

1 **MASTHING: a process-based model of mast seeding in European beech**

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14 **Summary**

15 Masting, the synchronised interannual variation in seed production, shapes forest regeneration and
16 many ecosystem processes, yet process-based models remain underdeveloped. Here we introduce
17 MASTHING (MASting THEory modellING), an individual-tree model coupling phenology, carbon
18 gain, resource storage, temperature cues, and environmental vetoes on reproduction. We
19 parameterised MASTHING for European beech (*Fagus sylvatica* L.) using 43 years of data from 100
20 trees across 11 sites in England to test alternative hypotheses about masting mechanisms. Three
21 formulations were compared: resource budget only (RB), and extensions with additive (RB+WC) and
22 interactive (RB×WC) temperature cue effects. Performance improved with complexity and was
23 highest when cue sensitivity depended on internal resource status. At the site-year scale, explained
24 variance increased from $R^2 = 0.58$ (RB) to $R^2 = 0.76$ (RB×WC), supporting that favourable cues
25 trigger strong reproduction only when sufficient resources have accumulated. The model reproduced
26 mast and failure years, partly captured long-term breakdown in masting intensity under climate
27 warming, and broadly predicted seed production during 2023-2025, although low-seed years were
28 less well predicted. Modelled resource and cue dynamics were sufficient to simulate short-term
29 variation and progressive weakening of reproductive pulses. MASTHING provides a platform for
30 testing masting hypotheses, evaluating climate change impacts, and supporting operational seed
31 forecasting.

32 **Keywords:** climate change, masting, fecundity, forest resilience, tree demography

33

34 **1. Introduction**

35 Masting, the synchronized interannual variability in seed production among individuals within a
36 population, is a common reproductive strategy in long-lived plants (Kelly & Sork, 2002; Journé *et*

37 *al.*, 2023). This variable reproduction enhances reproductive efficiency by reducing seed predation
38 and improving pollination success (Kelly *et al.*, 2001; Rapp *et al.*, 2013; Zwolak *et al.*, 2022). The
39 resulting boom-and-bust dynamics in seed supply have far-reaching implications for food webs,
40 nutrient cycling, and the dynamics of plant and fungal communities, as well as for forest ecosystems
41 and game management (Ostfeld & Keesing, 2000; Bisi *et al.*, 2018 Clark *et al.*, 2019; Pearse *et al.*,
42 2021; Tattoni *et al.*, 2025). Understanding the mechanisms underlying masting is therefore essential
43 for predicting changes in plant populations and ecosystem functioning (Hackett-Pain & Bogdziewicz,
44 2021) and for providing short-term forecasts of seed production to support decision-making (Elliott &
45 Kemp, 2016; Journé *et al.*, 2023). These needs are becoming particularly urgent as climate change
46 alters masting patterns, with large consequences for seed availability (Bogdziewicz *et al.*, 2023;
47 Jantzen *et al.*, 2026). At the same time, demand for reliable short-term forecasting is increasing as
48 seed supply for ecological restoration becomes a policy priority (Pearse *et al.*, 2021; Journé *et al.*,
49 2023; Oberklammer *et al.*, 2026). For example, the European Union’s Biodiversity Strategy for 2030
50 and the proposed EU Nature Restoration Law emphasise large-scale ecosystem restoration, which
51 requires a dependable supply of seeds. Accurate forecasting is therefore essential to ensure adequate
52 seed availability for restoration projects.

53 Building on this growing interest, recent decades have brought significant progress in
54 understanding the processes driving interannual variation and synchrony in seed production (Crone &
55 Rapp, 2014; Pearse *et al.*, 2016; Bogdziewicz *et al.*, 2024; Satake & Journé, 2026). These advances
56 open the way to models capable of reproducing masting dynamics, enabling near-term forecasting and
57 assessing climate change impacts on plant reproduction. However, most existing approaches remain
58 primarily statistical (Journé *et al.*, 2023; Wion *et al.*, 2025; Hirsch *et al.*, 2025; Oberklammer *et al.*,
59 2026). Process-based models offer a valuable alternative, as they explicitly represent underlying
60 biophysical mechanisms rather than relying on empirical relationships (Asse *et al.*, 2020; Mäkelä *et*
61 *al.*, 2000). This mechanistic foundation can improve predictive skill, especially under changing
62 environmental conditions, making such models powerful tools for ecological forecasting and
63 management (Briscoe *et al.*, 2022). Moreover, because masting operates over multiple years and is
64 difficult to manipulate experimentally (Bogdziewicz *et al.*, 2020a), process-based models provide a
65 means to test hypotheses and simulate scenarios that are otherwise impractical in field studies (Végh
66 & Kato, 2024).

67 Various models have been developed to explain masting, including those based on resource
68 budgets, weather cues, and resource-limited floral induction (Isagi *et al.*, 1997; Kelly *et al.*, 2013;
69 Monks *et al.*, 2016; Pearse *et al.*, 2016). Rather than acting independently, the General Model of
70 Masting (Bogdziewicz *et al.*, 2024) suggests that these mechanisms jointly regulate the transition to

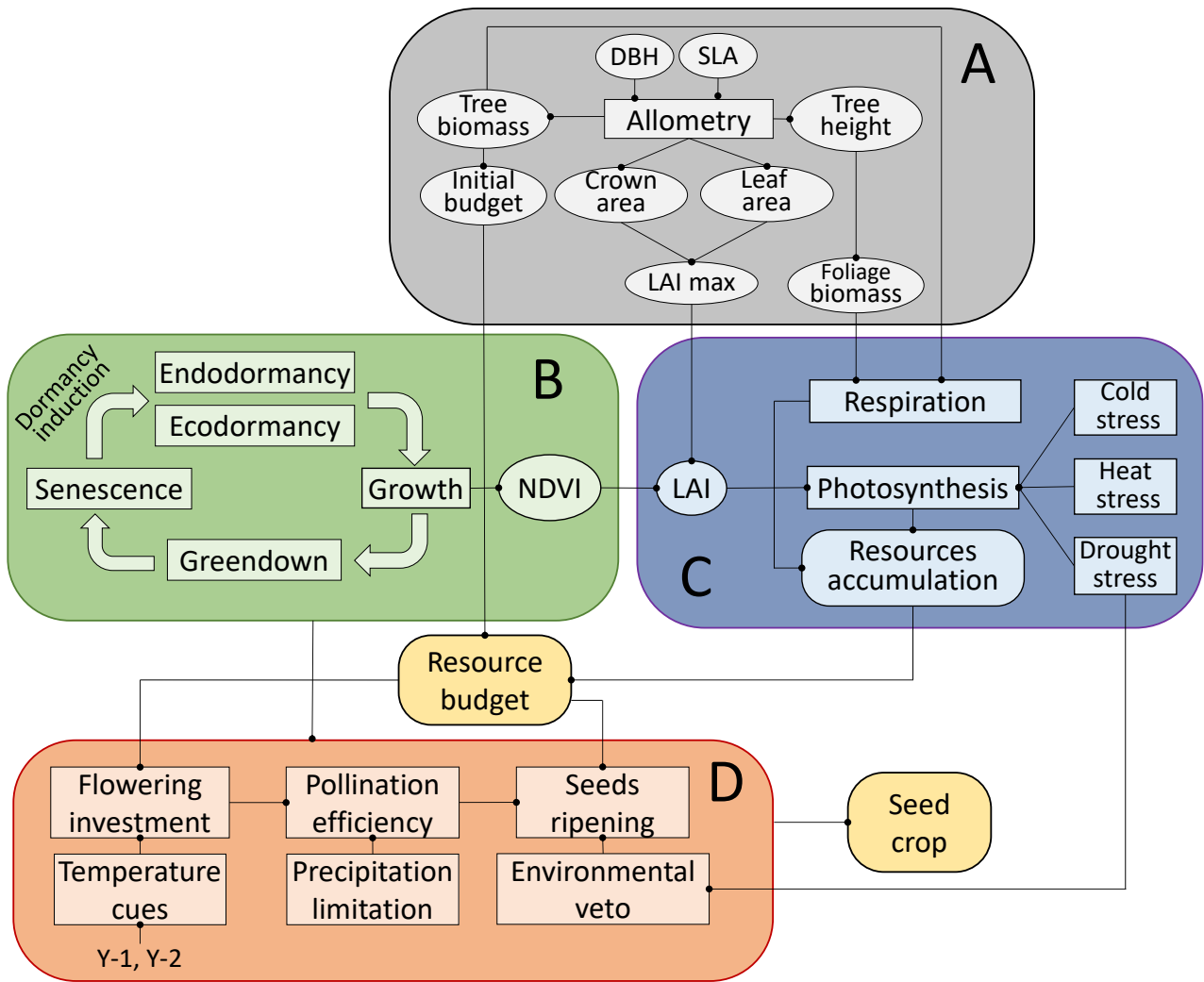
71 flowering to fruiting, with their relative importance varying across species. Resource budget models
72 propose that plants must accumulate sufficient resources before reproduction, often over multiple
73 years (Isagi *et al.*, 1997; Crone & Rapp, 2014), and experimental flower removal confirms that
74 reproduction depletes resources and limits subsequent flowering (Sala *et al.*, 2012; Ronc e *et al.*,
75 2023). In parallel, weather cue models suggest that plants evolved hypersensitivity to environmental
76 variability, triggering large seed crops under favourable conditions such as specific temperature
77 regimes (Janzen, 1971; Kelly *et al.*, 2013; Fern andez-Mart inez *et al.*, 2017; Yeoh *et al.*, 2017;
78 Bogdziewicz *et al.*, 2020b). Resource-limited floral induction links these mechanisms by proposing
79 that responses to weather cues depend on internal resource status (Monks *et al.*, 2016; Kelly *et al.*,
80 2025). For example, in *Nothofagus solandri*, nitrogen fertilization removed resource limitation,
81 resulting in a positive relationship between temperature during flower formation and seed production
82 that was absent in non-fertilized control stands (Smaill *et al.*, 2011). Together, these advances
83 provide a solid conceptual basis for process-based models of masting. However, such models remain
84 rare (Vacchiano *et al.*, 2018), and recent developments still require evaluation under changing climatic
85 conditions (V egh & Kato, 2024).

86 Here, we present MASTHING (MASting Theory modellING), a dynamic simulation model that
87 represents key processes underlying plant reproduction. The model proposes a resource budget
88 framework coupled to plant phenology, where carbon gained through photosynthesis is allocated to
89 reproduction as a function of internal resource status and environmental cues. We parameterised
90 MASTHING for European beech (*Fagus sylvatica*) using 43 years of seed production data (1980–
91 2022) from 100 trees across 11 sites in England (Packham *et al.*, 2008a; Bogdziewicz *et al.*, 2020c),
92 and evaluated its forecasting skill for 2023-2025. Using this framework, we tested whether the
93 proximate mechanisms hypothesised to drive masting in beech can reproduce observed reproductive
94 dynamics. We further investigated whether the model can reproduce the recent breakdown of
95 masting patterns linked to climate warming, characterised by reduced interannual variability and
96 synchrony in seed production (Bogdziewicz *et al.*, 2020c; 2023). This decline has been attributed to
97 more frequent temperature cues, which shorten resource recovery intervals and dampen reproductive
98 responses (Bogdziewicz *et al.*, 2021; Hackett-Pain *et al.*, 2025; Kelly *et al.*, 2025). MASTHING
99 provides a tool to evaluate this hypothesis under changing environmental conditions.

100 **2. Description**

101 **2.1. Model overview**

102 MASTHING is a process-based simulation model of individual tree reproductive cycles, derived
103 from the resource-budget theory of Isagi *et al.* (1997) and extended into a process-based framework
104 (Figure 1).



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Figure 1. Conceptual diagram of the MASTHING model showing interlinked modules and simulated processes. (A) variables associated with the tree allometry module; (B) phenological processes; (C) processes related to resource accumulation; (D) reproductive allocation. Lines and nodes connections indicate relationships among variables and modules.

