1	Patterns of selection across gene regulatory networks
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9	Abstract
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11	Gene regulatory networks (GRNs) are the core engine of organismal development. If we
12	would like to understand the origin and diversification of phenotypes, it is necessary to
13	consider the structure of GRNs in order to reconstruct the links between genetic
14	mutations and phenotypic change. Much of the progress in evolutionary developmental
15	biology, however, has occurred without a nuanced consideration of the evolution of
16	functional relationships between genes, especially in the context of their broader
17	network interactions. Characterizing and comparing GRNs across traits and species in a
18	more detailed way will allow us to determine how network position influences what
19	genes drive adaptive evolution. In this perspective paper, we consider the architecture
20	of developmental GRNs and how positive selection strength may vary across a GRN.
21	We then propose several testable models for these patterns of selection and
22	experimental approaches to test these models.
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24	Keywords

Development, gene regulatory networks, natural selection, gene regulation, protein
evolution

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29 **1. Introduction**

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Organisms assemble themselves through an orchestrated sequence of genes being 31 expressed in different combinations, at different times, in different cells. The logic 32 33 underlying this orchestration emerges largely from interactions between the genes themselves, and these interactions comprise vast and complex regulatory networks 34 capable of allowing single cells to construct things like mushrooms or hedgehogs. 35 Accordingly, in 2007 Wilkins [1] argued that a gene network-based approach was 36 necessary to advance the field of evolutionary developmental biology. At that time, evo-37 38 devo was largely focused on studies showing changes in the regulation of individual 39 genes associated with the evolution, and often convergent evolution, of morphological traits [2–4]. While this is still largely the state of the field, a larger philosophical question 40 41 continues to crystallize and become more urgent: Why do some genes seem to be more likely to facilitate morphological evolution than others? Drawing on concepts of gene 42 43 regulatory networks (GRNs) [5], Stern and Orgogozo [6] proposed that these genes 44 occupy unique positions within developmental networks such that they integrate many inputs and regulate many outputs. 45

Few studies have explicitly tested this idea, however [7], and the evolutionary 47 consequences of many other features of GRNs have also yet to be explored [5]. These 48 include the idea that some highly essential subnetworks, or network 'kernels', are 49 evolutionarily constrained, while other subnetworks that can be co-opted for different 50 51 functions, or network 'plug-ins', are more evolutionarily labile [5]. The type of gene 52 regulation circuitry could also indicate the degree of evolutionary constraint on different genes [8]. A larger body of evo-devo research has instead focused on other questions 53 concerning the genetics of adaptation, such as whether adaptive evolution is occurring 54 55 primarily in cis vs. trans sequences or via de novo mutations vs. standing variation [6,9]. The literature on adaptive trait evolution still remains relatively separate from the 56 growing body of literature on network evolution in other fields of biology. These 57 literatures include the study of network evolution in silico [10,11], as well as the wealth 58 of information on protein-protein interaction (PPI) networks and the distribution of 59 evolutionary rates across these PPI networks [12-14]. We propose that research in 60 61 these fields can help inform our predictions for the evolution of GRNs.

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Over a decade after Wilkins' essay [1], his proposed GRN-oriented reframing of evodevo still eludes us. The developmental GRNs for some traits have been described in great detail, such as the GRN for sea urchin embryogenesis, yet we still have little understanding of the role of selection in shaping such networks [15]. Some studies have begun to describe the distribution of selection using networks constructed from gene coexpression correlation matrices [16]. However, the conclusions we can make from these types of transcriptomic studies are limited by our lack of knowledge of gene regulatory interactions. In this perspective paper, we will discuss patterns in GRN structure and
key case studies of GRNs for adaptive traits before proposing several testable
hypotheses for how positive selection pressure could vary across this GRN topology.
We then consider how generalizable these predictions are across different types of
GRNs and recommend approaches to test these predictions.

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2. GRN structure and gene connectivity

There are two primary ways a GRN can evolve. First, a network can gain or lose 77 78 components, such as by cis-regulatory elements (CREs) gaining or losing new binding sites or proteins changing regulatory targets¹. Second, the timing, location, or level of 79 80 expression of genes within a network can evolve via changes to either component proteins or CREs. For example, a common hypothesis in studies of co-option is that 81 82 complete or partial networks are simply re-activated and redeployed at a different time 83 or location, without many changes to their components, to drive the development of new traits [19]. This evolution may occur at some positions in a network moreso than others, 84 so to understand gene evolution we must first characterize the structure of a network. 85 86

As discussed in the introduction, so-called input-output genes are well-known for their proposed role in driving morphological evolution due to their distinct network positions [20]. Input-output genes are identified as switch genes in a GRN, where they integrate the inputs of many upstream patterning genes to control the activation of many downstream cell differentiation genes. Many input-outputs are characterized by their

¹ GRNs can also expand in other ways, see: [17,18] for examples of how gene duplication and transposable element domestication can also drive GRN evolution.

strong phenotypic effects, where they are both necessary and sufficient for determining a trait of interest. For example, changes to any single known gene downstream of the input-output gene *shavenbaby* (*svb*) are not sufficient to promote or inhibit trichome development, but changes to *svb* expression itself are sufficient to alter trichome development [21]. *svb* is also necessary for trichome development [21]. To understand the network context such input-output genes inhabit, and the common properties of these networks, we can draw from research on other biological networks.

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100 The condition of some genes having more interactions than other genes, just as the 101 input-output gene is connected to many more genes than others, has been well-102 explored in other areas of network biology. Many networks in biology are considered 103 using the graph model of the scale-free network [22]. These networks are composed of nodes (in this case, genes) and edges (regulatory connections between genes). A few 104 nodes are connected to many other nodes ('hubs'), while most nodes have few 105 106 interactions. This distribution of connections can be described by the power law function. 107

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Recent work from Ouma et al. [23] using GRNs derived from protein-DNA interaction databases across four organisms found that these global GRNs fit the scale-free model. They found that most transcription factors only interacted with a few genes, while only a few transcription factors interacted with many genes, following the predicted power law distribution with different scaling exponents for different species. While they found that subnetworks of these GRNs also fit the scale-free model, it remains to be tested
whether specific developmental GRNs are truly scale-free [24].

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117 This general principle of a few genes with many connections and many genes with few 118 connections will likely hold true. Research on PPI networks can help us assess this 119 prediction and its implications. There are typically a few high-connectivity proteins and many low-connectivity proteins in a network, with connectivity defined as the number of 120 121 interactions per protein. These few high connectivity proteins are more likely to interact 122 with low connectivity proteins and less likely to interact with each other than expected by chance, forming networks that have many peripheral interacting genes and a few 123 124 central genes with many interactions [25]. Networks with this asymmetric distribution of 125 connectivity are generally highly robust to random errors but are extremely vulnerable to the removal of the high connectivity nodes [26]. Consistent with this predicted 126 127 robustness, evolved protein interaction networks are more resilient to the removal of 128 random nodes than randomized networks [27].

