# Processes and predictions in ecological models: logic and causality

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# 6 Abstract

7 To make credible ecological predictions for terrestrial ecosystems in a changing environment and

8 increase our understanding of ecological processes, we need plant ecological models that can be

9 fitted to spatial and temporal ecological data. Such models need to be based on sufficient

10 understanding of ecological processes to make credible predictions and account for the different

11 sources of uncertainty. Here, I argue (1) for the use of structural equation models in a hierarchical

12 framework with latent variables and (2) to specify whether our current knowledge of relationships

13 among state variables may be categorized primarily as logical (empirical) or causal. Such models will

14 help us to make continuous progress in our understanding of and ability to predict the dynamics of

15 terrestrial ecosystems and provide us with local predictions with a known degree of uncertainty that

16 are useful for generating adaptive management plans. The hierarchical structural equation models I

17 recommend are analogous to current general epistemological models of how knowledge is obtained.

18

19 *Keywords*: structural equation model; hierarchical model; ecological prediction;

### 21 Introduction

22 The climate and environment are changing, and the effects of these changes on ecosystems and 23 biodiversity are well documented (IPBES 2019). It is becoming increasingly important to develop 24 credible ecological predictions, but the limits of such a predictive approach are an open question. To 25 what extent is it possible to predict the future of ecosystems in a changing environment? What 26 ecological processes are most likely to dominate future ecosystem changes? How fast will ecosystem changes occur? Here, I focus on the vegetation component of the ecosystem as a dynamic system 27 28 that is influenced by climate, interactions among organisms and disturbances as an example of 29 attempts to develop predictive ecological models in general.

30 The conceptual framework and study methods of plant ecology, and therefore of plant ecological 31 models, are embedded in concepts of time and space. One of the few generalizations that we can 32 make about vegetation is that it is spatially heterogeneous, and the spatial patterns of the 33 vegetation depend mainly on the environment and historical legacies (Greig-Smith 1979; Ricklefs 34 2004; Svenning and Skov 2004; von Humboldt and Bonpland 1805). Even in a homogenous 35 environment, plant species are aggregated at large and small spatial scales. At a larger scale, plant 36 species are aggregated among sites due to random extinction events and limited possibilities for 37 colonization (Cordonnier et al. 2006; Leibold et al. 2004; MacArthur and Wilson 1967; Rees et al. 38 2001). Within sites, plants may be aggregated due to clonal growth, limited seed dispersal and size-39 asymmetric competition (Herben et al. 2000; Pacala and Levin 1997; Stoll and Weiner 2000). 40 Dominant plant species may affect the soil and lead to important feedback mechanisms, so the vegetation and soil may be described as a dynamic system in time and space, where different phases 41 42 of the vegetation simultaneously may co-occur in different patches (Watt 1947) or the ecosystem 43 can develop in a successional pattern.

Moreover, it is a truism that ecological processes occur in time, and they can only be understood 44 45 when temporal dynamics are taken into account (Damgaard 2019a; Damgaard and Weiner 2017; 46 Kratz et al. 2003; Pickett 1989). Generally, environments are non-stationary, and spatial and 47 temporal variability in ecological systems are of fundamental importance to ecosystem dynamics 48 (Chesson 2000b; Cushman 2010; Huston 1979). For example, the successional changes in tree-49 dominated ecosystems are expected to be highly erratic and unpredictable at the local scale due to 50 variable factors, such as herbivore abundance (Schippers et al. 2014), while often being highly predictable at a larger scale. Temporal changes in the water level of Atlantic wetlands have been 51 52 shown to affect both the nature of interspecific competitive relationships and the overall 53 importance of competition for regulating population growth (Merlin et al. 2015).

54 When studying ecological processes, the ecosystem is a useful conceptual entity that focuses 55 attention on important system properties (Tansley 1935). For example, Lenton et al. (2021) argue 56 that self-perpetuating feedback cycles involving biotic as well as abiotic components may be critical 57 for the stability and long-time success of ecosystems, and Tansley (1935) proposed that stable 58 ecosystems will outlast unstable ecosystems. Furthermore, when ecosystems are situated near 59 other ecosystems in a landscape, another level of emergent properties may arise among the 60 ecosystems at the landscape level (Leibold et al. 2004). For example, environmental variation within 61 a landscape may lead to a storage effect with coexistence of species that would not otherwise 62 coexist (Chesson 2000a; Chesson and Warner 1981).