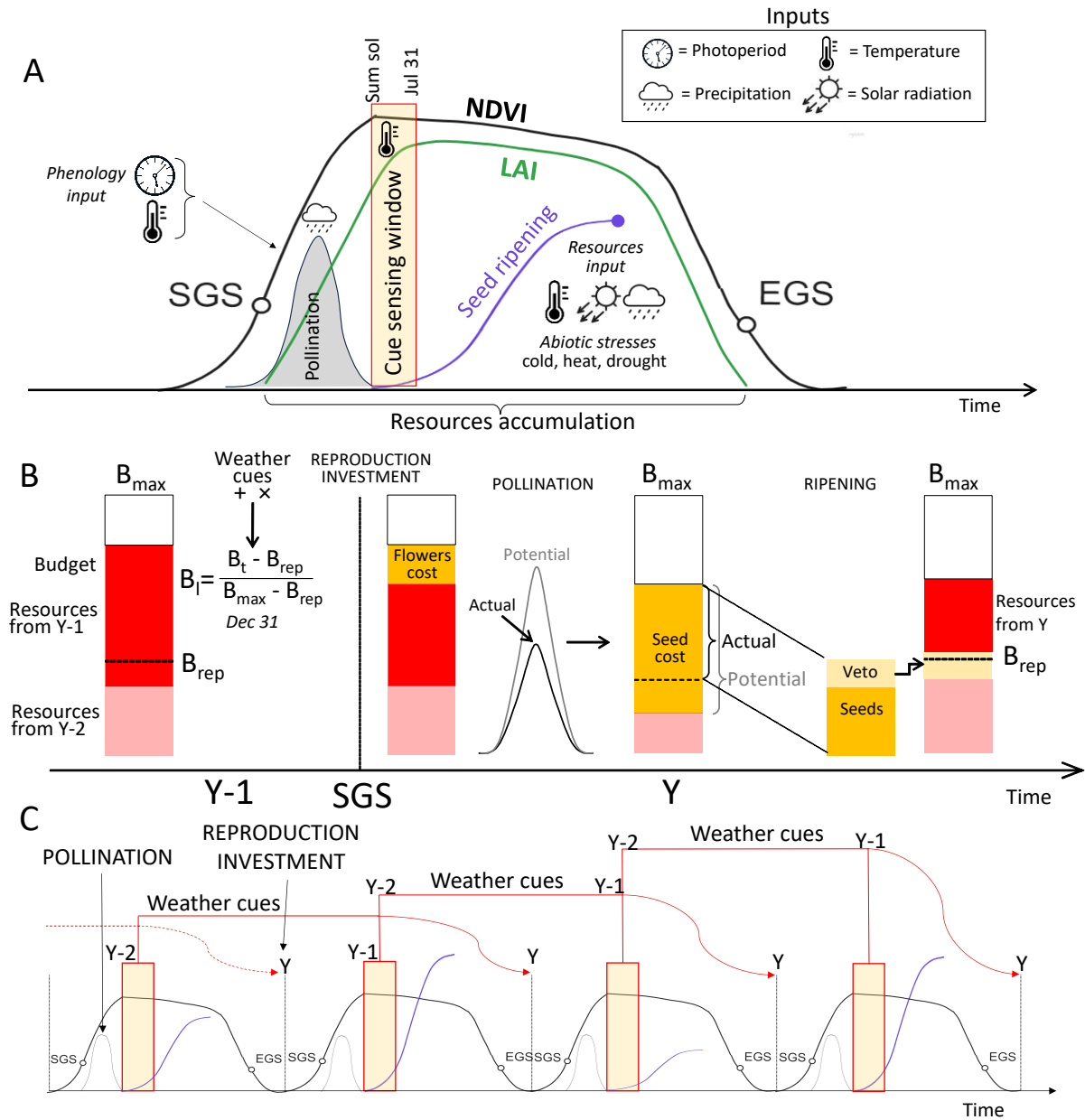
The model integrates four coupled modules, i.e., tree allometry, phenology, carbon balance, and reproductive allocation (Figure 1). It initializes an individual European beech tree from allometric relationships based on diameter at breast height (DBH, measured at 1.3 m), used to estimate crown area, tree height, and biomass partitioning among plant compartments (Figure 1A; Bartelink, 1997; Zianis & Mencuccini, 2004). Foliage biomass is converted into leaf area index using specific leaf area (SLA, $\text{m}^{-2} \text{kg}$) scaled to crown projection area, yielding maximum leaf area index (LAI_{max} , Figure 1A). Phenological dynamics are simulated using the SWELL model (Bajocco *et al.*, 2025), which describes the transition from dormancy to the growing season and the progression of key phenophases (Figure 1B). The resulting simulated Normalised Difference Vegetation Index (NDVI) is scaled over the growing season (bud burst – leaf fall) and used to derive daily leaf area index (LAI) by proportional scaling to LAI_{max} (Bregaglio *et al.*, 2023). Carbon

122 assimilation is computed using a light-use efficiency framework (Figure 1C; Monteith, 1972;
123 Medlyn, 1998). Gross primary production is driven by incoming radiation and downregulated by
124 temperature and water stress functions (Maselli *et al.*, 2020; Zhao *et al.*, 2019), while maintenance
125 respiration of woody and foliage tissues is represented using a temperature-dependent Q_{10}
126 formulation (Lin *et al.*, 2012). The daily net carbon balance updates the internal resource budget,
127 which represents the central state variable governing reproduction (Figure 1C). The resource budget
128 accumulates carbon over successive seasons and is evaluated at the end of each year, when it is
129 normalised between a baseline reproduction level (B_{rep} , g C m⁻²) and a maximum storage capacity
130 (B_{max} , g C m⁻²) to determine a normalised budget level (BL_t , $\in [0, 1]$). Reproductive allocation
131 (Figure 1D) links the internal resource budget to seed production through flowering investment,
132 pollination, and seed maturation, all potentially modulated by environmental conditions. A full
133 mathematical description of all model components is given in Supplementary Information S1.

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135 **2.1.1. Reproductive allocation, temperature cues and environmental filtering**

136 Reproductive investment is allocated sequentially to flowering and seed production (Figure
137 2). Flowering represents the initial reproductive cost, subtracted from the internal resource budget,
138 while the subsequent conversion of flowers into seeds depends on pollination success.
139 Environmental conditions can modulate reproductive outcomes at different stages within the
140 growing season (Figure 2A). Precipitation during flowering may reduce pollination efficiency
141 (Sofiev *et al.*, 2013), whereas drought during seed development can limit seed filling, acting as an
142 environmental veto (Figure 2B; Bogdziewicz *et al.*, 2018). Under such conditions, part of the carbon
143 initially allocated to reproduction is not converted into seeds and is retained within the internal
144 resource pool (Figure 2B). This carry-over links successive years, as retained resources contribute
145 to future reproductive potential and interact with prior reproductive costs and lagged climatic
146 forcing (Section 2.1.1; Figure 2C).



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Figure 2. Overview of the MASTHING model across temporal scales. (A) Within-year dynamics linking phenology, canopy development (NDVI = black; LAI = green), environmental forcing, and reproductive timing; the yellow bar indicates the temperature cue sensing window, the grey bell-shaped curve flowering and pollination, and the purple curve seed development; (B) Conceptual representation of reproductive allocation and environmental filtering, where carbon allocated to flowers and seeds may be reduced by pollination failure or drought, with unused resources retained in the internal budget; (C) Multi-year schematic showing how temperature cues from the two preceding years (Y-1 and Y-2; orange bars) contribute to reproductive potential in year Y. Grey lines show flowering, the purple line seed development, and the black line NDVI;

Environmental regulation is introduced through temperature cues derived from conditions during a fixed summer window. Following empirical evidence (Journé *et al.*, 2024), maximum daily temperatures between June 21 and July 31 are aggregated to define an annual flowering cue. To account for lagged responses in masting systems, cue information from the two years preceding

162 seed production (i.e., Y-1 and Y-2) is retained, combining an activating component from year Y-1
163 and an inhibitory legacy effect from year Y-2. These components are transformed through sigmoidal
164 response functions and combined into a composite climatic signal (TC_t), scaled between 0 and 1
165 (Figure S2).

166 Reproductive allocation depends on both internal resource status and climatic forcing. In the
167 resource-budget-only formulation (RB), allocation is determined solely by the normalised resource
168 level (BL_t). In weather-cue formulations (RB+WC and RB×WC), temperature cues contribute
169 additively to reproductive potential, acting either independently of or interactively with resource
170 availability. In the interactive case (RB×WC), cue sensitivity is modulated by resource availability,
171 producing a resource-gated response. Reproductive investment is computed as a continuous
172 function of these drivers and constrained by the available resource budget:

$$173 \quad I_{rep} = \min \left(B_t, B_{max} \cdot \frac{BL_t + TC_t}{2} \right) \quad [1]$$

174 where I_{rep} ($g C m^{-2}$) is reproductive investment, B_t is the current resource budget ($g C m^{-2}$), and
175 B_{max} is the maximum storage capacity ($g C m^{-2}$). BL_t represents the normalised resource level, while
176 TC_t the composite temperature cue derived from lagged climatic signals.

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178 **2.1.2. Model assumptions and implementation**

179 MASTHING is implemented in C# as a class library coupled with a console application for
180 execution and parameter optimisation, with code available in an open-access repository (Bregaglio
181 et al., 2026; <https://github.com/GeoModelLab/MASTHING>, DOI: 10.5281/zenodo.19660460). In
182 its current implementation, the resource budget is allocated exclusively to reproduction carbon
183 allocation to other sinks such as growth is not explicitly represented, though the framework can be
184 extended to multiple carbon pools by partitioning the resource budget into parallel compartments.
185 While carbon is not the only resource potentially limiting reproduction, the resource budget used
186 here functions as a proxy for overall physiological readiness, integrating the net carbon balance
187 across the growing season; explicit representation of other nutrient cycles is beyond the current
188 scope (Kabeya, 2021; Végé & Kato, 2024).

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190 **2.2. Calibration and evaluation**

191 **2.2.1. Input data**

192 Model calibration and evaluation were performed using individual-level observations of
193 beech (*Fagus sylvatica* L.) seed production collected across 11 locations in the UK from 1980 to 2025
194 (Hackett-Pain et al., 2025; Supplementary Figure S3). Sites span a latitudinal gradient from Woodbury

195 in the southwest to Benwell in the northeast, covering a range of climatic and edaphic conditions
196 representative of the UK beech distribution. Each site included between 8 and 20 monitored trees
197 (after excluding individuals with fewer than 10 years of observations), with observation periods
198 ranging from 1980 to 2025 across sites (Figure S3). DBH was measured during field sampling, as
199 detailed in Packham *et al.* (2008b) and Bogdziewicz *et al.* (2023). Seed production data from 1980-
200 2022 were used for model calibration and hypothesis testing, while data from 2023–2025 were used
201 to evaluate prospective forecasting performance on out-of-sample years. To parameterise the
202 phenological component of MASTHING, vegetation dynamics were derived from remotely sensed
203 MODIS NDVI imagery at 250 m resolution (8-day maximum value composite; Holben, 1986) over
204 the period 2001-2022, processed using the MODISTools package (Hufkens, 2023). Daily
205 meteorological inputs, including air temperature (°C), precipitation (mm), and incoming radiation
206 ($\text{MJ m}^{-2} \text{d}^{-1}$), were obtained for each site from the ERA5 reanalysis dataset (Copernicus Climate
207 Change Service), accessed via Google Earth Engine.

208

209 **2.2.2. Simulation experiments**

210 A set of simulation experiments was designed to evaluate the relative role of resource
211 dynamics and climatic cues in controlling reproductive investment. Three model formulations were
212 compared: a resource-budget-only model (RB), and two extensions including temperature cues, with
213 additive (RB+WC) and interactive (RB×WC) effects on reproductive allocation (Section 2.1.1.).
214 These formulations represent alternative ecological hypotheses regarding the mechanism underlying
215 mast seeding, in particular the RB×WC formulation consider that sensitivity to climatic cues depends
216 on internal resource status (Kelly *et al.*, 2025). Comparing model performance across formulations
217 therefore constitutes a test of these hypotheses rather than a conventional model selection exercise.
218 Each formulation was evaluated under two contrasting parameterisation strategies. In the first,
219 parameters were calibrated independently for each site (site-specific parameterisation) providing an
220 estimate of maximum attainable model performance. In the second, a single parameter set was
221 estimated jointly across all sites (domain-wide parameterisation) to evaluate model generality across
222 environmental gradients. All simulations were performed at the individual tree level. Outputs were
223 aggregated to the site-year level by computing the mean normalised reproductive investment across
224 all trees within each site and year.

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226 **2.2.3. Calibration methodology**

227 Model parameters were derived from a combination of literature sources and data-driven
228 calibration. The majority of parameters were fixed a priori to values reported in the literature, while

229 a subset for which no reliable species-specific estimates exist was estimated through optimisation
230 (Supplementary Table S1.6). Calibration was performed in two sequential steps. In the first step, the
231 photothermal threshold governing the onset of growth, greendown and senescence phases were
232 optimised against MODIS NDVI time series as the target variable. Optimisation was carried out using
233 a multi-start downhill simplex algorithm minimising the root mean square error (RMSE) between
234 simulated and observed NDVI. To mitigate the risk of equifinality and parameter collinearity, 10
235 independent optimisation runs were performed, each comprising 10,000 iterations. Model
236 transferability was assessed through a spatial split-sample approach, in which study sites were
237 randomly partitioned into calibration (50%) and validation (50%) subsets. Phenological parameters
238 were then averaged across sites and held fixed in the second. In the second step controlling the
239 reproductive component, five parameters were then optimised (Table S1.6) using the full 1980–2022
240 observational record, with R^2 between simulated and observed interannual variability in seed
241 production as the objective function. Rather than partitioning the time series into calibration and
242 validation subsets, we used the complete historical record to maximise the ecological signal available
243 for parameter estimation and to ensure that performance differences among the three formulations
244 (RB, RB+WC, RB×WC) reflect mechanistic differences rather than dataset partitioning choices. The
245 prospective forecasting performance of the model was then evaluated on the 2023–2025 data (years
246 not used in any stage of calibration), providing an independent evaluation of the operational
247 prediction skill under real-world conditions.

