# Decomposing phenotypic skew and its effects on the predicted response to strong selection

3	Joel L. Pick <sup>1,2*</sup> , Hannah E. Lemon <sup>1</sup> , Caroline E. Thomson <sup>1</sup> & Jarrod D. Hadfield <sup>1</sup>
4	<sup>1</sup> Institute of Evolutionary Biology, University of Edinburgh, Edinburgh,
5	United Kingdom
6	<sup>2</sup> Centre of Biodiversity Dynamics, Norwegian University of Science and
7	Technology, Trondheim, Norway
8	* Corresponding Author: joel.l.pick@gmail.com

The major frameworks for predicting evolutionary change assume that a phenotype's 9 underlying genetic and environmental components are normally distributed. However, 10 the predictions of these frameworks may no longer hold if distributions are skewed. 11 Despite this, phenotypic skew has never been decomposed, meaning the fundamental 12 assumptions of quantitative genetics remain untested. Here, we demonstrate that 13 the substantial phenotypic skew in the body size of juvenile blue tits (Cyanistes 14 caeruleus) is driven by environmental factors. Although skew had little impact on 15 our predictions of selection response in this case, our results highlight the impact 16 of skew on the estimation of inheritance and selection. Specifically, the non-linear 17 parent-offspring regressions induced by skew, alongside selective disappearance, can 18 strongly bias estimates of heritability. The ubiquity of skew and strong directional 19 selection on juvenile body size implies that heritability is commonly overestimated, 20 which may in part explain the discrepancy between predicted and observed trait 21 evolution. 22

Quantitative genetics describes how traits respond to selection in terms of selection and 23 Typically we use two equations to describe this, the breeder's equation (1)inheritance. 24 Chapter 12) and Lande's gradient equation (<sup>2</sup> Eq 7). The breeder's equation gives the 25 predicted response to selection as the heritability  $(h^2)$  multiplied by the selection differential 26 (S), whereas Lande's gradient equation describes the response to selection as the additive 27 genetic variance  $(V_A)$  of the trait multiplied by the selection gradient  $(\beta)$ . Although these 28 frameworks are generally thought to be interchangeable, they only converge when phenotypes 29 (and their genetic and environmental components) are normally distributed or fitness functions 30 (the relationship between a trait and fitness) are linear (<sup>3</sup> Chapter 29). Given that fitness 31 functions are highly unlikely to be linear in practice<sup>4;5</sup>, any deviation from normality can 32 lead to problems with the application of these equations. Consequently, normality is seen 33 as a fundamental assumption in quantitative genetics<sup>6-8</sup>, yet to our knowledge has not been 34 directly tested, despite the major consequences it has for how traits are predicted to respond 35 to selection 9-17. 36

The most natural interpretation of heritability in the context of the breeder's equation is the 37 slope of a *linear* parent-offspring (PO) regression  $^{12-14;18;19}$ , whilst S (the covariance between 38 a trait and fitness) describes the linear relationship between a phenotype and fitness. The 39 accuracy of the breeder's equation relies heavily on the linearity of both of these functions -40 if both are non-linear, the residuals from the linear functions may be correlated, creating a 41 'spurious response to selection'<sup>14</sup>. The linearity of the parent-offspring relationship breaks 42 down when the amount of skew (asymmetry) differs between genetic and environmental 43 components<sup>20;21</sup>, with genetic and environmental skew causing curvature in opposite directions 44 (Figure 1). Formally, a distribution is skewed when it has a non-zero third central moment. 45

<sup>46</sup> Whilst the gradient equation is robust to environmental skew, it doesn't correctly describe the <sup>47</sup> response to selection in the presence of genetic skew if the fitness function is non-linear (<sup>11</sup> Eq <sup>48</sup> 42). Environmental skew, through it's contribution to phenotypic skew, can, however, impact

the estimation of  $\beta$  when it is approximated using Lande-Arnold regression<sup>5;17;22</sup>.

<sup>50</sup> Although extensions to these two equations have been derived that allow for the non-linearity <sup>51</sup> of the PO-regression<sup>12</sup> and the non-normality of genetic values<sup>11</sup>, the majority of the work <sup>52</sup> in this area remains theoretical. Non-linearity in PO-regressions has been demonstrated in

the lab<sup>12;23–27</sup> and ad-hoc methods have been used to test for skew at the genetic level<sup>28;29</sup>. 53 Nevertheless, to our knowledge, no study has 1) relaxed the normality assumptions when 54 making statistical inferences to examine the origin and extent of skew at different levels, and 55 2) explored how observed patterns of natural selection interact with skew to determine how 56 well these two equations predict selection response in the wild. 57

Juvenile body size is under strong, persistent, directional selection across taxa<sup>30</sup>, yet is known 58 to show little response to this selection<sup>31</sup>. We show that juvenile body size is highly negatively 59 skewed (long tail of small individuals) across bird species, but the origin of this skew is 60 unknown. To determine this, we developed statistical methods to decompose the phenotypic 61 distribution into a set of skew-t distributions, and predict the shape of PO-regression based 62 on the estimated skew. We applied these methods to data from a long-term cross-fostering 63 experiment of a wild bird population. By estimating survival selection acting on juvenile body 64 size, we tested the robustness of the predicted response to selection from the breeder's and 65 gradient equations. 66

#### Results 67

#### Prevalence of Phenotypic Skew 68

Across 27 species of birds, tarsus length (a common measure of structural size) was substantially 69 negatively skewed (long tail of small individuals) in juveniles (coefficient of skew: -1.054 70 [-1.394, -0.686], pMCMC<0.001), but not adults (-0.302 [-0.641, 0.052], pMCMC=0.086), 71 with tarsus length being significantly more skewed in juveniles than adults (difference = -0.752

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[-1.124, -0.366], pMCMC<0.001; Figure 2). 73

#### Decomposing Phenotypic Skew 74

Using data on four juvenile body size traits (tarsus length, head-bill length, mass and wing 75 length), measured on 15 day old chicks from a long-term cross-fostering experiment on a wild 76 population of blue tits, we decomposed phenotypic skew into genetic, between- and within-nest 77 environmental components. We used a mixed model approach with skew-t distributed random 78 effects which allowed the extent and direction of skew to vary between these levels. There 79 was considerable phenotypic skew in all four traits, with the coefficient of skew ranging from 80 -0.51 to -1.60 (Figure 3). There was little evidence of genetic skew in any trait (Figure 3, 81 Tables S5, S8, S11 and S12 and further discussion in supplementary methods). Phenotypic 82 skew was instead driven by considerable environmental skew at both between- and within-nest 83 levels, with the relative magnitude of this skew varying between traits (Figure 3, Tables S6, 84 S9, S12 and S15). 85

Given the environmental origin of the negative phenotypic skew, we would expect a convex 86 PO-regression for all traits<sup>20</sup> (Figure 1c). By deriving a method to compute this non-linear 87 PO-regression (Equation 1), we can show that for all traits the slope in the lower tail of the 88 distributions is close to zero, but becomes steeper with increasing body size (Figure 3). 89

