1	Mini-review
2	Autocorrelation-informed home range
3	estimation: a review and practical guide
4	Inês Silva ^{1,2} , Christen H. Fleming ^{3,4} , Michael J. Noonan ⁵ , Jesse Alston ^{1,2} ,
5	Cody Folta ⁴ , William F. Fagan ⁴ , Justin M. Calabrese ^{1,2,4,6*}
6 7	¹ Center for Advanced Systems Understanding (CASUS), 02826, Görlitz, Germany
8	² Helmholtz-Zentrum Dresden-Rossendorf (HZDR), 01328, Dresden, Germany
9	³ Smithsonian National Zoo and Conservation Biology Institute, Virginia, USA
10	⁴ Department of Biology, University of Maryland, College Park, Maryland, USA
11	⁵ Department of Biology, University of British Columbia Okanagan, British Columbia, Canada
12	⁶ Helmholtz Centre for Environmental Research—UFZ, 01328, Leipzig, Germany
13	* Corresponding author: j.calabrese@hzdr.de
14	Running head: Guide to autocorrelated home range estimation
15	Abstract
16	1. Modern tracking devices allow for the collection of high-volume animal tracking data at
17	improved sampling rates over VHF radiotelemetry. Home range estimation is a key output
18	from these tracking datasets, but the inherent properties of animal movement can lead
19	traditional statistical methods to under- or overestimate home range areas.
20	2. The Autocorrelated Kernel Density Estimation (AKDE) family of estimators were designed
21	to be statistically efficient while explicitly dealing with the complexities of modern movement
22	data: autocorrelation, small sample sizes, and missing or irregularly sampled data. Although
23	each of these estimators has been described in separate technical papers, here we review how

these estimators work and provide a user-friendly guide on how they may be combined toreduce multiple biases simultaneously.

3. We describe the magnitude of the improvements offered by these estimators and their
 impact on home range area estimates, using both empirical case studies and simulations,
 contrasting their computational costs.

4. Finally, we provide guidelines for researchers to choose among alternative estimators and
an R script to facilitate the application and interpretation of AKDE home range estimates.

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Keywords: home range, tracking data, telemetry, kernel density estimation, movement process
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34 Introduction

35 An animal's home range was first defined in Burt (1943) as "the area traversed by the individual in its normal activities of food gathering, mating, and caring for young". Although this definition does not 36 provide a mathematical description or statistical method for estimation, it highlights how behavior 37 drives animal movement: areas selected by individual animals are usually distinct from the larger 38 areas an animal could explore given their movement abilities. Early translations into a statistical 39 definition include quantifying an animal's probability of using a given location (*i.e.*, utilization 40 distribution; Jennrich & Turner, 1969; Worton, 1989). The concept of home range has been redefined 41 42 by many authors over the years (Harris et al., 1990); here, we follow the definition of home range as the area repeatedly used throughout an animal's lifetime for all its normal behaviors and activities, 43 excluding occasional exploratory excursions outside of home range boundaries. The characteristic 44 temporal stability of a home range also highlights additional concepts: range residency, defined as 45 the tendency of an animal to remain within its home range; and timescale parameters that quantify 46 the weakness of this tendency, including the home range crossing timescale (τ), defined as the 47 48 average time required for an animal to cross the linear extent of its home range.

Home range area estimates are used to inform conservation practitioners and wildlife managers 49 about protected area sizes and to advocate for conservation policy changes (Bartoń et al., 2019; 50 Lambertucci et al., 2014; Linnell et al., 1997). It is thus crucial to provide a reliable and statistically 51 robust metric that is comparable across individuals, species, and sites. Natural landscapes are 52 becoming increasingly fragmented (Curtis et al., 2018; Hansen et al., 2020), imposing new 53 54 challenges at local, regional, and global scales, and unreliable estimations may hinder area-based conservation. Reliable estimates of home ranges, however, have proven to be deceptively difficult 55 to achieve, and have occupied generations of ecologists (Fieberg & Börger, 2012; Horne et al., 2020; 56 Jennrich & Turner, 1969; Worton, 1989). The inherent properties of animal tracking data create 57 unique analytical challenges. Specifically, animal movement data frequently feature some 58 combination of autocorrelation, small sample sizes, missing observations, or irregular sampling, 59 and home range estimators that are not designed to handle these issues can both under- and 60 61 overestimate the sizes of home ranges.

Though many home range estimators exist (Horne et al., 2020), Autocorrelated Kernel Density 62 Estimation (AKDE) was the first to explicitly account for temporal autocorrelation in the data 63 (Fleming et al., 2015). Since its introduction, AKDE has grown into a family of related techniques, 64 each aimed at mitigating a different source of bias that can affect home range estimates, including 65 unmodeled autocorrelation (Hemson et al., 2005; Kie et al., 2010; Swihart & Slade, 1997), 66 67 oversmoothing (Seaman & Powell, 1996; Worton, 1995), autocorrelation estimation bias (Cressie, 2015), and unrepresentative sampling in time (Frair et al., 2004; Horne, Garton, & Kimberly A. Sager-68 Fradkin, 2007; Katajisto & Moilanen, 2006). These biases are mitigated, respectively, by the original 69 AKDE (Fleming et al., 2015), the area-corrected AKDE (Fleming & Calabrese, 2017), the perturbative 70 Hybrid Residual Maximum Likelihood parameter estimation and parametric bootstrapping (Fleming 71 et al., 2019), and weighted AKDE (Fleming et al., 2018). Residual Maximum Likelihood (REML) is a 72 form of maximum likelihood estimation that reduces biases in variance/covariance estimation. 73

AKDE and associated corrections have been shown to outperform traditional home range 74 estimators across species, degrees of autocorrelation, and sample size (Noonan et al., 2019). The 75 ctmm workflow also allows researchers to partially account for the location errors associated with 76 their tracking datasets (Fleming et al., 2021). These methods can be run using the programming 77 language R (www.r-project.org) and the ctmm or amt packages (Calabrese et al., 2016; Signer & 78 Fieberg, 2021), or the ctmmweb graphical user interface (https://ctmm.shinyapps.io/ctmmweb; 79 80 Calabrese et al., 2021). In addition to offering flexible and open-source tools for home range estimation, these software programs allow easy documentation and implementation of new 81 methods by sharing code and workflows. Such reproducible methods can increase reliability and 82 transparency in ecology (Alston & Rick, 2020; Culina et al., 2020; Powers & Hampton, 2019; Signer 83 & Fieberg, 2021). 84

Because movement data often violates multiple assumptions of traditional methods, the individual 85 methodological advances offered by the AKDE family of home range estimators can and often 86 should be combined. The costs and benefits of each estimator have previously been described in 87 separate technical papers, so in this paper, we bring all of these estimation methods together in one 88 document. We describe their effects on the quality of home range estimates, both in isolation and 89 90 in combination, while evaluating how sample size interacts with multiple different sources of bias. We use tracking data from African buffalo (Syncerus caffer; Cross et al., 2009), lowland tapir (Tapirus 91 terrestris; Fleming et al., 2019), and jaguar (Panthera onca; Morato et al., 2018) as empirical case 92 studies to guide researchers through the application and value of these analyses. Finally, we use 93 simulations to show the improvements offered by combining these techniques and demonstrate 94 their application in real-world problems. We conclude by giving clear guidance on how ecologists 95 can choose among these alternatives to best achieve their study goals. We hope that this review 96 97 provides a practical guide to why and how to use AKDE methods to estimate home ranges that will 98 be useful for both researchers and practitioners who are unfamiliar with these methods.

