

1 **SUPERORGANISMAL ANISOGAMY: A COMPARATIVE TEST OF AN**  
2 **EXTENDED THEORY**

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7 **TEASER**

8 Behold the mighty ant queen and her tiny male consort. The eggs and sperm of their colony.  
9 But are they really? We investigate how well this metaphor works by developing theory to  
10 explain the evolution of anisogamy and comparatively testing it with data on queen-male size  
11 dimorphism in ants. Read on to discover some parallels and idiosyncrasies of evolution at  
12 life's different hierarchical levels.

13  
14 **ABSTRACT**

15 Multicellular organisms and superorganisms (e.g., ant colonies) are both products of major  
16 evolutionary transitions in individuality, and they share many analogous traits. Theory  
17 developed to explain the evolution of one such trait, anisogamy, has recently been adapted to  
18 explain its superorganismal analogue: large egg-like queens and small sperm-like males. To  
19 test this theory with comparative data, we first extended it to incorporate variation in how  
20 colonies with multiple queens arise. We then used data from 732 ant species to investigate the  
21 effects of colony size, worker caste number, and queen number on queen size (thorax  
22 volume) and queen-male dimorphism. Queen size and queen-male size dimorphism both  
23 increased with colony size and number of worker castes, consistent with predictions.  
24 Contrary to predictions, queen size and queen-male size dimorphism were not associated with  
25 queen number. To further understand the commonalities and idiosyncrasies of evolution at  
26 different hierarchical levels, future work should consider the adaptive and non-adaptive  
27 causes for correlated evolution between queen and male, and egg and sperm sizes.

28 **Keywords:** mixed model, sexual size dimorphism, polygyny, group size, eusociality, gamete  
29 competition, castes

30  
31 **INTRODUCTION**

32 A recurrent theme in the history of life on Earth has been for entities to transition from  
33 independent to group-level replication (Huxley 1912; Maynard Smith and Szathmáry 1995).  
34 The transitions from single celled to multicellular life and from solitary insects to  
35 superorganisms are archetypal examples. These major transitions required similar  
36 evolutionary problems to be solved and gave rise to many analogous traits (Bourke 2011;  
37 West et al. 2015; Boomsma 2022). Consequently, it has been argued that theory developed to  
38 explain the evolution of multicellular traits could be applied to their superorganismal  
39 equivalents, and vice versa (Wiernasz and Cole 2009; Helanterä 2016; Kennedy et al. 2017).  
40 This has been done verbally (Helanterä 2016) and mathematically modelled (Lehtonen and  
41 Helanterä 2020) for the superorganismal equivalent of anisogamy: large queens and small  
42 males. To validate the approach of applying theory from one major transition to another, we  
43 now need an empirical test of the model's predictions.

44 The superorganismal anisogamy model (Lehtonen and Helanterä 2020) predicts that queen  
45 size is a function of three parameters:  $x^* = \alpha + (\beta / K^2)$ . The  $\alpha$  parameter controls the  
46 relationship between individual size and survival,  $\beta$  controls the relationship between queen  
47 size and colony survival, and  $K$  is the number of queens. Male size is a function of just one  
48 parameter:  $y^* = \alpha$ . From this, the following predictions can be made. First, queen size should  
49 increase with colony size and worker caste number. This is because larger, more complex  
50 colonies need more starting resources to survive, resulting in a larger  $\beta$  term. Second, queen  
51 size should decrease rapidly with increasing queen number. When there are multiple queens  
52 (polygyny), colony survival depends on the sum of their resources. Third, queen size and  
53 male size should evolve independently of each other. This is because males do not contribute  
54 to colony survival once the queen is fertilised. Queens should, therefore, be larger than males  
55 in species with large colonies with multiple worker castes, but the size difference will depend  
56 on the number of queens per colony.