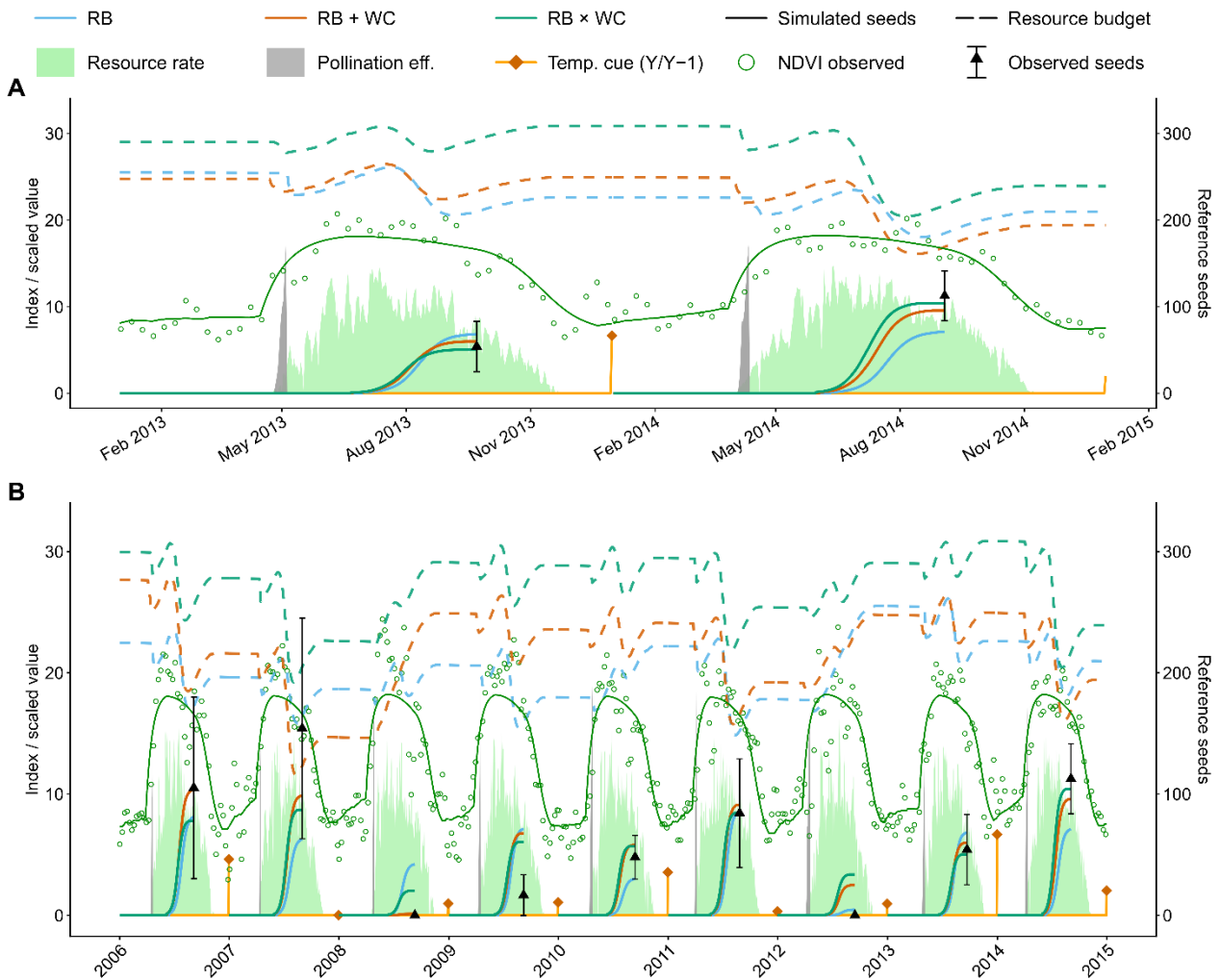
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249 **3. Results**

250 **3.1. Model behaviour and emergent dynamics**

251 Before evaluating model performance, we examined the internal dynamics generated by
252 MASTHING to assess whether the model reproduces the characteristic temporal patterns of mast
253 seeding (Figure 3), using the Buckholt site as an example.

254 Over two consecutive growing seasons (Figure 3A), the model captures the full sequence of
255 phenological and reproductive processes. Pollination efficiency peaked in spring and was sensitive to
256 precipitation-driven vetoes, while resource rate tracked canopy development over the summer
257 months. The resource budget declined progressively as reproductive investment increased, reaching
258 its minimum at the time of seed maturation, before recovering due to carbon assimilation in the last
259 part of autumn. Temperature cues from the preceding two years modulated the magnitude of
260 reproductive investment: the activating signal from Y–1 and the inhibitory legacy from Y–2
261 combined into a composite cue that differed between 2013 and 2014, generating contrasting seed
262 outputs despite broadly similar seasonal trajectories.



264

265 **Figure 3. Within- and among-year dynamics simulated by MASTHING for the Buckholt site.**
 266 (A) Two-year sequence (2013–2014) showing daily resource rate (green area), pollination efficiency
 267 (grey area), temperature cues (orange line and diamond, positioned at the last day of year Y-1),
 268 observed and simulated NDVI (open grey circles and lines), resource budget (dashed lines), simulated
 269 seed production (solid lines), and observed seed count with inter-tree variability (black triangle \pm
 270 SD). (B) Multi-year simulation (2006–2014) showing the same variables across consecutive growing
 271 seasons, illustrating interannual carry-over dynamics in resource budget and reproductive investment.
 272 In both panels, three model formulations are shown: resource-budget only (RB, blue), additive
 273 weather cue (RB+WC, orange), and interactive weather cue (RB×WC, green). All continuous model
 274 outputs are scaled to a common left axis for visualisation; reference seed counts are shown on the
 275 secondary right axis.

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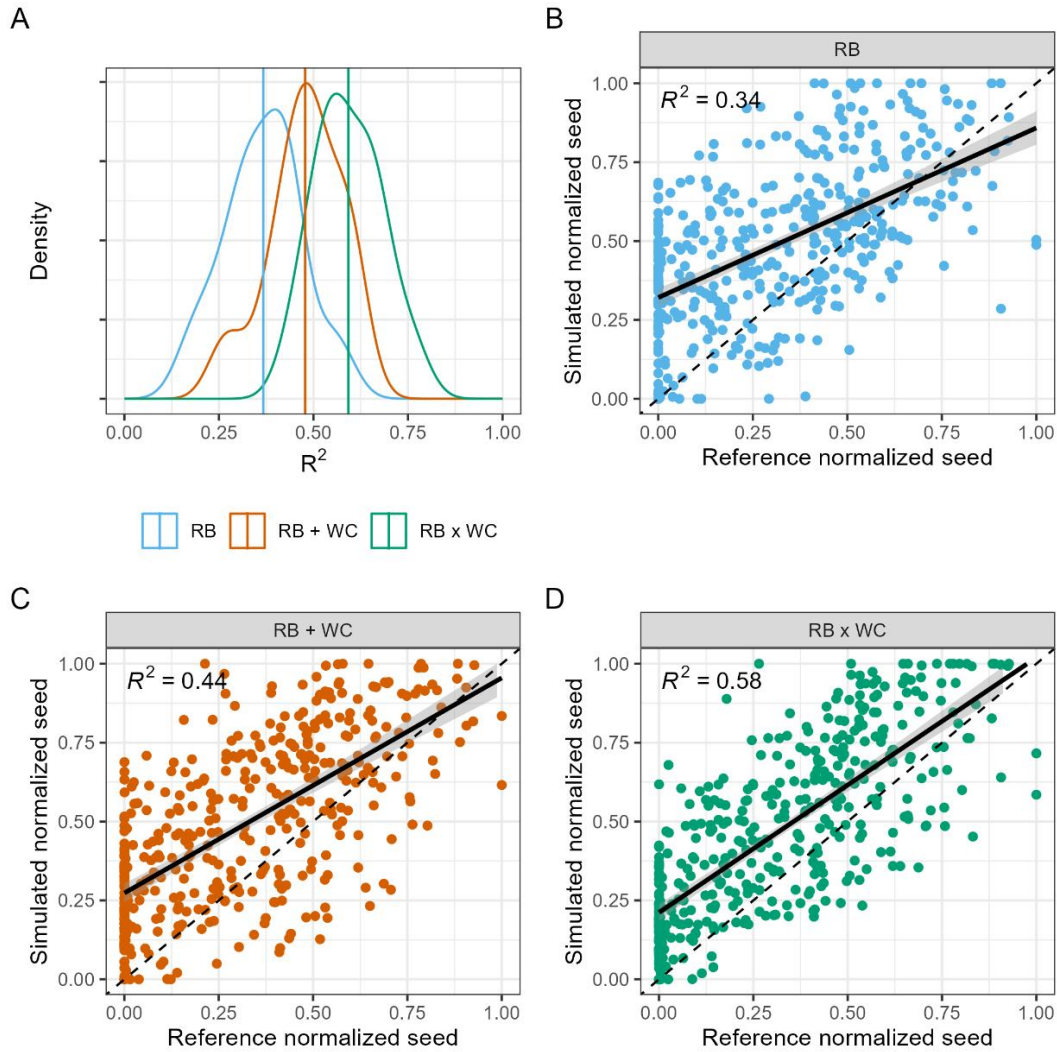
278 Over the multi-year period (Figure 3B), simulated time series revealed that most years emerge
 279 from the interaction between gradual resource accumulation and episodic depletion associated with
 280 reproductive investment. High seed production years coincided with strong reductions in the resource
 281 budget, followed by one or more recovery years during which carbon reserves were replenished.
 282 Conversely, low-seeding years were associated with incomplete resource recovery or unfavourable
 climatic conditions limiting reproductive allocation. Environmental veto processes were also

283 reproduced: adverse conditions during flowering or seed development reduced realised seed
284 production despite prior resource allocation, and the carbon initially committed to reproduction was
285 partially returned to the internal resource pool, dampening interannual variability in resource
286 depletion. The three model formulations diverged in their multi-year reproductive dynamics (Figure
287 3B). The resource-budget-only formulation (RB) produced relatively stable resource trajectories, with
288 seed production varying primarily with accumulated carbon and showing limited interannual contrast.
289 Incorporating temperature cues (RB+WC and RB×WC) introduced greater variability, with mast
290 years becoming more episodic and more tightly coupled to lagged climatic signals. In the interactive
291 formulation (RB×WC), cue sensitivity was modulated by internal resource status, so that favourable
292 temperature conditions triggered strong reproductive responses only when carbon reserves were
293 sufficient. These coupled endogenous and exogenous processes generated the characteristic boom–
294 bust cycles of mast seeding observed in European beech and provide the mechanistic foundation for
295 the model performance evaluation presented in the following sections.

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297 **3.2. Simulating mast seeding in beech**

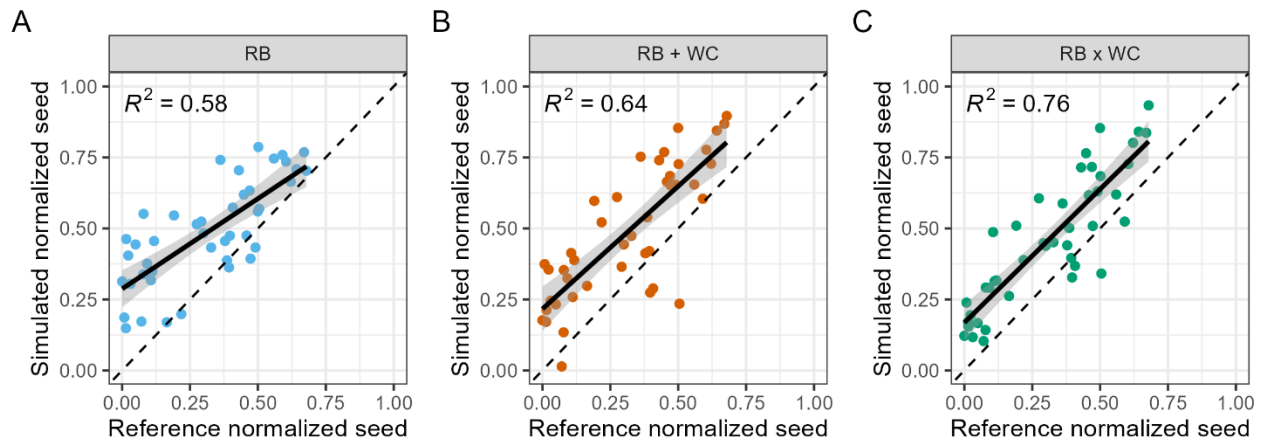
298 Model performance increased with the inclusion of weather cues and was highest when cue
299 effects depended on internal resource status. At the tree-year scale (Figure 4), explained variance
300 increased from $R^2 = 0.34$ in the resource-budget-only formulation (RB) to $R^2 = 0.44$ in the additive cue
301 model (RB + WC) and $R^2 = 0.58$ in the interactive model (RB×WC). The RB formulation reproduced
302 only a compressed version of the observed dynamics: simulated seed production remained relatively
303 high even when observed values approached zero, whereas high-seeding years were systematically
304 underestimated. Incorporating weather cues improved the separation between low- and high-seeding
305 years, yielding steeper fitted relationships and predictions closer to the 1:1 expectation. This effect was
306 strongest in the interactive formulation (RB×WC), indicating that responses to favourable weather cues
307 are better captured when modulated by internal resource status.



308

309 **Figure 4. Model performance across alternative formulations of reproductive allocation**
 310 **across tree-years.** (A) Distribution of model performance (R^2) for the three model formulations:
 311 resource budget only (RB; blue), resource budget with additive weather cues (RB+WC; orange), and
 312 resource budget with interactive weather cues (RB×WC; green). Vertical lines indicate median
 313 values for each formulation. (B-D) Relationship between observed (reference) and simulated
 314 normalised seed production for each model formulation: (B) RB, (C) RB+WC, and (D) RB×WC.
 315 Points represent mean normalised annual site observations, solid lines show fitted linear regressions,
 316 and shaded bands indicate 95% confidence intervals. The dashed 1:1 line denotes perfect agreement
 317 between observed and simulated values. Reported R^2 values quantify the proportion of variance
 318 explained by each model.

319 After aggregating prediction to the site-year level (Figure 5), model performance improved
 320 across all formulations, with R^2 raising from 0.58 (RB) to 0.64 (RB+WC) and 0.76 (RB×WC). All
 321 formulations performed better at the site-year level than at the tree-year scale, suggesting that part of
 322 the mismatch at finer resolution reflects among-tree variability that is averaged out at coarser spatial
 323 scales. The same ranking among formulations was retained after aggregation, with RB×WC providing
 324 the closest match to the observed range and the strongest discrimination between low- and high-seeding
 325 years (Figure 5C).