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99 Sources of bias and mitigation measures

Many biases, including most that affect home range estimates, are exacerbated by small sample 100 sizes. Conversely, large sample sizes in modern tracking datasets are typically achieved through 101 higher sampling frequencies, which exacerbate autocorrelation. Autocorrelation is a general 102 statistical property of variables measured across geographic and temporal space (Dale & Fortin, 103 2002; Legendre, 1993), as observations sampled more closely in space or time tend to be more 104 105 similar. In these conditions, it is thus important to distinguish between two different measures of sample size: absolute sample size (n) and effective sample size (N). Absolute sample size is simply 106 the total number of observations in a dataset. More relevant for home range estimation, however, 107 is the effective sample size. Specifically, the amount of information available to home range 108 estimators is governed not simply by the total number of observations, but by the number of range 109 crossings that occurred during the observation period (i.e., how many times an animal traversed the 110 linear extent of its home range). The effective sample size can be roughly estimated as T/τ , where 111 112 T is the temporal duration of the tracking dataset, and τ is the average home range crossing time parameter. Increasing sampling frequency leads to larger absolute sample sizes, but does not 113 increase the effective sample size commensurately. For autocorrelated data, the effective sample 114 size is necessarily smaller than the absolute sample size and, very frequently in practice, orders of 115 magnitude smaller (Fleming et al., 2019). In contrast, small absolute sample sizes commonly occur 116 in VHF tracking data but are becoming rarer in modern GPS tracking data. 117

We now describe each source of bias and the mitigation measure available to correct it, highlighting the difference each correction makes with real data from multiple case studies. We present the bias sources in order of their general importance, from the largest bias to the smallest. Note that this ranking refers to the typical magnitude of each type of bias, but the order may be different under some conditions.

123 Bias I: Unmodeled autocorrelation

124 Traditional home range estimators such as minimum convex polygons (MCPs) and kernel density estimators (KDEs) assume independently and identically distributed (IID) data. When these 125 techniques came into common use in the 1980s, the sheer difficulty of obtaining VHF location fixes 126 ensured that the time interval between successive observations was typically long enough for most 127 of the autocorrelation among observations to have decayed (Swihart & Slade, 1997; Worton, 1989). 128 The IID assumption at the heart of these techniques was therefore usually satisfied by VHF-guality 129 130 data (Harris et al., 1990). The situation began to change with the arrival of new technologies, most notably GPS tracking systems (Rempel et al., 1995), which now routinely feature large volumes of 131 data with much more frequent temporal sampling than is feasible for VHF-based animal tracking. 132 As autocorrelation arises from observations sampled closely in time also being located closely in 133 space, increasing sampling frequencies inevitably leads to more strongly autocorrelated tracking 134 data (De Solla et al., 1999). Automated, high-sampling frequency tracking data has undoubtedly 135 revolutionized movement ecology (Kays et al., 2015), but these advances have broken the armistice 136 between the statistical assumptions of traditional home range estimators and the reality of the 137 138 datasets now used to study animal movement (Boyce et al., 2010).

Specifically, feeding autocorrelated data into a home range estimator based on the IID assumption 139 yields negatively biased estimates (Noonan et al., 2019). Autocorrelation-induced underestimation 140 of home range areas is particularly pronounced when the effective sample size is small. In the recent 141 comparative study of Noonan et al. (2019), 368 out of 369 tracking datasets featured strong 142 autocorrelation, and roughly half were also plagued by small effective sample size. In these 143 conditions, conventional estimators-such as MCPs, KDEs, and local convex hull polygons-144 underestimate home range areas by a factor of ~2 to 13 (on average), depending on the method 145 and bandwidth optimizer, which is what determines how tightly KDEs conform to the data. 146

Accordingly, published estimates featuring these traditional methods may severely underestimate
 animal space-use requirements, hindering conservation and management decisions.

149 Mitigation Measure I: AKDE

Fortunately, it is not autocorrelation per se that causes errors in home range estimation, but rather 150 autocorrelation that is statistically 'unmodeled' (Calabrese et al., 2021). Home range estimators that 151 account for autocorrelation can therefore avoid the biases and violated assumptions of traditional 152 methods. Autocorrelated Kernel Density Estimation (AKDE) explicitly requires a movement model 153 that accounts for the autocorrelation in the tracking data (Figure 1) and then estimates the home 154 155 range while conditioned on the same movement model (Fleming et al., 2015). This model is identified via formal model selection among a range of plausible alternatives, currently spanning 156 from uncorrelated data (IID), correlated positions but uncorrelated velocities (Ornstein-Uhlenbeck 157 or OU; Uhlenbeck & Ornstein, 1930), to correlated positions and correlated velocities (Ornstein-158 Uhlenbeck foraging process or OUF; Fleming et al., 2014). In this framework, IID is both a candidate 159 model and one limit of a continuum of possibilities, rather than an a priori assumption. These 160 models are ranked based on Akaike's Information Criterion adjusted for small sample sizes (AICc) 161 by default, though the ctmm package also offers AIC, Bayesian Information Criterion (BIC), Leave-162 One-Out Cross-Validation (LOOCV), and Half-Sample Cross-Validation (HSCV). 163

Ad hoc measures such as data thinning (Harris et al., 1990; Rooney et al., 1998) are not necessary, as AKDE allows model assumptions to conform as closely as possible to empirical reality, instead of coercing the data to fit a model with unrealistic assumptions. Feeding IID data into AKDE will not have any adverse effects, as it will simply result in a conventional KDE estimate. This workflow also allows reliable confidence intervals to be determined for home range area estimates, which historically have not been applied to home range estimates. This measure of confidence is

- 170 fundamental for any statistical estimate (Pawitan, 2001), increasing the comparability of AKDE and
- 171 its relevance for biogeographical and conservation applications.



Figure 1. An example of autocorrelated data (individual six from the African buffalo dataset, available within the ctmm package), and the same data when it achieves independence (IID) after data thinning (from one fix per hour to one fix per week). We calculated the 95% contour of an Autocorrelated Kernel Density Estimation (AKDE) and a Gaussian reference function KDE (GRF-KDE). Displayed errors correspond to % bias of full dataset KDE and subset KDE against full dataset AKDE. N: effective sample size, n: absolute sample size.