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One network structure that can account for this variation in connectivity is the bow-tie structure. A bow-tie refers to a structure where there are two layers composed of many nodes and an intermediate layer that is composed of very few nodes that connects these two layers [28]. This central layer forms the core or 'knot' of the bow-tie (Fig. 1). The nodes at the core of the bow-tie have the highest number of connections [10]. Many types of networks, including metabolic and signaling pathways, can be characterized by this bow-tie structure [28]. Bow-ties are thought to be common across biological systems because they facilitate both robustness and evolvability of thesystem [10].

140	A directed bow-tie structure is composed of many inputs which are integrated by the few
141	nodes at the central core. These core nodes then regulate many outputs. This concept
142	can also be applied to developmental GRNs, where many upstream genes are inputs to
143	the input-output gene(s), which then targets many downstream genes to regulate
144	cellular differentiation [6,7]. Bow-tie networks can be distinguished from the hierarchical
145	null model by demonstrating that a gene (or genes) is connected to more genes both
146	upstream and downstream than others [28].
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149	3. The evolution of GRNs for rapidly-evolving morphological traits
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² This structure is also commonly described as an hourglass-shaped network [7]. Here we refer to it as a bow-tie structure to connect this concept from GRN studies with the literature on other types of biological networks [28] and to avoid confusion with the developmental hourglass model [29].

that it is the target of positive selection or is under relaxed constraint [30]. These CRE
mutations have resulted in parallel losses of trichomes in multiple *Drosophila* species
[2]. Thus, *svb* is considered a hotspot gene for morphological evolution.

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162 Another example of a hotspot gene for morphological evolution is optix, which is a 163 proposed input-output gene for wing patterning across butterflies [31]. There are many 164 known downstream genes of optix, as well as many candidate upstream genes [31–34]. Therefore, the optix butterfly wing color pattern GRN most likely fits the bow-tie 165 166 structure (Fig. 2). The adaptive convergent evolution of red wing color pattern mimicry in 167 Heliconius butterflies is due to selection on optix CREs [4,35,36]. We have evidence 168 that GRNs for rapidly-evolving morphological traits are evolving primarily by positive 169 selection acting on the CREs of the input-output genes from the svb and optix networks. We still have little information, however, on how positive selection acts on the broader 170 171 networks that host these genes.

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A recent study on the optix GRN was able to shed some light on the distribution of 173 174 selection throughout downstream elements of the network. Lewis et al. [34] combined 175 methods to detect selective sweeps with molecular approaches to characterize genes regulated by optix in order to identify genes under selection in the optix GRN that may 176 177 also be involved in adaptive wing pattern evolution. By identifying binding sites of the optix protein, and then determining which genes optix-bound CREs were regulating, 178 179 they were able to identify numerous direct targets of optix. Notably, optix-bound CREs 180 showed significantly elevated signals of selection compared to randomly-selected

181	CREs, although, interestingly, few of these genes showed nearly as great a signal of
182	selection as optix itself. This suggests that these directly downstream genes are targets
183	of positive selection but are less strongly selected upon than the regulatory region of the
184	input-output gene itself.
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187	3.2 GRN structure and the strength of positive selection
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189	Using the optix GRN as a case study (Fig. 2), we can predict how different levels within
190	a GRN for a rapidly-evolving adaptive trait may be more or less likely to be targets of
191	positive selection.
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193	3.2.1 Key predictions for the evolution of different levels of GRNs
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195	Prediction I: CREs of input-output genes are more likely to be under strong
196	positive selection than CREs of other genes in a GRN, while input-output gene
197	protein-coding regions are more likely to be constrained.
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199	An important prediction in modern evo-devo is that CRE sequences should drive trait
200	evolution more frequently than coding regions because they make up a much larger
201	percentage of the genome, and expected to have more trait-specific (and less
202	pleiotropic) effects on phenotypes [8,20]. Following this, we would further predict that
203	input-output gene CREs are more likely to be under positive selection than genes at

other positions in a GRN because the handful of input-output gene case studies, such
as *optix*, show these loci can have strong signatures of selection and population
structure compared to the rest of the genome.

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208 Conversely, the protein-coding regions for input-output genes may be more constrained 209 due to these transcription factors' involvement in other more ancestral developmental 210 processes. For example, svb is required for the production of all trichomes of Drosophila larvae and adults, and an isoform of svb is required for oogenesis [6,37], and optix is 211 212 known to be essential for eye morphogenesis in Drosophila and may have been co-213 opted to regulate red color pattern in butterflies relatively recently [31,38]. There is 214 considerable study on how proteins with a higher number of interaction partners are 215 more constrained and more likely to be under negative selection [13,39,40]. In contrast, the idea that the protein-coding sequence for a gene connected to more genes through 216 217 *cis*- interactions is more constrained is, to our knowledge, largely untested. One study 218 investigated this question by measuring natural variation in gene expression level in the 219 plant Capsella grandiflora to infer gene co-expression networks [16]. This study 220 determined gene connectivity by measuring the sum of correlations with other genes, 221 weighted by the strengths of correlations. The genes with higher connectivity scores 222 were more likely to be under negative selection, but the level of gene connectivity had 223 no detectable correlation with rate of fixations driven by positive selection. However, 224 interpretation of this result is limited by the fact that it is based on networks inferred from 225 gene expression and not functionally validated regulatory relationships.

Prediction II: Input gene protein-coding sequences are more likely to be under
 stronger stabilizing selection due to pleiotropy than those of output genes.

230 Proteins that are on the periphery of a PPI network, with the fewest interaction partners, 231 are more likely to be targets of positive selection [13,14]. We may predict a similar 232 pattern for genes with fewer connections to other genes in a network. Similar to input-233 output genes, upstream transcription factors are more likely to be involved in essential 234 developmental processes and to be more constrained than peripheral genes [8]. We 235 may expect an increase in pleiotropy in a protein's function to correlate with an increase 236 in constraint on the amino acid sequence. Likewise, this constraint does not necessarily 237 extend to the CREs of these genes [41].