#### <sup>90</sup> Selection on Juvenile Body Size

To quantify selection acting on body size, we estimated the linear and quadratic effects of body 91 size on survival from both day 15 to fledging and fledging to local recruitment in a bivariate 92 probit event-history model. As expected, all traits showed significant positive linear effects of 93 body size on survival at both stages, with survival increasing at larger body sizes (Figure 4, 94 Tables S16-19). Interestingly, all quadratic effects of juvenile size on survival between day 15 95 and fledging were positive, with these effects being suggestive and significant for mass and 96 wing length, respectively (Figure 4, Tables S16-19), indicating an accelerating effect of size 97 on offspring survival. In contrast, negative quadratic effects were typical for survival from 98 fledging to recruitment although this effect was only suggestive in the case of tarsus length 99 (Figure 4, Tables S16-19). The fitness functions over both events were generally concave 100 (Figure 4), which would indicate stabilising selection, but the hypothesis that the optimal 101 trait value lay outside of the observed phenotypic range for any trait could not be rejected 102 (proportion of iterations with an internal optimum: tarsus 0.853; head-bill 0.543; mass 0.757; 103 wing 0.017). 104

Using these fitness functions, we were able to estimate selection gradients ( $\beta$ ) for each trait by 105 taking the partial derivative of the individual relative fitness function with respect to the trait 106 and averaging it over the trait's distribution. However,  $\beta$  is more frequently approximated 107 using a Lande-Arnold regression of fitness on a trait<sup>22</sup> and phenotypic skew can bias this 108 approximation when the fitness function is not linear or quadratic (as is the case for survival 109 functions)<sup>22</sup>. To test this, we calculated the expected estimates of  $\beta$  that would be obtained 110 from the Lande-Arnold approach without ( $\beta_1$ ) and with ( $\beta_2$ ) a quadratic term fitted<sup>22;32;33</sup>, 111 over the posterior distribution of the survival models (Equations 10 and 11). Figure 4 shows 112 that generally there is little meaningful difference between estimates, with the exception of 113 wing length, where there is suggestive evidence that  $\beta_1$  would underestimate  $\beta$  by nearly 30% 114  $(\beta_1/\beta: 0.711 \ [0.532, 0.915], pMCMC=0.012).$ 115

### <sup>116</sup> Predicted Response to Selection

In the absence of genetic skew, the correct response to selection is given by Lande's gradient 117 equation  $(V_A\beta)$ , which for these traits gives: tarsus: 0.085mm [0.034, 0.127]; head-bill: 118 0.069mm [0.037, 0.102]; mass: 0.094g [0.052, 0.139]; wing: 0.175mm [0.077, 0.280]. The 119 breeder's equation is equal to the gradient equation when the Lande-Arnold regression without 120 the quadratic term gives good estimates of the selection gradient, irrespective of whether 121 the PO-regression is linear or not (i.e if  $\beta_1 = \beta$  then  $h^2S = V_A\beta$ ;<sup>3</sup> Chapter 29). Given 122 the similarity between  $\beta$  and  $\beta_1$  for tarsus, head-bill and mass, the breeder's equation will 123 therefore give accurate predictions of the selection response for these traits. However, it 124 underestimates the response to selection in wing length by nearly 30%, as the proportional 125 change in the predicted response to selection is equal to  $\beta_1/\beta$  (shown above). 126

#### <sup>127</sup> Selection Bias and Heritability Estimation

The heritability in the breeder's equation is the heritability *before* selection  $(h_b^2)$  which can be interpreted as the slope of the PO-regression averaged over all individuals irrespective of their fitness. However, direct estimates of the PO-regression can only be obtained from individuals

that survive to become parents and so to some extent measure the heritability after selection 131  $(h_a^2)$ ; note the terms heritability before and after selection are used in a broader sense than 132  $in^{14}$ , and capture a different bias; see<sup>3</sup> p171 for a clear explanation of Heywood's usage). 133 Since larger individuals are more likely to survive, and the PO-regression is steeper for these 134 individuals, direct estimates of the PO-regression are likely to be upwardly biased estimates 135 of heritability. To demonstrate this, we obtained direct estimates of the PO-regression from 136 the 182 individuals (118 male and 64 female) that were measured as chicks and survived to 137 produce offspring that were also measured. Although the estimated linear regression (blue line 138 in Figure 5) is similar to the predicted non-linear PO-regression (red line in Figure 5) for the 139 large surviving individuals (the linear and non-linear regressions fit the data equally well for all 140 traits; tarsus p = 0.195, head-bill p = 0.087, mass p = 0.060 and wing p = 0.052), the two 141 diverge substantially at small body sizes (Figure 5). In order to directly compare  $h_a^2$  and  $h_b^2$ , 142 we used the parameters of the quantitative genetic and survival models described above to 143 calculate  $h_a^2$  as the linear PO-regression weighted by the fitness of the parents (Equation 16) 144 and  $h_b^2$  as  $V_A/V_P$ . For tarsus, head-bill and mass,  $h_a^2$  was substantially and significantly higher than  $h_b^2$ , with a proportional increase in  $h_a^2$  of over 60% for head-bill and mass  $(h_a^2/h_b^2)$ : tarsus 145 146 1.223 [1.137, 1.333], pMCMC=0.002; head-bill 1.664 [1.421, 1.951], pMCMC<0.001; mass 147 1.645 [1.325, 2.046], pMCMC<0.001; wing 1.584 [0.373, 2.551], pMCMC=0.372). 148

Estimates of  $h_b^2$  will only be accurate if they do not suffer from the same selection bias 149 present in PO-regression. Our experimental cross-fostering design means that the majority 150 of information used to estimate  $V_A$  in our analysis comes from the comparison of siblings 151 (569 nests have chicks from at least 2 clutches), rather than parents and offspring (182 152 parent-offspring comparisons). Sibling comparisons are made before selection, and so should 153 not suffer from the same selection bias as parent-offspring comparisons. However, many 154 wild bird pedigrees rely largely on information from parent-offspring relationships to estimate 155 genetic effects - without partial cross-fostering and using social pedigrees (no within-nest 156 variation in relatedness), sibling comparisons provide little information on genetic effects 157 because they are confounded with common environment (nest) effects. As both PO-regression 158 and the animal model assume that the relationship between offspring and parental phenotypes 159 is linear, animal models relying mainly on the information from parent-offspring comparisons 160 may also be biased. To test this, we simulated data using the parameters from our quantitative 161 genetic and selection models for mass, assuming social and genetic monogamy, with and 162 without skew and with and without partial cross-fostering. As expected, environmental skew 163 caused  $h^2$  estimated from PO-regressions to be consistently and substantially upwardly biased 164 by a similar amount as we observed in our data, regardless of cross-fostering (estimated/simulated: 165 no cross-fostering 1.609; cross-fostering 1.616). Without cross-fostering (information mainly 166 from parent-offspring comparisons), estimates of  $V_A$ , and so heritability, from animal models 167 were upwardly biased, although less than in the PO-regressions (estimated/simulated:  $V_A$ 168 1.226,  $h^2$  1.228), whereas cross-fostering (information mainly from sibling comparisons) led 169 to the correct estimation of  $V_A$  and  $h^2$  (estimated/simulated: 1.012 and 1.015 respectively; 170 Table 1). 171