172 Bias II: Oversmoothing

Kernel density estimators are best-in-class tools for estimating unknown probability distributions
and are used in this capacity across the sciences (Chen, 2017; Silverman, 1986; Wang et al., 2013).
In the context of tracking data, KDEs estimate the probability distribution of locations, which is then
used to estimate the area of a home range (Powell, 2000; Worton, 1989). Typically, ecologists are
more interested in this area estimate than in the distribution itself.

Even when we account for autocorrelation (AKDE), kernel density estimators based on the Gaussian 178 179 reference function (GRF) remain biased owing to the natural tendency of the GRF approximation to 180 oversmooth (yielding a more spread-out distribution). This bias is estimator-specific, and may be either positive or negative (Kie et al., 2010; Worton, 1995): for GRF-KDEs-such as AKDE and h_{ref} 181 (Silverman, 1986)-this bias is positive and, all else being equal, leads to an overestimated home 182 range (Seaman & Powell, 1996). Importantly, for estimators that do not account for autocorrelation, 183 like h_{ref} but unlike AKDE, this positive bias can be masked by the often stronger negative bias caused 184 by unmodeled autocorrelation. For KDEs based on least-squares cross-validation, hLSCV, this bias is 185 typically negative (Blundell et al., 2001; Hemson et al., 2005) and exacerbates the autocorrelation-186 187 induced underestimation of home range areas.

188 Mitigation Measure II: KDE_c or AKDE_c

Fleming and Calabrese (2017) derived an improved KDE by calculating the bias in area estimation under a GRF approximation and applying a correction in an area-based coordinate system. By pulling the contours of the location distribution estimate inward towards the data without distorting its shape, this correction removes the tendency of GRF-based methods (including AKDE) to overestimate the area of home ranges, particularly at small *effective sample sizes* (**Figure 2**). Formally correcting the density function estimate allows us to calculate a more reliable home range area and confidence intervals. This correction can be applied to both conventional and autocorrelated GRF-KDEs (then termed KDE_c and AKDE_c, respectively), and is the default method within the ctmm package. As this source of bias is estimator-specific, the mitigation must also be estimator-specific, so this correction cannot be applied to non-GRF KDE approaches such as h_{LSCV} .



Figure 2. Autocorrelated Kernel Density Estimation (AKDE) and area-corrected AKDE (AKDE_c) calculated for one individual from the lowland tapir tracking dataset with: large *effective sample size* ($N \approx 1,566$), medium *effective sample size* ($N \approx 261$), and small *effective sample size* ($N \approx 30$). Displayed errors correspond to % bias of AKDE against AKDE_c of the same individual. Note that for large N values the estimates from AKDE and AKDE_c overlap considerably.

199 Bias III: Autocorrelation estimation bias

The main advantage of AKDE is that it accounts for the autocorrelated structure of animal movement data; for optimal performance, we need to estimate this autocorrelation correctly. Maximum Likelihood (ML) estimation is the standard approach to fitting movement models to animal tracking data (Horne, Garton, Krone, et al., 2007; Michelot et al., 2016) due to its versatility, widespread use, and relatively good performance (Pawitan, 2001). However, ML performs best at large sample sizes, while parameters related to variances and covariances tend to be underestimated in small sample size conditions (Cressie, 2015). As variance-associated 207 parameters are closely related to home range size, their underestimation propagates into 208 underestimated home range areas (Noonan et al., 2019).

209 Mitigation Measure III: pHREML and parametric bootstrapping

Residual Maximum Likelihood (REML) estimation is often used to improve (co)variance parameter 210 estimation with small sample sizes, but it can perform poorly for the class of movement models on 211 which AKDE depends (Fleming et al., 2019). To mitigate the small sample size bias in 212 autocorrelation model parameter estimates, Fleming et al. (2019) developed a series of REML-213 based estimators that focus on small effective sample sizes (perturbative REML; pREML), small 214 215 absolute sample sizes (Hybrid REML; HREML), or both small absolute and small effective sample sizes (perturbative Hybrid REML; pHREML). We focus on pHREML here (Figure 3) as it is the most 216 broadly applicable of these methods and has no serious disadvantages relative to the others, 217 because it combines the bias correction of REML and the stability of ML. It is currently the default 218 parameter estimation method in the ctmm package. 219



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Figure 3. AKDE_c calculated with Maximum Likelihood (ML) and with perturbative Hybrid REML (pHREML) for an individual within the jaguar dataset, showcasing its effect on large absolute but small effective sample size (reduce to a sampling duration of 3 *months*: n = 362 locations, N \approx 3.1), and both small absolute and small effective sample size (3 months thinned to n = 5 locations, N \approx 4). Displayed errors correspond to % bias of ML-fitted AKDE against pHREML-fitted AKDE.

The parametric bootstrap method (Efron, 1982) is another standard solution for the biases caused by ML estimation and can be applied on top of REML-based estimations to further reduce biases. In extreme cases where *effective sample sizes* are ~5 or less, parametric bootstrapping may result in substantial improvements. However, the high computational cost incurred by bootstrapped pHREML (**Supplementary File 1**), coupled with the usually modest improvements it provides, reinforce its use only as a last resort.

227 Bias IV: Unrepresentative sampling in time

From a statistical perspective, evenly spaced temporal sampling of tracking data ensures the widest 228 229 possible range of analytical options. In practice, however, many real-world issues can lead to animal locations being sampled irregularly in time: duty-cycling tags to avoid wasting battery during periods 230 of inactivity, acceleration-informed sampling, device malfunction, habitat-related signal loss, and 231 many other causes (DeCesare et al., 2005; Frair et al., 2004; Horne, Garton, & Kimberly A. Sager-232 Fradkin, 2007). When unaccounted for, such cases can yield biased datasets, causing area 233 estimates associated with over-sampled portions of home ranges to be too large and those 234 associated with under-sampled parts of home ranges to be too small (Fieberg, 2007). There is no 235 guarantee that these contrasting biases cancel each other out, so the overall home range area 236 estimate may be either positively or negatively biased. 237

238 Mitigation Measure IV: wAKDE

Weighted AKDE (or wAKDE) corrects for unrepresentative sampling in time (Fleming et al. 2018) through the larger bias addressed is *where* the area is distributed: it optimally upweights observations that occur during under-sampled times, while optimally downweighting observations occurring during over-sampled times. In IID data, optimal weights are uniform (*i.e.*, there is no temporal sampling bias, as all times are equally important) so there is no advantage to weighting. For autocorrelated data with highly irregular sampling, however, the difference between weighted and unweighted AKDE can be considerable (**Figure 4**).

In practice, very few tracking datasets are perfectly regular, so it is essential to handle data 246 irregularity appropriately. Missing data equate to a loss of information, and these errors can 247 propagate into biases in habitat selection or area-based conservation outputs (Frair et al., 2004). 248 For example, areas with good satellite reception (e.g., open flat landscapes) may appear over-used 249 even when animals did not spend more time in them compared to areas with poorer 250 reception. Shifting sampling schedules (based on behavioral or seasonal patterns) is a common 251 strategy employed in animal tracking projects, due to the trade-off between sampling intensity and 252 battery life (Brown et al., 2012); in these circumstances, weight optimization via wAKDE is critical 253 for comparisons between individuals or populations. 254



pHREML wAKDE_c

Sampling rate shifted from 1 fix every hour to 1 fix every 2 hours

Figure 4. A uniformly weighted AKDEc and an optimally weighted AKDEc (wAKDEc), calculated from an individual from the African buffalo dataset with an irregular sampling schedule likely due to a device malfunction (nicknamed "Pepper"; available within the ctmm package). Displayed errors correspond to % bias of AKDEc core area (50%) against wAKDEc core area (50%).