63 The goal of much ecological research is to understand the underlying causes of observed patterns, 64 which enables us to make credible ecological predictions. However, an observed ecological pattern 65 may be caused by several different processes and involve several important contingencies (Damgaard 2019a; Simberloff 2004; Vellend 2010), and the relationship between process and 66 67 pattern may be influenced by time lags of unknown duration (Svenning and Sandel 2013). 68 Consequently, although there is some level of generality, the quantitative importance of different 69 ecological processes is generally unknown and expected to differ among sites. The resulting variation 70 in vegetation dynamics among seemingly comparable sites leads to a level of complexity that limits 71 our ability to generalize our understanding of the ecological mechanisms underlying observed 72 patterns. While historical contingencies and variation among apparently similar sites preclude the 73 generalization of ecological findings, careful local studies of the mechanisms conducted at the 74 relevant spatial and temporal scales do provide causal information of the factors that determine 75 important community dynamic features (Simberloff 2004; Weiner 1995).

76 There is increasing awareness of the limitations of classical community ecological models, e.g. Lotka-77 Volterra-type competition models, to predict ecosystem effects of a changing environment (Clark et 78 al. 2020; Damgaard and Weiner 2021; Eigentler 2021; Martyn et al. 2020; Mayfield and Stouffer 79 2017; Neill et al. 2009; Vellend 2010). For example, it is widely appreciated that frequency-80 dependent species interactions, in which relatively rare species are favored over more common 81 species, may play an important role in plant species co-existence and community dynamics in plant 82 communities (Chisholm and Fung 2020; Connell et al. 1984). Species-specific soil-plant interactions 83 have received increasing interest as a potentially important and general mechanism for regulating 84 plant populations by hindering local establishment and growth of conspecific plant species in the 85 next generation (Aldorfová et al. 2022; Heinen et al. 2020; Mazzoleni et al. 2015a; Mazzoleni et al. 86 2015b; van der Putten et al. 2013). In an attempt to cope with the ecological complexity, Vellend 87 (2010) suggested partitioning all ecological processes that result in species abundance changes into

88 a logically complete set of disjunct categories: selection, drift, dispersal and speciation (the 89 nomenclature of these categories may be discussed in an ecological context, but the important 90 characteristic is that they are logically disjunct and complete). Historically, such a classification 91 scheme has been successful in evolutionary biology, and Vellend (2010) argued that the reason this 92 approach has not been used more in ecology is due to universal familiarity with ecological patterns. 93 For example, since prehistoric time it has been common knowledge that plant growth is reduced 94 when plants grow close together, and it therefore seems natural to focus on the effects of 95 competitive interactions rather than introducing a logically complete set of possible processes in 96 community ecology.

97 The quantitative scientific exploration of the underlying mechanisms that lead to observed

98 ecological patterns among ecological state variables in time and space relies on statistical analyses,

but often the investigation meets the obstacle summarized in the well-known phrase "correlation"

does not imply causality". More precisely and in the language of Jaynes (2003), the outcome of a

101 statistical analysis is the quantification of logic dependencies (see box 1).

102

#### 103 BOX 1

#### 104 **Probability theory: the logic of science**

105 In an inspiring book published after his death, Jaynes (2003) argues that probability theory in a

- 106 Bayesian setting may be thought of as a quantitative extension of Aristotelian logic, which enables us
- to engage meaningfully in plausible reasoning and provides a method for quantifying our belief in

108 different hypothesis. From a number of verbal statements of the necessary requirements to a

109 quantitative system of plausible reasoning, Jaynes develops the foundation of probability theory,

and show that Bayesian statistics is a mathematical consistent tool for quantifying and

111 communicating our uncertainties of a studied phenomenon (Cox 1946; Jaynes 2003).

- 112 Moreover, just as a true statement in the language of Aristotelian logic does not imply a causal
- 113 mechanism, logical dependencies expressed in the extended quantitative logic of probability theory
- do not imply causal dependencies (Jaynes 2003). Logic is the general science of all possible
- relationships between objects, whereas causality is a specific type of ordered relationship that we
- 116 hypothesize for the world to make sense.

117 The notion of an extended quantitative logic *sensu* Jaynes (2003) provides important insights into

the nature of plausible reasoning and how we do science; scientific discoveries are most often made

by generalization from an observed pattern using the induction principle, and extended quantitative

120 logic shows why this is indeed possible and works in practice. By observing a number of white swans

121 we may say something intelligent about the probability that the next swan we observe is white.