# 172 Discussion

A common assumption in quantitative genetics is that phenotypes, and their underlying 173 genetic and environmental components, are normally distributed. Here we demonstrate 174 that this assumption is commonly violated, and in four morphological traits the observed 175 negative phenotypic skew is driven by environmental, rather than genetic, skew. There 176 was strong directional viability selection acting on all four traits, with non-linear fitness 177 functions. Under these conditions the breeder's equation may give inaccurate predictions 178 for the response to selection, but Lande's gradient equation - which only assumes genetic 179 values are normally distributed - is expected to be accurate<sup>11</sup>. However, this assumes that 180 the methods used to obtain estimates of  $\beta$  and  $V_A$  are robust to deviations from normality. 181 Here we empirically demonstrate that common methods used to estimate both metrics can 182 produce biased estimates in the presence of environmental skew. 183

Perhaps the most striking result is the apparent absence of genetic skew. Theory shows that 184 directional selection can generate genetic skew, but the direction of the skew differs between 185 models. Under the infinitesimal (Gaussian descendants<sup>34</sup>) model (assumed in our analyses), 186 directional selection can drive a Gaussian distribution of breeding values to be skewed in 187 the direction of selection through the build up of linkage disequilibrium<sup>11;35;36</sup>. However, 188 stabilising selection may mitigate this (<sup>11</sup> Eq 46) and the breeding value distribution quickly 189 returns to normality if selection ceases (the skew quarters each generation for unlinked loci;<sup>35</sup> 190 p149). Finite allele models also generate genetic skew through changes in allele frequency. 191 Under the rare-alleles model, directional selection after a long period of stabilising selection 192 generates skew in the direction of selection<sup>10;11</sup> but sustained long term directional selection 193 (with new mutations, on average, having effects in the opposite direction) is expected to 194 drive skew in the opposite direction to selection<sup>37;38</sup>. Given juvenile body size appears to be 195 under sustained positive directional selection<sup>30</sup> and gene knockout studies in mice show that 196 loss-of-function mutations reduce size more often than increase it <sup>39</sup>, we would predict negative 197 genetic skew in our system. However, these models predict that the amount of skew generated 198 through selection should be small, consistent with our finding of no or negligible genetic 199 skew. Other processes, such as few loci, alleles of large effect, extreme allele frequencies 200 or substantial non-additive gene action, particularly directional dominance, could generate 201 greater levels of skew<sup>21;37;40;41</sup>. This seems unlikely for body size, which appears to be highly 202 polygenic<sup>42;43</sup>, although the finding that inbred individuals are on average smaller does suggest 203 some directional dominance<sup>44–47</sup> which would also generate skew in the opposite direction to 204 selection. Two other studies have looked at the distribution of breeding values (indirectly 205 through estimating the skew of breeding values estimated in a Gaussian model) and while 206 one also found little evidence of skew<sup>29</sup>, the other found skew in the opposite direction to 207 selection<sup>28</sup>. Lack of genetic skew would also be a consequence of selection acting on an 208 environmentally correlated trait, rather than acting directly on size<sup>48;49</sup> (discussed further 209 below). More widespread assessments of the prevalence of genetic skew are needed to assess 210 the generality of these results. 211

Environmental skew has received little attention from theoreticians, with most studies assuming that environmental effects are normally distributed <sup>11;12;14</sup>. There are, however, several biological processes that are known to induce environmental skew. As far as we are aware, these processes are all predicted to generate negative environmental skew, which fits with our

general observation of negative skew in juvenile body size across species (Figure 2). For 216 example, asymmetric competition, when larger individuals have a disproportionate negative 217 competitive effect on others, can drive negative skew<sup>50-53</sup>. Blue tits have moderate levels of 218 hatching asynchrony (hatching spread is approximately 2 days; see<sup>54</sup> for distribution across 219 bird species) which is expected to generate asymmetries in competitive ability 55 and therefore 220 skew at the within-nest level. However, the dominant source of phenotypic skew is at the 221 between-nest level (contribution to phenotypic skew relates to standardised skew and variance) 222 and so if asymmetric competition was the main driver of phenotypic skew, it would require 223 parental ability to be driven by asymmetric adult competition, perhaps through differences 224 in condition and/or territory quality. An alternative explanation is that (some) chicks have 225 yet to reach their asymptotic size by the time of measurement and so variation in their size 226 at this time is driven by variation in growth rate and asymptotic size. If variation in growth 227 rate is largely at the between-nest level and variation in the asymptote is largely genetic, as 228 has been suggested in great tits<sup>56</sup>, then the non-linearity of growth functions could result in 229 skew that is primarily environmental in origin (see<sup>57</sup> for a related result). This skew would be 230 expected to disappear further into development as all chicks reach their asymptotic size, but 231 due to the strong selective disappearance of small chicks this may not necessarily manifest 232 itself (see below). 233

The strong, negative environmental skew led the PO-regression in all traits to be convex. This 234 occurs because the long tail of small individuals are primarily small because of environmental 235 factors and so resemble their parents less than larger individuals. Most discussions of the 236 linearity of the PO-regression focus on how, in combination with a non-linear fitness function, 237 a non-linear PO-regression leads the breeder's equation to be inaccurate, through generating a 238 covariance between the residuals from a linear fitness function and the linear PO-regression<sup>3;14</sup> 239 (see also Figure S18). This 'spurious response to selection'<sup>14</sup> will be largest when the 240 non-linear fitness function and the PO-regression either have the same non-linear shape (e.g. 241 both concave) causing a positive covariance between residuals, leading the breeder's equation 242 to under-estimate the response to selection or opposite shapes (e.g. one concave and one 243 convex), creating negative covariance between residuals and so over-estimation of selection 244 response. Skew generates quite predictable and simple non-linearity in the PO-regression 245 (Figure 1), and so generally accelerating or decelerating fitness functions will be more likely 246 to generate a spurious response to selection, as is seen with wing length (Figure S18). 247

We additionally show that the selective disappearance of small individuals alongside a non-linear 248 PO-regression leads to  $h^2$  estimates that are biased towards the slope of the surviving large 249 individuals. This selection bias is particularly striking in estimates from PO-regression (approx 250 65% increase in  $h^2$  for mass and head-bill length; Figure 5) but importantly also occurs 251 in animal models applied to pedigrees where information about the genetic variance comes 252 primarily from parent-offspring comparisons (e.g. typical bird pedigrees without cross-fostering), 253 although to a lesser degree (23% increase in animal models compared to a 61% increase in 254 PO-regression; Table 1). This bias occurs because both PO-regression and the animal model 255 assume that the relationship between offspring and parental phenotypes is linear, and so 256 assumes the missing parent-offspring comparisons would follow the same slope. It is worth 257 noting that we simulated closed populations and so a higher relatedness structure than in 258 most wild bird populations, which are characterised by low recruitment and high immigration. 259 Thus, our simulations likely underestimated the possible bias in animal models. We also 260

demonstrated that cross fostering eliminated this bias in animal models. This occurs because cross-fostering shifts the majority of the information for estimating  $V_A$  from parent-offspring comparisons, to sibling comparisons, and sibling comparisons are made before selection whilst parent-offspring comparisons are made after.