255 **Combination of mitigation measures**

In practice, different sources of bias frequently occur together in the same datasets. This is a key 256 reason why home ranges are so difficult to estimate accurately. However, the mitigation measures 257 described above can be implemented simultaneously when necessary to combat multiple biases. 258 For example, if a tracking dataset features autocorrelation, small effective sample size, and irregular 259 temporal sampling, we can use pHREML to estimate and select the underlying movement model, 260 261 and then pass the selected model to an optimally weighted area-corrected AKDE (wakdec) to properly estimate home range area. The default settings in the ctmm package have been carefully 262 chosen to balance performance against computational cost, so in this example, only optimal 263 weighting would need to be manually selected by the user. Default values and alternative options 264 are discussed in more detail in the ctmm documentation (Fleming & Calabrese, 2021). 265

To quantify the level of improvement offered by each mitigation measure and to explore the tradeoff 266 between accuracy and computational cost, we performed a detailed simulation study. Our 267 simulations are based on an OUF movement model, which features both correlated velocities (i.e., 268 directional persistence), correlated positions, and restricted space use. We chose the OUF model 269 because it was the most frequently selected across all empirical GPS datasets in the Noonan et al. 270 (2019) study, with 240 out of 369 datasets. We set both the directional persistence and range 271 crossing timescales to one day, and varied the duration of the simulated datasets from 1 to 4,096 272 days in a doubling series, sampled hourly (except for bootstrapped pHREML wAKDEc which was 273 significantly more computationally intensive and impractical to simulate over the whole sampling 274 275 duration). This setup results in effective sample sizes that approximate the duration of each simulated dataset. We then sequentially fit home range estimators in the ctmm package to each 276 simulated dataset in the following order: KDE, AKDE, AKDE, pHREML AKDE, pHREML wAKDE, and 277 bootstrapped pHREML wAKDE_c. This represents a progression from no bias corrections (KDE) 278

through all possible bias corrections applied simultaneously, in order of the typical importance of the corrections. Each simulation was repeated 400 times. We calculated bias as the 95% area estimate of the method in question divided by the exact expectation value of the true 95% area (under the model from which the data were simulated), while the computational cost was the time the simulation took to complete in seconds. All simulations were performed in the R environment (version 3.5.2; R Core Team 2018) using the ctmm package (version 0.5.2; Calabrese *et al.* 2016) and conducted on the University of Maryland High Performance Cluster.

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Table 1. Mean improvement (%) in area estimation for each AKDE method compared to baseline KDE, over small (N < 32),</th>medium (32 > N < 512), and large effective sample sizes (N > 512). Numbers in red denote underperformance.

	Improvement over KDE			
Methods	Small N	Medium N	Large N	
AKDE	51.3%	-31.3%	-78.4%	
AKDEc	42.6%	48.3%	36.4%	
pHREML AKDE _c	59.8%	52.9%	40.4%	
pHREML wAKDE _c	59.4%	52.9%	43.1%	
Bootstrapped pHREML wAKDE $_{c}$	72.0%	NA	NA	

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Compared to conventional KDE, the original AKDE offered clear advantages for small effective 288 sample sizes, but failed to improve area estimation for medium and large effective sample sizes (N 289 > 32; Table 1). By solving the oversmoothing bias, AKDE_c improved over KDE for all effective sample 290 sizes. The next technique, pHREML-fitted AKDE_c (ctmm default settings) further improved over 291 conventional KDE and all previous measures, and stabilized the closest to 0% relative error after 292 only eight sampling days (Figure 5a). Additional mitigation measures do lead to an increasingly 293 higher computational cost: for the full sampling duration (4,096 days), pHREML-fitted wAKDE_c ran 294 on average 2.7 times longer than the original AKDE, and 230 times longer than a conventional KDE 295 296 (Figure 5b, Supplementary File 1). With an Intel i7 3.9GHz processor using a single core, and an hourly tracking dataset collected for a year, this could correspond to an increase from a few 297

seconds to approximately 45 minutes. However, unlike AKDE, conventional KDE does not run any
 autocorrelation model selection, or numerical optimization of parameter estimates.



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Figure 5. (a) Mean relative error (%) of the home range area estimation and **(b)** computational cost (log-transformed) for each method, by sampling duration (in days). Based on simulations (repeated 400 times) where the position and velocity autocorrelations were kept constant at 1 day and 1 hour, respectively. Error bars represent 95% confidence intervals. AKDE and AKDEc have almost overlapping performances, as well as pHREML-fitted AKDEc and pHREML wAKDEc.

301 **Discussion**

The techniques presented in this paper represent a family of home range estimators starting with conventional GRF-KDE and progressing through a series of estimation methods designed to mitigate bias arising when the core assumption of IID data is not met. These methods are implemented with efficient computational algorithms that work with both small and large animal tracking datasets. We have brought these techniques together in a single document to demonstrate
when each correction is applicable, the degree to which home range estimates can be improved,
and when and how they can be combined to handle the unique quirks of each tracking dataset to
yield accurate home range estimates.

The AKDE family of estimators are all implemented in the ctmm R package (Calabrese et al., 2016), 310 so we provide an annotated R script in the supplementary material of this paper to guide users 311 through the applications of these techniques (Supplementary File 2). The current default settings 312 313 are pHREML, for estimating movement model parameters, and (A)KDE_c, for estimating home ranges. The decision between KDEc and AKDEc is determined using model selection, and dependent 314 315 on whether the data are independently distributed or autocorrelated, respectively. We recommend that users keep pHREML and (A)KDE_c as the default settings and especially caution against 316 changing these settings for any effective sample sizes below 20. When working with legacy data 317 where small effective sample sizes are a serious concern, but additional data collection is not an 318 option, bootstrapped pHREML may be used as a method of last resort to obtain the best possible 319 home range estimates. However, due to the high computational cost of using pHREML, users 320 should decide on a bias threshold (typically > 1-5% with an initial pHREML estimate) before 321 applying this measure (see Supplementary File 2 for how to determine this bias threshold). Finally, 322 wAKDE_c can account for temporal sampling bias (*i.e.*, missing or irregular tracking data), but is 323 switched off by default due to its considerable computational cost (approximately 200 times longer 324 than KDE). 325

Most mitigation measures we have discussed here become increasingly valuable at small sample sizes (absolute and/or effective), allowing researchers to maximize the value of legacy datasets or to handle situations where larger *effective sample sizes* are impossible to obtain (*e.g.*, on smaller animals for which battery size limits the temporal duration of GPS lifespans). Nevertheless, the application of these analytical methods should not replace careful study design before data

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collection, tailored to address specific research questions (Fieberg & Börger, 2012). When the main goal of a study is home range estimation, the sampling duration should be many times larger than the average *range crossing time* of the focal species. This ensures that the *effective sample size* will be large enough to facilitate reliable estimation of the area of home ranges. Achieving this goal may require researchers to decrease the sampling rate of their devices to save battery power, although small *effective sample sizes* may be inevitable even in these conditions due to battery constraints, specific ranging behaviors, or short lifespans.