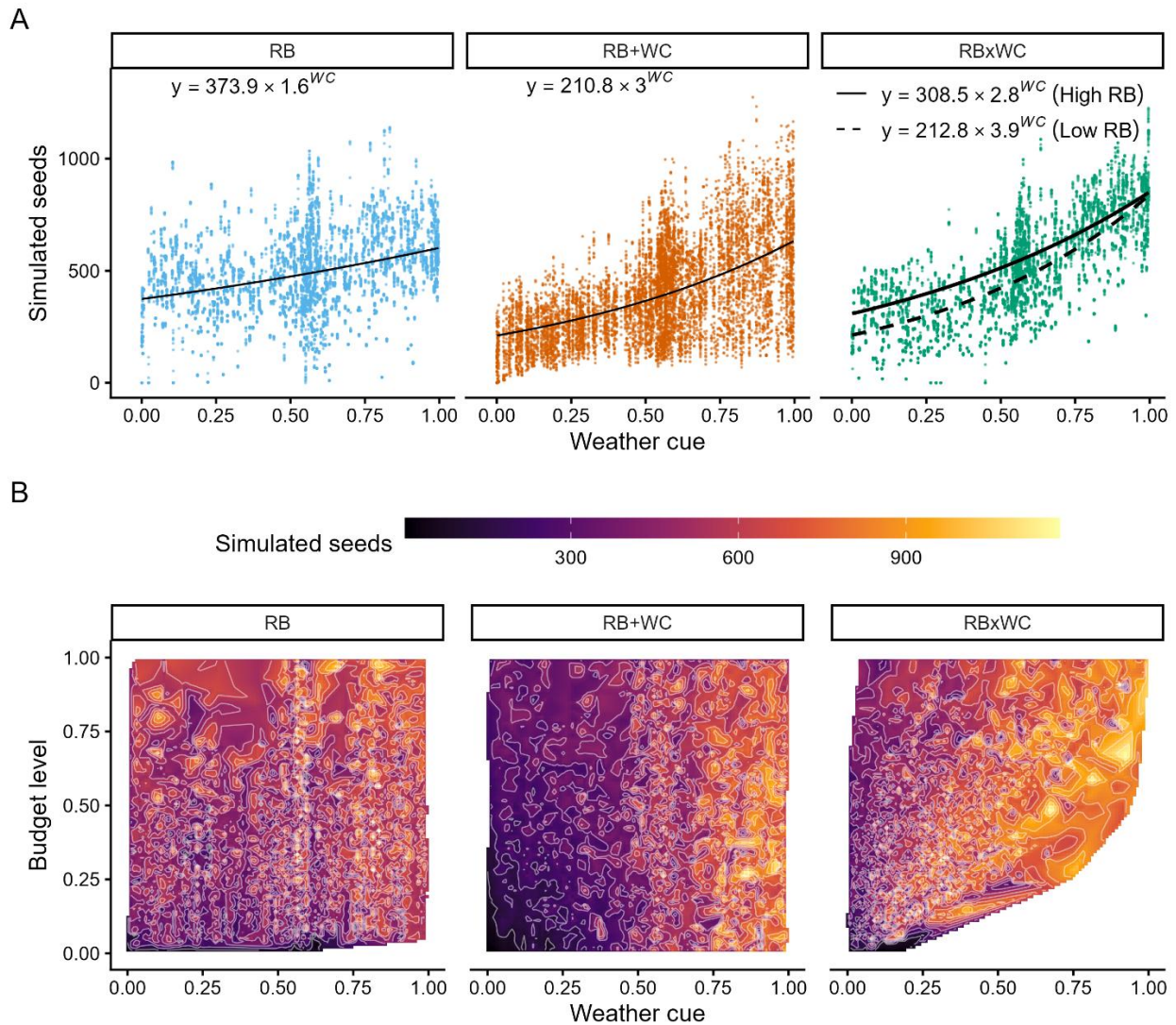
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327 **Figure 5. Model performance across alternative formulations of reproductive allocation,**
 328 **across site-years.** Relationship between observed (reference) and simulated normalised seed
 329 production for each model formulation: resource budget only (RB; A), resource budget with
 330 additive weather cues (RB+WC; B), and resource budget with interactive weather cues (RB×WC;
 331 C). Points represent mean normalised annual site-year observations, solid lines show fitted linear
 332 regressions, and shaded bands indicate 95% confidence intervals. The dashed 1:1 line denotes
 333 perfect agreement between observed and simulated values. Reported R^2 values quantify the
 334 proportion of variance explained by each model. Timeseries of observed and simulated data are
 335 presented in Figure S3.

336

337 Model performance was quite robust to the choice of parameterisation strategy. Under domain-
 338 wide calibration, where a single parameter set was estimated jointly across all 11 sites, the RB×WC
 339 formulation retained most of its predictive skill, with site-level R^2 values ranging from 0.39 to 0.58,
 340 compared to 0.45–0.75 under site-specific calibration (Figure S5). The reduction in performance was
 341 modest and consistent across sites, suggesting that the model captures processes that are largely
 342 transferable across the UK beech network rather than site-idiosyncratic responses.

343 Figure 6 illustrates how model formulations differ in the relationships between resource level,
 344 weather cues, and seed production. In the RB formulation, simulated seed production changed only
 345 weakly along the weather-cue gradient (Figure 6A). Because weather cues do not enter the reproductive
 346 allocation rule in this formulation, this shallow positive trend should not be interpreted as a direct cue
 347 effect. Instead, it likely arises because the seasonal conditions captured by the cue metric also covary
 348 with carbon gain and thus with the resource budget available for reproduction. Consistently, the RB
 349 heatmap is structured mainly along the budget axis, with limited variation across the cue axis (Figure
 350 6B). The cue-informed formulations differed in how weather and resources combined to determine
 351 seed output. In RB+WC, seed production increased with both budget level and cue strength, consistent
 352 with an additive contribution of the two drivers. In RB×WC, the effect of weather cues depended on
 353 internal resource status: favourable cues had a stronger effect when budgets were high, whereas low
 354 budgets constrained seed production even under strong cues (Figure 6A, B).



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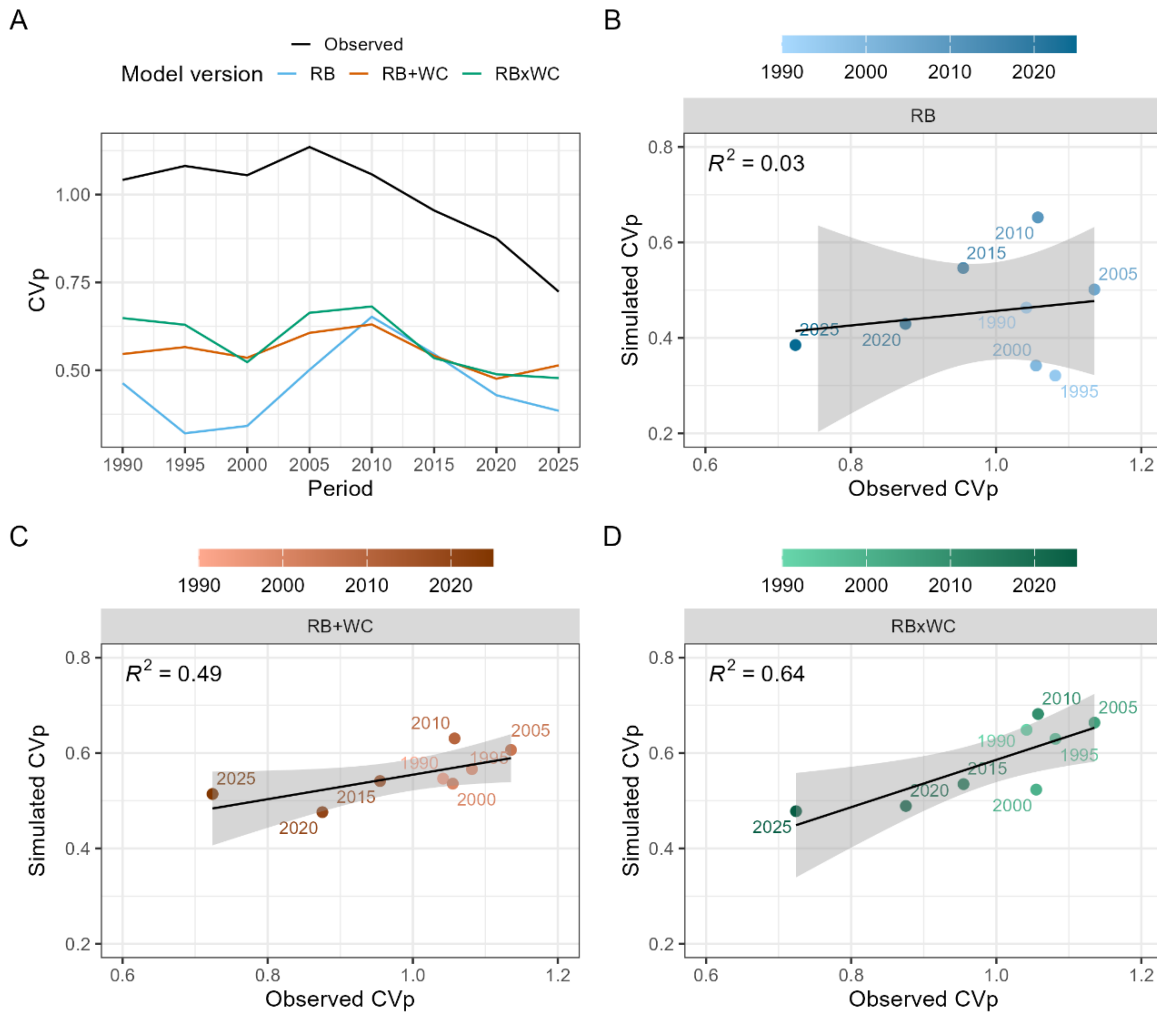
357 **Figure 6. Joint effects of resource budget and weather cues on simulated seed production.** (A)
 358 Relationship between weather cue and simulated seed production across model formulations. Points
 359 represent individual simulations, and lines show fitted exponential functions. In the interactive
 360 formulation (RB×WC), separate curves are shown for high (solid line) and low (dashed line)
 361 resource budget levels, illustrating how sensitivity to weather cues depends on internal resource
 362 status. (B) Heatmaps of mean simulated seed production across the two-dimensional state space
 363 defined by weather cue (x-axis) and resource budget level (y-axis). Colours range from dark (low)
 364 to light (high seed production). In the RB model, seed production depends primarily on resource
 365 availability, whereas in RB+WC it increases with both drivers independently. In RB×WC, high seed
 366 output is concentrated in the upper-right region of the state space, where both resource levels and
 367 weather cues are high, reflecting the multiplicative interaction between internal state and
 368 environmental forcing.

369

370 3.3. Modelling masting under climate change

371 Observed interannual variation in seed production remained high from the 1980–1990 to the
 372 2000–2005 window and then declined sharply, with CV_p peaking at approximately 1.22 around 2005

373 and decreasing to about 0.72 in the 2020–2025 window (Figure 7A). All three model formulations
 374 underestimated the absolute magnitude of interannual variability throughout the time series, with
 375 simulated CVp consistently below observed values by approximately 0.5–0.6 units across all windows.
 376 They nonetheless reproduced part of the temporal structure, with agreement between simulated and
 377 observed CVp improving markedly with model complexity (Figure 7B-D).
 378



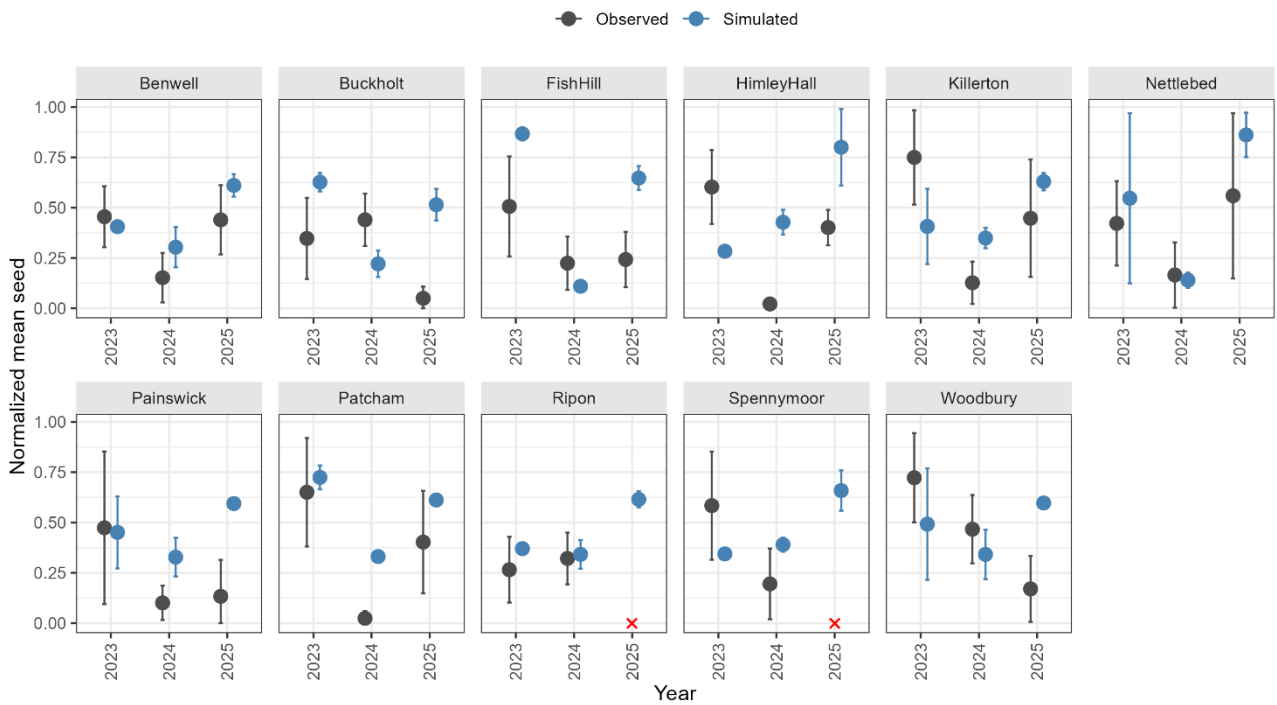
379
 380 **Figure 7. Temporal dynamics of masting intensity across model formulations.** (A) Observed and
 381 simulated changes in masting intensity (interannual variation in seed production, CVp) over time in
 382 UK beech populations. The black line shows observed dynamics; coloured lines represent simulations
 383 for resource budget only (RB; blue), resource budget with additive weather cues (RB+WC; orange),
 384 and resource budget with interacting weather cues (RB×WC; green). CVp is calculated using 10-year
 385 moving windows with a step-size of 5 years; values are reported as the final year of each window (e.g.,
 386 1990 corresponds to 1980–1990). (B–D) Relationship between observed and simulated CVp across
 387 time windows for each model formulation: RB (B), RB+WC (C), and RB×WC (D). Point color
 388 indicates the time window, ranging from light (earlier periods) to dark (more recent periods). Solid
 389 lines show fitted linear regressions with 95% confidence intervals. Trends in the proportion of
 390 reproductive failures are shown in Figure S6.
 391

392 The RB formulation showed virtually no correspondence with observed temporal dynamics (R^2
 393 = 0.03), with simulated CVp varying independently of observed values across time windows. Simulated
 394 values ranged from ~ 0.33 (1995) to ~ 0.62 (2010), remaining well below the observed range (~ 1.08 –
 395 1.22) throughout the series, and showing a partial recovery after 1995 that has no clear counterpart in
 396 the observations. The additive formulation (RB+WC) captured a larger share of the temporal variance
 397 ($R^2 = 0.49$), with simulated CVp ranging from ~ 0.55 to ~ 0.63 and correctly ranking many windows in
 398 terms of relative masting intensity, though still substantially underestimating the observed magnitude.
 399 The interactive formulation (RB \times WC) showed the strongest agreement ($R^2 = 0.64$), with simulated
 400 CVp ranging from ~ 0.50 to ~ 0.65 and the temporal sequence of windows more consistently reflected.
 401 Earlier high-intensity windows (around 2005–2010) were correctly associated with higher simulated
 402 CVp (~ 0.65), and more recent windows (2020–2025) with lower values (~ 0.50).

