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42	

### Abstract

The concept of evolvability-the capacity of a population to produce and maintain evolutionarily 44 45 relevant variation—has become increasingly prominent in evolutionary biology. Although 46 paleontology has a long history of investigating questions of evolvability, often invoking 47 different but allied terminology, the study of evolvability in the fossil record has seemed 48 intrinsically problematic. How can we surmount difficulties in disentangling whether the causes 49 of evolutionary patterns arise from variational properties of traits or lineages rather than due to selection and ecological success? Despite these challenges, the fossil record is unique in offering 50 51 growing sources of data that span millions of years and therefore capture evolutionary patterns of 52 sustained duration and significance otherwise inaccessible to evolutionary biologists. 53 Additionally, there are a variety of strategic possibilities for combining prominent neontological 54 approaches to evolvability with those from paleontology. We illustrate three of these possibilities with quantitative genetics, evolutionary developmental biology, and phylogenetic models of 55 56 macroevolution. In conclusion, we provide a methodological schema that focuses on the 57 conceptualization, measurement, and testing of hypotheses to motivate and provide guidance for 58 future empirical and theoretical studies of evolvability in the fossil record. 59

Keywords: constraints, disparity, evo-devo, evolutionary potential, integration, macroevolution,
 modularity, quantitative genetics, variability, versatility

### 63 1. Introduction

The term "evolvability" refers to those characteristics that confer a disposition to evolve 64 65 under a causal stimulus, such as natural selection. In most modern usages, evolvability is tied to 66 the ability of a population to produce and maintain evolutionarily relevant genetic variation 67 (Crother and Murray 2019). Evolvability has become increasingly prominent in evolutionary 68 biology through studies that adopt approaches from quantitative genetics (Hansen and Houle 2008), evolutionary developmental biology (evo-devo) (Hendrikse et al. 2007, Tiozzo and 69 Copley 2015), phylogenetic models of macroevolution (Hunt and Slater 2016), and experimental 70 71 evolution (Colegrave and Collins 2008). 72 Although paleontology has a long history of investigating questions of evolvability (e.g., 73 Eldredge and Gould 1972, Simpson 1944), often invoking different but allied terminology (e.g., 74 constraint or versatility sensu Vermeij 1973a, b), the study of evolvability in the fossil record has 75 seemed intrinsically problematic. This is largely because of difficulties in disentangling whether 76 the causes of evolutionary patterns arise from variational properties of traits or lineages 77 ('evolvability' features) or properties of the abiotic or biotic environment (sources of selection 78 and ecological success), both of which might generate similar if not indistinguishable outcomes 79 in deep time (Jablonski 2017a, b, 2020, Jackson 2020). These difficulties are often viewed as a 80 rationale for investigating questions about evolvability using other, primarily neontological 81 approaches because they harbor the promise of discriminating between variational contributions 82 and selective components, especially through experimental manipulation of variables related to trait generation or selective regime under highly controlled conditions (Colegrave and Collins 83 84 2008, Payne and Wagner 2019).

85 Importantly, this rationale ignores the distinctive empirical resources that paleontological 86 studies bring to questions about evolvability. Despite the challenges of disentangling the 87 variational and environmental causal factors responsible for evolutionary trajectories in the 88 history of life, the fossil record is unique in offering data that span millions of years and 89 therefore capture evolutionary processes of sustained duration and significance that are otherwise 90 inaccessible to evolutionary biologists (Bell 2014, Dilcher 2000, Jablonski and Shubin 2015; 91 Jackson 2020). Studies of the differential rates of evolution in lineages and the propensity for 92 specific traits to contribute to adaptive radiations can relate directly to evolvability and may be 93 best seen empirically in the realm of the fossil record. At a minimum, it is critical to find an 94 appropriate balance between what paleontology is uniquely positioned to offer to the study of 95 evolvability, and what is impossible as a result of the absence or loss of pertinent information. 96 Paleontology not only offers an unparalleled and ever-increasing data resource, but its 97 value is augmented when combined strategically with other approaches to evolvability. Consider 98 first the intersection of quantitative genetics and paleontology. A pioneering study (Cheverud 99 1988) suggested that a standardized summary of the multivariate phenotypic relationships among 100 a set of traits (i.e., the P matrix, or phenotypic variance-covariance matrix), which can be derived 101 from fossil evidence, could serve as a reliable proxy for the standardized summary of 102 multivariate genetic relationships among a set of traits (i.e., the G matrix, or additive genetic 103 variance-covariance matrix), whose geometry shapes the direction of evolution in response to 104 selection (Lande 1979). Subsequently, a number of studies have profitably analyzed 105 morphological traits using fossil data that take advantage of this proxy inference (e.g., 106 Brombacher et al. 2017a, Hunt 2007, Renaud et al. 2006). Another example is found in 107 combining evo-devo approaches with paleontology. On the assumption that ontogenetic

108 processes are conserved from fossil taxa to their modern relatives, sufficient developmental 109 information can yield predictions about which traits and lineages may be more likely to produce 110 abundant phenotypic variation relevant to evolutionary processes (Urdy et al. 2013), such as 111 models of mammalian molar development predicting the evolvability of different dental traits 112 (e.g., Jernvall 2000, Salazar-Ciudad and Jernvall 2010). A third example is how evolvability has 113 been analyzed using phylogenetic models at the level of macroevolution, where different modes 114 of evolutionary change for traits (e.g., directional selection or punctuated equilibrium) can be 115 correlated with key variables such as speciation rates in a lineage (Rabosky 2012). Increased 116 evolvability was implicated in dramatic morphological evolution via changes to the structure of 117 developmental modules using phylogenetic models (Parins-Fukuchi 2020).

118 Our aim in the present paper is to make an explicit case for studying evolvability in the 119 fossil record with special attention to the advances that can be derived from fruitful cross-120 disciplinary collaborations in evolutionary biology. We begin by recalling touchstones in the 121 history of paleontology where questions about evolvability were under scrutiny, sometimes in 122 the guise of alternative terminology, and accent the unique position of the fossil record for 123 informing questions about evolvability. Next, we illustrate in detail how paleontology is working 124 in combination with other approaches to yield new insights into evolvability, focusing on three 125 primary partnerships: quantitative genetics, evo-devo, and phylogenetically-informed 126 macroevolutionary modeling. In conclusion, we offer a methodological schema that focuses on 127 the conceptualization, measurement, and testing of hypotheses for investigating evolvability that 128 yields several potential avenues of research on outstanding questions that exploit both the 129 distinctive contribution of paleontology and the interdisciplinary synergy available with other

approaches in evolutionary biology. Overall, this generates a strong motivation for empirical andtheoretical studies of evolvability in the fossil record.