57 The superorganismal anisogamy model is analogous but not identical to gamete competition  
58 models for the evolution of anisogamy. While there are several such models (e.g., Kalmus  
59 1932; Scudo 1967; Parker et al. 1972; Knowlton 1974), the most closely analogous to ours is  
60 the game theoretical model of Bulmer and Parker (2002). The  $\alpha$  and  $\beta$  parameters of these  
61 two models are analogous: in Bulmer and Parker (2002) the  $\alpha$  parameter controls the  
62 relationship between gamete size and gamete survival, and  $\beta$  controls the relationship  
63 between initial zygote size and offspring survival. There is no analogue for the number of  
64 queens ( $K$ ) described above. Broadly speaking, in anisogamy theory  $\beta$  is hypothesised to be  
65 correlated with multicellular complexity, while  $\alpha$  is not, because a gamete remains a single  
66 cell by definition, regardless of how complicated the adult organism is. Similarly,  $\beta$  here is  
67 hypothesised to be correlated with colony complexity, while  $\alpha$  is not, assuming that the  
68 requirements of the body plan of an individual are not directly related to how complicated the  
69 colony is.

70 In the original superorganismal anisogamy theory (Lehtonen and Helanterä 2020), multi-  
71 queen colonies arise when two or more queens co-found a colony. This is known as primary  
72 polygyny. However, multi-queen colonies can also arise via secondary polygyny (Hölldobler  
73 and Wilson 1977; Bourke and Franks 1995). This occurs when new queens remain in their  
74 natal colony, join an existing colony, or when colonies fuse. As secondary polygyny appears  
75 to be more common in ants than primary polygyny (Boomsma et al. 2014; Bell-Roberts et al.  
76 2024), we modified the original superorganismal anisogamy theory to determine what effect  
77 this has on the evolution of queen size and queen-male dimorphism. We describe this  
78 modification below and report how it changes the model's predictions. We then test these  
79 predictions using a phylogenetic comparative analysis across 732 ant species.

80

## 81 MODEL

82 The superorganismal anisogamy theory is built on the idea that dispersing males and future  
83 queens are analogous to the gametes of multicellular organisms, i.e. sperm/eggs or  
84 pollen/seeds. Once mated, queens form an incipient colony which is equivalent to a zygote.  
85 This zygote-like stage makes the superorganismal life cycle similar to that of multicellular  
86 organisms. Queen size is under selection because colony survival depends on colony growth  
87 rate – the number of workers produced (the equivalent of somatic growth). Larger queens  
88 produce more workers, increasing colony survival through the initial growth period.

89 The model was built by adapting gamete competition theory to fit the reproductive biology of  
90 superorganisms. Gamete competition theory examines the requirements for the evolution of  
91 anisogamy in relation to size-specific survivorship of gametes and zygotes. In the

superorganismal case, we are interested in size-specific survivorship of queens, males, and incipient colonies, and how this leads to queen–male dimorphism.

**Table 1.** Model notation.

Variable / parameter	Notation	Notes
probability a queen founds a colony alone	$p$	
total resource allocation to queens and males	$M$	allocation to queens and males assumed equal
resources allocated to a single queen: resident value (mutant value)	$x (\hat{x})$	determines queen size
resources allocated to a single male: resident value (mutant value)	$y (\hat{y})$	determines male size
number of queen offspring: resident value (mutant value)	$n_x (\hat{n}_x)$	$n_x = M/x$
number of male offspring: resident value (mutant value)	$n_y (\hat{n}_y)$	$n_y = M/y$
parameter controlling relationship between individual size and individual survival (analogous to gamete survival)	$\alpha$	assumed to be the same for queens and males
parameter controlling relationship between queen size and colony survival (analogous to zygote survival)	$\beta$	
individual survival to mating and colony founding	$g(z) = e^{-\alpha/z}$	$z$ stands for $x, y, \hat{x}, \hat{y}$
colony survival	$s(z) = e^{-\beta/z}$	$z$ stands for $x$ or $\hat{x}$ except when there are multiple queens