Although AKDEs provide reliable home range area estimations in the conditions presented in this 338 manuscript, there are scenarios in which they fail. A known issue of KDE methods is that their 339 estimates can spill over discontinuities, such as hard boundaries (e.g., coastal lines and water 340 sources for terrestrial species, land for aquatic species) or three-dimensional features (e.g., steep 341 terrain, impermeable barriers), and have difficulties resolving narrow movement corridors (Guo et 342 343 al., 2019; Péron, 2019; Silverman, 1986; Worton, 1995). The positive bias from boundary spillover is likely less influential than the negative bias due to unmodeled autocorrelation; nevertheless, it is 344 possible to correct for hard boundaries by following the workflow presented in appendix 3 of 345 Noonan et al. (2019). Kernel density methods also fail to adequately resolve non-stationary behavior 346 and nomadism (Lichti & Swihart, 2011; Nandintsetseg et al., 2019), as nomadic species lack site 347 fidelity to movement pathways or key sites (e.g., breeding or wintering areas). Addressing non-348 stationarity requires home range estimates that accommodate multiple centers and allowing for 349 variation in use patterns (Breed et al., 2017). In addition, a misspecified model due to migratory 350 351 behaviors will affect the accuracy of AKDE area outputs due to the stationary movement models being leveraged (OU, OUF, IID). However, if an animal is not range resident, then the data are not 352 appropriate for any home range estimation method. 353

Moving forward, we hope to address two remaining challenges in home range estimation: location error and resource selection (which includes boundary interactions). Home range estimation is not

as sensitive to location error as fine-scale quantities, such as speed estimation (Noonan et al., 356 2019). However, any biological inferences can become compromised if location errors are 357 comparable to the relevant movement scales. At present, locations errors can be partially 358 accounted for in the autocorrelation modeling stage of the ctmm workflow (Fleming et al., 2021). 359 First, the autocorrelation and bandwidth calculations are error-informed, which mitigates various 360 biases in autocorrelation and bandwidth estimates that would otherwise occur had location error 361 been ignored. Second, location estimates are fed through a Kalman smoother before kernel 362 placement, which counteracts overdispersal. However, there are two adjustments that could 363 provide further improvements. First, more erroneous location estimates could be optimally 364 downweighted in the sense of Fleming et al. (2018), which would increase statistical efficiency. 365 Second, instead of employing a Kalman smoother that is only consistent with normal distributions, 366 the data could be nonlinearly smoothed via iteration. Finally, the inclusion of resource selection 367 parameters into KDE has been considered by Guo et al. (2019) and Péron (2019). Resource selection 368 369 can include the respecting of hard boundaries, as well as softer habitat preferences. The influence 370 of resource selection on AKDE can be considered at various stages, including autocorrelation modeling, bandwidth optimization, and kernel shape, and will likely take multiple research efforts to 371 fully implement in a general use software solution. 372

Only by estimating home ranges in a comparable way across sampling schedules, study designs, 373 and behavioral idiosyncrasies can wildlife researchers provide wildlife managers and practitioners 374 with accurate information for conservation planning and land-use decision-making. Movement 375 ecology has reached an inflection point where it is no longer possible to ignore autocorrelation: 376 using autocorrelated tracking datasets with estimators that assume IID data will result in 377 underestimated home range areas (Noonan et al. 2019). Although further technological advances 378 will only increase the amount of autocorrelation present in tracking data, autocorrelation is often 379 still present even in VHF data and should not be overlooked. We have provided guidelines to obtain 380

accurate home range area estimates with the AKDE family of home range estimators which, in their 381 current form, provide the most reliable and flexible solution for home range area estimation. These 382 methods were explicitly designed to work synergistically, eliminating discrepancies between 383 empirical reality and estimator assumptions that drive home range under- or overestimation with 384 385 conventional techniques. Furthermore, these techniques can be implemented with open source software and code (Calabrese et al., 2016, 2021), and new movement processes can be easily 386 added into the AKDE workflow as they are developed. This flexibility "future proofs" the AKDE family 387 of analyses by allowing it to be tailored to new datasets, movement behaviors, and species as 388 necessary. 389

Author contributions

391 CHF, MJN, WFF and JMC conceived the ideas. CF conducted the simulations. JMC and IS led the 392 writing of the manuscript. All authors contributed critically to the draft and gave final approval for 393 publication.

394

395 **Conflict of Interest statement**

The authors declare no conflict of interest.

397

398 Data availability statement

All empirical datasets used in the manuscript are currently openly accessible: the African buffalo tracking data are archived in the MoveBank Data Repository (Cross et al., 2016) and partially included in the ctmm package (Fleming & Calabrese, 2021); lowland tapir tracking data are archived in the Dryad Digital Repository (Fleming et al., 2019); jaguar tracking data are available as a data paper (Morato et al., 2018) and partially included in the ctmm package (Fleming & Calabrese, 2021). Simulation data and the code required to reproduce the R tutorial are available on GitHub (https://github.com/ecoisilva/AKDE_minireview).

406

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Supplementary file 1: Computational costs



KDE

Supplementary figure 1. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the **Kernel Density Estimation (KDE)** method. Based on simulations (repeated 400 times) of different sampling durations (1 to 4,096 days).

AKDE



Supplementary figure 2. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the Autocorrelated Kernel Density Estimation (AKDE) method. Based on simulations (repeated 400 times) of different sampling durations (1 to 4,096 days).

AKDE_c



Supplementary figure 3. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the **area-corrected Autocorrelated Kernel Density** Estimation (AKDE_c) method. Based on simulations (repeated 400 times) of different sampling durations (1 to 4,096 days).

pHREML AKDE_c



Supplementary figure 4. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the area-corrected Autocorrelated Kernel **Density Estimation** method fitted with **perturbative Hybrid REML (pHREML AKDE**_c). Based on simulations (repeated 400 times) of different sampling durations (1 to 4,096 days).

pHREML wAKDE_c



Supplementary figure 5. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the weighted, area-corrected, Autocorrelated Kernel Density Estimation method fitted with perturbative Hybrid REML (pHREML wAKDE_c). Based on simulations (repeated 400 times) of different sampling durations (1 to 4,096 days).