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# 133 2. Evolvability and Paleontology: Classical Studies and Controversies

134 The modern concept of evolvability focuses on the variational properties of traits, 135 especially how the relationship between genotype and phenotype mediated by development 136 establishes the potential or capacity of traits to respond to drift and selection (Houle 1992, 137 Wagner and Altenberg 1996). Many paleontological studies examine phenotypic variation, 138 including those pertaining to taxonomic richness, morphological disparity, functional diversity, 139 and morphological change in single or multiple related lineages, but few directly invoke the term 140 "evolvability" or attempt to connect directly with its modern meanings. However, some classics 141 in paleontological literature stand out as pioneering ideas closely aligned with and sometimes 142 pre-dating the modern evolvability concept. For example, in Tempo and Mode in Evolution, G.G. 143 Simpson noted that the "capacity of ... animals to differ" is distinct from the expression of 144 differences among individuals (i.e., realized variation) and the inheritance of phenotypes 145 (Simpson 1944, 30), a perspective he saw explicitly in earlier paleontological discussions (e.g., 146 Rosa 1899). In a related vein, Vermeij (1973b) claimed that there was an "increase in potential 147 versatility of form" through geological time, which he supported with an example where the 148 number of parameters required to describe coiling in gastropods increased over the Phanerozoic. 149 According to Vermeij, groups with a greater potential versatility of form replaced those that 150 exhibited this capacity to a lesser degree (Vermeij 1973a).

Beyond these classic exemplars, there is a rich literature on the temporal dynamics of
morphological disparity among taxa that points to changing patterns of new traits and trait

153 combinations over long time spans (reviewed in Foote 1997, Hughes et al. 2013); some groups, 154 once evolved, seem constrained in morphospace, whereas previously occupied morphospaces, 155 once vacated, are sometimes not reoccupied. While these patterns are the combined outcome of 156 both evolvability and ecological success or failure (i.e., selection), the potential for evolvability 157 explanations has long been recognized, usually considered in terms of evolutionary constraints— 158 the lack of evolvability in some guise (Allmon and Ross 1990, Blake 1980, Erwin 2007, Gould 159 1989, Jablonski 2020, Maynard Smith et al. 1985, Raup 1967, Wright 2017). This connection 160 between morphospace exploration and evolvability was perhaps most explicit in discussions of 161 the dramatic explosion of disparity in the Cambrian Period. Two classes of (non-mutually 162 exclusive) hypotheses have been commonly considered: (i) those that emphasize ecological 163 opportunities afforded by nearly unoccupied early Paleozoic ecosystems or environmental 164 triggers such as changes in the amount of dissolved oxygen in seawater that facilitate the 165 formation of biomineralized skeletons, and (ii) those that posit genetic or developmental 166 processes facilitating elevated expression of morphological variation in the Cambrian (Erwin 167 1994, Erwin and Valentine 2013, Valentine 1995, Webster 2007, Webster 2019). The first class 168 of explanation invokes selection, whereas the second relates to evolvability. 169 Similarly, stasis within fossil species can be explained by mechanisms that are either 170 extrinsic, related to natural selection, or intrinsic, related to the variational potential of 171 populations. Eldredge and Gould's (1972) original suggestion for the cause for stasis was that 172 variational constraints would be relaxed at speciation. This particular explanation did not fare 173 well, as Gould himself later acknowledged (Gould 2002), but more modern versions suggested

175 with other traits (Hansen and Houle 2004, 2008). In opposition to these explanations are those

that stasis may result when traits lack variation or if most variation is bound up in correlations

174

that view stasis as a consequence of stabilizing natural selection (Charlesworth et al. 1982, Estesand Arnold 2007, Hunt and Rabosky 2014).

178 Extinction as a failure of evolvability is implicit in Van Valen's Red Queen Hypothesis 179 (Van Valen 1973), which envisions species at a constant risk of extinction because they must 180 continually adapt in the face of changing environments and to other species that are continually 181 improving. However, studies that explicitly test whether evolvability (as reflected in, for 182 example, trait variation) protects against species extinction are still quite rare (Hopkins 2011, 183 Kolbe et al. 2011, Liow 2007). Quantitative genetics suggests distinctive strategies for measuring 184 trait variation in the fossil record that can provide further unique insights into evolvability on 185 geological time scales.

186

### 187 **3.** Quantitative Genetics in the Rock Record

# 188 *3.1 Estimating G-matrices from P-Matrices Drawn from Fossils*

189 Evolutionary quantitative genetics is a theoretical framework linking selection and 190 genetic variation to evolutionary change (Lynch and Walsh 1998; Walsh and Lynch 2018). 191 Central to this framework is the "Lande equation" (Lande 1976, 1979, Lande and Arnold 1983), 192 which permits the response to selection to be decomposed into the (a) pattern of genetic variation 193 and covariation among traits (summarized in the *genetic* variance-covariance [G] matrix, see 194 below), and (b) strength and direction of selection on individual traits (e.g., from environmental 195 factors). This decomposition formally separates evolutionary change into evolvability-related 196 and selection-related components. Since most traits do not exist as autonomous units and are unable to respond to selection independently of other traits (Cheverud 1982a, Hansen et al. 197 198 2003a, Hansen and Houle 2008, Lande 1979, Lynch and Walsh 1998, Walsh and Blows 2009), a

multivariate theoretical formulation of natural selection and variation is necessary to gain a moresatisfactory understanding of evolutionary change.

201 In the Lande equation,  $\Delta z = \mathbf{G}\beta$ ,  $\Delta z$  is the response to selection (a vector with trait 202 changes for multiple traits), **G** is the additive genetic variance-covariance matrix (or **G**-matrix) 203 among those traits, which quantifies the role of the genetic system in evolution, and  $\beta$  is the 204 selection gradient, which quantifies the amount and direction of selection on each trait 205 independent of other traits (Fig. 1). Hansen and colleagues (Hansen et al. 2003a, Hansen and 206 Houle 2008, Hansen et al. 2003b) later used the Lande equation to develop a theoretical 207 framework connecting the G-matrix to short-term evolutionary potential through the concept of 208 evolvability (Houle 1992), which describes a population's ability to evolve in the direction of 209 selection when stabilizing selection is absent (Hansen and Houle 2008). One way of calculating a 210 trait's evolvability is to divide its additive genetic variance by the trait mean squared (i.e., 211 evolvability equals a mean-standardized additive genetic variance). This measure of evolvability 212 predicts an expected proportional response to selection that is as strong as that on fitness. For 213 example, an evolvability of 0.10 means the expected response in the trait mean per generation is 214 10% given selection as strong as selection on fitness itself. Typically, observed directional 215 selection is on the order of 10% as strong as the selection on fitness (Hereford et al. 2004). This 216 concept of evolvability also can be used to generate hypotheses about the direction and strength 217 of selection ( $\beta$ ) responsible for past evolutionary change ( $\Delta z$ ).

218

#### [Figure 1 near here]

For many evolutionary biologists and paleontologists, quantitative genetics seems
irrelevant for studies of macroevolution, including paleontology, because of empirical evidence

221 and theoretical considerations that imply G can evolve rapidly (e.g., Pigliucci 2006). If G is 222 likely to evolve within short time scales, then its power to predict evolution is severely limited. 223 Although we know G can evolve (Steppan et al. 2002), directions of diversification among 224 populations are often aligned with above-average genetic variation. Schluter (1996) was the first 225 to show empirically that G can be sufficiently stable to have a detectable influence on the 226 direction of evolution across macroevolutionary timescales and also suggested that genetic 227 constraints would predict phenotypic divergence along "lines of least genetic resistance"— 228 phenotypic divergence in directions aligned with above-average additive genetic variance (Fig. 229 1B). Several studies have found such a pattern (e.g., Bégin and Roff 2004, Blows and Higgie 230 2003, McGlothlin et al. 2018). More recently, the concept of evolvability has been used as a 231 general framework to compare genetic variation measured within populations with rates of 232 phenotypic divergence among populations across traits. There is growing evidence that 233 evolvability can predict patterns of macroevolution at surprisingly long-time scales. For 234 example, Bolstad et al. (2014) found that patterns of genetic variation in contemporary 235 populations of *Dalechampia* predicted macroevolutionary divergence within the genus. Houle et 236 al. (2017) showed that standing genetic variation within a population of Drosophila 237 melanogaster was strongly correlated with phenotypic divergence across the Drosophilidae, 238 which represents 40 million years of evolution. These studies suggest that evolutionary 239 quantitative genetics may be applicable to much longer time scales than were considered 240 previously. Paleontologists are well situated to contribute to the testing of the generality of these 241 results.