Previous work in this system has shown that selection differentially eliminates negative environmental, 265 but not genetic, deviations for mass over the course of development<sup>58</sup>. This was interpreted 266 as mass being an environmentally correlated target of selection rather than the true target 267 (i.e. no causal relationship between size and survival)<sup>48</sup>. However, incorporating skew into 268 our models challenges this interpretation as, under our model, size is the true target of 269 selection. As the long tail of small individuals are small for environmental reasons, the selective 270 disappearance of these individuals drives the observed decrease in environmental variance and 271 skew though ontogeny. Given the selective disappearance previously observed was prior to the 272 measurements analysed here<sup>58</sup> it seems likely that the environmental skew we observe is an 273 underestimation of the true skew, meaning we are likely underestimating the true non-linearity 274 of the PO-regression. Multivariate methods would account for this selective disappearance<sup>59</sup>, 275 however, these proved too complex to implement in this instance. 276

Given the consistent negative environmental skew we see across the four traits, and the 277 conserved nature of negative phenotypic skew in juvenile (but not adult) size across bird 278 species, we believe a concave PO-regression for juvenile size traits might be a general finding. 279 As found here, juvenile body size is also generally under strong viability selection across 280  $taxa^{30}$ . Together, this suggests that previous heritability estimates of juvenile size are likely 281 to have been systematically over-estimated, especially as a large proportion are based on 282 PO-regressions<sup>60</sup>. Indeed, tarsus length heritability estimates from PO-regressions have been 283 shown to be consistently larger than those from animal models<sup>60</sup>. Juvenile size is a hallmark 284 trait of evolutionary stasis, whereby traits that should respond to selection in the wild appear 285 not to. Although these results do not fully explain this stasis, they do show that the predicted 286 response to selection may be being substantially overestimated in traits with non-Gaussian 287 phenotypic distributions. 288

Lande-Arnold regression is by far the most common method for estimating  $\beta^{5;32;61}$  and is 289 known to be unbiased in the presence of phenotypic skew only if the fitness function is linear 290 or quadratic and this quadratic term is modelled<sup>22</sup>. Although the estimated survival functions 291 deviated from a quadratic for all traits, estimates of  $\beta$  were close to those that would have 292 been obtained under Lande-Arnold regression including the quadratic term ( $\beta_2$ ) for all traits, 293 and without the quadratic term ( $\beta_1$ ) for three traits. The near equivalence of these different 294 estimates seems at odds with the conclusions of Bonamour et al.<sup>17</sup>, who demonstrate that 295 selection gradients approximated with Lande-Arnold regression are biased in the presence of 296 phenotypic skew. However, Bonamour et al. only modelled the linear term in the Lande-Arnold 297 regression ( $\beta_1$ ) whilst assuming a quadratic fitness function - had the quadratic term also been 298 included, the linear term in the Lande-Arnold regression ( $\beta_2$ ) would have been unbiased (<sup>22</sup>,<sup>3</sup> 299 Chapter 29), in correspondence with our wing length results ( $\beta_1$  underestimated  $\beta$ , but  $\beta_2$ 300 did not). However, there is no reason to believe including a quadratic term in a Lande-Arnold 301 regression will generally result in a good approximation of  $\beta$ . Indeed, Morrissey & Sakrejda<sup>5</sup> 302 compared  $\beta$  with that approximated from a quadratic Lande-Arnold regression and found quite 303 large proportional differences (approx. 30%), although small differences in absolute terms. 304

We therefore urge caution in assuming that our results are a general statement about the accuracy of Lande-Arnold regression under non-normality.

Quantitative genetics uses two main frameworks to predict how traits will respond to selection. 307 Here we demonstrate how both of these frameworks are affected by skew at the environmental 308 and genetic levels. Genetic skew can lead both the breeder's equation and Lande's gradient 309 equation to be inaccurate. Although little or no genetic skew has been found in the few 310 studies that have tried to quantify it, it remains unknown to what extent this is a generality, 311 and will be highly dependent on the genetic architecture of specific traits. In the absence of 312 genetic skew, the gradient equation presents an accurate prediction of selection response<sup>11</sup>, 313 although environmental skew provides challenges to the accurate estimation of both  $\beta$  and  $V_A$ . 314 Whilst the breeder's equation may provide a more intuitive way of thinking about selection 315 response, the extensions to this framework that allow for non-linearity<sup>12</sup> are complex and 316 computationally expensive. We therefore recommend a focus on the gradient equation (and 317 its extensions<sup>11</sup>) in wild systems, where fitness functions are highly likely to be non-linear and 318 trait distributions are commonly skewed. 319

# 320 Methods

This study was preregistered (see https://osf.io/7qyp4/). We have highlighted in the following sections where our methods deviate from those planned.

#### 323 Meta-analysis of Skew

We collected raw data on juvenile and adult tarsus length from several sources: we used a mailing list to request data, we searched the dryad repository for 'tarsus', we emailed groups with known long-term avian datasets that were not represented in these sources and included any tarsus length data that we otherwise encountered. When datasets from different studies of the same population overlapped in time, we use the largest single dataset available. Datasets were taken from <sup>43;62–99</sup>.

Sample standardised skew was estimated from raw data z as

$$\frac{\frac{1}{n}\sum_{i=1}^{n}(z_{i}-\hat{\mu})^{3}}{\left[\frac{1}{n}\sum_{i=1}^{n}(z_{i}-\hat{\mu})^{2}\right]^{3/2}}\frac{\sqrt{n(n-1)}}{n-2}$$

with sampling variance as

$$\frac{6n(n-1)}{(n-2)(n+1)(n+3)}$$

where n is sample size and  $\hat{\mu}$  the estimate of the trait mean<sup>100</sup>.

Using these data, we ran a random-effect meta-analytic model in MCMCglmm with age (juvenile or adult) as a fixed factor and random effects of species and study. Models were run for 65000 iterations, with a burnin of 15000 and a thinning intervals of 50. The priors for the random-effect variances were scaled (by 100)  $F_{1,1}$  and the prior for the residual variance was inverse-gamma with a shape and scale of 0.001. The fixed effects had a diffuse normal prior (mean=0, variance= $10^{10}$ ).