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This pleiotropy may also potentiate adaptive evolution in other ways. More pleiotropic 239 240 proteins could have more binding domains and more opportunities to interact with new 241 partners, so we might expect stronger positive selection on their regulation than less 242 pleiotropic proteins, although this prediction has not been tested. In other cases, we 243 might expect more pleiotropic genes to be regulated by more pleiotropic CREs, so the 244 evolution of these CREs may or may not also be constrained [8,42]. Therefore, unlike 245 for protein-coding sequences, it is difficult to predict whether there is a difference in 246 selection strength on upstream vs. downstream gene CREs. Future work on cisregulatory grammar and interaction dynamics will help resolve this [43,44]. 247 248

249 Prediction III: Traits evolving rapidly under positive selection are controlled by250 more fragile GRNs.

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252 For a robust GRN, mutations and genetic variation will generate less phenotypic 253 variation that can be subject to selection. By contrast, we might expect traits that are 254 rapidly-evolving under positive selection to be controlled by more fragile networks. In 255 this case, fragility meaning that minor mutations, such as in individual CREs, are likely 256 to have substantive phenotypic effects [35]. A trade-off between robustness and 257 innovation has been predicted on short time scales, and recent empirical work shows 258 GRNs for rapidly-evolving adaptive traits are more fragile than previously thought 259 [35,45]. However, the extent of this trade-off is still an active area of investigation. 260 Robustness can also increase later opportunities for selection on a GRN in the longterm [45]. 261

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263 Prediction IV: Evolutionary drift is likely to be more prominent than positive264 selection in robust GRNs.

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Often, networks that are observed to be under developmental systems drift (DSD) – the process by which homologous traits diverge in their genetic mechanism via neutral evolution – are thought to be more robust [46]. This is because this drift suggests that there is some level of functional redundancy among nodes in the network. DSD can occur at different positions in a network. Nahmad et al. [47] found that neutral evolution in the regulation of genes at different positions in the GRN that controls ant wing

272	polyphenism can result in similar effects in wing size. It is still unclear, however, if there
273	is any predictability in how robustness and redundancy are distributed across different
274	aspects of GRNs. Robustness can be an emergent property under long periods of
275	stabilizing selection or it can be selected for when there are many perturbations to a trait
276	[48,49]. Whatever the origin of robustness may be, we would expect GRNs for older
277	homologous traits and early developmental stages to be more robust than younger and
278	later-acting GRNs. This idea is supported by gene expression and modeling data
279	comparing early and late networks [50]. Furthermore, older traits also simply have had
280	longer to evolve robustness, and therefore, by extension, we would expect DSD to
281	occur more often in older GRNs.
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295 gene has little effect on the rate and strength of positive selection on that gene's CREs 296 (Fig. 3a). Changes in both upstream and downstream gene CREs may result in 297 expression in a new spatiotemporal domain and changes in the trait. For one well-298 studied trait – abdominal pigmentation in *Drosophila* – it appears there is change 299 occurring both upstream and downstream in the network that can explain pigmentation 300 variation within and between species [51]. These genes also show some evidence of 301 selection [52,53]. It is challenging, however, to differentiate which genes may truly be input-output genes until the network is better characterized. Abdominal pigmentation is 302 303 an excellent target for future work given the many genes associated with variation in this 304 trait that can be evaluated further to compare the frequency of selective sweeps on 305 different types of genes [54].

306

Another model is that CREs of upstream genes are under pleiotropic constraint while 307 CREs of downstream genes are under positive selection (Fig. 3b). This model may be 308 309 more likely if the input genes' CREs are all also shared (possibly through co-option) as 310 part of more ancient, essential GRNs [8,55]. We may expect that input genes are more 311 likely to be involved in network kernels that have dense circuitry. These input genes' 312 CREs are thus more likely to be constrained, such as by requiring a precise order of 313 cooperatively-binding transcription factors to activate an essential function [55]. How 314 widespread this type of constraint is on the regulation of upstream genes is unclear. 315 Some ancient CREs have been found to drive adaptive trait evolution, and some 316 upstream genes with constrained CREs can also gain new, possibly more evolutionarily 317 labile CREs [35,56]. More research is needed to determine whether the regulation of318 upstream genes is more often constrained than downstream genes.

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A third alternative model posits that some traits may be evolving rapidly, primarily by 320 321 changes in upstream patterning, so the CREs of upstream genes may be under positive 322 selection while the regulatory architecture of the downstream genes is functionally 323 conserved (Fig. 3c). We expect this to occur in cases where a GRN was co-opted to 324 reproduce a structure at a new location or timepoint. For example, the development of 325 the novel adult male-specific posterior lobe in Drosophila melanogaster is driven by a 326 GRN co-opted from the development of the larval posterior spiracle. This co-opted GRN 327 shares many of its downstream genes and enhancers with its ancestral GRN [57]. The origin of the novel trait is most likely due to changes in upstream patterning. 328 Downstream terminal effectors may also be highly conserved such that upstream genes 329 330 are evolving more by contrast. An interesting observation consistent with this model 331 comes out of the many studies of adaptive wing patterning evolution in Lepidoptera, where selection on a pigmentation gene has never been found to be the primary driver 332 333 of wing color pattern evolution in nature, even for simple color switches [4,58,59].

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In terms of selection on protein sequences, downstream proteins may be the least constrained and most likely to be under positive selection (Fig. 3d). There are many examples of downstream protein structural changes involved in adaptive evolution of melanism, for example [60–62]. Interestingly, these genes tend to be receptors or signaling proteins in the melanin pathway, not the terminal effectors. It has been

340 proposed that further downstream genes evolve more slowly because they occupy a 341 more stable cellular environment [63]. These cases suggest that the downstream proteins for this melanic trait are generally much more evolutionarily labile than 342 upstream transcription factors. This is consistent with the research on PPIs that proteins 343 344 on the periphery of a network should be under the strongest positive selection 345 compared to other proteins, but we need more comprehensive and comparative studies to determine whether selection is indeed mainly targeting coding regions of these 346 347 downstream genes [13].

348

We could also observe positive selection on an upstream gene or genes (Fig. 3e). While 349 350 we would expect upstream transcription factors to be more evolutionarily constrained 351 due to pleiotropy, there could be positive selection for transcription factor modularity by evolving additional DNA binding or protein binding domains [64]. We might expect this 352 353 for younger transcription factors that do not have many essential roles and are less 354 constrained in their structure. This upstream protein evolution could also occur after a gene duplication event, which could release this gene from constraint and allow for the 355 356 duplicate gene to diverge and gain a new role in regulating the input-output gene or 357 other upstream genes [65].

358

It is also worth considering that a cofactor for the input-output gene could be under positive selection to interact with the input-output gene and activate different suites of genes (Fig. 3f). Cofactors can increase the capacity for the network core to activate modules of differentiation genes in specific spatial contexts and are critical for the development of specific tissues and cell types [66]. We also expect core proteins to be
evolutionarily constrained because changes to their binding domains would affect many
processes at once. However, the less conserved regions of the protein structure can
evolve more easily and allow new protein-protein interactions. This can avoid the
potential pleiotropic costs of changes to the binding domains themselves [67].