403

404 3.4. Application: forecasting

405 We used the RB \times WC model to forecast site-level seed production for 2023–2025, with all
 406 calibrations based exclusively on 1980–2022 observational data (Figure 8).



407

408 **Figure 8. Site-level forecasts of normalised seed production for 2023–2025.** Observed (grey)
 409 and simulated (blue) normalised seed production across UK beech sites, generated using the
 410 RB \times WC model calibrated on 1980–2022 data. Points represent mean normalised seed production
 411 per site and year; vertical lines indicate among-tree variability. The 2025 observation was
 412 unavailable for Ripon and Spennymoor (×).
 413

414 Forecast accuracy varied among sites and years. The 2023 crop was generally well

415 reproduced, with simulated values close to observations at most sites. The 2024 low-production year
416 was captured at several sites including Benwell, Killerton, and Nettlebed, where the model correctly
417 predicted below-average seed output. However, the 2025 crop was systematically overestimated: at
418 sites where observed production remained low or moderate (e.g., Buckholt, Painswick, Patcham,
419 Woodbury, HimleyHall, FishHill), simulated values were substantially higher than observations.
420 This pattern suggests that the model does not fully capture the persistence of low-production
421 conditions across consecutive years, possibly reflecting limitations in how the resource budget
422 recovers after repeated low-seed years. Observations for 2025 were unavailable for Ripon and
423 Spennymoor at the time of writing.

424

425 **4. Discussion**

426 Our study shows that a process-based model integrating resource dynamics and weather cues
427 can reproduce key features of masting in European beech. Weather cues were necessary to match
428 observed site-level dynamics, whereas the resource-budget-only formulation performed substantially
429 worse. Model performance improved consistently with formulation complexity, both at the tree-year
430 scale ($R^2 = 0.34$ for RB, 0.44 for RB+WC, 0.58 for RB×WC; Figure 4) and after aggregating to the
431 site-year scale ($R^2 = 0.58$, 0.64 and 0.76 , respectively; Figure 5). This confirms that weather cues
432 improved model fit and that this improvement was strongest when cue sensitivity depended on
433 internal resource status. The consistent ranking across spatial scales supports the idea that favourable
434 weather cues trigger strong reproduction only when trees have sufficient stored resources (Monks *et al.*,
435 2016; Kelly *et al.*, 2025). Model performance was asymmetric, with high-seeding years
436 reproduced more closely than low-seeding (failure) years. This is an improvement over earlier
437 forecasting models that struggled at both ends of the distribution (Journé *et al.*, 2023), but also an
438 indication that the mechanisms producing very low seed crops remain incompletely represented
439 (Oberklammer *et al.*, 2026). The temporal analysis of interannual variability (CVp) showed that
440 agreement between simulated and observed CVp across time windows improved markedly with
441 model complexity, from RB ($R^2 = 0.03$) to RB+WC ($R^2 = 0.49$) and RB×WC ($R^2 = 0.64$; Figure 7),
442 indicating that the interactive formulation successfully captured the relative ranking of high- and low-
443 variability periods. However, all formulations systematically underestimated the absolute magnitude
444 of CVp throughout the series and underestimated the sustained long-term decline in masting intensity
445 observed after 2005, suggesting that the effects of increasingly frequent cue years on resource
446 depletion and recovery are not yet fully represented. The 2023-2025 forecasts show that the model
447 captures broad short-term variation in seed production among sites and years, but the underestimation
448 of the long-term decline in masting intensity may partly explain the weaker forecasting performance

449 in recent years. MASTHING provides a useful tool for hypothesis testing and near-term forecasting,
450 while clearly indicating where further refinement is needed for long-term prediction.

451 The contrast between the resource-only model formulation and the cue-informed models
452 clarifies how different processes contribute to masting dynamics. Resource dynamics alone generated
453 interannual variation in seed production, but they produced too few zero-seed years and failed to
454 align reproduction with the observed timing of mast and failure years. Thus, fluctuations in resource
455 acquisition by themselves were not sufficient to reproduce the empirical masting patterns, consistent
456 with the notion that resource matching alone cannot explain mast years (Kelly, 1994; Pearse *et al.*,
457 2016). At the same time, even in the RB-only model, seed production showed a shallow positive
458 relationship with weather cue strength (exponential base = 1.6; Figure 6A), despite the absence of an
459 explicit cue effect. In our model, this relationship emerges because warmer summers enhance
460 photosynthesis and resource accumulation, not because temperature acts as a flowering cue. This is
461 interesting as it suggests a plausible starting point for the evolutionary argument proposed by Janzen
462 (Janzen, 1971, 1976): hypersensitivity to weather cues may build on a pre-existing physiological
463 sensitivity of reproduction to weather variation, which selection then amplifies into a stronger, cue-
464 driven response. That interpretation is consistent with the idea that selective amplification acts on
465 initially modest synchrony among individuals responding to the same environmental signal,
466 eventually producing stronger interannual variation and synchrony (Bogdziewicz *et al.*, 2020b).
467 Adding weather cues steepened the response substantially (base = 3.0 in RB+WC; Figure 6A),
468 improving the temporal correspondence between simulations and observations, and this improvement
469 was strongest when cue sensitivity depended on internal resource status: in the RB×WC formulation,
470 trees with high resource budgets showed a steeper response to cues (base = 2.8) than those with low
471 budgets (base = 3.9 on the low-budget curve, but starting from a lower intercept), producing the
472 strongly nonlinear surface visible in Figure 6B. Under that formulation, mast and failure years were
473 more often reproduced in the correct years, and high-seeding years were captured more closely. This
474 suggests that resource-dependent cue sensitivity captures an important component of reproductive
475 timing that was missing from earlier forecasting models (Journé *et al.*, 2023).

476 The observed decline in interannual variation in seed production in the UK, and more broadly
477 across the beech range (Foest *et al.*, 2024; 2025; Jantzen *et al.*, 2026), was captured only partially
478 across model formulations, with the RB×WC formulation reproducing the sustained downward trend
479 most closely. Observed CVp peaked at approximately 1.22 around 2005 and declined to ~0.72 by
480 2025. Simulated formulations remained within a narrower range (~0.38–0.65), but the RBxWC
481 formulation was able to track the sustained decrease (Figure 7D). Empirical analyses attribute this
482 breakdown to increasing summer temperatures, which increase the frequency of flowering cues

483 (Bogdziewicz *et al.*, 2021). More frequent cues are thought to shorten recovery intervals between
484 large seed crops, leading to progressive resource depletion and, in turn, weaker responses to
485 subsequent cues (Hackett-Pain *et al.*, 2025). Our simulations are consistent with this mechanism in
486 relative terms: under the RB×WC formulation, increased cue frequency generated a long-term
487 decline in variability, indicating that the model can recover the directional breakdown in masting
488 intensity. At the same time, the magnitude of this decline remained weaker than observed. Resource
489 budgets fluctuated, but they did not decline through time enough to reduce reproductive
490 responsiveness to the extent seen in the empirical record. This likely reflects the current allocation
491 scheme, in which reproductive investment increases smoothly with cue strength and resource level,
492 remains bounded, and is constrained by available reserves, while annual carbon gain allows partial
493 recovery. These features buffer the system against chronic depletion, dampening the progressive
494 weakening of masting intensity that is observed empirically. Notably, while the RB×WC formulation
495 successfully ranked time windows by their relative variability ($R^2 = 0.64$ across periods; Figure 8B–
496 D), it still underestimated CV_p by approximately 0.5–0.6 units throughout the series, indicating that
497 the model captures the temporal ordering of high- and low-variability periods and the overall decline
498 through time, but not their absolute magnitude. The results suggest that the model underestimates the
499 strength of depletion feedbacks needed to reproduce the observed breakdown in masting
500 quantitatively. One additional potential improvement would be to replace the current sigmoidal cue
501 response with a steeper, potentially exponential function, so that repeated warm summers generate
502 stronger reproductive drawdown and more pronounced resource depletion (Fernández-Martínez *et al.*
503 *et al.*, 2017). MASTHING now provides a mechanistic platform for testing alternative hypotheses about
504 how increasing cue frequency, resource depletion, and carry-over effects interact to drive the climate-
505 related breakdown of masting.

506 The model also showed useful short-term forecasting ability. When calibrated with data from
507 1980-2022 and projected forward, it reproduced broad year-to-year variation in seed production
508 during 2023-2025, as well as some of the among-site differences in crop size. At the same time,
509 performance was uneven: seed production was generally overestimated in 2024 and 2025, especially
510 at sites where the observed crop was low or intermediate. Thus, the model captures broad variation
511 in seed production better than it predicts the exact magnitude. This pattern likely reflects the same
512 limitation identified in the long-term CV_p analysis the model's resource budget recovers too readily
513 after reproductive events, preventing the carry-over depletion that may sustain low-production
514 conditions in consecutive years. Thus, the model captures broad interannual variation in seed
515 production better than it predicts the exact magnitude of low or consecutive poor crops, a pattern
516 consistent with the broader challenge in mast forecasting of predicting extreme outcomes (Journé *et*

517 *al.*, 2023; Wion *et al.*, 2025). Even so, such forecasts can have clear operational value (Pearse *et al.*,
518 2021; Oberklammer *et al.*, 2026). Anticipating relatively productive years can support seed
519 collection, nursery planning, staff allocation, and storage preparation, and also adaptively set game
520 management and hunting bags for pulsed-resource consumers (Bisi *et al.*, 2018), while identifying
521 likely poor years may help avoid unnecessary financial and organisational investment. MASTHING
522 therefore already provides a useful forecasting framework, even if further refinement is needed to
523 improve prediction of low seed crops and local departures from observed seed production.

524 Beyond predictive performance, MASTHING provides a conceptual advance over purely
525 statistical approaches by explicitly tracking the physiological pathways linking weather, phenology,
526 carbon balance, and reproduction. Because the model resolves resource dynamics at daily resolution,
527 it can be used to test the contribution of specific mechanisms by modifying cue functions or activating
528 and suppressing heat, cold, and drought effects. The comparison among model formulations
529 presented here is itself an example of this hypothesis-testing capacity: the contrasting response
530 surfaces in Figure 6 directly illustrate how alternative assumptions about resource–cue coupling
531 translate into different predictions, and the CVp analysis (Figure 7) identifies the specific aspect of
532 masting dynamics, i.e., the long-term decline in interannual variability, that current formulations fail
533 to capture and that future refinements should target. A particular strength of the framework is the
534 coupling of reproduction to canopy phenology, which controls the seasonal timing of carbon
535 acquisition and reproductive decisions. In the current implementation, weather cues are evaluated
536 within a fixed post-solstice window (Journé *et al.*, 2024), but the model structure would also allow
537 cue perception to be linked directly to phenological development. Such an extension could improve
538 the representation of state-dependent cue expression, potentially helping to explain both extreme
539 mast years and the long-term changes in masting intensity documented here and elsewhere (Foest *et*
540 *al.*, 2024, 2025; Jantzen *et al.*, 2026). Because the model is relatively parsimonious in its input
541 requirements and can be transferred through parameter recalibration, MASTHING also provides a
542 flexible framework for extending this approach to other masting species, allowing cross-species tests
543 of whether the same resource–cue coupling mechanisms underlie masting across taxa.

544 To summarise, we developed MASTHING, a process-based model that integrates phenology-
545 driven resource acquisition, a dynamic resource budget, temperature-based flowering cues, and
546 environmental vetoes during pollination and seed ripening. The model reproduced key features of
547 European beech masting across multiple scales, especially the timing of mast and failure years and
548 short-term site-level variation in seed production, with highest performance when cue sensitivity
549 depended on internal resource status (Kelly *et al.*, 2025). At the same time, low-seeding years were
550 less well captured than high-seeding years, and the 2025 crop was systematically overestimated

551 across sites. Although the model reproduced the observed long-term decline in masting intensity, it
552 underestimated its magnitude, as the CVp analysis showed that simulated trajectories remained less
553 variable than the observed series despite correctly ranking high- and low-variability periods. These
554 mismatches point to specific processes that require refinement, particularly the strength of resource
555 depletion feedbacks and the shape of the cue-response function under increasing cue frequency.
556 Nonetheless, the results show that a process-based framework can translate current mechanistic
557 understanding into both insight on long-term change and useful short-term forecasts, provide a
558 platform for testing alternative hypotheses about resource–climate coupling, and identify the specific
559 limitations that must be addressed to improve the quantitative accuracy of long-term prediction of
560 masting dynamics under climate change.