Supplementary figure 6. Relative home range area, *i.e.*, where the true home range area is scaled to 1, versus computational cost (in logarithmic scale) for the **boostrapped**, **weighted**, **area-corrected Autocorrelated Kernel Density Estimation** method fitted with **perturbative Hybrid REML (Bootstrapped pHREML wAKDE**_c). Based on simulations (repeated 400 times) of different sampling durations (1 to 4 days).

Supplementary file 2: Autocorrelation-informed home range estimation with the ctmm R package

Introduction

Home range estimation is a key output from animal tracking datasets, but the inherent properties of animal movement can lead traditional methods to under- or overestimated their size. Autocorrelated Kernel **Density Estimation (AKDE)** methods were designed to be statistically efficient while explicitly dealing with the complexities and biases of modern movement data, such as *autocorrelation, small sample sizes*, and *missing or irregularly sampled data*.

This tutorial is a companion piece to our manuscript "Autocorrelation-informed home range estimation: a review and practical guide". The **AKDE** family of home range estimators will be run using **R software** (https://www.r-project.org/) and the ctmm package (Calabrese et al., 2016). For any definitions, check the main manuscript or the *Glossary*. The techniques and mitigation measures available in this package include:

Method	When to run?	What does it do?	R function
AKDE	Tracking data is autocorrelated	Estimates range distributions from autocorrelated data, by conditioning on an autocorrelation model.	akde(…, debias = FALSE)
AKDEc	If using GRF-based KDEs (such as AKDE)	Removes the tendency of Gaussian reference function (GRF) methods to overestimate the area of home ranges.	akde(…, debias = TRUE)
pHREML	Small (absolute and effective) sample sizes	Improves upon ML and REML autocorrelation estimation, mitigating small sample size biases.	<pre>ctmm.select(, method = "pHREML")</pre>
wAKDEc	Irregular sampling schedules or missing data	Upweights observations that occur during under-sampled times, while downweighting those occurring during over-sampled times.	akde(…, weights = TRUE)
Parametric bootstrap	Extremely small effective sample size	Calculates and corrects for autocorrelation estimation biases, by simulating from an approximate sampling distribution.	ctmm.boot()

 $AKDE_c$ and pHREML are default arguments within the akde() and ctmm.select() functions, respectively. Both measures will run automatically if arguments debias and method are left unspecified. For most situations, we recommend keeping both of these arguments as the default.

```
# Installing & loading package:
install.packages("ctmm")
library(ctmm)
```

We provide a guide to **home range estimation** using the following workflow:

- Step 1. Formatting and loading an animal tracking dataset;
- Step 2. Checking for the *range residency* assumption;
- Step 3. Selecting the best-fit movement model through model selection;
- Step 4. Feeding a movement model into the home range estimator;
- Step 5. Evaluating additional biases, applying mitigation measures.

Data Preparation

We will use two datasets, both available within the ctmm package: African buffalos (Syncerus caffer), and Mongolian gazelles (Procapra gutturosa). Information on the data collection protocol is available in Cross et al. (2009) and Fleming et al. (2014). The ctmm package requires data to conform to Movebank naming conventions (https://www.movebank.org/node/2381). We recommend uploading your data to Movebank (http://www.movebank.org/) as this will facilitate data preparation, and ensure that your data are correctly formatted for ctmm. If needed, Movebank allows you to keep your data private.

We will focus on the simplest data structure:

- animal ID or ID An individual identifier for each animal tracked;
- timestamp or t The date and time corresponding to a sensor measurement;
 - Example: 2021-01-01 18:31:00.000
 - * Format: yyyy-MM-dd HH:mm:ss.SSS
- longitude or x The geographic longitude of the location as estimated by the sensor.
 - **Example**: -121.1761111
 - * Units: decimal degrees, WGS84 reference system.
- latitude or y The geographic latitude of the location as estimated by the sensor;
 - Example: -41.0982423
 - * Units: decimal degrees, WGS84 reference system.

Location can also be described as UTM locations instead of latitude/longitude. In this case, you should provide UTM easting, UTM northing, and UTM zone. For all terms and conventions, please see the full
vocabulary list here: http://vocab.nerc.ac.uk/collection/MVB/current/.

Step 1. – Formatting and loading an animal tracking dataset

You can import data into R through the read.table() or read.csv() functions; make sure to navigate to the appropriate folder or working directory. For example:

```
# First, list all files in your current directory:
list.files() # make sure this leads to the location of your file
```

Second, load the correct file:

```
animal0_longlat <- read.csv(here("example_data_longlat.csv"))
head(animal0_longlat)</pre>
```

```
## ID timestamp longitude latitude
## 1 animal0 2005-07-14 05:35 30.59648 65.24774
## 2 animal0 2005-07-14 07:35 30.53256 65.27085
## 3 animal0 2005-07-14 08:34 30.52398 65.26446
## 4 animal0 2005-07-14 09:35 30.52848 65.25948
## 5 animal0 2005-07-14 10:35 30.53382 65.26643
## 6 animal0 2005-07-14 11:34 30.49970 65.27868
animal0_utm <- read.csv(here("example_data_utm.csv"))
head(animal0_utm)</pre>
```

##	ID	timestamp	UTM.Easting	UTM.Northing	UTM.zone		
## :	animal0	2005-07-14 05:35	387730.0	7238204	36N		
## 2	2 animal0	2005-07-14 07:35	384846.3	7240894	36N		
## 3	3 animal0	2005-07-14 08:34	384418.1	7240197	36N		
## 4	l animalO	2005-07-14 09:35	384606.5	7239634	36N		
## !	5 animal0	2005-07-14 10:35	384885.8	7240399	36N		
## (3 animal0	2005-07-14 11:34	383347.9	7241826	36N		
# Finally, convert to telemetry object:							

animalOa <- as.telemetry(animalO_longlat)

Minimum sampling interval of 59 minutes in animal0

Geocentric coordinates not found. Looking for UTM coordinates.

Minimum sampling interval of 59 minutes in animal0

```
# if left unspecified, as.telemetry() will assume timezone = UTC
```

Both these files represent the same individual, with either *longitude/latitude*, or UTM coordinates (*easting*, *northing*, and *UTM zone*). The **as.telemetry()** function will immediately identify the columns if they are correctly named, then output the minimum sampling interval for each individual in the dataset. In this example, **animal0** has a minimum sampling interval of 59 minutes.

1.1. Buffalo tracking data

For this tutorial, we will use data already prepared into a list of telemetry objects. We can load it directly from the ctmm R package with the data() function:

```
data("buffalo")
animal1_buffalo <- buffalo[[4]] # selecting individual number 4
head(animal1_buffalo)
##
                   timestamp longitude latitude
                                                          t
                                                                    х
                                                                              V
## 17517 2006-04-25 05:09:00 31.73749 -24.19705 1145941740 -51803.35 -2715.663
## 17518 2006-04-25 06:09:00 31.73653 -24.19929 1145945340 -51569.29 -2845.660
## 17519 2006-04-25 07:09:00
                             31.73946 -24.20100 1145948940 -51340.72 -2576.353
## 17520 2006-04-25 08:09:00
                             31.73987 -24.20092 1145952540 -51344.11 -2533.788
                             31.74086 -24.20365 1145959740 -51029.45 -2474.771
## 17521 2006-04-25 10:09:00
## 17522 2006-04-25 11:09:00 31.74098 -24.20370 1145963340 -51022.23 -2463.655
```

Plotting locations:
plot(animal1_buffalo)



This dataset showcases an irregular sampling schedule: the buffalo nicknamed "*Pepper*" had a sampling rate shift from one fix every hour to one fix every two hours. We will use this dataset to highlight data irregularity and the **wAKDE** mitigation measure.