122 Therefore, I have chosen here to use the term "logical dependency" instead of "(statistical)

association" or "correlation", which are more commonly used in the relevant literature. More

124 practically, the use of the concept of extended quantitative logic and Bayesian statistics impose us to

125 estimate the uncertainties of our predictions.

126

127 The distinction between logical and causal dependencies is subtle and not always clear, but 128 important nonetheless. Logical dependencies are investigated using probability theory by calculating 129 the plausibility of different hypotheses when knowledge is limited, and even though it is assumed 130 that the calculated probabilities are determined by causal dependencies, the calculation of such 131 probabilities may be decoupled from causal dependencies. For example, if we want to know if a 132 plant experienced competition from a neighboring plant at day t, when we know that the plant experienced competition at a later day  $t + \tau$ , then we may calculate the probability P (competition 133 134 at day t | competition at day  $t + \tau$ ). Such calculations allow us to make ecological predictions, even 135 though the estimated relationship is not a causal dependence, since the outcome at a later day 136 cannot influence the outcome at an earlier day. It can also be shown that the accumulation of new 137 causally-independent data may lead to logical dependencies when investigating the plausibility of 138 multiple hypotheses (Jaynes 2003).

139 Logical and causal dependencies are not distinct entities, but form a continuum from almost pure 140 logical (statistical) relationships to primarily causal relationships, and often the development of a 141 credible causal hypothesis, i.e. scientific knowledge, goes through a process of collecting relevant 142 data and investigating data by increasingly refined steps of inductive reasoning (Jaynes 2003). The 143 distinction is further complicated by unmeasured confounding factors that affect observed 144 independent variables. These confounding factors may lead to "spurious correlations" or omitted 145 variable bias (Gelman and Hill 2007). The effect of the confounding factors could potentially be 146 teased out in an analysis of instrument variables or using structural equation models (Grace 2021; 147 Rinella et al. 2020), and causal independence may be inferred from randomized experimental 148 manipulations or controlled manipulations using the logical do-operator introduced by Pearl (Lindley 149 2002; Pearl 2009). However, many important ecological processes operate at such large spatial and 150 temporal scales that experimental manipulations are impossible (Shipley 2016), although it may be 151 possible in some cases to combine the information from manipulated experiments and large-scale 152 observational studies (Benedetti-Cecchi et al. 2018).

# 153 Structural equation models

154 The combined effect of both logical and causal dependencies among state variables at the 155 ecosystem level can be effectively modelled using structural equation models, where the observed 156 logical dependencies are modeled using hypothesized causal relationships that often are specified as 157 a directed acyclic graph (Grace et al. 2010; Grace et al. 2012; Shipley 2016; Wright 1921). The 158 hypothesized causal relationships summarize the domain knowledge of the relevant ecological process and may be obtained using differential equation models or general assumptions of mass 159 160 conservation. However, it is important to note that typically the causal relationships in structural 161 equation models are assumed to be linear functions (but see Grace et al. 2012). This means that 162 structural equation models normally do not compare the likelihood of different functional forms of the dependencies among the observed state variables, i.e. the nature of the ecological processes 163 164 that link the observed variables is not investigated. For example, in a typical structural equation 165 model of the possible dependencies between the observed growths of two plant species, it is not 166 addressed whether the growth data may be adequately explained by Lotka-Volterra type of 167 interspecific competition or whether it is relevant to assume some additional form of frequency-168 dependency (e.g. Clark et al. 2020; Damgaard and Weiner 2021). This insensitivity to the underlying processes that link the measured ecological state variables in the hypothesized causal network may 169 170 be critical for the ecological predictions that are made using a fitted structural equation model. For 171 example, if frequency-dependency plays a role in interspecific competitive interactions, then more 172 species can coexist (Chisholm and Fung 2020).

173 Consequently, when specifying structural equation models it is important to model the underlying 174 ecological mechanisms in more detail than is usually done and to apply hypothesized mechanistic 175 functional relationships among state variables, e.g. by assuming that plant growth decreases with 176 the relative frequency of the plant species in a non-linear way (Damgaard and Weiner 2021), or by 177 replacing linear relationships with sigmoid growth functions, which are known to capture population 178 ecological mechanisms at a sufficiently high level of aggregation to allow statistical treatment 179 (Damgaard 2005; Damgaard and Weiner 2008). In this way, logical dependencies in structural 180 equation models may be replaced by dependencies of a more causal nature, and in my opinion, the 181 adopted terminology of logical and causal dependencies used here highlights this overall ecological 182 research agenda. Clark et al. (2020) warn against the use of process models of relatively high 183 complexity due to the risk of overfitting, but if frequency-dependency or feedback cycles are important ecosystem features, then such a level of model complexity is needed in order to make 184 185 credible ecological predictions.

