the magnitude of con-specific aggregation of species 1 in the simulations. The performance is the absolute value of Spearman correlation between parameter ISA and the metric.

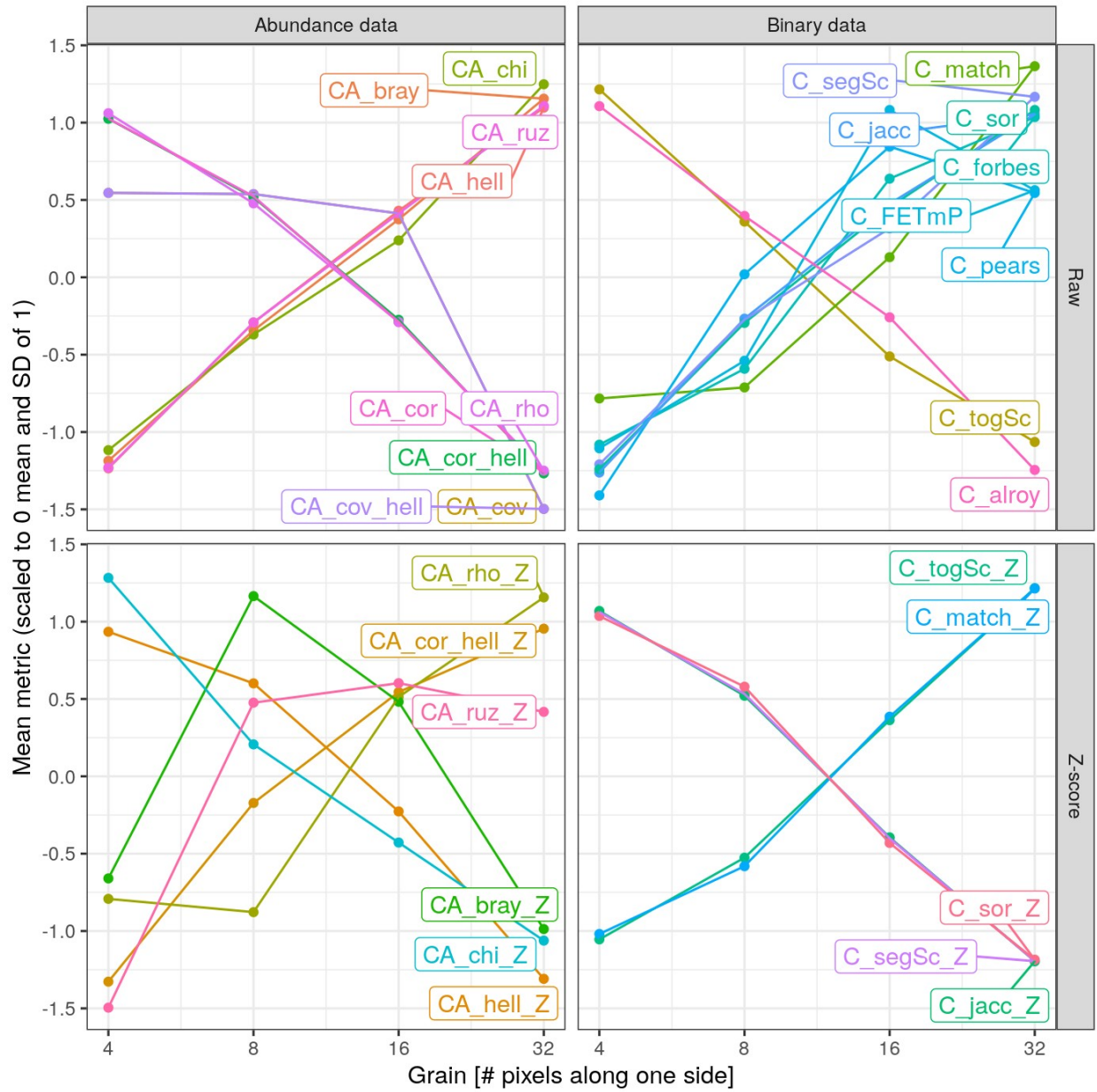


Figure S8 Relationships between mean metrics of ISA and spatial grain that was used to aggregate point patterns. The y-axis is the scaled (to 0 mean and SD of 1) value of the mean across all simulations at a given grain.

Supplementary references

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