We begin by writing the fitness functions for queens and males for the original model (these correspond to equations 2.1 and 2.2 in Lehtonen and Helanterä (2020), see Table 1 for notation):

$$g(\hat{x})s(\hat{x}) \quad (1.1)$$

$$g(\hat{y}) \frac{n_x g(x)s(x)}{n_y g(y)} \quad (1.2)$$

The fitness of a mutant daughter is the product of her own survival  $g(\hat{x})$  to colony founding and the survival of the colony  $s(\hat{x})$ . For a mutant son, average fitness is the quotient of the number of successfully founded colonies  $n_x g(x)s(x)$  and the number of males surviving to mate  $n_y g(y)$  (which yields the mean number of colonies founded by a mating male), multiplied by the probability  $g(\hat{y})$  that the mutant son itself survives to mate. We incorporate secondary polygyny by introducing the parameter  $p$  which is the probability a queen founds a colony alone. Fitness of a mutant daughter is then found by multiplying mutant offspring fitness by the probability  $p$  a queen founds a colony alone. Now, the fitness of a mutant daughter is the product of the probability she starts a new colony alone  $p$  multiplied by the fitness defined in equation (1.1), plus the probability she takes advantage of an existing colony  $(1 - p)$ , in which case she only has to survive to this point (probability  $g(\hat{x})$ ) because the colony has already been successfully founded. Fitness of mutant sons follows the logic of equation (1.2), taking into account the fitness output from both newly founded colonies and ‘exploited’ colonies: fitness of a mutant son is simply its probability of surviving to mate, multiplied by fitness per male surviving to mate.

$$pg(\hat{x})s(\hat{x}) + (1 - p)g(\hat{x}) \quad (2.1)$$

$$g(\hat{y}) \frac{n_x (pg(x)s(x) + (1-p)g(x))}{n_y g(y)} \quad (2.2)$$

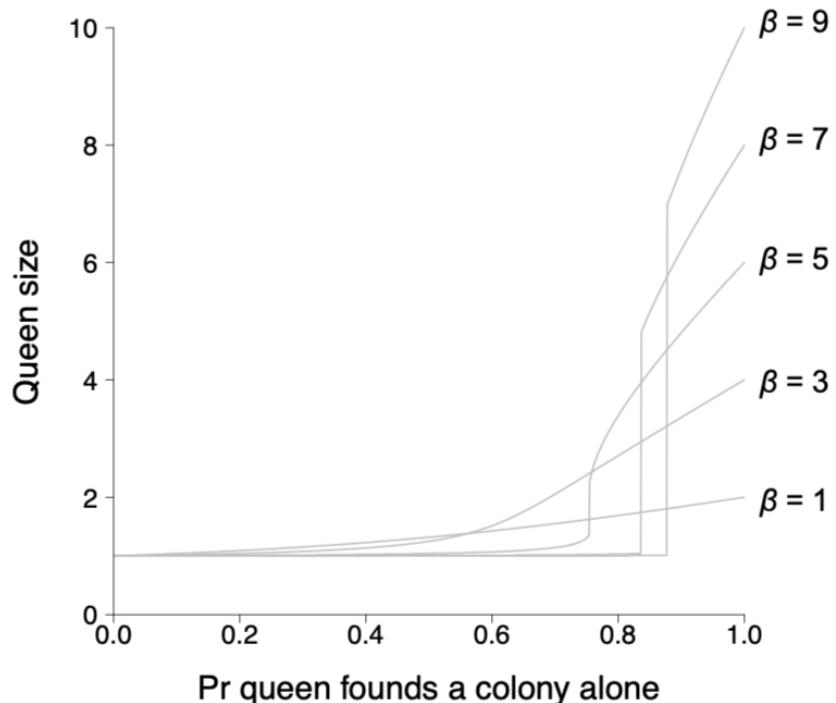
The total fitness a focal mother gains via mutant offspring is:

$$\hat{w}_x = \hat{n}_x (pg(\hat{x})s(\hat{x}) + (1 - p)g(\hat{x})) \quad (3.1)$$

$$\hat{w}_y = \hat{n}_y g(\hat{y}) \frac{n_x (pg(x)s(x) + (1-p)g(x))}{n_y g(y)} \quad (2.2)$$