Grace et al. (2010), Shipley (2016) and others have made similar arguments concerning the use of
structural equation models for making stronger inferences and better predictions in ecology. Here, I
add to these points (1) the separation of logical from causal relationships in the analysis, thus
making (2) the link to Jaynes's epistemological framework more direct.

190 Usually, there is sizeable variation in the measured independent variables due to measurement and 191 sampling errors in ecological studies (Muff et al. 2015; Yanai et al. 2018). Such measurement errors 192 are typically not taken into account in ecological and environmental modelling, where measured 193 independent variables are treated as if they are constant entities. This is unfortunate, since it has 194 been shown that even unbiased and normally distributed sampling and measurement errors may 195 lead to important model and prediction bias, a phenomenon known as "regression dilution" (Carroll 196 et al. 2006; Damgaard 2020b; Damgaard and Weiner 2021; Detto et al. 2019). Another typical 197 problem in the analysis of ecological experiments is the use of the language of the experimental 198 design, e.g. "control" and "treatment", as orthogonal fixed independent factors, although there is 199 often large variation and covariation among the variables that are manipulated in the experiment, 200 e.g. soil humidity and temperature, which are the real independent variables of interest in the study 201 and the ones on which inferences and conclusions are based (Damgaard et al. 2018).

How can we best improve the empirical modelling of plant ecological processes in space and time in
order to make credible ecological predictions? Following the suggestion by Clark (2005; 2007) and
several others, I argue for combining structural equation models (Grace et al. 2010; Pearl 2009;
Shipley 2016) with the flexibility of hierarchical models with latent variables in a Bayesian setting for
investigating logical and causal plant ecological dependencies in a coherent way and, at the same
time, model the different sources of uncertainty (Clark 2007; Damgaard 2019b).

# 208 Hierarchical models

209 The use of hierarchical models with latent variables allows us to partition and model the different 210 sources of uncertainty (Clark 2005; 2007; Wikle 2003). For example, in an empirical study of 211 competitive plant growth there may be i) sampling and measurement errors when determining the 212 size of plants at different times using non-destructive measuring methods, ii) structural uncertainty 213 in the form of competitive interactions, e.g. whether frequency-dependent competitive effects play 214 a role or not and iii) the possible confounding effects of unmeasured variables on individual plant 215 performance at both an early and later growth stage due to spatial variation in soil nutrients, 216 pathogens and other factors (Fig. 1).

217 The effect of sampling and measurement uncertainty is accounted for in hierarchical models by 218 introducing latent variables that model the true, but unknown, value of different state variables 219 (Clark 2007; Gelman and Hill 2007). The logical link between the latent variables and the 220 corresponding observed data depends on the type of data and the measurement method. For 221 example, in a study where plant biomass is measured destructively and it is known that the variance 222 increases with the mean, then it may be appropriate to model the observed biomass by a gamma 223 distribution with latent variables as mean parameters and a common scale parameter expressing the 224 relationship between the mean and the variance. In a multi-species study of pin-point plant cover 225 data, it may be appropriate to model the observed number of pin-point hits by a reparametrized 226 Dirichlet-multinomial distribution, in which the latent variables are the relative mean cover of the 227 different species and where the expected inter-specific spatial aggregation at the plot level is 228 modelled by a parameter (Damgaard 2015; 2018).

When fitting fine-grained ecological data, it is relevant to examine how well different process
models are supported by the data (e.g. Clark et al. 2020; Damgaard and Weiner 2021) by estimating
the expected out-of-sample prediction error of the different functional models using the WatanabeAkaike or other information criteria (Gelman et al. 2014), although the predictive performance of a
model may be a poor measure of whether the correct causal relationships has been specified (Arif
and MacNeil 2022).

In the absence of prior knowledge and when modelling spatial and temporal vegetation data on
relatively large scales, it may be a useful strategy to keep it simple and model changes using logically
complete sets of ecological process categories such as those suggested by Vellend (2010), of which
selection at the community level is the most important category. Alternatively, it may be attractive
to model some of the processes that are not of immediate interest by flexible non-parametric
models if there is a real concern that some of the hypothesized functional relationships may be
misspecified (Walker 2013).