561

562 **Acknowledgements**

563 This study was funded by the Italian Ministry of Agriculture, Food Sovereignty and Forestry
564 (MASAF, SOFIA, DM 0656382), by Ferrero Trading Lux (HAZIMUT project) and by the European
565 Union (ERC, ForestFuture, 101039066). Views and opinions expressed are, however, those of the
566 authors only and do not necessarily reflect those of the European Union or the European Research
567 Council. Neither the European Union nor the granting authority can be held responsible for them. AI
568 tools (Claude, Chat-GPT) were used to improve the clarity and readability of portions of this
569 manuscript. All scientific content, analyses, and interpretations remain entirely the work of the
570 authors, who take full responsibility for the accuracy of the information presented.

571

572 **Author Contributions Statement**

573 All authors designed the study, SBr developed the model with input from FC, CF, SBa, AHP, MB.
574 SBr, AHP, MB, and FC co-wrote the paper. All authors revised the text and approved the submission.

575

576 **Declaration of interests**

577 No competing interests to declare.

578

579 **Data and code availability statement**

580 The data that support the findings of this study are available from with the permission of dr. Andrew
581 Hacket-Pain. Data requests should be addressed to andrew.hacket-pain@liverpool.ac.uk. The
582 MASTHING source code is openly available at <https://github.com/GeoModelLab/MASTHING> and
583 archived on Zenodo (<https://doi.org/10.5281/zenodo.19660460>). The MASTHING source code is

584 openly available at <https://github.com/GeoModelLab/MASTHING> and archived on Zenodo
585 (<https://doi.org/10.5281/zenodo.19660460>).

586

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753

754 **Supplementary Information**

755 **S1. Full model description**

756 MASTHING (MASting THEory modellING) is a process-based model that simulates mast seeding
757 dynamics by coupling tree structure, phenology, carbon balance, environmental forcing, and
758 reproductive allocation. The model operates at a daily time step and is driven by meteorological inputs
759 (air temperature, precipitation, incoming radiation) together with tree structural attributes derived
760 from diameter at breast height (DBH). At the core of the framework is a dynamic pool of mobile
761 carbon reserves, hereafter referred to as the resource budget (B_t , g C m⁻²), which integrates daily
762 carbon gains from photosynthesis and losses due to maintenance respiration and reproductive
763 allocation. All fluxes are expressed per unit crown projection area (CPA, m²). Reproductive
764 investment is represented as a continuous function of internal resource status and climatic cues, rather
765 than a threshold-based switching mechanism, enabling evaluation of alternative hypotheses about
766 resource-climate coupling.

767

768 **S1.1. Allometric Initialisation**

769 Tree structural properties are initialised from DBH (cm), the only required tree-level input. Crown
770 projection area (CPA, m²), tree height (H, m) and aboveground biomass components are derived from
771 species-specific allometric relationships (Bartelink, 1997; Zianis & Mencuccini, 2004):

$$772 \text{ CPA} = 0.4064 \times \text{DBH}^{1.2830} \quad (\text{SE1.1})$$

$$773 \text{ H} = \exp(1.4192 + 0.5358 \times \ln(\text{DBH})) \quad (\text{SE1.2})$$

$$774 \ln(B_{\text{tot}}) = -1.3816 + 2.3485 \times \ln(\text{DBH}) \quad (\text{SE1.3})$$

$$775 \ln(B_{\text{stem}}) = -1.6015 + 2.3427 \times \ln(\text{DBH}) \quad (\text{SE1.4})$$

$$776 \ln(B_{\text{branch}}) = -5.2898 + 2.9353 \times \ln(\text{DBH}) \quad (\text{SE1.5})$$

$$777 \text{ B}_f = 0.0001663 \times \text{DBH}^2 \times \text{H} + 0.224 \quad (\text{SE1.6})$$

$$778 \text{ LA} = 3.38 \times \text{CPA}^{1.028} \quad (\text{SE1.7})$$

$$779 \text{ LAI}_{\text{max}} = (\text{B}_f \times \text{SLA}) / \text{CPA} \quad (\text{SE1.8})$$

780 where B_{tot} (kg DM) is total aboveground biomass, B_{stem} and B_{branch} (kg DM) are stem and branch
781 biomass, B_f (kg DM) is foliage biomass, LA (m²) is total leaf area, LAI_{max} is maximum leaf area index,
782 and SLA (m² kg⁻¹) is species-specific leaf area (Table S1.6). This formulation links biomass allocation
783 directly to canopy structure, ensuring consistency between structural variables and photosynthetic
784 capacity.

785 **S1.2. Carbon Balance Module**

786 Daily carbon dynamics are computed as the balance between gross primary production (GPP , g C m⁻²
787 d⁻¹) and maintenance respiration. GPP is estimated using a light-use efficiency approach:

788 $GPP_t = \varepsilon \times GSR_t \times 0.5 \times f_{int} \times f_T \times f_{stress}$ (SE1.9)

789 where ε is light use efficiency (g C MJ⁻¹), GSR_t is global solar radiation (MJ m⁻² d⁻¹), 0.5 is the PAR
 790 fraction, $f_{int} = 1 - \exp(-0.5 \times LAI)$ is the canopy interception fraction, f_T is a temperature response
 791 function (Yan & Hunt, 1999), and $f_{stress} = \min(f_{heat}, f_{cold}, f_{water})$ is the most limiting abiotic stress factor.
 792 The temperature response of photosynthesis follows the asymmetric function of Yan & Hunt (1999),
 793 which returns zero below a minimum ($T_{min,gro}$, °C) and above a maximum ($T_{max,gro}$, °C) temperature
 794 threshold:

795 $f_T = 0$, if $T_{avg} \leq T_{min,gro}$ or $T_{avg} \geq T_{max,gro}$ (SE1.10a)

796 $f_T = [(T_{max,gro} - T_{avg}) / (T_{max,gro} - T_{opt,gro})] \times [(T_{avg} - T_{min,gro}) / (T_{opt,gro} - T_{min,gro})]^\alpha$ otherwise (SE1.10b)

797 where $T_{avg} = (T_{max} + T_{min}) / 2$ is mean daily air temperature (°C), T_{opt} , is the optimum temperatures for
 798 growth (°C), and the exponent α controls the asymmetry of the response:

799 $\alpha = (T_{opt} - T_{min,gro}) / (T_{max,gro} - T_{opt})$ (SE1.10c)

800 The function rises from zero at $T_{min,gro}$, reaches a maximum of 1.0 at T_{opt} , and returns to zero at $T_{max,gro}$.
 801 Maintenance respiration is computed separately for woody (stem + branches; $R_{wood,t}$, g C m⁻² d⁻¹) and
 802 foliar ($R_{leaf,t}$, g C m⁻² d⁻¹) components using a Q₁₀ formulation:

803 $R_{wood,t} = r_w \times Q_{10}^{(T_{avg} - 25)/10} \times (B_{stem} + B_{branch}) \times 0.5 \times 1000 / CPA$ (SE1.11a)

804 $R_{leaf,t} = r_l \times Q_{10}^{(T_{avg} - 25)/10} \times B_{foliage} \times (LAI / LAI_{max}) \times 1000 / CPA$ (SE1.11b)

805 where r_w and r_l are base respiration rates for wood and leaves respectively (g C g⁻¹ DM d⁻¹), and T_{avg}
 806 is mean daily air temperature (°C). The factor 0.5 accounts for the carbon content of dry biomass.

807 Heat stress reduces photosynthesis when daily maximum temperature (T_{max} , °C) exceeds the growth
 808 maximum temperature ($T_{max,gro}$, °C). The response is a logistic sigmoid transitioning to zero at the
 809 critical heat temperature ($T_{crit,heat}$, °C):

810 $m_{heat} = (T_{max,gro} + T_{crit,heat}) / 2$ (SE1.12a)

811 $w_{heat} = T_{crit,heat} - T_{max,gro}$ (SE1.12b)

812 $f_{heat} = 1 / (1 + \exp(10 / w_{heat} \times (T_{max} - m_{heat})))$ (SE1.12c)

813 where $f_{heat} = 1$ when $T_{max} < T_{max,gro}$ (no stress) and $f_{heat} \rightarrow 0$ as T_{max} approaches $T_{crit,heat}$.

814 Cold stress reduces photosynthesis when daily minimum temperature (T_{min} , °C) falls below the
 815 growth minimum temperature ($T_{min,gro}$, °C). The transition occurs between the critical cold
 816 temperature ($T_{crit,cold}$, °C) and $T_{min,gro}$:

817 $m_{cold} = (T_{min,gro} + T_{crit,cold}) / 2$ (SE1.13a)

818 $w_{cold} = T_{min,gro} - T_{crit,cold}$ (SE1.13b)

819 $f_{cold} = 1 / (1 + \exp(10 / (-w_{cold}) \times (T_{min} - m_{cold})))$ (SE1.13c)

820 where $f_{cold} = 1$ when $T_{min} > T_{min,gro}$ and $f_{cold} = 0$ when $T_{min} \leq T_{crit,cold}$.

821 Reference evapotranspiration (ET_0 , mm d⁻¹) is computed using the Hargreaves method:

822 $ET_0 = (1/\lambda) \times 0.0023 \times ((T_{max} + T_{min})/2 + 17.8) \times (T_{max} - T_{min})^{0.5} \times R_a$ (SE1.14)

823 where λ is the latent heat of vaporization (MJ kg⁻¹), and R_a is extraterrestrial radiation (MJ m⁻² d⁻¹)
824 computed from site latitude and day of year. A water availability index is then derived from the
825 cumulative balance of ET_0 and precipitation (P , mm) over a moving window of 30 days (WS_{days}):

826 $I = (\sum ET_0 - \sum P) / (\sum ET_0 + \sum P + \varepsilon)$ (SE1.15a)

827 $W_{avail} = 1 - (I + 1) / 2$ (SE1.15b)

828 where $\varepsilon = 10^{-6}$ is a small constant for numerical stability, $I \in [-1, +1]$, and $W_{avail} \in [0, 1]$ (0 =
829 maximum drought, 1 = no stress). The water stress multiplier for GPP is then:

830 $f_{water} = 0.5 \times (W_{avail} - W_{thresh}) + 1, \quad \text{if } W_{avail} < W_{thresh}$ (SE1.15c)

831 $f_{water} = 1, \quad \text{if } W_{avail} \geq W_{thresh}$ (SE1.15d)

832 where W_{thresh} is the water stress threshold parameter.

833 The resource budget evolves daily as:

834 $B_t = \max(0, B_{t-1} + GPP_t - R_{tree,t})$ (SE1.16)

835 where B_t (g C m⁻²) is the resource budget at day t , GPP_t is gross primary production, and $R_{tree,t} =$
836 $R_{wood,t} + R_{leaf,t}$ is total maintenance respiration. The maximum resource budget (B_{max} , g C m⁻²) is set
837 as a fixed fraction of total aboveground biomass:

838 $B_{max} = f_B \times B_{tot}$ (SE1.17)

839 where f_B is the resource budget fraction (calibrated; Table S1.6), a calibrated parameter controlling
840 the size of the mobile carbon pool relative to structural biomass. The minimum budget required to
841 initiate reproduction (B_{min} , g C m⁻²) is defined as a threshold fraction of B_{max} :

842 $B_{min} = \theta \times B_{max}$ (SE1.18)

843 where θ is the reproduction threshold (calibrated; Table S1.6). The budget is initialised at the midpoint
844 of the feasible range:

845 $B_0 = (B_{min} + B_{max}) \times 0.5$ (SE1.19)

846 At the end of each growing season (31 December), the budget is normalised to a dimensionless budget
847 level (BL) serving as the internal state variable for reproductive allocation (Section S1.4):

848 $BL_t = (B_t - B_{min}) / (B_{max} - B_{min}), \quad BL_t \in [0, 1]$ (SE1.20)

849 **S1.3 Phenological Module**

850 Tree phenology is simulated using the process-based SWELL model, which tracks dormancy
851 induction, endodormancy, ecodormancy, growth, greendown, and senescence phases through
852 photothermal accumulation. Phenological progression controls the seasonal window of carbon
853 acquisition and the timing of reproductive decisions. A full description is provided in Bajocco et al.
854 (2025). The growing season (phenoCode 3–5) determines the period over which GPP_t is computed
855 and LAI scales with canopy development: LAI increases linearly with growth completion during leaf

856 expansion and declines proportionally to NDVI during senescence. The onset of flowering is
 857 triggered when growth completion reaches the parameter Flo_{time} (expressed as a percentage of the full
 858 growth forcing requirement, Table S1.6).