Robustly estimating G normally requires measurements of large numbers of families of
known pedigree. Properly estimating G is a major undertaking even in living populations

244 (Charmantier et al. 2014, Dochtermann 2011, Steppan et al. 2002); it is close to impossible for 245 most taxa found in the fossil record. Fortunately, the phenotypic variance-covariance matrix, P, 246 is both estimable in many paleontological settings and a possible proxy for G. P is the sum of G 247 and other sources of phenotypic variation, notably the effects of the environment. Cheverud 248 (1988) conjectured that **P** can be proportional to **G** based on three cogent arguments (Fig. 2). 249 First, quantitative traits have reasonably high heritabilities (Hansen et al. 2011), meaning that G 250 accounts for a large proportion of the variation measured by **P**. Second, the non-genetic variation 251 in **P** arises through the same developmental and physiological pathways that structure **G**, and 252 thus may have a similar pattern (Cheverud 1984). Finally, if the first two legs of the conjecture 253 hold, estimates of **P** may better estimate the true **G** than direct estimates of **G**. The precision of a 254 G matrix is a function of the number of families, while the precision of a P matrix is a function 255 of the (much larger) number of individuals measured.

256

# [Figure 2 near here]

Evidence for and against Cheverud's conjecture has accumulated (de Oliveira et al. 2009, Kohn and Atchley 1988, Martínez-Abadías et al. 2012, Porto et al. 2009, Roff 1995, 1996, 1997, Simons and Roff 1996). The validity of the conjecture in non-morphological traits is controversial (Atchley et al. 1981, Hadfield et al. 2007, Lofsvold 1986), while a recent review confirms that **P** and **G** are generally similar for the morphological traits that paleontologists can measure (Sodini et al. 2018). Therefore, using **P** as an estimate of **G** enables paleontologists to strategically utilize evolutionary quantitative genetic tools.

An important cautionary note when estimating **P** from fossil data is that the population variance of fossil samples may be inflated due to changes in the population mean over the timescale captured by the sample. However, fossil samples have been found to show levels of

267 trait variances and covariances similar in magnitude with estimates from extant, non-time-268 averaged populations (Hunt 2004). In addition, the richness of the fossil record varies substantially among taxa and not all fossil species have sufficient sample size to robustly 269 270 estimate **P**. Cheverud (1988) suggested at least 40 individuals were needed for a reasonably 271 accurate **P** for **G** substitution, but larger sample sizes are required as the number of traits increase 272 and to accurately estimate some evolvability statistics (Grabowski and Porto 2017). One 273 potential solution is to use P (or G) matrices from extant species as a substitute for unknown 274 fossil G matrices (Ackermann and Cheverud 2004, Baab 2018, Grabowski et al. 2011, 275 Grabowski and Roseman 2015, Hansen and Voje 2011, Young et al. 2010). This assumes that 276 the estimated **P** or **G** from the extant population is similar enough to **G** in the ancestral extinct 277 population. Based on similarities between closely related extant species, a wide array of work 278 (both neontological and paleontological) assumed that the P (or G) from an extant population is 279 representative of the ancestral G, which has allowed researchers to make evolutionary inferences 280 from phenotypic data across macroevolutionary timescales in ways that would be impossible 281 otherwise (Ackermann and Cheverud 2004, Baab 2018, de Oliveira et al. 2009, Grabowski et al. 282 2011, Marroig and Cheverud 2010, Rolian 2009, Young et al. 2010). 283 Paleontological studies that estimate P matrices exemplify how some paleontological

model systems are well-suited for exploring a potential role of evolvability in macroevolution.
Hunt's (2007) study on phenotypic divergence in the ostracode genus *Poseidonamicus* is one
example. Analyzing morphological traits from 51 fossil samples spanning a time-interval of
about 40 million years, Hunt showed a positive relationship between phenotypic variation within
fossil samples and the directions of evolutionary change in different lineages—a relationship that
weakened with elapsed time. The ability to study the duration of the effect of trait variation on

290 evolutionary change exemplifies a unique advantage paleontological data bring to the study of 291 evolvability. Another example is Brombacher et al. (2017b), who estimated the phenotypic 292 variances from 75 samples of two fossil lineages of planktonic foraminifera (Truncorotalia 293 crassaformis and Globoconella puncticulata) across 500,000 years, and concluded that the 294 within-sample covariance generally predicted evolution from one sample to the next. However, 295 major changes in climate caused this prediction to break down. A similar conclusion was reached 296 by Renaud et al. (2006) in their investigation of how variational properties of fossil samples of 297 two closely related rodent species affected their evolution.

298 Perhaps the best example of a paleontological study system that can connect the concept 299 of evolvability from quantitative genetics to long-term phenotypic evolution is work on the 300 bryozoan genus Metrarabdotos (Cheetham et al. 1994). This capitalized on the clonal nature of 301 bryozoans, which permits estimates of the broad-sense G matrix (a quantification of the effects 302 of entire genotypes on resemblance between individuals) from variation among genetically 303 identical zooids within a colony. In contrast, the G matrix of the Lande equation, also known as 304 the narrow-sense G matrix, measures just the part of inheritance that causes offspring to 305 resemble their parents. Evidence suggests that broad-sense and narrow-sense G matrices may be 306 similar to each other for morphological traits that can be measured from fossils. Although 307 methodological issues obfuscate the original conclusions on evolutionary tempo and mode 308 within the clade (Voje et al. 2020), this work—along with that of others (Alex et al. 2016, 309 Brombacher et al. 2017b, Hunt 2007, Renaud et al. 2006)-exemplifies how evolutionary 310 quantitative genetics and the concept of evolvability can be operationalized in the fossil record. 311

312 *3.2 Allometry, Evolvability, and Fossils* 

313 Another theoretical framework that connects paleontological data to evolvability is the 314 study of allometry (Gould 1966, Huxley 1932, Lande 1985). Allometry is commonly expressed as a power function in the form of  $Y = aX^b$ , where X is overall size and Y is the size of a part. 315 316 Depending on the level of comparison, three conceptually distinct kinds of allometry can be 317 defined: (1) ontogenetic allometry characterizes variation among individuals at different growth 318 stages from embryo to adult, (2) static allometry characterizes variation among individuals of the 319 same life stages (typically adults), and (3) evolutionary allometry characterizes variation across 320 species (Cheverud 1982b). The past decade saw developments in the concepts and tools used to 321 study allometry in the context of quantitative genetics and evolvability (Houle et al. 2011, 322 Pélabon et al. 2013, Voje et al. 2014). Ontogenetic and static allometries are particularly relevant 323 for evolvability because they are summary statistics of two-dimensional P when one of the two 324 traits is overall size. Size is often a "line of least evolutionary resistance" (Marroig and Cheverud 325 2005) and traits are commonly more evolvable in the direction predicted by the allometric 326 relationship compared to other directions, similar to the concept of "genetic lines of least 327 resistance" (e.g., Schluter 1996; Fig. 1B). Furthermore, the direction of trait evolution predicted 328 by the allometric relation is often found to be conserved among taxa (Voje et al. 2014; Fig. 3), 329 suggesting that patterns of developmental and genetic constraints are at play in channeling the 330 evolutionary response in the trait in relation to changes in overall size (Pélabon et al. 2014).