242 In more complicated ecological models, it is important to specify whether the hypothesized 243 dependencies among the state variables may be categorized as primarily logical or causal. In any 244 case, when using relatively simple models it becomes increasingly important to quantify the 245 uncertainties and restrain from making predictions outside the spatial and temporal domain of the 246 data. For example, in a spatial and temporal comprehensive, but coarse-grained, study of vegetation 247 changes in wet heathlands and how these changes were affected by the environment, changes in 248 cover of selected species were modelled by simple linear models, thus ignoring any higher-order 249 community dynamic effects (Damgaard 2019b). Instead, care was taken to partition spatial and

250 temporal effects and different sources of uncertainty in a hierarchical model, which enabled short-251 term ecological predictions that may be used for generating local adaptive management plans 252 (Damgaard 2020a). In this particular case, spatial and temporal effects were separated by assuming 253 that the state of plant communities in the first year of the sampled time series was controlled by 254 spatial processes, which included the effects of the environment, as well as historical legacies, 255 contingencies and succession history at the site level prior to initiating sampling. The temporal 256 processes were then modelled in a state-space model based on the observed yearly changes in 257 vegetation cover during the sampling period (Fig. 2). In ecological systems with significant among-258 site dispersal, it may be relevant to model the effect of the dispersal in spatial and temporal 259 diffusion models (e.g. Wikle 2003).

Ideally, the possible confounding effects of unmeasured variables should be investigated using an
instrument variable analysis (Gelman and Hill 2007; Rinella et al. 2020). However, this is often not
possible and, instead, we may account for possible confounding effects of unmeasured variables by
modeling the unexplained covariance between the observed variables, such as the unexplained
covariance between early and later growth stages (Fig. 1).

It is noteworthy that the treatment of measurement errors and causal dependencies in structural
equation models in a hierarchical setting mimics general epistemological models (see Box 2) and,
consequently, provides a general recipe for how to link models with data and causal hypotheses into
a mathematical framework.

269

#### 270 BOX 2

#### 271 General epistemological models

272 From a more general epistemological point of view, hierarchical models with latent variables mirror 273 well-known theoretical philosophical models of how knowledge of the world is obtained. Kant (1781) 274 suggested that there is a fundamental division between a world of phenomena ("Das ding an sich") 275 and the observer. When the observer senses a certain phenomenon (the object), a representation of 276 the object transcends into the mind of the observer and starts to make sense (a posteriori 277 knowledge). In this process, the representation of the object is merged with several sources of 278 relevant *a priori* knowledge, such as the concepts of causality, space and time. 279 In a hierarchical model, data corresponds to Kant's phenomena, and the latent variables and their 280 relationships correspond to the transcended representation of the objects in the mind of the

281 observer. Similarly, Wittgenstein (1922) described how we make mental pictures of objects and how

282 these pictures are models of reality. He suggested that the relationship among the different picture 283 elements corresponds to the relationship among the objects and, thus, provides a representation of 284 the structure of the reality. For example, in proposition 2.15 he writes: "That the elements of the 285 picture are combined with one another in a definite way, represents that the things are so combined 286 with one another. This connection of the elements of the picture is called its structure, and the 287 possibility of this structure is called the form of representation of the picture." (Wittgenstein 1922). This description is almost a definition of hierarchical structural models where the "pictures" 288 289 corresponds to quantitative latent variables, although the latter is a more restricted concept.

#### 290 Discussion

291 It is important to partition and model the different types of observed variance, and hierarchical 292 models are often the best tool for this purpose. For example, in a relatively fine-grained study of 293 plant competitive growth of Festuca ovina and Agrostis capillaris it was concluded that the inclusion 294 of frequency-dependence and measurement error improved model performance greatly, but taking 295 possible unmeasured variables into account did not. Furthermore, when sampling and measurement 296 errors were taken into account, the resulting ecological prediction differed qualitatively from the 297 corresponding non-hierarchical models without latent variables (Damgaard and Weiner 2021). In a 298 study of tree fecundity Clark et al. (2004) found that random variation among individual trees and 299 among years dominated the variation in tree fecundity. If this random variation was omitted from 300 the analysis, parameter estimates would have been biased and led to qualitatively erroneous 301 conclusions. They also found that estimated random variation could partly explain the observed 302 pattern of coexistence among the tree species.