We solved these equations numerically by substituting the functions from Table 1 and finding the values of the evolving traits that maximise fitness (see supplementary material for matlab code). We hold  $\alpha$  constant, because this is assumed to be equivalent for queens and males but

124 allow  $\beta$  to vary from one to nine and  $p$  between 0 and 1. The numerically calculated  
125 equilibria are shown in Figure 1.



126  
127 **Figure 1.** Queen size as a function of the probability a queen starts a new colony alone ( $p$ ). The value  
128 of  $\beta$  increases from one to nine while  $\alpha$  is fixed at one. The effect of increasing  $\alpha$  is to shift the  
129 intercept of each slope upwards.

130 When queens always start a new colony alone ( $p = 1$ ), the results coincide with the original  
131 model ( $\text{queen size } x^* = \alpha + \beta$ ), which shows that queens are larger when  $\beta$  is higher. When  
132 queens sometimes forgo independent colony founding and instead join / remain in an existing  
133 colony ( $p < 1$ ), queen size increases with  $p$ , but the rate of increase is moderated by  $\beta$  (Figure  
134 1). When  $\beta$  is low, queen size increases gradually as the probability of founding a new  
135 colony alone increases. When  $\beta$  is high, queens remain small until a threshold probability of  
136 founding a new colony alone is reached ( $p > 0.8$ ). At this point queens increase rapidly in  
137 size. When queens never start a new colony alone ( $p = 0$ ), queen size is equal to  $\alpha$ . This  
138 seems biologically unrealistic, however. If there are no primary foundresses in the  
139 population, secondary polygyny could not exist as there are no colonies to remain in.

140 Regarding predictions, if queens sometimes join or remain in an existing colony ( $p < 1$ ),  
141 queens should be smaller, whatever the value of  $\beta$ . This will reduce the extent of queen-male  
142 size dimorphism in multi-queen colonies compared with single queen colonies. When  
143 colonies need more starting resources to survive, i.e.  $\beta$  is high – which is assumed to be the  
144 case for large, complex colonies – large queens are only expected if the probability of  
145 founding a colony alone is high. Overall, the original predictions that queen size should  
146 increase with colony size and worker caste number, but decrease with queen number, remain  
147 unchanged. These effects may be more difficult to detect under secondary polygyny,  
148 however, because of the threshold effect.

149

## 150 COMPARATIVE TEST

### 151 Methods

152 *Overview*

153 Our phylogenetic comparative analysis to test the predictions of the superorganismal  
154 anisogamy model involved three steps: i) collecting data on queen and male ant sizes from  
155 digital museum images; ii) collecting data on colony size, worker caste number, and queen  
156 number for as many of these species as possible from published databases; iii) building  
157 statistical models to determine the effects of colony size, worker caste number, queen  
158 number, and their interactions, on the evolution of queen size and queen-male dimorphism.

159 *Data Collection*

160 Queen and male sizes were estimated from images on Antweb. One queen and one male per  
161 species were measured, using type specimens when possible. Two measurements were taken  
162 for each individual: maximum mesosoma (alitrunk) width and length. Scale bars on the full-  
163 sized images allowed the measurements to be taken at a resolution of < 0.05 mm. Queen and  
164 male volumes were then approximated as mesosoma (thorax) volume ( $width \times length$ )<sup>3/2</sup>  
165 and natural log transformed. In total, we obtained data on queen and male sizes for 732  
166 species (Table S1). Queen-male dimorphism was calculated as: log queen thorax volume –  
167 log male thorax volume. Positive values indicate that queens are larger than males, negative  
168 values that males are larger than queens.