331

#### [Figure 3 near here]

The study of allometry has a rich history within paleontology. Gould's (1974) famous study of the antler size of the Irish elk *Megaloceros giganteus* shows two results relevant for evolvability. First, the Irish elk had the predicted antler size of a species of its size from the pattern of evolutionary allometry across 20 extant species of the subfamily Cervinae. Second,

within-species static allometry was similar to the among-species evolutionary allometry of antler
and body size. Gould concluded that the seemingly extravagant antlers of the Irish elk evolved
through heterochronic extrapolation of the common allometry of Cervinae. Work on horse-skull
morphology is another example of allometric relationships in paleontology (Radinsky 1984,
Robb 1935a, b). The similarity between the slope of ontogenetic and static allometry of the
modern horse and evolutionary allometry among fossil horses was interpreted as constraining the
morphological divergence in the family Equidae in morphospace (Simpson 1944).

343 The fossil record provides critical data to examine the hypothesis that morphological 344 evolution is constrained to follow the direction of ontogenetic and static allometry due to low 345 evolvability of the allometric slope ('the allometric-constraint hypothesis', reviewed in Pélabon 346 et al. 2014, Voje et al. 2014). The previously mentioned study by Brombacher et al. (2017a) 347 looked at traits in relation to size and tested the allometric-constraint hypothesis in two lineages 348 of planktonic foraminifera. They estimated the static allometric slope at time step t and evaluated 349 whether this predicted the direction of evolution in the bivariate means at time step t+1. Within a 350 constant climatic phase, the static allometric slope predicted the direction of among-population 351 morphological divergence, whereas the static slope failed to do so for the divergence across 352 different climatic phases. This pattern corroborates the idea that allometry serves as a constraint 353 over relatively short time scales, but that allometric slopes evolve and facilitate evolution away 354 from the common allometric trajectory on longer timescales (Houle et al. 2019, Tsuboi et al. 355 2016, Voje and Hansen 2012, Voje et al. 2014). Within the same conceptual framework, Firmat 356 et al. (2014) revealed a pattern supporting the allometric constraints in dental morphology of 357 rodents, but again over a relatively short time scale (~600,000 years). The traits studied by both 358 Brombacher et al. (2017a) and Firmat et al. (2014) were weakly correlated with size, which

359 means that evolvability is only modestly reduced in directions away from the allometric

360 relationship. It would be interesting to investigate sets of traits in the fossil record that show a

361 stronger association with overall body size in future assessments of the evolvability of allometric

362 slopes and the predictability of allometry on trait evolution.

363

# 364 4. Evolutionary Developmental Paleontology

365 *4.1 Fossil Evo-Devo* 

Evolvability is at the center of evo-devo (Hendrikse et al. 2007). One key intersection 366 367 between evo-devo and paleontology concerns morphologies recorded by fossils but not present 368 among extant taxa, including intermediate states in important evolutionary transitions. Proximate 369 developmental processes that underpin major evolutionary transitions have been inferred for an 370 increasing number of examples, such as the mammalian inner ear (Luo 2011, Luo et al. 2015, 371 Urban et al. 2017; Wang et al. 2019; Wang et al. 2021), arthropod segmentation (Chipman and 372 Edgecombe 2019), tetrapod limbs (Stewart et al. 2020), and turtle shells (Lyson and Bever 2020, 373 Schoch and Sues 2020). Insights from these paleo-evo-devo studies provide a richer 374 understanding of how evolutionary innovations arise and of their importance in the history of life 375 (Erwin 2012, Jablonski 2020, Wagner 2014; Urdy et al. 2013). However, cases in which 376 researchers use developmental information to make predictions about the generation of 377 phenotypic variation are most relevant to the topic of evolvability. Sufficient knowledge of 378 developmental processes, coupled with assumptions or evidence that they are conserved from 379 fossil taxa to their modern relatives, can offer an alternative to the quantitative genetic approach 380 for predicting which traits and lineages may be more likely to produce abundant variation for 381 natural selection and other evolutionary processes (Jackson 2020). For example, the structure of

382 some gene regulatory networks may greatly limit the realization of variation in certain body plan 383 traits, leading to their profound stability over time (Davidson and Erwin 2006). Cell-reflecting 384 structures in ostracod carapaces offer another example. These structures allow for cell divisions 385 to be inferred from ontogenetic changes in reticulation (Liebau 1991, Okada 1981), and it has 386 been shown that some divisions in these sequences can be much more variable than others, 387 shaping the variation present in fossil and modern populations (Hunt and Yasuhara 2010). In the 388 remainder of this section, we discuss two trait systems—vertebral counts in amniotes and tooth development in mammals-for which the intersection of evo-devo, evolvability, and 389 390 paleontological data have been especially productive.

391

### 392 *4.1.1 Vertebrae counts in amniotes*

393 The regionalization of the axial skeleton in amniotes has been well studied in terms of 394 variation and evolutionary divergence. Vertebrae are divided into presacral, sacral, and caudal 395 series, with the presacral series further subdivided into cervical, thoracic and lumbar series. It has 396 long been known that the counts of vertebrae in these different series tend to be conserved in 397 mammals but are more variable in reptile groups. Müller et al. (2010) showed that this pattern of 398 variability is ancient: mammals share their conserved variation with basal synapsids, whereas 399 even basal reptile groups show high evolutionary lability in vertebrae counts in different axial 400 regions. Cervical (neck) vertebrae counts, in particular, are nearly invariant among mammals; 401 only manatees and three-toed sloths differ from the canonical mammalian complement of seven 402 (Narita and Kuratani 2005). In contrast, many reptile groups are extremely variable in their 403 vertebrae counts. Sauropterygians (pliosaurs, plesiosaurs, and their relatives) can have anywhere

404 from 6 to 76 neck vertebrae (Soul and Benson 2017), and total vertebral counts in snakes can
405 differ by several hundred across species (Lindell 1994).