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How generalizable are these predictions across developmental GRNs? 371

372 Our predictions – and much of our understanding of GRNs – come from study of the 373 development of rapidly-evolving, adaptive morphological traits. However, GRNs can be 374 considered at many spatial and temporal scales, from the set of genes that underlies an entire developmental stage to the set of genes responsible for a specific discrete trait. 375 376 Whether our predictions can be applied across developmental GRNs is unclear. There 377 are some cases where GRNs are not under positive selection. These may include highly-conserved, essential GRNs [5]. There are also some specific developmental 378 379 stages where the networks are much more constrained given the high degree of 380 conservation across taxa, such as the genes underlying the midembryogenesis period 381 of development [8,29,68].

382

383 Further, we assume that the networks controlling the development of these

morphological traits fit a bow-tie structure, with a distinct input-output gene or genes that

are much more connected to other genes than these other genes are connected to each

386	other in the network. This assumption has not been rigorously tested. With more
387	research on gene regulatory relationships, we can better model the structures of GRNs
388	and how these structures can vary. Perhaps, for example, bow-tie GRNs are more
389	commonly seen as a feature of more rapidly-evolving traits (e.g. color patterns), while
390	more deeply conserved traits (e.g. embryonic patterning) tend towards different
391	structures. Presently, however, we cannot say how generalizable these ideas are
392	beyond that they are almost certainly not universally applicable – there are simply too
393	few case studies.
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396	5. Experimental methods for GRN evolution
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398	5.1 Inferring networks and patterns of selection
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400	To test whether the proposed models (or, more likely, combinations of models) of
401	positive selection across GRNs hold for adaptive morphological traits, and whether
402	these patterns are found more broadly across developmental GRNs, we need two types
403	of information. We need first to characterize the GRN for traits of interest, and then we
404	need to determine the patterns of selection across the genome. Experimental methods
405	for the latter have been well-developed: We know that the selection across genomes is
406	not evenly distributed, and many studies have extensively investigated individual loci
407	that show strong signals of selection and are involved in morphological evolution [7,69].

inferred from co-expression correlation matrices generated from bulk RNA-seq data.
While these data can be very informative, the actual regulatory relationships between
genes remain unknown [70]. Here, we discuss first how these networks can be
described in more detail, and then how these data can be integrated with tests for
selective sweeps to relate network position to gene evolution.

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5.1.1 Characterizing GRNs

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417 There are many tools that can help improve our understanding of regulatory interactions 418 and confirm causality between interactions. One of the most critical pieces of 419 information is to understand where key transcription factors are binding in the genome, 420 and to infer their target genes. Analyzing transcription factor genes that have been associated with trait evolution by using chromatin immunoprecipitation and sequencing 421 (ChIP-seq), or similar methods, is a key step in characterizing GRNs [71]. For binding 422 423 sites that are not located at the promoter of a gene, the target gene can be identified using chromosome conformation capture methods (e.g., Hi-C, 4C, etc.) to determine 424 425 whether the bound DNA region physically interacts with the promoter of a gene [72]. 426 These inferences can be further supported using gene expression data [72,73]. Many 427 methods have been developed for network inference from single cell RNA sequencing 428 (scRNA-seq) data that leverage analysis across cell types and timepoints [74]. scRNAseg data can also be integrated with analysis of chromatin accessibility [72]. For 429 430 humans, yeast, and other organisms with large amounts of pre-existing molecular data, 431 GRNs can be predicted by integrating known protein-protein interactions, gene

expression, and binding motif data [75,76]. These data can further expand our
knowledge of upstream and downstream genes in the network that can be later
confirmed using functional tests.

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436 Functional tests of candidate genes can confirm not only that the gene is involved in the 437 trait of interest, but also the direction of regulation. We can knock out, knock down, or drive expression of a key transcription factor and assay for changes in the expression of 438 439 candidate downstream genes. Alternatively, we can use genetic tools to manipulate the 440 expression of multiple genes in a hypothesized network to test whether they are in the same network and to determine the relative position of these genes. Reporter 441 442 constructs can also assist in validating the role of particular CREs in driving expression in a particular region. CRISPR/Cas9 technology has made all of these approaches 443 much more accessible in emerging model systems [77]. 444

445

446 While inferring GRNs requires a lot of experiments, some of this work has already been completed in a handful of study systems. We suggest that GRNs that have been studied 447 448 in depth in various model systems are ripe to be used in comparative evolutionary 449 studies by extending work into related species. Comparative analysis of these GRNs 450 could then shed light on the patterns in evolution across different levels of the network. 451 For example, comparative work on neural crest cell development in other vertebrates in addition to chicks has illuminated the evolution of the cranial neural crest by successive 452 453 additions of components to the network from an ancestral trunk-like lineage [78]. 454 Another recent study compared the well-characterized sea urchin endomesoderm GRN

with a newly constructed sea star GRN for the same trait, finding both shared and
unique modules [79]. Thus, there are quite a few promising systems for exploring GRN
evolution.

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5.1.2 Detecting positive selection

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It will be exciting to combine functional GRN models with tests for signals of positive selection. There are a number of methods to detect positive selection using variation within and between species [80–82]. Since selection can be tested at both micro- and macroevolutionary scales, we can also compare the patterns of selection across networks that may emerge at different time scales. Testing for positive selection can also be useful for building the GRN for a particular trait since regions under selection will have some functional role in a phenotype.

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469 Many tests for selection on genes are based on the ratio of the rate of nonsynonymous substitutions to the rate of synonymous substitutions (d_N/d_S) . There is no equivalent to 470 471 this statistic for CREs. Positive selection in CREs has been identified using tests for 472 selective sweeps and divergence in substitution rate in specific regions across taxa 473 [36,83,84]. In principle, future work on CRE evolution could also leverage analysis of 474 motif composition in a similar way to synonymous and nonsynonymous changes to genes. These tests would require a sophisticated understanding of what affects a 475 476 motif's affinity for specific transcription factors and how transcription factors' binding 477 sites differ from their canonical motifs in different taxa. Despite these complications, it is worthwhile to analyze the motifs of a CRE in the event that transcription factor binding is
conserved despite sequence divergence. These functionally-conserved CREs have
been identified at deep evolutionary time scales [85]. Understanding what changes to
CREs are meaningful and are more likely to be the result of positive selection and what
changes are due to drift can be aided by characterizing motifs.

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484 **5.2 Limitations and challenges**

485

There are several common limitations and biases to studies of the type mentioned above. The main challenge moving forward will be scaling up experiments to sufficiently characterize a GRN, or many GRNs, to answer questions of network position and selection. Choosing a few transcription factors that are well-described and known to be under strong selection can help focus this research, but it also introduces bias in the description of the network's structure. This streetlight effect is unavoidable unless we endeavor to describe every unknown gene that is associated with a trait.