169 Data on colony size, worker caste number, and queen number were extracted from the  
170 comparative database compiled by Bell-Roberts et al. 2024. This database consists of 794 ant  
171 species and was assembled using previous comparative analyses on ants (Hölldobbler and  
172 Wilson 1990; Hughes et al. 2008; Burchill and Moreau 2016; Blanchard and Moreau 2017),  
173 the Global Ant Genomics Alliance database (Vizueta et al. 2025), and via keyword searches  
174 in Google Scholar. Colony size is the number of workers in mature colonies and queen  
175 number is the average number of queens observed per colony. Worker caste number was  
176 treated as a binary trait with species having one or more than one non-reproductive caste.  
177 Species-level averages were taken when multiple estimates of these parameters were reported  
178 per species. In total, colony size estimates were available for 154 of the species in our data  
179 set, worker caste number for 187 species, and queen number for 52 species. For 46 species  
180 we had data on both colony size and queen number, and for 46 species we had data on both  
181 worker caste number and queen number. Consequently, sample sizes vary between analyses  
182 (Table S1). Our dataset excludes species that are supercolonial, social parasites or  
183 parthenogens, species with gamergates and species that use inter-lineage hybridization for  
184 caste determination. These species violate the assumptions of the superorganismal anisogamy  
185 model.

186 We sampled 50 trees at random from the posterior distribution of ant phylogenies from  
187 Economo et al. (2018). Each tree was pruned to match the 732 species in our data set using  
188 the *Ape* R package (Paradis and Schliep 2019). Phylogenetic uncertainty was account for by  
189 running all analyses described below across these 50 trees.

190 *Statistical Analyses*

191 We plotted the phylogenetic distribution of queen-male dimorphism onto one of the  
192 phylogenies chosen at random. Ancestral states were estimated on this phylogeny using  
193 maximum likelihood, corresponding to a Brownian motion model of trait evolution, in the  
194 *Phytools* R package (Revell 2024). This was done for data visualisation only. Bayesian  
195 Phylogenetic Mixed Models (BPMMS) with parameter expanded priors for random effects  
196 were used for our analyses (*MCMCglmm* R package, Hadfield 2010). We investigated the  
197 sensitivity of our results to the choice of prior by re-running all the models described below  
198 with an inverse Gamma prior. The results from these analyses are quantitatively similar and  
199 are reported in Table S2.

200 To estimate the phylogenetic correlation between queen size and male size, we used a multi-  
201 response BPMM. Our response variables were queen thorax volume and male thorax volume  
202 (both natural log transformed, Gaussian). The global intercept was removed to estimate trait-  
203 specific intercepts. We estimated the phylogenetic and residual (co)variances in these traits  
204 by fitting two  $2 \times 2$  unstructured variance-covariance matrices (R code: *phylo\_r\_mods*). The  
205 phylogenetic correlation between queen size and male size was then calculated as

206  $s_{x,y}/\sqrt{s_x^2 s_y^2}$ . Where  $s_{x,y}$  is the covariance between queen size and male size and  $s_x^2$  and  $s_y^2$   
207 the variances. We estimated the major axis regression slope of the phylogenetic relationship  
208 (Warton et al. 2006) between queen size and male size as  $(1/2s_{x,y}) \left( s_y^2 - s_x^2 + \right.$   
209  $\left. \sqrt{(s_y^2 - s_x^2)^2 + 4s_{x,y}^2} \right)$ .

210 The effects of colony size, worker caste number, and queen number on queen size were  
211 determined using five models. In each model, queen thorax volume (natural log transformed)  
212 was the response variable (Gaussian) and phylogeny was included as a random effect. Colony  
213 size (natural log transformed) was the fixed effect in the first model (R code: *qn\_col\_mods*),  
214 worker caste number (binary) was the fixed effect in the second model (R code:  
215 *qn\_caste\_mods*), and queen number (natural log transformed) was the fixed effect in the third  
216 model (R code: *qn\_num\_mods*). In the fourth model, we fit the interaction between colony  
217 size and queen number (both natural log transformed; R code: *qn\_int\_mods*) and in the fifth  
218 model we fit the interaction between worker caste number and queen number (natural log  
219 transformed; R code: *qn\_cqn\_mods*). These interactions allow the relationship between queen  
220 size and our proxies of  $\beta$  (colony size and worker caste number) to be moderated by queen  
221 number, in line with our theoretical finding that large queens are only expected when  $\beta$  is  
222 high and queens have a high probability of founding a new colony alone.