## 337 Study population

We used data from a nest-box population of blue tits (*Cyanistes caeruleus*), on the Dalmeny 338 estate, Edinburgh, United Kingdom, collected from 2011 to 2018, with 253 nest-boxes over 339 two sites. Detailed methods are described in <sup>58;101</sup>. Briefly, all nests were visited regularly until 340 the discovery of the first egg, and then daily for egg cross-fostering, when eggs were weighed. 341 From 2011-2013 and 2016-2018 a partial egg cross-fostering design was used to enable additive 342 genetic and nest-of-rearing effects on offspring size to be separated <sup>58</sup>. In 2014-2015 a mixture 343 of full and partial cross-fostering was used as part of a separate experiment. Full details of 344 cross-fostering can be found in <sup>102</sup>. After egg laying was complete, nests were left undisturbed 345 for 11 days and then checked daily for hatching. At hatching (day 0), all chicks were uniquely 346 marked (within a nest). The chicks had blood samples taken at day 3 and were given a unique 347 metal ring at day 9. At day 15, chick's tarsus, wing and head-bill lengths were measured and 348 they were weighed. For the morphometric measurements, one chick from each nest was 349 measured twice in order to account for measurement error<sup>58</sup>. From day 10, adults were 350

caught at the nest in order to identify them; blood samples and morphometric measurements were taken and the birds were uniquely ringed. At the end of the season we checked all nests and recorded any dead chicks left in the nest. From this we could infer which chicks fledged. Chicks were considered recruited if they were recaptured as breeders in subsequent years. Permission to monitor, catch and ring the birds was given by Scottish Natural Heritage and the British Trust for Ornithology and permission to take blood samples was granted by the UK Government's Home Office. All permission and licenses were granted to JDH.

Social parentage was assigned through catching parents at the nest. When no female was caught, the social female was assigned a dummy mother identity. When no male was caught, the social father was assigned as the genetic sire with the largest proportion of paternity in a nest, either a male caught at a different nest that year, or an unsampled male assigned a dummy identity.

For the assignment of genetic parentage and chick sex, genotypes were obtained using blood 363 and tissue samples from adults and chicks. Genotyping and pedigree reconstruction largely 364 followed protocols outlined in 58 and 101. However, adults not caught in the focal year but 365 that were known to be alive (because they were caught in subsequent years and were aged 2 366 years or over) were allowed to be parents of chicks in the focal year. The distance between 367 the nest-of-origin of the chicks and the nest at which these candidate parents were caught in 368 the subsequent year was fitted as a covariate. Mothers were allowed to be polygamous when 369 (half) sib-ships were assigned to chicks with unknown fathers (see Supplementary Methods). 370 When assigning chick sex, we used morphological sexing of recruits over molecular sexing from 371 chicks (sexing didn't match for 5 chicks). 372

For our analysis we included data on chick size measured at day 15 post-hatching, collected on 373 this project from 2011-2018, and additionally chick recruitment data from 2019 and 2020. We 374 included all nests for which hatching date was known. Although similar morphological data 375 was collected in 2010, we excluded all records from this year as egg size was not measured. 376 Egg size was used to account for nest-of-origin effects in our models (see below). We also 377 excluded data from an additional two nests where egg size was not measured, from chicks for 378 which molecular sexing was not successful (n=20 chicks) and where we did not have one of 379 the day 15 measurements (n=11 chicks). In total, we had records of 5123 day 15 chicks in 380 715 nests, with 642 chicks repeatedly measured. 381

## 382 Statistical analysis

All models were run in a Bayesian framework. From all models posterior means and 95% credible intervals are presented. A p-value for the fixed effects and covariances in these models was approximated (pMCMC) as two times the smaller number of iterations where the parameter value is either less than zero or greater than zero<sup>103</sup>. We use a threshold of 0.005 to refer to results as significant and those between 0.05 and 0.005 as suggestive<sup>104</sup>.

#### **Decomposing phenotypic skew using hierarchical models**

We modelled the four traits (tarsus length, head-bill length, mass and wing length) measured at day 15 using linear mixed effects models with sex (2 level factor), year (8 level factor), time of day (continuous - hours from midnight) and egg size (continuous) as fixed. Additive genetic

and nest-of-rearing effects were modelled as random. Because we have repeated measurements 392 of tarsus, wing and head-bill lengths, we additionally modelled measurement error effects in 393 these traits, by including bird identity effects, which are equivalent to the residuals in a model 394 without repeat measures, and the residuals are measurement error effects<sup>58</sup>. In contrast to 395 past analyses<sup>58;101</sup>, we do not model nest-of-origin effects but rather include egg size as a 396 covariate to account for these effects (see<sup>58</sup> and Supplementary materials). As estimating 397 skew-t distributed random effects (see below) is parameter heavy, including a covariate rather 398 than a random effect is preferable, especially as nest-of-origin effects are very small for these 399 traits<sup>58;101</sup>. 400

Skew due to the fixed effects was obtained by multiplying the fixed effect design matrix by the 401 fixed effects and estimating the parameters for the skew-t distribution of the resulting variable. 402 These were used when calculating the non-linear parent offspring regression and when plotting 403 the sample skew. This method assumes that the joint distribution of the covariates is equal to 404 the empirical distribution we observe. In combination with a diffuse prior on the fixed effects, 405 this assumption probably leads to a small inflation in the estimated (absolute) skew. Time 406 of day was excluded from this estimate as any skew induced by this is due to our sampling 407 design rather than being biologically relevant. 408

In order to estimate skew in in the random effects, we fitted random effects with skew-t 409 distributions. The residuals for the repeat measured traits were treated as Gaussian as these 410 represent measurement errors. As with the normal distribution, the skew-t distribution<sup>105-108</sup> 411 has a location  $\xi$  and scale  $\omega$  parameter, but also parameters  $\delta$  and  $\nu$  which modify the skew and 412 tailness, respectively. The distribution converges on a normal distribution when  $\delta = 0$  and  $\nu$ 413 approaches infinity. As  $\delta$  moves away from 0 and  $\nu$  decreases the (absolute) skew in a variable 414 increases, with the sign of  $\delta$  signifying the direction of the skew. The skew-t distribution is 415 unbounded and readily allows for considerable amounts of positive and negative skew. The 416 reasons for the use of this distribution are further discussed in the supplementary materials. 417 Our approach to modelling the additive genetic effects is to extend standard quantitative 418 genetic models by allowing the base population breeding values to have a skew-t distribution, 419 with normally distributed Mendelian sampling deviations in the descendants (with variance 420  $\omega^2(1-\overline{F})/2$  where  $\overline{F}$  is the average inbreeding coefficient of the individual's parents). This 421 assumes that inheritance occurs under the Gaussian descendants infinitesimal model 34;109; i.e. 422 the Mendelian sampling deviations are normally distributed within families, and any genetic 423 skew results from selection. In practice, however, the Mendelian sampling deviations are largely 424 confounded with residual effects in our data because there are few parent-offspring comparisons 425 (due to high migration and low recruitment) and so inferences are probably quite robust to 426 any violation of the Gaussian descendants assumption. Initially we tried to fit this model in an 427 animal model framework, but due to poor mixing we chose to approximate the model using 428 a dam-sire model. This model discards information about the Mendelian-sampling deviations 429 and subsumes them in the residual effects which then come from a mixture distribution<sup>110</sup>. 430 Given there is little information in our data about the Mendelian-sampling deviations the 431 dam-sire and animal models are expected to give almost identical answers (see Supplementary 432 Materials). Although this method allows us to directly estimate skew in breeding values, when 433 the environmental residuals are skew-t, as assumed here, the mixture distribution does not 434 have standard from. Here, we approximate the mixture distribution as skew-t and although 435 we cannot derive the full distribution of the environmental residuals we are able to obtain their 436