406 Is the rarity of evolutionary changes in vertebral counts, especially in the neck region, 407 caused by constraints (i.e., a low evolvability) of this suite of traits in mammals (Jones et al. 408 2018)? The simplest variational cause for a lack of evolutionary change is the lack of genetic 409 variation. If mammalian development (almost) always produces axial skeletons with exactly 410 seven neck vertebrae, then this trait would have (near) zero evolvability. Perhaps surprisingly, 411 this seems not to be the case: studies of different mammal species have documented variation in 412 cervical counts (Galis 1999, Galis et al. 2006, ten Broek et al. 2012, Varela-Lasheras et al. 2011). 413 However, these studies also demonstrate that individuals bearing variant numbers of cervical 414 vertebrae almost always bear other skeletal or soft-tissue anomalies, including lethal cancers. 415 Therefore, evolutionary changes are limited not by the absence of variation, but instead by strong 416 genetic correlations between vertebral counts and other traits that dramatically lower organismal 417 fitness. The result is that very little of the variation in vertebral patterning is available for 418 adaptive evolution.

419 The explanation that cervical vertebral counts are conserved in mammals because of low 420 evolvability has been extended to consider differences in evolvability across other vertebral traits 421 and between different lineages. Thoracic vertebrae variants are also associated with negative 422 developmental anomalies, but the association is weaker than for cervical variants (Galis et al. 423 2006). Indeed, vertebral counts are less conserved in the thoracic region of mammals (Narita and 424 Kuratani 2005). Some have argued that the two mammal lineages with evolutionary shifts in 425 cervical vertebrae, manatees and sloths, have been able to do so because their relatively low 426 metabolism can reduce the harmful side effects, especially those related to cancers (Varela-

Lasheras et al. 2011). Similarly, the lower incidence of cancer in birds and other reptiles may be
related to the greater evolutionary lability of vertebral counts in these groups (Galis 1999),
though additional factors can be identified that likely play a role (Varela-Lasheras et al. 2011).

430

# 431 *4.1.2 Molar development in mammals*

Developmental biologists have extensively explored the mouse as a model system for tooth development, with several decades of work elucidating the gene expression patterns and tissue interactions associated with tooth formation. Given that the fossil record of mammalian teeth is especially rich, there is great potential to marry this archive of tooth form with an accumulating understanding of tooth development.

437 Generative models of tooth formation have been crucial to making predictions about the 438 evolvability of different dental traits (Jernvall 2000, Ortiz et al. 2018, Polly 1998, Salazar-439 Ciudad and Jernvall 2010). For example, the Inhibitory Cascade (IC) model makes predictions 440 about the relative size of molars in the tooth row. Kavanagh et al. (2007) developed this model 441 based on the experimental demonstration in mice that the first molar (M1) inhibits the formation 442 of the second (M2), which, in turn, inhibits the third molar (M3). They then postulated a 443 quantitative relationship that captured this behavior, with a parameter that represents the 444 relationship between signal activation and inhibition in the developing tooth precursors. This 445 model predicts that molars can develop on a continuum between equal sized (M1 = M2 = M3) 446 and increasingly M1 dominated (M1 > M2 > M3), depending on the relative strength of 447 activators to inhibitors. Moreover, the model predicts that M2 should always account for  $\frac{1}{3}$  of 448 total molar size when three molars are present and that the slope between M2/M1 and M3/M1449 should be exactly two. The IC model proposes that variation in relative tooth size should

therefore be highly structured, with some configurations arising easily and others essentially
forbidden (e.g., M2 > M1). Assuming the IC model is strictly true, evolvability should therefore
be high in some dimensions and absent in others.

453 Initial data published with the IC model indicated that relative molar sizes in murine 454 rodents followed its predictions (Kavanagh et al. 2007). Many subsequent studies have applied 455 the IC model to other mammal groups, both extant and fossil. Halliday and Goswami (2013) 456 assessed a large sample that included fossil mammals dating back to the Jurassic and found that 457 molar ratios in most, but not all, taxa were similar to the IC predictions (Fig. 4). Other studies 458 reported on different mammal clades, which yielded results that sometimes comported with IC 459 predictions, but other times did not (Asahara 2013, Evans et al. 2016, Polly 2007, Renvoisé et al. 460 2009, Wilson et al. 2012). All the above studies looked at predicted (mean) tooth morphologies. 461 As an independent prediction of the IC model, Roseman and Delezene (2019) derived the 462 expected variances and covariances of tooth dimensions and found that these predictions were 463 generally not matched closely by data from primates (see also Vitek et al. 2020).

464

### [Figure 4 near here]

465 Like all models, the IC is a simplification of reality and therefore should not be expected 466 to fully reproduce patterns in nature. Moreover, the experimental evidence that prompted the 467 development of this model was drawn from a single mouse species. Many of the studies that 468 found patterns at odds with IC predictions postulated that these deviations could result from 469 evolutionary changes in tooth development processes that occurred between the focal clade and 470 mice (reviewed in Roseman and Delezene 2019). This is to be expected because development 471 evolves, and predictions based on an unchanged developmental program will thus decay in 472 usefulness with increasing evolutionary time. It is noteworthy that the IC predictions were at

473 least sometimes supported in taxa tens to hundreds of millions of years diverged from modern
474 mice. Therefore, differences in evolvability due to features captured in developmental models
475 can be quite persistent, perhaps much more so than those based on inferences from quantitative
476 genetic parameters such as the G or P matrix.

477

# 478 *4.2 Integration and modularity*

479 Phenotypes are composed of parts recognized with anatomical names. For example, 480 tetrapod bodies can be divided into forelimbs, hindlimbs, and axial regions, and these may be 481 subdivided further. Morphological parts can be associated or integrated with others because they 482 are specified by common genes, influenced by shared developmental pathways, or work together 483 to achieve a particular function (e.g., locomotion for forelimbs and hindlimbs in many tetrapods) 484 (Klingenberg 2008, Olson and Miller 1958). Empirical studies repeatedly suggest that such 485 associated parts tend to be more correlated with each other than with unassociated parts. For 486 example, individuals with larger than average forelimbs also will have larger than average 487 hindlimbs. Modules refer to groups of traits that are integrated with each other but relatively 488 independent of other sets of traits.

Modularity and integration clearly describe the apportionment of evolvability among traits, but the consequences for evolution depend on the relationship between modularity and selection. If the directions of selection are random over long time periods, phenotypic evolution will occur more rapidly in the directions of modular variation but less rapidly in other directions, leaving the overall rate of evolution unchanged from a non-modular architecture. Alternatively, modularity could be adaptive if mutually correlated traits are frequently selected in a direction consistent with their correlations. In this case, modular architecture will minimize the pleiotropic

496 effects of adaptation on other modules and minimize the costs of adaptation. This enhances the 497 overall rate of evolution (Cheverud 1996, Kirschner and Gerhart 1998, Riedl 1978, Wagner and 498 Altenberg 1996). The claim that modularity is aligned with likely directions of selection is 499 plausible, especially for modules related to function, though to date it is not well assessed by 500 empirical evidence, perhaps due to the scarcity of estimates of natural selection on suites of traits 501 (Melo et al. 2016). Modules are frequently identified on the basis of developmental, anatomical, 502 or functional knowledge of the suite of traits under consideration or are inferred empirically from 503 the patterns of covariation among traits (Goswami and Polly 2010, Klingenberg 2008), rather 504 than from the nature of selective forces. The overall impact of modularity on evolution depends 505 on whether modular architecture changes the overall evolvability. If modularity is achieved by 506 reduction of variability in non-modular directions, it can readily reduce evolvability relative to a 507 less-modular architecture (Hansen 2003).