223 To determine the effects of colony size, worker caste number, and queen number on queen-  
224 male dimorphism, we repeated these five models but with queen-male dimorphism in thorax  
225 volume (Gaussian) as the response variable (R code: *di\_col\_mods*, *di\_caste\_mods*,  
226 *di\_num\_mods*, *di\_int\_mods*, *di\_cqn\_mods*). We modelled the effects of colony size, caste  
227 number, and queen number separately, as well as their interactions, because main effects in  
228 models with interactions are conditional, representing the effect of each variable on the  
229 response when the other fixed effect is zero.

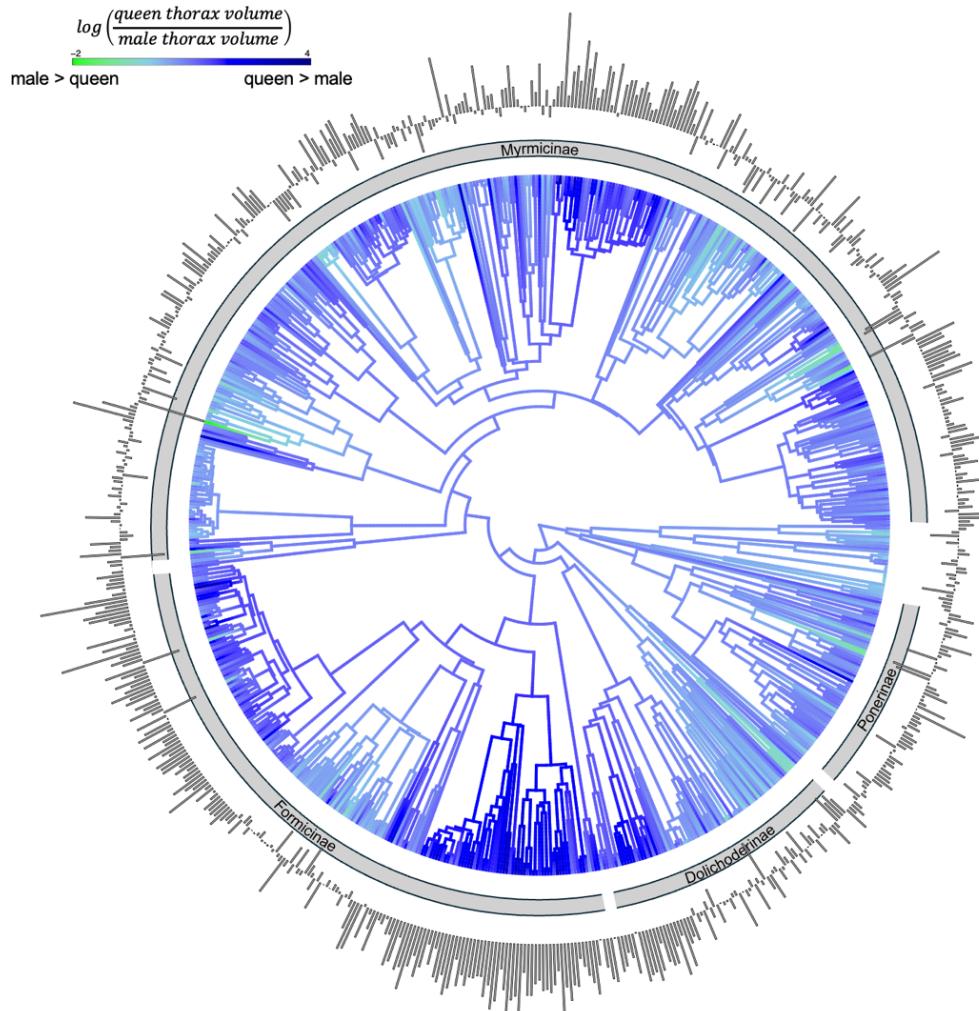
230 Each BPMM described above was run on each of the 50 ant phylogenies we sampled. The  
231 number of iterations per tree was 1 100 000 with a burn-in of 100 000 iterations and a  
232 thinning interval of 1000 iterations, giving a posterior distribution of 1000 iterations (and an  
233 effective sample size of 1000 for each parameter in our preliminary analyses). Twenty  
234 iterations were then sampled from each tree (every 50<sup>th</sup>) and combined to give 1000 iterations  
235 in total (i.e. 20 \* 50) in the posterior distribution of each parameter. Model convergence was  
236 examined by calculating the degree of autocorrelation between posterior samples and by  
237 inspecting traces of posterior distributions. Posterior modes and 95% credible intervals (CI)  
238 from the posterior distributions of each parameter are reported in the results. Significance is  
239 based on whether the CI includes zero. We report the phylogenetic heritability ( $H^2 =$   
240 phylogenetic variance / total variance) of each model in the results. Full details are provided  
241 in the supplementary R code.