variance and skew. These models provided little evidence for genetic skew in any trait and so
we reverted to an animal model with normally distributed breeding values - the animal model
approach having the advantage that the environmental residual skew can then be directly
estimated. The dam and sire effects were modelled in a multi-membership model where the
two sets of effects were constrained to having the same skew-t distribution.

Initially, we intended to model chick mass over ontogeny in a multivariate framework (see 442 preregistration), as in previous studies of this population<sup>58;101</sup>. However, implementing the 443 required multivariate skew-t models proved too challenging. Since there is strong directional 444 selection on chick body mass throughout ontogeny<sup>58;101</sup>, our estimates of skew at day 15 445 are likely underestimates as the univariate analysis used will fail to account for selective 446 disappearance prior to day 15<sup>58;101</sup>. We also planned to have a global box-cox parameter 447 in case there was a single transformation that would make everything linear and additive. 448 However, given the problems we had with implementing more complex models, we chose not 449 to include this additional complexity. 450

It should also be noted that estimates from these skew-t models seem to be more sensitive 451 to unmodelled heteroskedasticity than standard Gaussian mixed effects models, even when 452 skew exists, and this can lead to biased fixed effect and variance estimates. This led us 453 to fit a reduced set of fixed effects compared with previous analyses<sup>58;101</sup> and outlined in 454 our pre-registration (see Supplementary materials). To partly address this issue we also ran 455 equivalent Gaussian models for all skew-t models, and present the results in the Supplementary 456 materials. There were small differences the between models but the results remain qualitatively 457 the same (see SM; Figure S17, Tables S4-15). 458

These models were run using Stan (version 2.21.0)<sup>111</sup> using the cmdstanr package (Stan 459 Development Team, 2019) in R (version 4). Four chains were run for each model with 460 a warmup of 4000 iterations and 6000 iterations post-warmup, with the exception of the 461 dam-sire wing length model which was run with a warmup of 5000 iterations and 10000 462 iterations post-warmup. Convergence of individual chains was visually assessed, as well as 463 ensuring that the Gelman-Rubin diagnostic (R-hat) across chains was less than  $1.1^{112}$ . We 464 used diffuse normal priors for fixed effects (mean=0 and standard deviation=100), half-Cauchy 465 priors (mean=0 and standard deviation=10) for standard deviations and uniform priors from 466 -1 to 1 for  $\delta$  and 4 to 40 on  $\nu$ . The choice of priors is discussed further in the Supplementary 467 materials. 468

#### <sup>469</sup> Non-Linear Parent-Offspring Regression

The PO-regression function is defined as  $E[z_o|z]$  where  $z_o$  is the phenotype of offspring from a parent with phenotype z. Assuming random mating and environmental values in the offspring  $(e_o)$  are independent of parental phenotypes this becomes  $\frac{1}{2}E[g|z] + \frac{1}{2}E[g] + E[e_o]$  under the Gaussian descendants assumption, where g is breeding value. Have  $\theta_g$  be the parameters of the breeding value distribution and  $\theta_e$  the parameters of the environmental distribution. Then,

$$E[g|z] = \frac{\int (z-e)p(z-e|\theta_g)p(e|\theta_e)de}{\int p(z-e|\theta_g)p(e|\theta_e)de}$$
(1)

The integrals have to be evaluated numerically, which is time consuming, and so the regression function was evaluated at the posterior mean of the parameters from the skew-t animal models to give  $E[z_o|z]$  for each trait (Figure 5). Also, note that in the presence of pre-breeding survival selection, the term  $\frac{1}{2}E[g]$  in the intercept of the regression function should be replaced by  $\frac{1}{2}(E[g] + \Delta g)$  where  $\Delta g$  is the change in mean breeding value due to selection such that  $E[g] + \Delta g$  is the expected breeding value of the other parent<sup>14</sup>.

#### 482 Selection on chick body mass

Given that we were not able to model chick body mass in a multivariate framework, we did 483 not model survival throughout ontogeny as originally planned (see preregistration), but rather 484 modelled survival from day 15 to fledging and fledging to recruitment. We modelled this as 485 an event history in a probit regression (binomial error distribution and probit link function) 486 including a quadratic effect of chick size at day 15 on both events, allowing us to model the 487 stabilising component of selection. These models accounted for measurement error in tarsus, 488 head-bill and wing lengths, using the repeated measurements of these traits. Originally we 489 planned to correct our measurements for time of day effects (see preregistration). However, 490 these effects proved to be very small and for most traits non-significant (see Supplementary 491 Results). We therefore decided not to add this extra complexity into our models. 492

Sex, day of hatching within the nest, year, clutch size, male presence, nest hatch date were 493 also included as fixed effects. All fixed effects were allowed to differ between the two events. 494 Finally we modelled the 2x2 covariance matrix of nest-of-rearing effects. This model was 495 run using Stan. Four chains were run for each model with 5000 iterations and a warmup of 496 2500 iterations with a thinning interval of 10. Convergence of chains was assessed as above. 497 Diffuse priors for fixed effects (mean=0 and standard deviation=100), half-Cauchy priors for 498 all standard deviations (mean=0 and standard deviation=10) and LKJ priors on correlations 499 with shape= $2^{113}$  were used. 500

#### 501 The Individual Relative Fitness Function

Partitioning the linear predictors for each survival event (1: day 15 to fledging, 2: fledging to recruitment) into a part due to the trait and a part due to remaining terms (denoted  $\eta$ ), and assuming that the distribution of  $\eta^{(1)}$  and  $\eta^{(2)}$  are bivariate normal conditional on the trait z, then the absolute fitness function has the form:

$$W(z) = F_{MVN}\left(\mathbf{s}|\boldsymbol{\Sigma}\right) \tag{2}$$

where  $F_{MVN}$  is the multivariate normal cumulative density function in which the first argument is the quantile to be evaluated and the second argument is the (co)variance of the variates (the means are zero and are therefore not given). For event *i* 

$$s^{(i)} = E[\eta^{(i)}] + \frac{COV(\eta^{(i)}, z)}{\mu_2}(z - \mu) + \beta^{(i)}z + \frac{1}{2}\gamma^{(i)}z^2$$
(3)

where  $\beta^{(i)}$  and  $\frac{1}{2}\gamma^{(i)}$  are the linear and quadratic effect of the trait on event *i*,  $\mu$  is the trait mean and  $\mu_i$  the *i*<sup>th</sup> central moment of the phenotypic distribution.

$$\Sigma^{(i,j)} = COV(\eta^{(i)}, \eta^{(j)}) - \frac{COV(\eta^{(i)}, z)COV(\eta^{(j)}, z)}{\mu_2} + COV(u^{(i)}, u^{(j)}) + \delta^{(i,j)}$$
(4)

where  $u^{(i)}$  are the nest effects for event i and  $\delta^{(i,j)} = 1$  when i = j and represents the residual variance.