508 Paleontologists have assessed patterns of integration and modularity within abundantly 509 preserved species, explored differences in modularity between closely related species (Gerber 510 and Hopkins 2011, Webster and Zelditch 2011a, b), and tracked changes in modularity and 511 integration within lineages (Goswami et al. 2015, Maxwell and Dececchi 2013). In other cases, 512 modularity has been assessed in extant populations and then applied to fossil taxa not normally 513 preserved in high abundance (e.g., Young et al. 2010). All these studies provide important 514 information about the stability of trait variational patterns, as well as about whether evolutionary 515 divergence is shaped by the developmental organization of traits. Other studies address what is 516 sometimes called "evolutionary modularity" (e.g., Felice et al. 2019, Larouche et al. 2018, 517 Parins-Fukuchi 2020). This approach also looks at associations among sets of traits, but the 518 variation examined is between species rather than within species. This body of work is

interesting but less easily related to evolvability because, absent information about genetic
variation or development within species, it is not possible to determine variational versus
selective causes for these patterns.

522

# 523 5. Comparative Methods, Macroevolution, and Paleontology

524 Phylogenetically-informed macroevolutionary modeling is another area where increased 525 integration with paleontology is possible and being realized. In particular, recent developments 526 in phylogenetic comparative methods (PCMs) have led to an explosion of neontological interest 527 in the study of macroevolutionary processes and patterns (reviewed in Garamszegi 2014, 528 O'Meara 2012, Pennell and Harmon 2013). This is a direct consequence of the development of 529 novel and powerful statistical models of trait and lineage evolution. As a result, there is a 530 growing overlap in the type of research questions that paleontologists and neontologists can ask 531 regarding long-term evolvability (Hunt and Slater 2016): What role does evolvability play in 532 regulating lineage diversity and morphological disparity through time? How can we explain 533 stasis over macroevolutionary timescales? To what extent can evolutionary novelties shape the 534 patterns or rates of diversification? Can shifts in modularity induce changes in the rate of 535 morphological diversification?

536 One of the benefits of this increased overlap in research interests is the emergence of 537 interdisciplinary approaches, such as the addition of fossil data to molecular phylogenies (e.g., 538 Slater et al. 2012) or the application of comparative methods to trees derived from fossil data 539 (e.g., Mitchell et al. 2019). Another important benefit is the realization that paleontologists and 540 neontologists working in a comparative framework can share a common set of mathematical 541 models. This unification is essential for evolvability research because it provides the field with a

robust statistical framework in which to test hypotheses regarding the impact of intrinsicorganismal properties on long term evolutionary dynamics.

544 Quantitative genetic and developmental approaches to evolvability are clearly applicable 545 at short time scales, but genetic and developmental systems evolve over longer time scales, 546 which means that the evolvability of clades may diverge over time (but see Tsuboi et al. 2018). 547 In addition, long term evolvability must encompass not only a lineage's ability to respond to 548 selection, but also its capacity to survive repeated rounds of large-scale changes in its biotic and 549 abiotic environment (Jablonski 2017a). Evolvability research on macroevolutionary time scales 550 is, therefore, necessarily more complex than studies at microevolutionary time scales (Jablonski 551 2008). This makes it even more challenging to disentangle whether macroevolutionary patterns 552 arise from variational properties of traits or lineages rather than selection or ecological 553 opportunity.

554 At the macroevolutionary level, the confluence of phylogenetic methods with 555 paleontological data allows researchers to focus on clade-level properties as a rich source of data. 556 We highlight the study of two such properties: (a) morphological disparity and (b) lineage 557 diversification through speciation and extinction rates.

558

559 *5.1 Disparity* 

560 One of the clearest routes for combining neontological and paleontological data in the 561 study of long term evolvability is through analyses of disparity or morphological diversity. 562 Studies of disparity have traditionally been used to test the idea that the exploration of the 563 morphospace is limited by the availability of ecological space (Harmon et al. 2003, Hughes et al. 564 2013, Yoder et al. 2010). Ecological opportunity would then be the major determinant of the rate

of morphological diversification (Rainey and Travisano 1998) and the opening of adaptive zones would help to explain large radiations (Simpson 1944). Increasingly, however, biologists have come to recognize that intrinsic organismal factors might play a role in regulating the occupation of a multivariate morphospace (Wagner 2018). In particular, the pathways followed by a lineage are shaped not only by externally imposed evolutionary processes, but also by variational properties that steer evolution along paths with abundant variation and constrain it away from pathways that lack such variation.

572 A classic example is observed in mammals following the Cretaceous-Paleogene (K-Pg) 573 extinction (Archibald and Deutschman 2001, Raia et al. 2013, Slater 2013). While several 574 mammalian lineages survived the K-Pg extinction event, they have since followed remarkably 575 different morphological diversification patterns. Placentals have diversified into a large array of 576 forms, encompassing species that are aerial, arboreal, fossorial, aquatic or cursorial with body sizes that vary anywhere from 2 g to 1.5 x 10<sup>8</sup> g (Wilson and Reeder 2005). Marsupials, on the 577 578 other hand, have remained far more conservative and display lower disparity than placentals for 579 several skeletal elements, such as the mandible and dentition (Echarri and Prevosti 2015), skull 580 (Bennett and Goswami 2013), shoulder girdle (Sears 2004), and limb bones (Cooper and Steppan 581 2010). Several authors have argued that the low disparity in skeletal forms among marsupials is a 582 consequence of their altricial reproductive strategy, which requires juvenile marsupials to climb 583 to one of their mothers' teats soon after birth and suckle earlier and for longer than placentals 584 (Lillegraven 1975, Smith 2006). This strategy requires an early ossification of facial and limb 585 skeletal elements (Bininda-Emonds et al. 2007, Sánchez-Villagra 2002) so that the neonate can 586 both climb and suckle properly. Early ossification of skeletal structures, in turn, may limit the

range of forms easily generated during marsupial ontogeny, which would allow for more derived skeletal morphologies and thereby limit ecomorphological diversification of the group (Fig. 5).

589

588

# [Figure 5 near here]

590 Vermeij hypothesized that the number of dimensions in which the phenotype is capable 591 of varying, which he termed versatility, is correlated with disparity (Vermeij 1973b). He pointed 592 to the possibility that increasing versatility facilitated the evolution of more complex forms and 593 enabled the evolution of key innovations that opened up new adaptive zones. More generally, 594 increasing the dimensionality of possible phenotypes may allow the exploitation of a wider 595 variety of ecological roles within each adaptive zone. Versatility is therefore a higher-level 596 property not tied to any particular phenotype, enlarging the nature of evolvability characteristics 597 that can influence disparity.

598 One of the main reasons why disparity provides fruitful grounds for integrating 599 paleontological and neontological approaches to evolvability is that the mechanics of 600 phylogenetically-informed disparity analysis is highly similar whether fossil taxa are 601 incorporated or not. The main necessary components are essentially the same: (1) a tree with 602 branches scaled to time units, (2) scores for each taxon in the morphological trait of interest, (3) 603 a model for evolutionary change, and (4) the evolvability hypothesis being tested. However, 604 several initial studies have demonstrated that even incorporating a little fossil information into a 605 phylogenetic backbone can go a long way toward improving parameter estimates of the 606 statistical models used for testing differential evolvability hypotheses (e.g., Pyron and Burbrink 607 2012) and the ability to differentiate between evolutionary models (e.g., Slater et al. 2012).