1.2. Gazelle tracking data

```
data("gazelle")
animal2_gazelle <- gazelle[[11]] # selecting individual number 11</pre>
head(animal2_gazelle)
##
                                    t
                х
                            у
## 2742
         18152.70
                   -8539.799
                                    0
## 2743
         15931.16 -32069.788 1306800
## 2744
         17678.84 -28632.329 1396800
## 2745
         23135.50 -23820.789 1486800
## 2746 -20310.78
                  20348.792 2419200
## 2747 -17920.31
                  20598.668 2509200
# Plotting locations:
plot(animal2_gazelle)
```



Mongolian gazelles have a **home range crossing time** of a few months, and with a maximum longevity around 10 years, it is impossible to get a considerable **effective sample size** no matter the study duration (Fleming et al., 2019). We will use this dataset to highlight how to check **effective sample size** and apply the **parametric bootstrap** mitigation.

Data Analysis

Step 2. – Checking for the range residency assumption

First, we want to check if our first tracking dataset (animal1_buffalo) can be used for home range estimation by checking for **range residency**. To achieve this, we calculate the **semi-variance function (SVF)**, and visualize it through the **variogram()** function.

Variograms are an unbiased way to visualize *autocorrelation* structure, representing the average square displacement (y-axis) over a specific time lag (x-axis). To facilitate interpretation, we have the **SVF** of animal1_buffalo zoomed out (right) to showcase all time lags and (left) zoomed in to showcase time lags up to two months:

```
level <- 0.95 # we want to display 95% confidence intervals
xlim <- c(0,2 %#% "month") # to create a window of 2 months
SVF <- variogram(animal1_buffalo)
par(mfrow = c(1,2))
plot(SVF, fraction = 1, level = level)
abline(v = 1, col = "red", lty = 2) # adding a line at 1 month
plot(SVF, xlim = xlim, level = level)
abline(v = 1, col = "red", lty = 2)
```



We can see that the variogram flattens (*i.e.*, reaches an asymptote) after approximately **1 month** (red line). This also indicates at how coarse the timeseries needs to be to assume independence (no autocorrelation), and corresponds to when traditional methods —such as **minimum convex polygons (MCPs)** and **Kernel Density Estimators (KDEs)**— could be applied without violating their assumptions.

Step 3. – Selecting the best-fit movement model through model selection

It is necessary to choose a home range estimator that accounts for the autocorrelated structure of the data, now that we see that it is **not** independently and identically distributed (non-IID). We need to test what movement model may explain the autocorrelated structure of our tracking data. We can run different movement processes with **maximum likelihood (ML)** or other parameter estimators, such as **perturbative Hybrid REML (pHREML)**. To facilitate further comparisons, we will run both ML and pHREML with the ctmm.select function.

Calculate an automated model guesstimate: GUESS1 <- ctmm.guess(animal1_buffalo, interactive = FALSE)</pre>

```
# Automated model selection, starting from GUESS:
FIT1_ML <- ctmm.select(animal1_buffalo, GUESS1, method = 'ML')</pre>
FIT1_pHREML <- ctmm.select(animal1_buffalo, GUESS1, method = 'pHREML')</pre>
## reminder: it will default to pHREML if no method is specified.
summary(FIT1_ML)
## $name
## [1] "OUF anisotropic"
##
## $DOF
                            speed
##
        mean
                  area
   11.24296 20.01326 747.72143
##
##
## $CI
##
                                    low
                                                         high
                                              est
## area (square kilometers) 431.446013 706.20245 1047.55828
## t[position] (days)
                               6.775273 12.18604
                                                     21.91786
## t[velocity] (minutes)
                              31.861346
                                         35.81413
                                                     40.25730
## speed (kilometers/day)
                              15.948352 16.54124
                                                     17.13385
summary(FIT1_pHREML)
## $name
## [1] "OUF anisotropic"
##
## $DOF
##
                            speed
        mean
                  area
##
    10.34454 15.65772 746.09401
##
## $CI
##
                                    low
                                                         high
                                              est
## area (square kilometers) 439.064822 773.50766 1201.09155
## t[position] (days)
                               6.664052 13.36206
                                                     26.79221
## t[velocity] (minutes)
                              31.807736
                                         35.75689
                                                     40.19636
## speed (kilometers/day)
                              15.949646 16.54326
                                                     17.13658
```

Within these summaries, **\$name** provides the selected best-fit model, **\$DOF** provides information on the degrees of freedom (where **\$DOF["area"]** corresponds to the **effective sample size** of the home-range area estimate), and **\$CI** are the parameter outputs (area, position autocorrelation timescale, velocity autocorrelation timescale, and speed).

The typical pool of candidate models includes isotropic (when diffusion is the same in every direction; symmetrical) and anisotropic (when diffusion varies with direction; asymmetrical) variants. The automated model selection shows that *OUF anisotropic* (anisotropic Ornstein-Uhlenbeck foraging process) is our best-fit model. This movement process features a home range, correlated positions, and correlated velocities. To check the full model selection table, we can run the following command:

	$\Delta AICc$	$\Delta \text{RMSPE} (\text{km})$	DOF[area]
OUF anisotropic	0.0000	2.224045	15.657669
OU anisotropic	295.0898	2.634793	9.638283
OUF isotropic	330.2236	3.564231	11.204035
OUf anisotropic	1890.8878	0.000000	333.620712

FIT1_pHREML_verbose <- ctmm.select(animal1_buffalo, GUESS1, verbose = TRUE)
summary(FIT1_pHREML_verbose)</pre>

By adding the argument verbose = TRUE we have access to the model selection table. By default, model selection is based on *Akaike's Information Criterion adjusted for small sample sizes* (AICc). The ctmm package also offers BIC, LOOCV, and HSCV. LOOCV seems to work slightly better for very small datasets, but we recommend AICc for the majority of datasets.

Step 4. – Feeding a movement model into the home range estimator

Now we can fit this movement process into the akde() function, and estimate the home range of animal1_buffalo. This function currently defaults to the area-corrected AKDE, or AKDEc (Fleming & Calabrese 2017):

```
# Run an area-corrected AKDE:
UD1_ML <- akde(animal1_buffalo, FIT1_ML)
UD1_pHREML <- akde(animal1_buffalo, FIT1_pHREML)
summary(UD1_pHREML)$CI # home range area estimation
## low est high
## area (square kilometers) 429.6573 756.9343 1175.357
```

We have calculated our home range for animal1_buffalo, resulting in an estimation of 757 km² (with 95% confidence intervals: 430–1,175 km²).