The partial derivative of W(z) with respect to z is given by

$$\frac{\partial W(z)}{\partial z} = f_N\left(s^{(1|2)}|\mathbf{\Sigma}^{(1|2)}\right) \left(\frac{COV(\eta^{(1)},z)^2}{\mu_2} + \beta^{(1)} + \gamma^{(1)}z - \frac{\mathbf{\Sigma}^{(1,2)}}{\mathbf{\Sigma}^{(2)}} \left(\frac{COV(\eta^{(2)},z)^2}{\mu_2} + \beta^{(2)} + \gamma^{(2)}z\right)\right) \\ F_N\left(s^{(2)}|\mathbf{\Sigma}^{(2)}\right) + f_N\left(s^{(2)}|\mathbf{\Sigma}^{(2)}\right) \left(\frac{COV(\eta^{(2)},z)^2}{\mu_2} + \beta^{(2)} + \gamma^{(2)}z\right) F_N\left(s^{(1|2)}|\mathbf{\Sigma}^{(1|2)}\right)$$
(5)

where  $f_N$  and  $F_N$  are the density and cumulative density functions for a centred normal distribution, and

$$s^{(1|2)} = s^{(1)} - \frac{\Sigma^{(1,2)}}{\Sigma^{(2)}} s^{(2)} \qquad \Sigma^{(1|2)} = \Sigma^{(1)} - \frac{(\Sigma^{(1,2)})^2}{\Sigma^{(2)}} \tag{6}$$

Solving Equation 5 to find the stationary point(s), and therefore the optimal trait value, is difficult. Instead we evaluated the derivative of Equation 5 at the minimum and maximum observed trait value and assessed whether the derivative at the minimum is positive and negative at the maximum. This condition implies an optimal trait value within the range of observed trait values.

#### 521 Selection Gradients

The Lande-Arnold method<sup>22</sup> for estimating the selection gradient is only robust to phenotypic skew if the fitness function is quadratic and both the mean-centered trait value and its square are fitted in the regression<sup>3;22</sup>. We therefore computed three selection gradients. Using the notation in<sup>33</sup>, we calculated our best estimate of it<sup>114</sup>,

$$\beta = E\left[\frac{\partial w(z)}{\partial z}\right] = \int \frac{\partial w(z)}{\partial z} p(z) dz \approx \frac{1}{n} \sum_{i=1}^{n} \left. \frac{\partial w(z)}{\partial z} \right|_{z_{i}}$$
(7)

where p(z) is the probability density function for z, w(z) is the relative fitness function obtained by dividing W(z) by mean fitness ( $E[W] = \int W(z)p(z)dz$ ) and  $z_i$  are the observed trait values. Put simply, we calculated the mean partial derivative of individual fitness function (from Equation 5) across our observed phenotypic distributions, divided by mean fitness.

530 The linear selection differential is defined as

$$S = \int zw(z)p(z)dz - \mu \approx \frac{1}{n} \sum_{i=1}^{n} z_i w(z_i) - \hat{\mu}$$
(8)

<sup>531</sup> and the quadratic selection differential as

$$C = \int (z-\mu)^2 p(z)w(z)dz - \mu_2 \approx \frac{1}{n} \sum_{i=1}^n (z_i - \hat{\mu})^2 w(z_i) - \hat{\mu}_2$$
(9)

From these we can calculate the expected linear regression coefficient from the Lande-Arnold method when only the linear term was fitted:

$$\hat{\beta}_1 = \frac{\hat{S}}{\hat{\mu}_2} \tag{10}$$

<sup>534</sup> and the linear regression coefficient from the Lande-Arnold method when both the linear and <sup>535</sup> quadratic term are fitted (Eq. 29.28a from<sup>3</sup>):

$$\hat{\beta}_2 = \frac{(\hat{\mu}_4 - \hat{\mu}_2^2)\hat{S} - \hat{\mu}_3\hat{C}}{\hat{\mu}_2(\hat{\mu}_4 - \hat{\mu}_2^2) - \hat{\mu}_3^2}$$
(11)

Selection cannot operate on between-sex differences in trait values (the average fitness of the two sexes is constrained to be equal) and we assume that selection does not operate on between-year differences in trait values (which might occur if juvenile size impacts on adult survival). We therefore estimated each  $\beta$  as the average of each sex by year combination (Figure 4 e-h), calculated across the posterior distribution of the survival model.

#### 541 Response to Selection

The extension of Lande's gradient equation to a non-normal distribution of genetic effects is (combining Equations 26 and 42 from<sup>11</sup>):

$$\Delta \mu = \sum_{j=1}^{\infty} K^{j+1}(g) \frac{1}{j!} \int \frac{\partial^j w(z)}{\partial z^j} p(z) dz$$
(12)

where  $K^{j}(x)$  denotes the  $j^{\text{th}}$  cumulant of x, which up to the third cumulant (skew) is

$$\Delta \mu = V_A E \left[ \frac{\partial w(z)}{\partial z} \right] + \frac{S_A}{2} E \left[ \frac{\partial^2 w(z)}{\partial z^2} \right]$$
(13)

where  $S_A$  is the skew in the additive genetic effects. When the distribution of additive genetic values is normal and/or the fitness function is linear, Equation 12 reduces to Lande's gradient equation

$$\Delta \mu = V_A E \left[ \frac{\partial w(z)}{\partial z} \right] = V_A \beta \tag{14}$$

 $_{\rm 548}$   $\,$  since all cumulants >2 of the genetic distribution are zero.

#### 549 Heritability

We compared how well our inferred non-linear PO-regression (Equation 1) performed at predicting offspring phenotype compared to linear single-parent mid-offspring regression. Using the 182 individuals (118 male and 64 female) that were measured as chicks at day 15 and survived to produce offspring that were also measured at day 15, we fitted a weighted (by family size) regression with our inferred non-linear PO-regression fitted as an offset. We then compared the fit of this model to an identical model but where the raw parental phenotype was also fitted as a covariate with a free parameter.

<sup>557</sup> We then compared estimates of the heritability before and after selection ( $h_b^2$  and  $h_a^2$ , respectively).