493

Necessarily, any description of a network for a specific character involves decisions of what is and is not included as part of the network. No GRN is an island: The development of a late-acting GRN for a trait will often be contingent upon proper early development of the organism. How we should make these decisions of what is and is not considered part of a trait's underlying network is an open question. Some suggest that every gene expressed in the cells that give rise to a trait should be considered part of the GRN for that trait – a viewpoint growing in popularity with respect to disease 501 states [86]. Most evo-devo studies include genes in the network for a trait if they have 502 functional or other molecular evidence to support its inclusion. More data on the gene 503 regulatory networks underlying traits will help us understand how best to characterize 504 them and whether the bow-tie model fits or if a different structure is more 505 representative.

506

507 It is also important to consider that often a gene may be located at different network positions depending on the trait or network scale considered. For example, different 508 509 strains of Drosophila melanogaster have different patterns of trichomes on the legs. 510 Initially, it seemed surprising that these differences were not facilitated by changes in 511 CREs regulating svb expression, as was found for larval trichome pattern. Instead, 512 differences in leg trichomes were mediated by changes to the CREs of a different gene, miR-92a. This finding could be explained by differences between the larval and leg 513 514 trichome GRNs [87]. Thus, the selective pressure on any individual gene or CRE can be 515 affected by its different network positions and roles for different traits. Further, even 516 within the network for the same trait, a gene can also play multiple roles and occupy 517 different network positions, such as both regulating (upstream of) and being regulated 518 by (downstream of) the input-output gene.

519

520 Generally, to identify genes that underlie adaptive morphological evolution, they must 521 meet two conditions: i) they have detectable effects on phenotype and ii) they have 522 detectable signatures of selection. The literature reviewed in this paper is thus biased to 523 focus on large- and intermediate-effect size genes with evidence of recent divergence. These examples demonstrate that large- and intermediate-effect genes do in fact drive adaptation, as can be predicted under some evolutionary scenarios [88]. However, these data are likely not representative of the entire spectrum of genetic variation underlying trait evolution including all minor effect genes, especially for complex developmental traits [89]. More research aimed at detecting polygenic selection across networks can reveal whether gene network position is less important in this evolutionary regime [82].

531

532 Finally, complete knowledge of every GRN and every gene's regulation and function is still probably not sufficient to predict gene evolutionary rates at different network 533 534 positions due to the potential effects of population size and structure [90]. In small 535 populations, mutations that have a larger effect on the network structure may be more likely to be fixed, whereas in larger populations, we might expect this to occur less 536 537 often. This is because small populations tend to accumulate deleterious mutations, and 538 a mutation that significantly changes gene interactions is more likely to be deleterious 539 compared to a mutation that slightly alters expression of a downstream gene [90]. 540

541 6. Conclusion

542

543 Characterizing GRNs and patterns of selection across them is clearly not a small task, 544 but it can lend great insight into the evolution of adaptive traits. Positionality within a 545 network has long been proposed as an important factor in the evolution of genes within 546 a regulatory network, and many studies have tested for similar patterns of selection 547 across different components of signaling and metabolic pathways [28]. Due to the paucity of thoroughly characterized developmental GRNs, especially for rapidly 548 549 adapting traits, this guestion has still not been addressed. Open guestions include 550 whether evolution at the CREs of input-output genes is the primary driver of 551 morphological evolution and whether there are common patterns in how selection varies 552 across GRNs. We are well-positioned with molecular techniques available today to 553 address these network-related gene evolution guestions. As GRNs are the bridge between genotype and phenotype, the better we can understand regulatory networks, 554 555 the better we can understand the mechanisms of adaptation. 556 Acknowledgments 557 558 The authors would like to thank Omid Saleh Ziabari, Sonia Messar, and members of the 559 Reed lab for helpful comments and discussion. We are also grateful to Adam Wilkins 560 561 and one anonymous reviewer for their thoughtful feedback. This work was supported by NSF GRFP DGE-1650441 to JMCM and NSF grant IOS-2128164 to RDR. 562 563 References 564 565 A.S. Wilkins, Between "design" and "bricolage": Genetic networks, levels of 566 [1] selection, and adaptive evolution, Proc. Natl. Acad. Sci. U. S. A. 104 (2007) 8590-8596. 567

- E. Sucena, I. Delon, I. Jones, F. Payre, D.L. Stern, Regulatory evolution of
 shavenbaby/ovo underlies multiple cases of morphological parallelism, Nature. 424
 (2003) 935–938.
- 571 [3] M.D. Shapiro, M.A. Bell, D.M. Kingsley, Parallel genetic origins of pelvic
- ⁵⁷² reduction in vertebrates, Proc. Natl. Acad. Sci. U. S. A. 103 (2006) 13753–13758.
- 573 [4] R.D. Reed, R. Papa, A. Martin, H.M. Hines, B.A. Counterman, C. Pardo-Diaz,
- 574 C.D. Jiggins, N.L. Chamberlain, M.R. Kronforst, R. Chen, G. Halder, H.F. Nijhout, W.O.
- 575 McMillan, optix drives the repeated convergent evolution of butterfly wing pattern
- 576 mimicry, Science. 333 (2011) 1137–1141.
- 577 [5] E.H. Davidson, D.H. Erwin, Gene regulatory networks and the evolution of animal 578 body plans, Science. 311 (2006) 796–800.
- 579 [6] D.L. Stern, V. Orgogozo, Is Genetic Evolution Predictable?, Science. 323 (2009)
 580 746–751. https://doi.org/10.1126/science.1158997.
- 581 [7] D.L. Stern, The genetic causes of convergent evolution, Nat. Rev. Genet. 14
 582 (2013) 751–764.
- 583 [8] E.H. Davidson, I. Peter, Genomic Control Process, Academic Press, 2015.
- 584 [9] R.D.H. Barrett, D. Schluter, Adaptation from standing genetic variation, Trends
- 585 Ecol. Evol. 23 (2008) 38–44.
- 586 [10] H. Kitano, Biological robustness, Nat. Rev. Genet. 5 (2004) 826–837.
- 587 [11] S. Cussat-Blanc, K. Harrington, W. Banzhaf, Artificial gene regulatory networks-A
- 588 review, Artif. Life. 24 (2018) 296–328.
- 589 [12] B. Lehne, T. Schlitt, Protein-protein interaction databases: keeping up with
- 590 growing interactomes, Hum. Genomics. 3 (2009) 291–297.