608

# 609 *5.2 Lineage diversification*

610 Another promising route for integration of neontological and paleontological data in the 611 study of long term evolvability is through analyses of lineage diversification rates caused by 612 extinction and speciation. There are several proposed routes by which organismal or population 613 properties can affect diversification. At the trait level, morphological novelties are capable of 614 reshaping lineage diversification rates, sometimes causing bursts of diversification (Rabosky et 615 al. 2013). The study of such key innovations or trait-dependent diversification has enjoyed a 616 significant revival in modern phylogenetics with the development of trait-dependent speciation 617 and extinction models (FitzJohn 2010, 2012, Goldberg and Igić 2012, Goldberg et al. 2011, 618 Magnuson-Ford and Otto 2012). In principle, such approaches can separately estimate effects of 619 traits on speciation and extinction, using only observations from extant taxa and a phylogeny 620 connecting them. However, these methods perform unreliably under many conditions when their 621 strict assumptions are violated (Rabosky and Goldberg 2015), and more general arguments cast 622 doubt on extant-only data being able to recover historical diversification dynamics (Louca and 623 Pennell 2020). As a result, fossil data may be especially informative for testing whether traits— 624 including those related to evolvability-influence speciation and extinction rates. Indeed, it is 625 reasonable to hypothesize that high evolvability, through enhanced generation of potentially 626 adaptive variants, can protect against extinction. In the fossil record, this survival could be 627 disguised as pseudo-extinction. Evolvability also may plausibly influence the formation of new 628 species as it can enhance responses to natural selection, which can be important under scenarios 629 of ecological speciation (Schluter 2009) or for the survivorship of incipient species as they 630 become established (Allmon and Sampson 2016).

However, tests for such associations between evolvability and speciation or extinctionface a complication. The propensity to speciate or go extinct are properties of lineages, not traits

633 (though traits, of course, can influence these probabilities). Differences in variation-and 634 therefore, evolvability—are commonplace among traits. For example, the first principal 635 component in multivariate trait datasets commonly accounts for a majority of the variance, 636 whereas the trailing principal components harbor only trivial amounts of variation. If 637 evolvability itself can evolve (Wagner and Draghi 2010), then this implies at least the possibility 638 of differences in evolvability across lineages, but the frequency and strength of such differences 639 are unclear. Taxonomic differences have been documented for genetic features related to 640 evolvability, such as overall rates of mutation (Lynch 2010) and recombination (Stapley et al. 641 2017). Developmental or morphological features that have been associated with evolvability 642 differences among clades include growth strategy in regular versus irregular echinoids (Hopkins 643 and Smith 2015), the loosening of allometric relationships (Tsuboi et al. 2018), and the breaking 644 of left-right symmetry in bivalves (Jablonski 2020).

645 Despite this obstacle, we noted earlier that several paleontological studies tested if 646 extinction was predicted by phenotypic variation (Kolbe et al 2011, Hopkins 2011, Liow 2007). 647 These studies captured variation levels using morphometric analysis of skeletal elements (Kolbe 648 et al. 2011, Hopkins 2011) or through expert, but qualitative, opinions judging certain species to 649 be unusually variable (Liow 2007). For the measured variation to be relevant for extinction, the 650 focal traits must be construed as proxies for overall phenotypic variation, or they must be 651 selectively important enough to influence adaptation and population survival. We do not know of 652 other analyses of variation and extinction, or any studies that perform analogous analyses for 653 origination, though the possibility is discussed in some detail by Jablonski (2020). Vermeij's 654 (1973a) claim that taxa with higher versatility tend to preferentially replace those of lower

versatility implies that this evolvability-related characteristic should increase speciation ordecrease extinction, and possibly both together.

657

# 658 6. Conclusions and Prospects: Evolvability in the Fossil Record

659 Although evolvability is not commonly invoked by many paleontologists, the examples 660 we have presented provide ample warrant for paleontologists to actively incorporate the concept 661 of evolvability into investigations of the fossil record. Our enthusiasm should, however, be 662 tempered with caution; disentangling the role of evolvability and the forces that cause evolution 663 is always challenging. With these two points in mind, we offer a methodological schema for 664 paleontologists and their interdisciplinary collaborators to initiate investigations of evolvability. 665 To enable such a study, three distinct aspects must be addressed a priori: conceptualization (what 666 counts as evolvability?); measurement (how is evolvability empirically measured, directly or indirectly?); and testing (what strategies are used to evaluate hypotheses about evolvability?). 667 668 The conceptualization of evolvability differs across the approaches canvassed herein. 669 Classic studies focused on how variational properties could influence the propensity for 670 evolutionary stability versus change, within the span of individual lineages, and more broadly 671 over the history of life. Vermeij (1973a, b) used the potential versatility of form, whereas others 672 have concentrated on morphological disparity (e.g., Hughes et al. 2013). Within quantitative 673 genetics, evolvability is conceptualized specifically as the short-term evolutionary potential for a 674 population to evolve in the direction of selection (Hansen and Houle 2008). Within evo-devo, 675 evolvability is conceptualized in terms of how developmental processes can structure trait 676 variation that is subject to selection and drift. Within phylogenetic macroevolutionary modeling, 677 evolvability is analyzed retrospectively and is based on different measures of the evolutionary

success of lineages (e.g., disparity or rates of speciation and extinction). Although interesting
theoretical relationships might obtain between these different meanings, a clearly specified
conceptualization is crucial for initiating an inquiry.

681 Once evolvability is conceptualized in a particular way, the next issue is to address 682 methodologically is how evolvability will be measured. For instance, Vermeij operationalized 683 "potential versatility of form" as the number of parameters required to describe coiling in 684 gastropods. In quantitative genetics, short-term evolvability is defined as the mean-standardized 685 additive genetic variance. In evo-devo studies, developmental considerations may form the basis 686 for statements of relative evolvability (e.g., cervical vertebrae should be less evolvable than 687 thoracic vertebrae in mammals), but these may not readily predict magnitudes of such effects. 688 The specific type of measurement utilized will limit the kinds of evolutionary inference that 689 might be drawn in distinctive ways that must be explicitly appreciated.

690 Finally, with evolvability operationalized, the final step in the methodological sequence 691 is testing. Armed with measures or predictions of relative evolvability across traits or lineages, 692 researchers can then measure evolutionary differences to assess the degree to which divergences 693 match evolvability predictions. Are changes larger in more evolvable traits or lineages? Are low-694 evolvability traits or directions in morphospace especially conserved? Do lineages whose 695 characteristics indicate high evolvability attain greater morphological disparity or experience 696 greater diversification? To the extent that evolvability predictions are upheld, the argument is 697 supported that variation—and not just selection—is important in shaping long-term evolutionary 698 changes. When evolvability does not predict empirical divergences, it is likely that natural 699 selection has been the dominant process determining the evolutionary outcomes. Compilation of

numerous such tests can help to establish the relative importance of these two components of
evolution for different kinds of traits, in different lineages, and over different time scales.