The heritability can be defined as the regression coefficient of a linear mid-PO-regression, and can be calculated before selection

$$h_b^2 = 2 \frac{COV(z_o, z)}{\mu_2} = \frac{V_A}{V_P}$$
 (15)

560 or after selection

$$h_a^2 = 2 \frac{E[w(z)z_o z] - E[w(z)z_o] E[w(z)z]}{E[w(z)z^2] - E[w(z)z]^2}$$
(16)

The posterior distribution of  $h_b^2$  was evaluated directly, but the  $i^{th}$  posterior sample of  $h_a^2$ was obtained by simulating  $10^4$  values of z and  $z_o$  using the parameters sampled at the  $i^{th}$  iteration of the trait model, calculating expected fitness for each sampled z using the parameters sampled at the  $i^{th}$  iteration of the fitness model, and then evaluating the relevant expectations.

#### 566 Simulations

To test how different sampling designs and standard estimation procedures (PO-regression 567 and Gaussian animal model) impact estimates of heritability in the presence of skew and 568 selection, we simulated data according to the posterior mean of the parameters from our 569 skew-t quantitative genetic and selection models for mass. A closed population with 1000 570 breeding pairs was simulated over three generations, with 10 measured full-sib offspring per 571 pair. Four scenarios were simulated: either nests were not cross-fostered or they were paired 572 and five offspring reciprocally crossed, and the random effects were either skew t-distributed 573 (with  $\omega$ ,  $\delta$  and  $\nu$  parameters set to their posterior means) or they were normally distributed but 574 with matching variance. The probability of a chick recruiting to be a parent was obtained by 575 applying the estimated survival model for chick mass to the simulated phenotype. Each of the 576 four scenarios were simulated 2000 times and for each data set the heritability was estimated 577 directly using PO-regression and as the estimate of the additive genetic variance over the sum 578 of all variances estimated from a Gaussian animal model fitted in ASRemI-R<sup>115</sup>. 579

## **Data availability**

All data and code can be found at https://doi.org/10.5281/zenodo.5794316.

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## **Author contributions**

JLP and JDH conceived and designed the project. JLP, HEL, CET and JDH generated the data. JLP and JDH analysed the data and wrote the paper. All authors have read and approved the paper.

## **593** Competing interests

<sup>594</sup> The authors declare no competing interests

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## **Figures and Tables**



Figure 1: The effects of different distributions of breeding values (G) and environmental values (E) on the distribution of phenotypes (P) and the shape of the PO-regression. When both genetic and environmental values are normally distributed (a), as typically assumed, there is a linear PO-regression. Negative genetic (b) and environmental (c) skew affect the shape of the parent-offspring relationship in opposite directions, whilst inducing the same phenotypic skew. If genetic and environmental distributions are skewed in the same direction (d) their effects on the parent-offspring relationship can cancel each other out, giving a linear parent-offspring relationship, despite considerable phenotypic skew. If genetic and environmental are skewed in opposite directions (e), although they may can cancel each other out at the phenotypic level, they induce a highly non-linear parent-offspring relationship. 1-5) are all simulated with a heritability ( $V_A/V_P$ ) of 0.5.



Figure 2: Skew in the distribution of avian tarsus lengths across different species, measured as the coefficient of skew. In the boxplots, the center line shows the median; box limits show upper and lower quartiles; whiskers show 1.5x interquartile range; points show outliers. Numbers above the plots show the number of estimates, and species in parenthesis. The red points show the skew in our blue tit data.



Figure 3: Decomposition of variance and skew in juvenile body size traits in blue tits. Top plots shows the phenotypic distribution of the traits, with the red line showing the distribution predicted from the skew models. The middle rows show the variance and skew (top and bottom, respectively) for each component for all four traits, with all model estimates coming from the skew-t animal model, except the genetic skew which was estimated in the skew-t dam-sire model (see methods). ME stands for measurement error. The bottom row shows the predicted shape of the PO-regression based on the model estimates.



Figure 4: Average (over years and sexes) fitness functions (a-d) and selection gradients (e-h) for tarsus length, head-bill length, mass and wing length, respectively, from day 15 to recruitment. In plots a-d, solid lines show the posterior mean fitness functions, dotted lines show the 95% credible intervals, and points show the average survival of measured individuals from day 15 to recruitment in equally spaced intervals. The size of the points is proportional to the square root of the sample size. The phenotypic distribution of the traits is shown, with the grey vertical line showing the phenotypic mean. The direction and significance of the effect of the trait on fitness is also shown, 'F' and 'R' are survival from day 15 to fledging and from fledgling to recruitment respectively, and 'L' and 'Q' and linear and quadratic effects. In plots e-h,  $\beta$  refers to the selection gradient derived from this fitness function,  $\beta_1$  and  $\beta_2$  refer to the approximations from the Lande-Arnold regression excluding and including a quadratic term, respectively. In all plots 'NS' indicates p > 0.05, '\*' indicates 0.05 > p > 0.005 and '\*\*' p < 0.005.



Figure 5: PO-regressions for four body size traits. Top panels show distribution of all chicks (red) and those that survived to recruit (blue), representing the distribution of potential parents before and after selection, respectively. Scatter plots show mid-offspring versus single parental traits. Values are corrected for year, sex and time of day at which they were measured, and the size of the points is proportional to the square root of the family size. The red line is the predicted non-linear PO-regression based on the posterior means of the parameters from the skew-t quantitative genetic model and the blue line is the fit of a weighted (by family size) linear regression to the actual data. These are not corrected for measurement error. Lower panels show the comparison between heritabilities calculated before  $(h_b^2)$  and after  $(h_a^2)$  selection, calculated across the posterior distribution of the skew-t animal model trait models. In these lower plots all heritabilities account for measurement error. In all plots 'NS' indicates p > 0.05, '\*' indicates 0.05 > p > 0.005 and '\*\*' p < 0.005.

Table 1: Estimates (mean $\pm$  SE) of heritability and additive genetic variance from PO-regression and Gaussian animal models (AM) across 2000 simulated data sets. Three-generation simulations were set up with either no cross-fostering (N) or with nests paired and half of each nest's offspring reciprocally crossed (X). Phenotypes were simulated according to the model estimated for chick mass exactly (skewed) or as Gaussian with matching variance. The probability of a chick recruiting to be a parent was obtained by applying the estimated survival model for chick mass.

	Simulated	Gaussian		Skewed	
		Ν	Х	Ν	Х
$h^2 \ PO$	0.138	$0.139{\pm}0.001$	$0.140{\pm}0.001$	0.223±0.001	0.224±0.001
$h^2 \; AM$	0.138	$0.137{\pm}0.001$	$0.135{\pm}0.000$	$0.170 {\pm} 0.001$	$0.141{\pm}0.000$
$V_A AM$	0.148	$0.146{\pm}0.001$	$0.144{\pm}0.000$	$0.181{\pm}0.001$	$0.150{\pm}0.000$