- 591 [13] P.M. Kim, J.O. Korbel, M.B. Gerstein, Positive selection at the protein network
- 592 periphery: evaluation in terms of structural constraints and cellular context, Proc. Natl.
- 593 Acad. Sci. U. S. A. 104 (2007) 20274–20279.
- 594 [14] H.B. Fraser, A.E. Hirsh, L.M. Steinmetz, C. Scharfe, M.W. Feldman, Evolutionary
- rate in the protein interaction network, Science. 296 (2002) 750–752.
- 596 [15] I.S. Peter, E.H. Davidson, The endoderm gene regulatory network in sea urchin
 597 embryos up to mid-blastula stage, Dev. Biol. 340 (2010) 188–199.
- 598 [16] E.B. Josephs, S.I. Wright, J.R. Stinchcombe, D.J. Schoen, The Relationship
- 599 between Selection, Network Connectivity, and Regulatory Variation within a Population
- of Capsella grandiflora, Genome Biol. Evol. 9 (2017) 1099–1109.
- 601 [17] K. Voordeckers, K. Pougach, K.J. Verstrepen, How do regulatory networks
- evolve and expand throughout evolution?, Curr. Opin. Biotechnol. 34 (2015) 180–188.
- 603 [18] C. Feschotte, Transposable elements and the evolution of regulatory networks,
- 604 Nat. Rev. Genet. 9 (2008) 397–405.
- 605 [19] E. McQueen, M. Rebeiz, On the specificity of gene regulatory networks: How
- does network co-option affect subsequent evolution?, Curr. Top. Dev. Biol. 139 (2020)375–405.
- 608 [20] D.L. Stern, V. Orgogozo, The loci of evolution: how predictable is genetic
 609 evolution?, Evolution. 62 (2008) 2155–2177.
- 610 [21] A.P. McGregor, V. Orgogozo, I. Delon, J. Zanet, D.G. Srinivasan, F. Payre, D.L.
- 611 Stern, Morphological evolution through multiple cis-regulatory mutations at a single
- 612 gene, Nature. 448 (2007) 587–590.
- 613 [22] R. Albert, Scale-free networks in cell biology, J. Cell Sci. 118 (2005) 4947–4957.

- 614 [23] W.Z. Ouma, K. Pogacar, E. Grotewold, Topological and statistical analyses of
- 615 gene regulatory networks reveal unifying yet quantitatively different emergent
- 616 properties, PLoS Comput. Biol. 14 (2018) e1006098.
- 617 [24] A.D. Broido, A. Clauset, Scale-free networks are rare, Nat. Commun. 10 (2019)618 1017.
- 619 [25] S. Maslov, K. Sneppen, Specificity and stability in topology of protein networks,
 620 Science. 296 (2002) 910–913.
- 621 [26] R. Albert, H. Jeong, A.L. Barabasi, Error and attack tolerance of complex
- 622 networks, Nature. 406 (2000) 378–382.
- 623 [27] R. Maddamsetti, Selection maintains protein interactome resilience in the long-
- term evolution experiment with Escherichia coli, Genome Biol. Evol. (2021).
- 625 https://doi.org/10.1093/gbe/evab074.
- 626 [28] T. Friedlander, A.E. Mayo, T. Tlusty, U. Alon, Evolution of bow-tie architectures in
- 627 biology, PLoS Comput. Biol. 11 (2015) e1004055.
- [29] N. Irie, S. Kuratani, The developmental hourglass model: a predictor of the basic
- 629 body plan?, Development. 141 (2014) 4649–4655.
- 630 [30] N. Frankel, D.F. Erezyilmaz, A.P. McGregor, S. Wang, F. Payre, D.L. Stern,
- 631 Morphological evolution caused by many subtle-effect substitutions in regulatory DNA,
- 632 Nature. 474 (2011) 598–603.
- [31] L. Zhang, A. Mazo-Vargas, R.D. Reed, Single master regulatory gene
- 634 coordinates the evolution and development of butterfly color and iridescence, Proc. Natl.
- 635 Acad. Sci. U. S. A. 114 (2017) 10707–10712.

- [32] H.M. Hines, R. Papa, M. Ruiz, A. Papanicolaou, C. Wang, H.F. Nijhout, W.O.
- McMillan, R.D. Reed, Transcriptome analysis reveals novel patterning and pigmentation
 genes underlying Heliconius butterfly wing pattern variation, BMC Genomics. 13 (2012)
 288.
- 640 [33] J.J. Hanly, R.W.R. Wallbank, W.O. McMillan, C.D. Jiggins, Conservation and
- flexibility in the gene regulatory landscape of heliconiine butterfly wings, Evodevo. 10(2019) 15.
- [34] J.J. Lewis, S.M. Van Belleghem, R. Papa, C.G. Danko, R.D. Reed, Many
- 644 functionally connected loci foster adaptive diversification along a neotropical hybrid
- c45 zone, Sci Adv. 6 (2020). https://doi.org/10.1126/sciadv.abb8617.
- [35] J.J. Lewis, R.C. Geltman, P.C. Pollak, K.E. Rondem, S.M. Van Belleghem, M.J.
- Hubisz, P.R. Munn, L. Zhang, C. Benson, A. Mazo-Vargas, C.G. Danko, B.A.
- 648 Counterman, R. Papa, R.D. Reed, Parallel evolution of ancient, pleiotropic enhancers
- underlies butterfly wing pattern mimicry, Proc. Natl. Acad. Sci. U. S. A. 116 (2019)
- 650 24174–24183.
- [36] M. Moest, S.M. Van Belleghem, J.E. James, C. Salazar, S.H. Martin, S.L. Barker,
- 652 G.R.P. Moreira, C. Mérot, M. Joron, N.J. Nadeau, F.M. Steiner, C.D. Jiggins, Selective
- sweeps on novel and introgressed variation shape mimicry loci in a butterfly adaptive
- 654 radiation, PLoS Biol. 18 (2020) e3000597.
- 655 [37] C. Salles, M. Mével-Ninio, A. Vincent, F. Payre, A germline-specific splicing
- 656 generates an extended ovo protein isoform required for Drosophila oogenesis, Dev.
- 657 Biol. 246 (2002) 366–376.

[38] M. Seimiya, W.J. Gehring, The Drosophila homeobox gene optix is capable of
inducing ectopic eyes by an eyeless-independent mechanism, Development. 127
(2000) 1879–1886.

[39] D.M. Krylov, Y.I. Wolf, I.B. Rogozin, E.V. Koonin, Gene loss, protein sequence
divergence, gene dispensability, expression level, and interactivity are correlated in
eukaryotic evolution, Genome Res. 13 (2003) 2229–2235.

association between pleiotropy and transcription factor evolution, Genome Biol. Evol. 8
(2016) 3159–3170.

K.N. Chesmore, J. Bartlett, C. Cheng, S.M. Williams, Complex patterns of

667 [41] D. Molodtsova, B.A. Harpur, C.F. Kent, K. Seevananthan, A. Zayed, Pleiotropy

668 constrains the evolution of protein but not regulatory sequences in a transcription

regulatory network influencing complex social behaviors, Front. Genet. 5 (2014) 431.

670 [42] G. Sabarís, I. Laiker, E. Preger-Ben Noon, N. Frankel, Actors with Multiple Roles:

671 Pleiotropic Enhancers and the Paradigm of Enhancer Modularity, Trends Genet. 35

672 (2019) 423–433.

664

[40]

673 [43] G.A. Jindal, E.K. Farley, Enhancer grammar in development, evolution, and 674 disease: dependencies and interplay, Dev. Cell. 56 (2021) 575–587.