303 The current poor performance of ecological predictions is probably due to the relatively low quantity 304 and quality of spatial and temporal ecological data. The increasing use of advanced technology in 305 ecological monitoring, such as drones and satellites, may allow us to make better predictions. As 306 fine-grained plant growth data at increasing spatial scales become available, it may be feasible to fit 307 structural equation models, in which different hypothesized species interaction processes are 308 statistically compared. By increasing the resolution of spatial and temporal ecological data, it should 309 become possible to increase both prediction precision and accuracy. At the limit of better and better 310 local data and increasingly detailed understanding of the ecological processes, the increase in 311 predictive performance may reach a boundary. If the intrinsic boundary of ecological predictive performance is low due to historical or other contingencies, it may be necessary to rethink our 312 313 current strategy of adaptive management of ecosystems based on ecological predictions in nature 314 conservation.

315 For some ecosystems that operate on relatively small temporal and spatial scales, such as microbial 316 decomposer systems, it may be possible to perform manipulative experiments that allow us to test 317 and validate complete causal hypotheses of the system dynamics. However, the relevant temporal 318 and spatial scales of most ecosystems are so large that a purely experimental approach is not 319 feasible, so in our modelling of ecosystem processes we must recognize that our current ecosystem 320 knowledge is incomplete and not be overconfident in hypothesized causal mechanisms. 321 Consequently, ecological models with both causal and logical dependencies will be needed in the 322 attempt to make ecological predictions. The goal of ecology as a science, however, is to increase our 323 mechanistic understanding of the different processes that determine the abundances and 324 distributions of species, and thereby enable us to convert assumed logical dependencies into more 325 causal dependencies among state variables in our structural equation models. The current state of 326 structural equation models in plant ecology, where many dependencies are strictly based on logical 327 and statistical arguments, will act as a guide into where knowledge is missing and suggest future 328 research agendas. Moreover, it is important to capture the causal mechanisms at a sufficiently high 329 level of aggregation to allow statistical treatment of available ecological data in a structural equation 330 model. It is not necessary, or even desirable, to model all the known mechanistic details, such as 331 modelling every single birth and death event using individual based models.

332 In my opinion, the image of plant ecology as a "soft" science, which plays a disproportionally small 333 role in political decisions, hinges on our failure as a scientific community to make credible 334 predictions where uncertainties are quantified. Currently, the majority of plant ecological 335 predictions, from local management plans of natural habitats to global assessments of biodiversity, 336 are broad verbal statements without any attempts to quantify the uncertainty of the predictions. To 337 communicate credibility of the verbal predictions, a common practice is to call on the consensus of 338 experts. For example, in a report from IPBES (2019) 150 selected experts extracted the content of 339 more than 15,000 scientific publications to make a global assessment of biodiversity, and the 340 obtained conclusions, including the recommended actions, were approved at a plenary meeting. 341 How is such a process even possible and what is the role of the assembled ecological data in the 342 15,000 scientific publications in reaching a consensus for the recommended actions? No body of 343 even distinguished experts can grasp the complexity of ecosystem dynamics in a changing 344 environment and fairly assess the wealth of relevant spatial and temporal data in round-table and 345 panel discussions. When good data are available, it would be better to apply a quantitative 346 modelling approach, where the uncertainty of the effects of the recommended actions may be 347 assessed in a systematic way. The results of the quantitative analyses can then be interpreted by 348 experts for decision makers.

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# 352 Figures

353 Fig. 1. : Hierarchical model of competitive plant growth from plants at an early and later growth

354 stage. The true, but unknown, plant size at the early and later growth stage is modelled by latent

- variables (squares) and denoted *X*, *Y*, respectively. The latent variables are logically linked to the
- observed data (circles), which are denoted *x*, *y*, respectively, with the corresponding latent variables
- 357 as mean values. The sampling and measurement uncertainty are modelled with  $\sigma_x$  and  $\sigma_y$ ,
- 358 respectively. The competitive growth process is modelled by the structural function, *F*, which
- depends on X and possibly on some measured environmental variables  $z_m$ . The effect of
- unmeasured variables affecting both earlier and later growth stages is modelled by  $\sigma_{xy}$  as the part of
- 361 the covariance between the early and later growth stages that is not explained by the independent
- 362 factors in the structural model.

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Fig. 2. Outline of a structural equation model where the spatial and temporal processes are separated. The spatial variation in vegetation cover in 2007 is modelled by nitrogen deposition (Ndep), soil pH (pH), soil type and precipitation (Precipit.). The yearly change in vegetation cover from 2007 to 2014 (only a single yearly change is shown in the figure) is modelled by all the former variables as well as grazing. The square boxes are latent variables and the oval boxes are data. The full black arrows denote spatial processes, the dotted black arrows denote temporal processes and the grey arrows denote the modelling of sampling and measurement error (Damgaard 2019b).

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