702 This three-step methodological schema offers a general template for approaching a 703 variety of outstanding questions on evolvability in the fossil record (Box 1). These include major 704 theoretical questions such as the relative importance of variation versus selection in the history of 705 life, as well as more granular issues such as the timescales over which variational patterns, and 706 thus evolvability predictions, are stable. Attention to the specifics of the schema provides 707 detailed guidance for novel empirical and theoretical studies of evolvability in the fossil record. 708 Paleontology, with its unique access to temporal data from the history of life, is positioned to 709 make distinctive contributions to studies of evolvability and especially in interdisciplinary 710 collaborations with other approaches in evolutionary biology.

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1177

1178 Figure 1. Geometry of the Lande equation. The three elements of the Lande equation are the direction and the magnitude of selection ( $\beta$ , dotted arrow), the amount of additive genetic 1179 1180 variance in the direction of trait change (G, grey circle/ellipse) and the response to selection ( $\Delta z$ , black arrow). The closed black and open grey points represent the trait mean before and after the 1181 1182 selection event, respectively. (A)  $\Delta z$  and  $\beta$  point in the same direction as there is no genetic 1183 covariance between the two traits. (B) The evolutionary response is deflected towards the 1184 direction with the largest amount of genetic variance (red dotted line) due to the genetic covariance between trait 1 and trait 2. The direction with the largest amount of genetic variance 1185 1186 (i.e., the direction with highest evolvability) is what Schluter (1996) named the "line of least resistance." In the context of allometry (see Section 3.2), the direction of trait evolution predicted 1187 1188 by the allometric relationship will be similar to the "genetic line of least resistance" if P closely

- 1189 resembles G.
- 1190



1193	Figure 2. Heritability, proportionality of G and P, and Cheverud's conjecture. Panels
1194	schematically illustrate how G and P are related and how trait heritability affects the
1195	relationship. (A) and (B) show proportional G and P, (C) and (D) show disproportional G and P.
1196	(A) and (C) show traits with heritability of 0.5 (i.e., 50% of phenotypic variation is attributable to
1197	genetic variation), and (B) and (D) show traits with heritability of 0.2. In each panel, the dark
1198	grey ellipse represents the P-matrix and the light grey ellipse represents the G-matrix. In panels
1199	(C) and (D), G is rotated to be maximally dissimilar to P. Cheverud's conjecture holds in
1200	situations depicted in panel (A) and (B). In highly heritable traits, represented by (C), there is an
1201	upper limit on the dissimilarity between G and P.
1202	



1205

1206 Figure 3. Brain mass - body mass allometry within and among species of the teleost order 1207 Perciformes. Grey lines represent the allometric relationship between brain mass and body mass 1208 among adult individuals within species (static allometry), whereas a dashed line represents the 1209 same relationship across species (evolutionary allometry). Static allometries are estimated using 1210 the Ordinary Least Squares. Evolutionary allometry is based on the phylogenetically-informed regression method reported in Tsuboi et al. (2018): log10(brain mass) = log10(body mass) x 1211 1212 0.496 - 1.73. Circles are species means (n = 94 species). The allometric slope of static (mean = 1213 0.45, SD = 0.02) are similar to the slope of evolutionary allometry, which suggests that the static 1214 slopes are conserved over geological time scales and constrained in the direction of brain size 1215 evolution in Perciformes. 1216



Figure 4. Area of third molar (M3) compared to the second molar (M2), each relative to the area of the first molar (M1). Each point represents tooth measurements from the tooth row of an individual mammal; many extinct and extant mammal groups are represented. Black line indicates the relationship predicted by the inhibitory cascade (IC) model of tooth development. Grey areas indicate tooth proportions that the strict IC model cannot produce. Most taxa have tooth dimensions consistent with the IC model, although some, such as rodents (blue diamonds), are more compatible than others, such as condylarths (red squares). Data are from Halliday and Goswami (2013). 





1232 Figure 5. Constraints on marsupial ecomorphological diversification. (A) Example of an 1233 early ossifying skeletal element in marsupials. Here we illustrate two stages of cranial bone development in koalas (Phascolarctos cinereus). Note the relative early ossification of the 1234 1235 dentary and maxilla (red) when compared to other cranial bones (gray). (Modified from Supplemental Fig. 5 in Spiekman and Werneburg 2017.) (B) Example of morphological disparity 1236 patterns observed when comparing placentals (blue) and marsupials (green). In this example, 1237 1238 disparity patterns were obtained for forelimb traits. (Modified from Fig. 4 in Cooper and Steppan 2010.) (C) Phylogenetic time tree of mammalian families. (Modified from Fig. 1 in Meredith et 1239 1240 al. 2011.) 1241

1243		<b>BOX 1 - Outstanding Questions on Evolvability in the Fossil Record</b>
1244		
1245 •	• G	eneral
1246		
1247	0	Is evolvability a major factor affecting differences in divergence among traits and
1240		ather trade offer modiated by natural selection (Vermaii 2015)?
1249	0	Are there secular trends in evolvability such that early appearing lineages may produce
1250	0	more phenotypic variation (Webster 2019) or have less potential versatility in form
1252		(Vermeii 1973a) compared to later appearing ones?
1253	0	Does short-term evolvability, based on quantitative genetic theory, predict evolvability
1254		over longer time scales? Can other evolvability-related properties, such as developmental
1255		bias, be reliably measured in the fossil record (Jackson 2020)?
1256		
1257 •	Pa	aleontology and Quantitative Genetics
1258		
1259	0	Are phenotypic covariance (P) matrices usually good proxies for additive genetic (G)
1260		matrices?
1261	0	How stable are <b>G</b> and <b>P</b> matrices over time?
1262	0	Over what time scales are <b>G</b> and <b>P</b> predictive of evolutionary divergence?
1263	0	Is the predictive power of <b>G</b> and <b>P</b> for evolutionary divergence due to genetic constraints
1264		or is selection shaping G and P to align with the direction of divergence?
1265	D	alcontology and Eve days
1200	P Pa	aleontology and Evo-devo
1207	0	Over what time scales are developmental processes conserved enough to make useful
1269	0	predictions about evolvability? Will this generally be longer than <b>G</b> and <b>P</b> matrices are
1270		stable?
1271	0	How much insight can be derived about how modules originate and evolve from
1272		sampling fossil species? Do modules tend to form from the splitting of larger modules or
1273		from the integration of formerly independent units (Wagner and Altenberg 1996)?
1274	0	There are many methods available for inferring modules from trait covariation, but they
1275		generally lack a strong theoretical basis. Can considerations of evolvability inform which
1276		methods are most appropriate or even suggest new approaches for recognizing modules?
1277	0	What is the relationship between evolvability and innovation? Can the propensity for a
1278		lineage to produce novelties be operationalized, or are these processes too historically
1279		contingent to permit a general framework (Erwin 2019)?
1280	п	
1281	) Pa	aleontology and Phylogenetic Macroevolution
1282	0	There are well de symptoted differences in evelvebility energy traits. And there also
1203 1287	0	substantial differences in evolvability across lineages?
1204	$\circ$	Is low evolvability associated with species extinction? Is high evolvability associated
1286	0	with radiation? How sensitive are existing methods for testing these associations with
1287		phylogenetic or paleontological data?
1288	0	What is the relative importance of evolvability and selection in macroevolution?
	-	