675 [44] B. Lim, M.S. Levine, Enhancer-promoter communication: hubs or loops?, Curr.
676 Opin. Genet. Dev. 67 (2021) 5–9.

677 [45] S. Ciliberti, O.C. Martin, A. Wagner, Innovation and robustness in complex

⁶⁷⁸ regulatory gene networks, Proc. Natl. Acad. Sci. U. S. A. 104 (2007) 13591–13596.

[46] C.K. Ewe, Y.N. Torres Cleuren, J.H. Rothman, Evolution and developmental
system drift in the endoderm gene regulatory network of Caenorhabditis and other
nematodes, Front. Cell Dev. Biol. 8 (2020) 170.

[47] M. Nahmad, L. Glass, E. Abouheif, The dynamics of developmental system drift
in the gene network underlying wing polyphenism in ants: a mathematical model, Evol.
Dev. 10 (2008) 360–374.

- 685 [48] A. Wagner, Does evolutionary plasticity evolve?, Evolution. 50 (1996) 1008.
- 686 [49] M.-A. Félix, A. Wagner, Robustness and evolution: concepts, insights and
- challenges from a developmental model system, Heredity (Edinb.). 100 (2008) 132-
- 688 140.
- [50] K.E. Sears, J.A. Maier, M. Rivas-Astroza, R. Poe, S. Zhong, K. Kosog, J.D.
- 690 Marcot, R.R. Behringer, C.J. Cretekos, J.J. Rasweiler 4th, Z. Rapti, The relationship
- 691 between gene network structure and expression variation among individuals and
- 692 species, PLoS Genet. 11 (2015) e1005398.
- [51] J.H. Massey, P.J. Wittkopp, The Genetic Basis of Pigmentation Differences
- 694 Within and Between Drosophila Species, Genes and Evolution. (2016) 27–61.
- 695 https://doi.org/10.1016/bs.ctdb.2016.03.004.
- 696 [52] J.E. Pool, C.F. Aquadro, The genetic basis of adaptive pigmentation variation in
- Drosophila melanogaster, Molecular Ecology. 16 (2007) 2844–2851.
- 698 https://doi.org/10.1111/j.1365-294x.2007.03324.x.
- [53] S. Jeong, M. Rebeiz, P. Andolfatto, T. Werner, J. True, S.B. Carroll, The
- volution of gene regulation underlies a morphological difference between two
- 701 Drosophila sister species, Cell. 132 (2008) 783–793.

- 702 [54] L.M. Dembeck, W. Huang, M.M. Magwire, F. Lawrence, R.F. Lyman, T.F.C.
- 703 Mackay, Genetic Architecture of Abdominal Pigmentation in Drosophila melanogaster,
- 704 PLoS Genet. 11 (2015) e1005163.
- 705 [55] M. Rebeiz, N.H. Patel, V.F. Hinman, Unraveling the tangled skein: The evolution
- of transcriptional regulatory networks in development, Annu. Rev. Genomics Hum.
- 707 Genet. 16 (2015) 103–131.
- 708 [56] A.C. Thompson, T.D. Capellini, C.A. Guenther, Y.F. Chan, C.R. Infante, D.B.
- Menke, D.M. Kingsley, A novel enhancer near the Pitx1 gene influences development
- and evolution of pelvic appendages in vertebrates, Elife. 7 (2018).
- 711 https://doi.org/10.7554/eLife.38555.
- 712 [57] W.J. Glassford, W.C. Johnson, N.R. Dall, S.J. Smith, Y. Liu, W. Boll, M. Noll, M.
- 713 Rebeiz, Co-option of an Ancestral Hox-Regulated Network Underlies a Recently
- Evolved Morphological Novelty, Developmental Cell. 34 (2015) 520–531.
- 715 https://doi.org/10.1016/j.devcel.2015.08.005.
- 716 [58] E.L. Westerman, N.W. VanKuren, D. Massardo, A. Tenger-Trolander, W. Zhang,
- R.I. Hill, M. Perry, E. Bayala, K. Barr, N. Chamberlain, T.E. Douglas, N. Buerkle, S.E.
- 718 Palmer, M.R. Kronforst, Aristaless Controls Butterfly Wing Color Variation Used in
- 719 Mimicry and Mate Choice, Curr. Biol. 28 (2018) 3469-3474.e4.
- 720 [59] K. Tunström, A. Woronik, J.J. Hanly, P. Rastas, A. Chichvarkhin, A.D. Warren, A.
- Kawahara, S.D. Schoville, V. Ficarrotta, A.H. Porter, W.B. Watt, A. Martin, C.W. Wheat,
- A complex interplay between balancing selection and introgression maintains a genus-
- wide alternative life history strategy, BioRxiv. (2021) 2021.05.20.445023.
- 724 https://doi.org/10.1101/2021.05.20.445023.

- M.W. Nachman, H.E. Hoekstra, S.L. D'Agostino, The genetic basis of adaptive
 melanism in pocket mice, Proc. Natl. Acad. Sci. U. S. A. 100 (2003) 5268–5273.
- 727 [61] J.A.C. Uy, E.A. Cooper, S. Cutie, M.R. Concannon, J.W. Poelstra, R.G. Moyle,
- 728 C.E. Filardi, Mutations in different pigmentation genes are associated with parallel
- melanism in island flycatchers, Proc. Biol. Sci. 283 (2016).
- 730 https://doi.org/10.1098/rspb.2016.0731.
- 731 [62] H.R. McRobie, N.D. Moncrief, N.I. Mundy, Multiple origins of melanism in two
- species of North American tree squirrel (Sciurus), BMC Evol. Biol. 19 (2019) 140.
- [63] K. Julenius, A.G. Pedersen, Protein evolution is faster outside the cell, Mol. Biol.
- 734 Evol. 23 (2006) 2039–2048.
- [64] A.M. Cheatle Jarvela, V.F. Hinman, Evolution of transcription factor function as a
 mechanism for changing metazoan developmental gene regulatory networks, Evodevo.
 6 (2015) 3.
- [65] H. Innan, F. Kondrashov, The evolution of gene duplications: classifying and
 distinguishing between models, Nat. Rev. Genet. 11 (2010) 97–108.
- 740 [66] B.M. Spiegelman, R. Heinrich, Biological control through regulated transcriptional
 741 coactivators, Cell. 119 (2004) 157–167.
- [67] K.J. Brayer, V.J. Lynch, G.P. Wagner, Evolution of a derived protein–protein
- interaction between HoxA11 and Foxo1a in mammals caused by changes in
- intramolecular regulation, Proc. Natl. Acad. Sci. U. S. A. 108 (2011) E414–E420.
- 745 [68] F. Galis, T.J.M. van Dooren, J.A.J. Metz, Conservation of the segmented
- germband stage: robustness or pleiotropy?, Trends Genet. 18 (2002) 504–509.