859 **S1.4 Reproductive Allocation**

860 Annual reproductive investment is determined by the combined effects of internal resource status and
 861 post-solstice temperature cues, incorporating both current-year and lagged climatic signals.
 862 Temperature cues are derived from mean daily maximum temperature during the post-solstice sensing
 863 window ($T_{sol,y}$, DOY 172–212). Cues from the current year (Y–1 relative to seed production,
 864 activating signal) and the preceding year (Y–2, inhibitory signal) are incorporated, reflecting the
 865 lagged structure typical of masting systems (Journé et al., 2024). Each signal is transformed through
 866 a sigmoid response function:

$$867 \quad g_T(T, BL) = BL / (1 + \exp(\sigma \times s_T \times (T_{sol,y} - T_{mid}))) \quad (SE1.21)$$

868 where $\sigma = -1$ for the activating signal (warm summers promote reproduction) and $\sigma = +1$ for the
 869 inhibitory signal, s_T controls sensitivity (Table S1.6), and T_{mid} is the midpoint of the cue temperature
 870 range ($^{\circ}C$). The midpoint T_{mid} and the temperature range of the cue function are not fixed a priori but
 871 are derived from the site-specific meteorological record. For each site, the mean post-solstice
 872 maximum temperature is computed annually:

$$873 \quad T_{sol,y} = \text{mean}(T_{max,d}) \text{ for } d \in [172, 212] \text{ in year } Y \quad (SE1.22a)$$

874 The cue temperature range is then defined as:

$$875 \quad T_{min,cue} = \min(T_{sol,y}) \text{ over all years} \quad (SE1.22b)$$

$$876 \quad T_{max,cue} = \max(T_{sol,y}) \text{ over all years} \quad (SE1.22c)$$

$$877 \quad T_{mid} = (T_{min,cue} + T_{max,cue}) / 2 \quad (SE1.22d)$$

878 This data-driven scaling ensures that the sigmoid response spans the full range of climatic variability
 879 observed at each site, so that the normalised cue signal reflects relative rather than absolute
 880 temperature anomalies. As a result, T_{mid} and the cue range are site-specific quantities computed from
 881 the historical meteorological record rather than calibrated parameters. In the RB+WC formulation BL
 882 $= 1$, so cues act independently of resource status; in RB \times WC, BL is the actual normalised budget
 883 level, modulating cue sensitivity by internal resource status. The final weather cue is a weighted
 884 combination of the two years' signals:

$$885 \quad TC_t = w_T \times g_T(T_{Y-1}, BL) + (1 - w_T) \times g_T(T_{Y-2}, BL) \quad (SE1.23)$$

886 where w_T is the weight assigned to the current-year signal (Table S1.6). Reproductive potential (RP)
 887 emerges as a continuous function of resource availability and climatic forcing:

$$888 \quad RP_t = BL_t \quad (\text{RB formulation}) \quad (SE1.24a)$$

$$889 \quad RP_t = (BL_t + TC_t) / 2 \quad (\text{RB+WC, RB}\times\text{WC formulations}) \quad (SE1.24b)$$

890 Reproductive investment (I_{rep} , g C m⁻²) is computed as the minimum of available reserves and
 891 potential investment, and partitioned between flowering and fruit development:

$$892 \quad I_{rep} = \min(B_t, RP_t \times B_{max}) \quad (SE1.25a)$$

$$893 \quad I_{seed} = I_{rep} / (1 + c_{ff}) \quad (SE1.25b)$$

$$894 \quad I_{flow} = I_{rep} - I_{seed} \quad (SE1.25c)$$

895 where c_{ff} is the flowers-to-fruit cost (Table S1.6), the additional carbon cost of flower production
 896 relative to seed ripening. Realised reproduction is further reduced by unfavourable conditions during
 897 flowering and seed development. Pollination efficiency is computed as a sigmoidal function of daily
 898 precipitation during the flowering window ($F_{lo_{time}} \pm F_{lo_{duration}} / 2$):

$$899 \quad f_{poll} = 1 / (1 + \exp(k \times (P_{day} - P_{mid}))) \quad (SE1.26)$$

900 where $P_{mid} = P_{lim} / 2$, P_{lim} is the precipitation threshold limiting pollination (Table 1.6) and k is a
 901 sensitivity term derived from P_{lim} . High precipitation during anthesis reduces pollination efficiency,
 902 scaling down flowering and ripening investment proportionally. During the greendown phase, seed
 903 ripening progresses following a logistic function of greendown completion ($GD\%$, %), modulated by
 904 water stress:

$$905 \quad f_{rip} = 1 / (1 + \exp(-k_r \times (GD\% - 50))) \quad (SE1.27)$$

906 where $k_r = 0.09$ is a fixed parameter controlling the steepness of the ripening response. Resources
 907 saved by incomplete ripening under drought stress are returned to the budget. After reproduction, the
 908 remaining resource budget is carried over to the following year:

$$909 \quad B_{t+1,init} = B_t - I_{rep} + R_{veto} \quad (SE1.28)$$

910 where R_{veto} (g C m⁻² d⁻¹) represents resources recovered from incomplete seed ripening. This carry-
 911 over links past reproductive investment to future carbon availability, generating the interannual
 912 feedbacks characteristic of masting systems.

913

914 **S1.5 Model formulations**

915 Three alternative formulations of reproductive allocation were evaluated. In the RB formulation,
 916 reproduction depends exclusively on internal reserves ($RP_t = BL_t$; SE1.24a), and temperature cues do
 917 not enter the allocation rule. In the RB+WC formulation, cues contribute additively to reproductive
 918 potential (SE1.24b) but act independently of resource status ($BL = 1$ in SE1.21), so warm post-solstice
 919 temperatures promote reproduction regardless of current reserves. In the RB×WC formulation, cue
 920 sensitivity is explicitly modulated by the normalised budget level ($BL = BL_t$ in SE1.21), so favourable
 921 cues amplify reproduction only when reserves are sufficient. These three formulations represent
 922 alternative hypotheses about resource–climate coupling and are compared against the same
 923 observational dataset (Section 2.2).

924 **S1.6 Model Parameters**

925 **Table S1.6. Key parameters of the MASTHING model for *Fagus sylvatica*.**

Module	Parameter	Symbol	Value	Source
<i>Allometry</i>	CPA coefficient	—	0.4064	Literature
	CPA exponent	—	1.2830	Literature
	Height intercept (ln)	—	1.4192	Literature
	Height slope	—	0.5358	Literature
	Biomass intercept (ln)	—	-1.3816	Literature
	Biomass slope	—	2.3485	Literature
	Specific leaf area	<i>SLA</i>	23	Literature
<i>Carbon balance</i>	Light use efficiency	ϵ	3.0 g C MJ ⁻¹	Literature
	Min. growth temperature	$T_{min,gro}$	3.5 °C	Literature
	Opt. growth temperature	T_{opt}	18.0 °C	Literature
	Max. growth temperature	$T_{max,gro}$	30.0 °C	Literature
	Critical heat temperature	$T_{crit,heat}$	38.0 °C	Literature
	Critical cold temperature	$T_{crit,cold}$	1.0 °C	Literature
	Wood respiration rate	r_w	3×10 ⁻⁵ g C g ⁻¹ DM d ⁻¹	Literature
	Leaf respiration rate	r_l	2×10 ⁻⁴ g C g ⁻¹ DM d ⁻¹	Literature
	Q ₁₀ coefficient	Q_{10}	1.8	Literature
	Water stress memory	—	30 days	Literature
	Water stress threshold	W_{thresh}	0.5	Literature
	Resource budget fraction	f_B	Calibrated	—
	Reproduction threshold	θ	Calibrated	—
Initial budget fraction	—	0.5 × (B _{min} + B _{max})	Derived	
<i>Reproduction</i>	Flowering time	Flo_{time}	5	Fixed
	Flowering duration	$Flo_{duration}$	12 % growth completion	Fixed
	Pollination precip. threshold	P_{lim}	Calibrated	—
	Flower-to-fruit cost	c_{ff}	0.14	Fixed
	Cue sensitivity	s_T	2.8	Fixed
	Current-year cue weight	w_T	Calibrated	—
	Cue temperature midpoint	T_{mid}	Site-specific (SE1.22)	Derived
	Cue temperature range	$T_{min,cue} - T_{max,cue}$	Site-specific (SE1.22b-c)	Derived
Ripening steepness	k_r	0.09	Fixed	

926

927 Parameters estimated through optimisation are indicated as 'Calibrated'; fixed parameters derived
 928 from literature or ecophysiological constraints are indicated accordingly.

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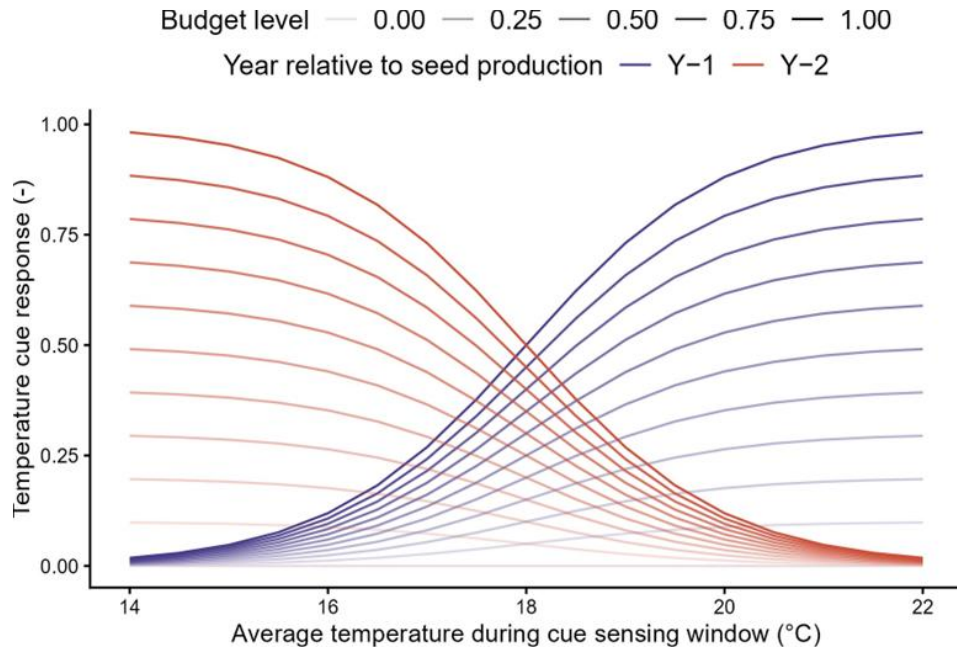
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940 **S2. Resource-modulated temperature cue functions**

941



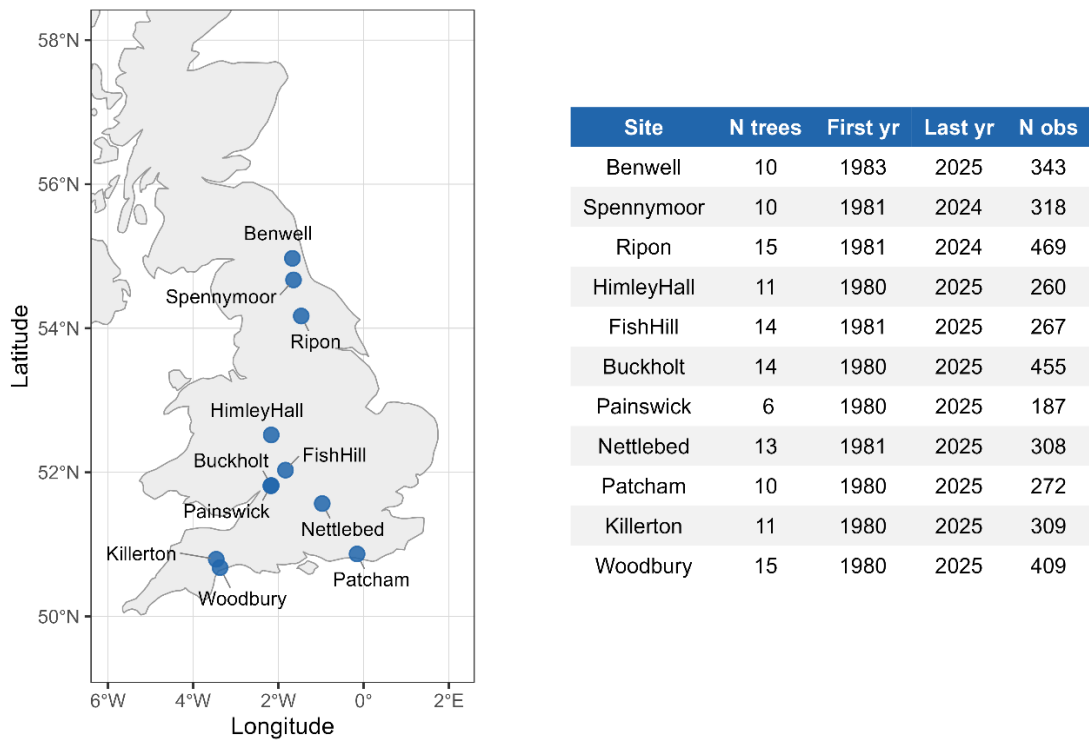
942

943 **Figure S2.** Resource-modulated temperature cue functions controlling reproductive investment.
944 The curves represent theoretical sigmoidal relationships illustrating how temperature cues in year
945 Y-1 (blue, activating effect) and year Y-2 (red, inhibitory legacy effect) contribute to reproductive
946 investment as a function of average temperature during the cue-sensing window. Each set of curves
947 represents different levels of resource availability (budget level, ranging from 0 to 1), with line
948 transparency decreasing as resource availability declines. The y-axis shows the scaled cue response
949 (0–1). Higher resource availability amplifies the magnitude of both activating and inhibitory
950 responses, whereas low resource levels dampen their effects. These functions are not fitted to
951 empirical data but represent assumptions built into the model to capture the expected nonlinear
952 sensitivity of reproductive timing to thermal conditions.