Step 5. – Evaluating additional biases, applying mitigation measures

5.1. Buffalo tracking data

```
summary(UD1_pHREML)$DOF["area"] # effective sample size of animal1
## area
## 15.65772
nrow(animal1_buffalo) # absolute sample size
## [1] 1725
```

Our output here also reveals more information regarding our dataset: the effective sample size (N) and the absolute sample size (n). We can return this measure with the summary function: in our case, the N for animal1_buffalo is 15.7. Comparatively, our absolute sample size is easy to output, as it is the total number of observations within our dataset (n = 1,725).

As mentioned earlier, animal1_buffalo had a device malfunction that led GPS fixes to shift from one fix per hour, to one fix every two hours. As such, this individual is particularly suited for a weighted AKDEc (or wAKDEc), so we can re-run the function with weights set to TRUE:

UD1w_pHREML <- akde(animal1_buffalo, FIT1_pHREML, weights = TRUE)
summary(UD1w_pHREML)\$CI # home range area estimation (weighted)
low est high</pre>

area (square kilometers) 432.2234 761.4551 1182.376

Our new home range area estimation for animal1_buffalo is 761 km² (with 95% confidence intervals: 432-1,182 km²). We can now plot our home range estimate for animal1_buffalo:

```
# Creating an extent that includes both UDs at the 95% CI level:
EXT <- extent(list(UD1_ML, UD1_pHREML, UD1w_pHREML), level = 0.95)</pre>
```

```
# Plotting pHREML (with and without weights) side-by-side:
par(mfrow = c(1,2))
plot(animal1_buffalo, UD = UD1_pHREML, ext = EXT)
title(expression("pHREML AKDE"["C"]))
plot(animal1_buffalo, UD = UD1w_pHREML, ext = EXT)
title(expression("pHREML wAKDE"["C"]))
```



For animal1_buffalo, the difference between model parameter estimators is not substantial; we only have a ~5.7% AKDE area underestimation by ML compared to pHREML. However, the data fits the spatial locations much better.

(1 - summary(UD1_ML)\$CI[1,2] / summary(UD1w_pHREML)\$CI[1,2]) * 100

[1] 5.742588

5.2. Gazelle tracking data

We can also check the difference with animal2_gazelle's tracking data, where the small effective sample size issue is clearer:

GUESS2 <- ctmm.guess(animal2_gazelle, interactive = FALSE)
FIT2_ML <- ctmm.select(animal2_gazelle, GUESS2, method = 'ML')
FIT2_pHREML <- ctmm.select(animal2_gazelle, GUESS2, method = 'pHREML')</pre>

UD2_ML <- akde(animal2_gazelle, FIT2_ML) UD2_pHREML <- akde(animal2_gazelle, FIT2_pHREML)

With animal2_gazelle, we have a more substantial area underestimation by ML compared to pHREML (~15.2%). We can also see that our *effective sample size* is only 4.5, with an *absolute sample size* of 49 ($N \ll n$).

```
(1 - summary(UD2_ML)$CI[1,2] / summary(UD2_pHREML)$CI[1,2] ) * 100
```

[1] 15.19245
summary(UD2_pHREML)\$DOF["area"] # effective sample size

area
4.528926
nrow(animal2_gazelle) # absolute sample size

[1] 49

At this point, we have selected a movement process, fed it into a home range area estimation with different model parameter estimators, and corrected for irregular sampling rates. With **small effective sample sizes**, it is important to see if **parametric bootstrapping** may be worth it to further reduce our estimation error. In order to do so, we can check the expected order of bias from pHREML:

```
# Expected order of pHREML bias:
1/summary(FIT2_pHREML)$DOF['area']^2
```

```
## area
```

0.04875392

The bias is currently $\mathcal{O}(5\%)$ ("in the order of" 5%). As such, we will run parametric bootstrapping for animal2_gazelle. The relative error target is 1% by default (argument error = 0.01), but can be adjusted if necessary.

start_time <- Sys.time() # start recording running time
BOOT <- ctmm.boot(animal2_gazelle, FIT2_pHREML, trace = 2)
note: this function incurs substantial computational cost, may take hours.
(total_time <- Sys.time() - start_time) # output running time</pre>

summary(BOOT)

```
## $name
## [1] "OUF isotropic"
##
## $DOF
##
        mean
                  area
                            speed
##
    3.196957 3.530735 10.000358
##
## $CI
##
                                     low
                                                   est
                                                               high
## area (square kilometers) 3429.704883 14089.021613 32137.455223
## t[position] (months)
                                0.000000
                                              1.781242
                                                           3.758819
## t[velocity] (hours)
                                2.248230
                                             10.481973
                                                          48.870349
## speed (kilometers/day)
                                5.590052
                                              8.072361
                                                          10.551247
```

1/summary(BOOT)\$DOF['area']^3 # expected order of bias

area ## 0.02271981

We can see that the expected order of bias was reduced to 2.3%, which is comparable to the numerical error target of 1%. To reduce the numerical error further, we would need to change the default relative error target of ctmm.boot, but the computational cost would continue to increase, and the comparably large statistical bias (2%) would remain.

Now we will calculate the **AKDEc** based on the estimated parameters, and plot the home range of animal2_gazelle. Because of small effective sample size, we set optimal weights to TRUE for improved statistical efficiency:

UD2_bpHREML <- akde(animal2_gazelle, BOOT, weights = TRUE)
summary(UD2_bpHREML)\$CI</pre>

low est high
area (square kilometers) 3231.504 13274.82 30280.25

Finally, we have calculated our home range for animal2_gazelle, with an estimated area of 13,274 square

kilometers (with 95% confidence intervals: 3,231-30,280 km²). Our uncertainty with animal2_gazelle is substantially higher than with animal1_buffalo, as expected due to the small effective sample size.

```
# Creating an extent that includes both UDs at the 95% CI level:
EXT <- extent(list(UD2_pHREML, UD2_bpHREML), level = 0.95)
# Plotting pHREML and bootstrapped-pHREML side-by-side:
par(mfrow = c(1,2))
plot(animal2_gazelle, UD = UD2_pHREML, ext = EXT)
title(expression("pHREML AKDE"["C"]))
plot(animal2_gazelle, UD = UD2_bpHREML, ext = EXT)
title(expression("Bootstrapped pHREML wAKDE"["C"]))
```



The results presented here were generated with R version 4.1.1, and ctmm version 0.6.0.

Glossary

- *Home range*: the area repeatedly used throughout an animal's lifetime for all its normal behaviors and activities, excluding occasional exploratory moves.

- Range residency: the tendency of an animal to remain within their home range.
- Home range crossing time: the time required for an animal to cross the linear extent of its home range.
- Absolute sample size (n): the observations in a dataset.

- Effective sample size (N): number of range crossings that occurred during the observation period. Can be roughly estimated by dividing the duration of the tracking dataset by the average home range crossing time parameter.

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