- 747 [69] C.W. Ahrens, P.D. Rymer, A. Stow, J. Bragg, S. Dillon, K.D.L. Umbers, R.Y.
- Dudaniec, The search for loci under selection: trends, biases and progress, Mol. Ecol.
 27 (2018) 1342–1356.
- [70] R. De Smet, K. Marchal, Advantages and limitations of current network inference
 methods, Nat. Rev. Microbiol. 8 (2010) 717–729.
- 752 [71] A. Barski, K. Zhao, Genomic location analysis by ChIP-Seq, J. Cell. Biochem.
 753 107 (2009) 11–18.
- 754 [72] S. Jiang, A. Mortazavi, Integrating ChIP-seq with other functional genomics data,
- 755 Brief. Funct. Genomics. 17 (2018) 104–115.
- 756 [73] C. Angelini, V. Costa, Understanding gene regulatory mechanisms by integrating
- 757 ChIP-seq and RNA-seq data: statistical solutions to biological problems, Front. Cell
 758 Dev. Biol. 2 (2014) 51.
- 759 [74] H. Nguyen, D. Tran, B. Tran, B. Pehlivan, T. Nguyen, A comprehensive survey of
- regulatory network inference methods using single cell RNA sequencing data, Brief.
- 761 Bioinform. 22 (2021). https://doi.org/10.1093/bib/bbaa190.
- 762 [75] K. Glass, C. Huttenhower, J. Quackenbush, G.-C. Yuan, Passing messages
- between biological networks to refine predicted interactions, PLoS One. 8 (2013)
- 764 e64832.
- 765 [76] S. Aibar, C.B. González-Blas, T. Moerman, V.A. Huynh-Thu, H. Imrichova, G.
- Hulselmans, F. Rambow, J.-C. Marine, P. Geurts, J. Aerts, J. van den Oord, Z.K. Atak,
- J. Wouters, S. Aerts, SCENIC: single-cell regulatory network inference and clustering,
- 768 Nat. Methods. 14 (2017) 1083–1086.

- 769 [77] A.F. Gilles, M. Averof, Functional genetics for all: engineered nucleases,
- 770 CRISPR and the gene editing revolution, Evodevo. 5 (2014) 43.
- 771 [78] M.L. Martik, S. Gandhi, B.R. Uy, J.A. Gillis, S.A. Green, M. Simoes-Costa, M.E.
- Bronner, Evolution of the new head by gradual acquisition of neural crest regulatory
- circuits, Nature. 574 (2019) 675–678.
- [79] G.A. Cary, B.S. McCauley, O. Zueva, J. Pattinato, W. Longabaugh, V.F. Hinman,
- 775 Systematic comparison of sea urchin and sea star developmental gene regulatory
- networks explains how novelty is incorporated in early development, Nat. Commun. 11
- 777 (2020) 6235.
- 778 [80] T.R. Booker, B.C. Jackson, P.D. Keightley, Detecting positive selection in the
- genome, BMC Biology. 15 (2017). https://doi.org/10.1186/s12915-017-0434-y.
- 780 [81] P. Pavlidis, N. Alachiotis, A survey of methods and tools to detect recent and
- strong positive selection, J. Biol. Res. . 24 (2017) 7.
- 782 [82] M. Fagny, F. Austerlitz, Polygenic adaptation: Integrating population genetics and
- gene regulatory networks, Trends Genet. 37 (2021) 631–638.
- [83] M.E. Mathyer, E.A. Brettmann, A.D. Schmidt, Z.A. Goodwin, I.Y. Oh, A.M.
- 785 Quiggle, E. Tycksen, N. Ramakrishnan, S.J. Matkovich, E. Guttman-Yassky, J.R.
- Edwards, C. de Guzman Strong, Selective sweep for an enhancer involucrin allele
- identifies skin barrier adaptation out of Africa, Nat. Commun. 12 (2021).
- 788 https://doi.org/10.1038/s41467-021-22821-w.
- 789 [84] A. Berrio, R. Haygood, G.A. Wray, Identifying branch-specific positive selection
- throughout the regulatory genome using an appropriate proxy neutral, BMC Genomics.
- 791 21 (2020) 359.

- 792 [85] E.S. Wong, D. Zheng, S.Z. Tan, N.L. Bower, V. Garside, G. Vanwalleghem, F.
- Gaiti, E. Scott, B.M. Hogan, K. Kikuchi, E. McGlinn, M. Francois, B.M. Degnan, Deep
- conservation of the enhancer regulatory code in animals, Science. 370 (2020)
- 795 eaax8137.
- 796 [86] E.A. Boyle, Y.I. Li, J.K. Pritchard, An expanded view of complex traits: From
- 797 polygenic to omnigenic, Cell. 169 (2017) 1177–1186.
- 798 [87] S. Kittelmann, A.D. Buffry, F.A. Franke, I. Almudi, M. Yoth, G. Sabaris, J.P.
- 799 Couso, M.D.S. Nunes, N. Frankel, J.L. Gómez-Skarmeta, J. Pueyo-Marques, S. Arif,
- A.P. McGregor, Gene regulatory network architecture in different developmental
- 801 contexts influences the genetic basis of morphological evolution, PLoS Genet. 14
- 802 (2018) e1007375.
- 803 [88] H.A. Orr, The population genetics of adaptation: The distribution of factors fixed
 804 during adaptive evolution, Evolution. 52 (1998) 935.
- 805 [89] M.V. Rockman, The QTN program and the alleles that matter for evolution: all 806 that's gold does not glitter, Evolution. 66 (2012) 1–17.
- 807 [90] D.L. Stern, Evolution, development, and the predictable genome, Roberts &
- 808 Company, Greenwood Village, CO, 2010.
- 809
- 810



812

813 Figure 1: The bow-tie GRN consists of an input-output gene that is functionally connected to

814 many genes upstream and downstream. The upstream and downstream genes can also be

815 connected to other genes but not to nearly as many. Some developmental GRNs may fit the null

816 hierarchal model, where there is little appreciable difference in connectivity between genes in the

817 network.



820 Figure 2: Levels of the optix GRN regulating wing color pattern in Heliconius butterflies. The 821 GRN for wing color pattern is modeled as a bow-tie structure, with optix acting as the input-output 822 gene. optix is likely directly regulated by many upstream genes (inputs) and is known to directly 823 target many downstream genes (outputs). Direct targets of optix include (a) intermediate factors that 824 initiate downstream cascades that can be turned on or off, such as *dome/wash* as well as (b) 825 directly-targeted terminal effectors, such as the pigmentation enzyme ebony. The optix network 826 contains more regulatory relationships than shown here, and the number of inputs and outputs 827 involved in this GRN is likely much higher than illustrated [34,35].