953

954

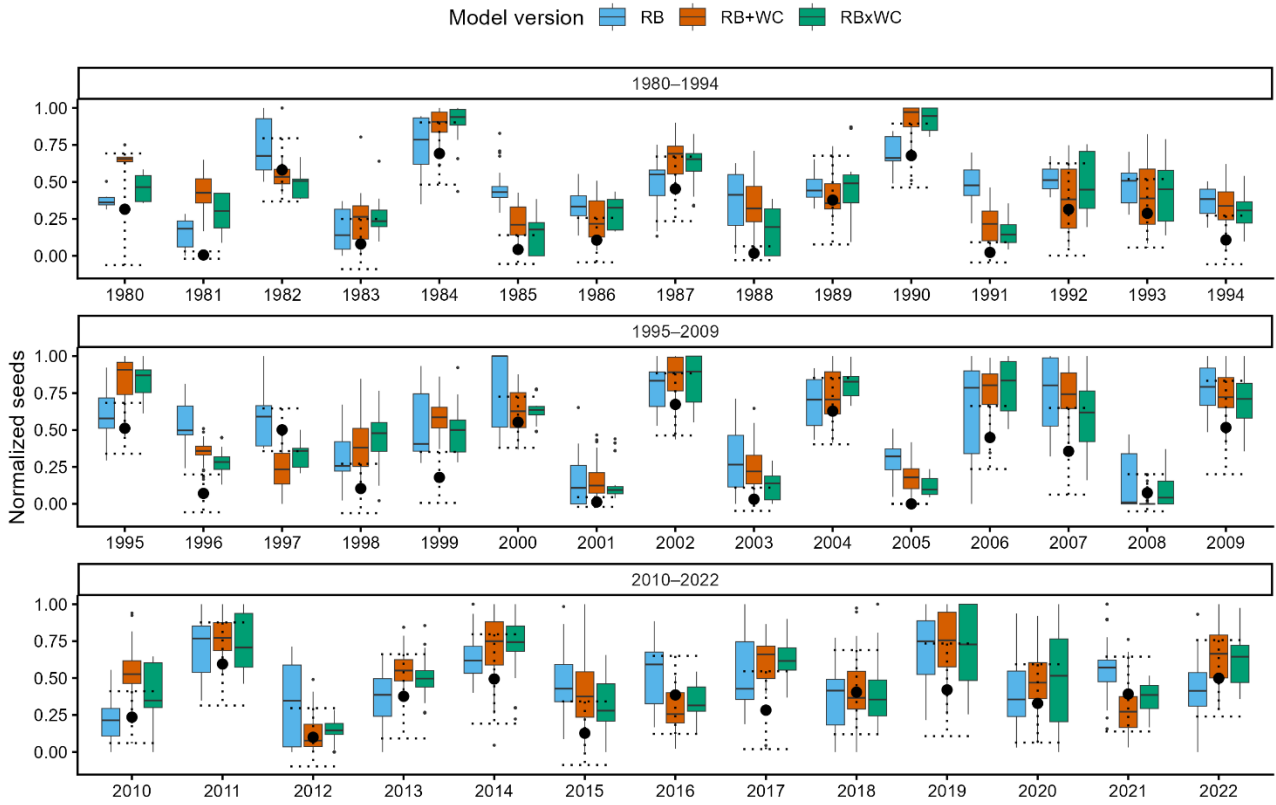
955 **S3. Study sites overview**



956

957 **Figure S3.** Geographic distribution and characteristics of the 11 UK beech study sites. Left panel:
 958 site locations across England. Right panel: site-level summary statistics including number of
 959 monitored trees (after excluding trees with fewer than 10 years of observations), observation period,
 960 and total number of seed production records
 961

962 **S4. Time series of observed and simulated data for the three model versions**

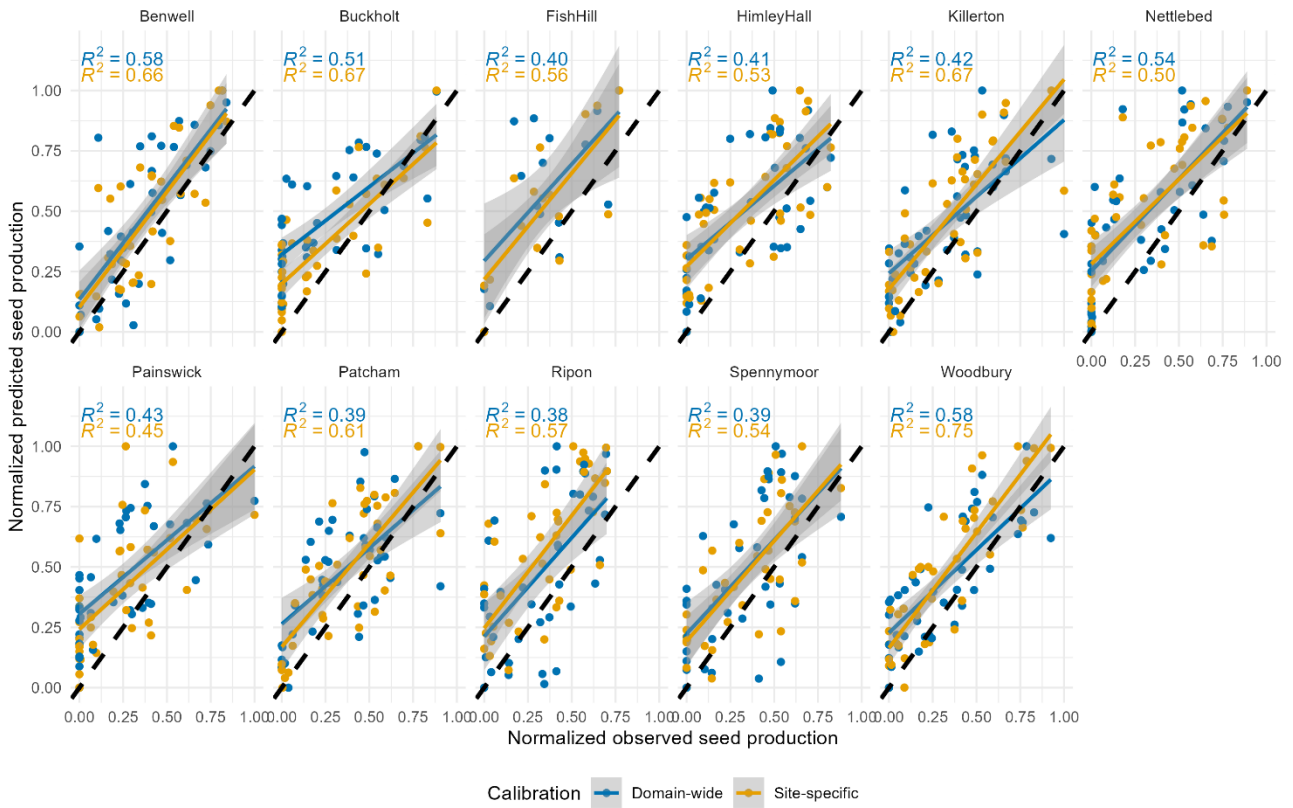


963
 964 **Figure S4.** Time series of observed and simulated normalised seed production across model
 965 formulations. Each panel covers a sub-period of the calibration window (1980–1994,
 966 1995–2009, 2010–2022). For each year, boxplots show the distribution of simulated normalised seed production
 967 across trees and sites for the three model formulations: resource budget only (RB; blue), resource
 968 budget with additive weather cues (RB+WC; orange), and resource budget with interactive weather
 969 cues (RB×WC; green). Boxes span the interquartile range, horizontal lines indicate the median,
 970 whiskers extend to 1.5× the interquartile range, and dots indicate outliers. Filled circles show the
 971 mean observed normalised seed production across sites for each year.
 972

973 Simulated and observed normalised seed production are compared annually across the full calibration
 974 period in Figure S4. All three formulations reproduce the broad interannual structure of the observed
 975 time series, with mast years (e.g., 1992, 2002, 2014, 2019) generally associated with higher simulated
 976 values and failure years (e.g., 1995, 2001, 2012) with lower ones. The RB formulation tends to
 977 produce narrower distributions and less extreme low values, consistent with the absence of a direct
 978 cue mechanism. The cue-informed formulations (RB+WC and RB×WC) show greater year-to-year
 979 variability and more frequent alignment between simulated distributions and observed values,
 980 particularly in mast years. Across all formulations, low-production years are less well captured than
 981 high-production years, with observed near-zero values often falling below the lower tail of the
 982 simulated distribution.
 983

984 **S5. Site-level model performance under site-specific and domain-wide parameterisation**

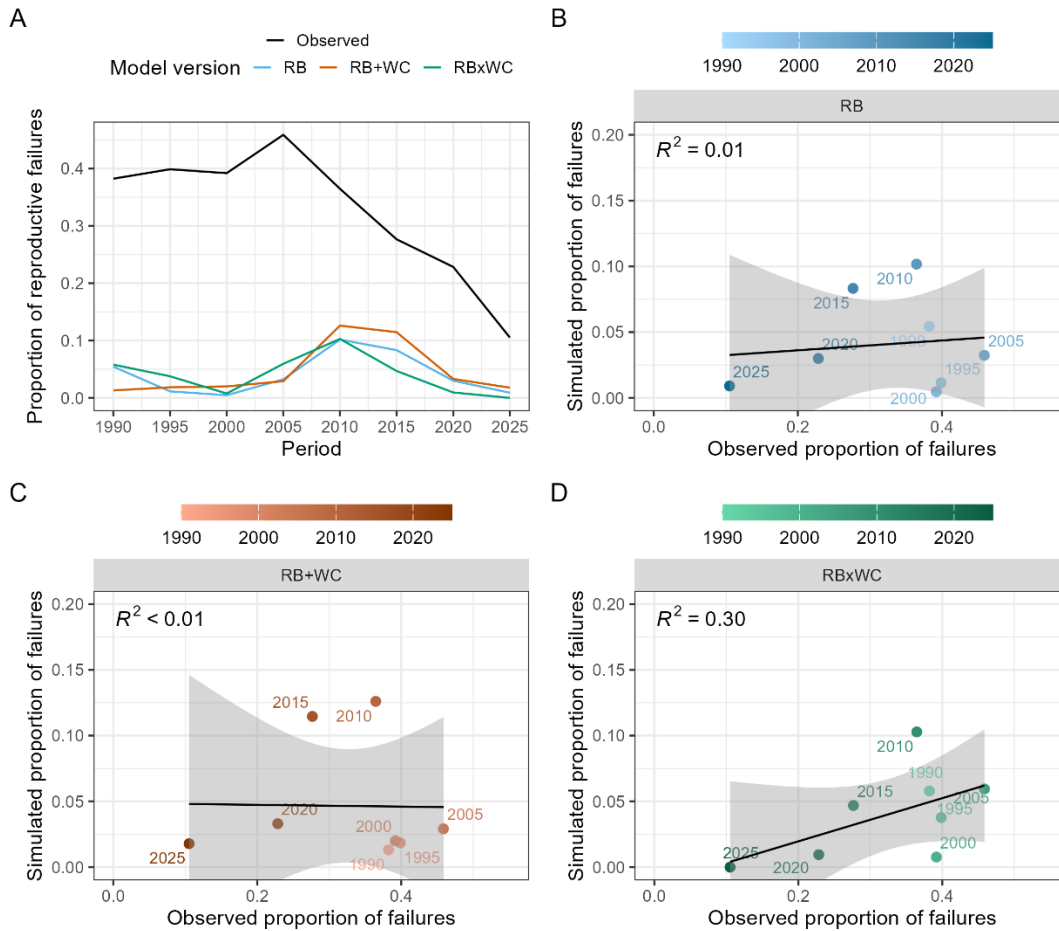
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987 **Figure S5.** Site-level model performance under site-specific and domain-wide parameterisation
 988 strategies for the RBxWC formulation. Each panel shows the relationship between observed and
 989 simulated normalised seed production at a single site, with separate regression lines for site-specific
 990 (orange) and domain-wide (blue) calibration. R^2 values are reported for each strategy. The dashed 1:1
 991 line denotes perfect agreement. Domain-wide calibration uses a single parameter set estimated jointly
 992 across all sites; site-specific calibration optimises parameters independently per site.

993 Model performance was robust to the choice of parameterisation strategy. Under domain-wide
 994 calibration — where a single parameter set was estimated jointly across all 11 sites — the RBxWC
 995 formulation retained most of its predictive skill, with site-level R^2 values ranging from 0.39 to 0.58,
 996 compared to 0.45–0.75 under site-specific calibration (Figure S5). The reduction in performance was
 997 modest and consistent across sites, suggesting that the model captures processes that are largely
 998 transferable across the UK beech network rather than site-idiosyncratic responses. This result
 999 supports the use of domain-wide parameterisation for operational forecasting at unsampled locations.

1000 **S6. Temporal dynamics of reproductive failure across model formulations**



1001

1002 **Figure S6.** (A) Observed and simulated proportion of reproductive failure years (defined as
 1003 normalised seed production < 0.05) computed over 10-year moving windows with a 5-year step,
 1004 reported as the final year of each window (e.g., 1990 corresponds to 1980–1990). The black line
 1005 shows observed dynamics; coloured lines show simulations for RB (blue), RB+WC (orange), and
 1006 RBxWC (green). (B–D) Relationship between observed and simulated failure proportions across time
 1007 windows for each model formulation. Point color indicates the time window, ranging from light
 1008 (earlier periods) to dark (more recent periods). Solid lines show fitted linear regressions with 95%
 1009 confidence intervals.

1010

1011 The proportion of reproductive failure years declined substantially over the study period, from
 1012 approximately 0.39 around 1990 to 0.11 by 2025 (Figure S6A). All three model formulations
 1013 underestimated failure frequency throughout the series, with simulated values remaining below 0.13
 1014 across all periods and all formulations, well below the observed range. Agreement between simulated
 1015 and observed failure proportions across time windows was poor for RB ($R^2 = 0.01$) and RB+WC (R^2
 1016 < 0.01), with both formulations showing no meaningful correspondence with the temporal ordering
 1017 of observed failure rates. The RBxWC formulation showed modest but non-trivial improvement (R^2
 1018 $= 0.30$; Figure S6D), correctly associating more recent low-failure periods with lower simulated
 1019 failure frequencies, though it still failed to reproduce the magnitude of the observed decline. These
 1020 results are consistent with the CVp analysis and confirm that the long-term reduction in reproductive
 1021 variability, including both the weakening of interannual variation and the decline in failure frequency,
 1022 is not captured by any of the current model formulations.