242

## 243 Results

244 Queen thorax volume was larger than male thorax volume in 72% of the 732 measured  
245 species (Figure 2). There was a strong phylogenetic correlation between log transformed

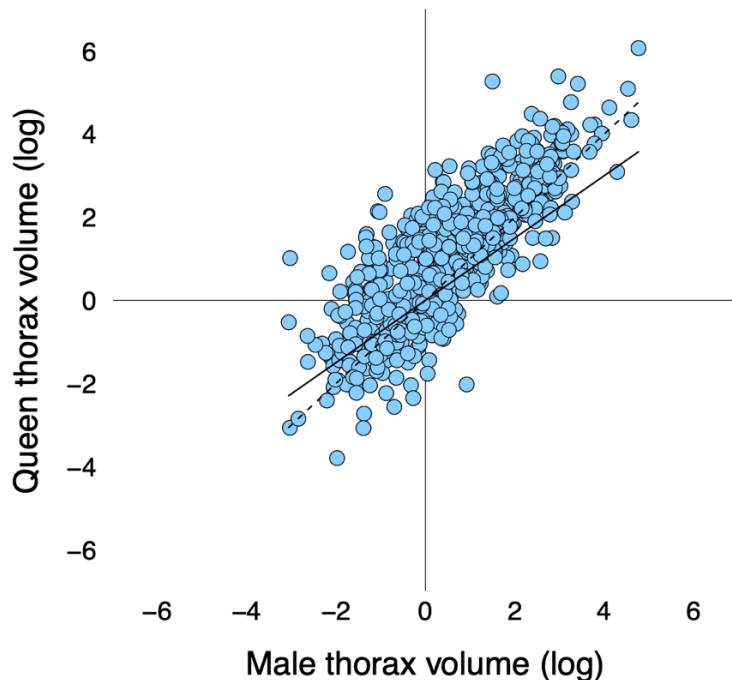
246 queen and male thorax volumes (phylogenetic  $r = 0.92$ , CI = 0.87 to 0.94, N = 732 species).  
 247 Both queen and male thorax volumes (log transformed) showed high phylogenetic heritability  
 248 (queen phylo  $H^2 = 0.82$ , CI = 0.74 to 0.89; male phylo  $H^2 = 0.83$ , CI = 0.74 to 0.89). This  
 249 indicates that queens of closely related species tend to have similar thorax volumes, and  
 250 likewise for males.



251  
 252 **Figure 2.** The phylogenetic distribution of queen-male dimorphism in thorax volume across 732 ant  
 253 species. Outward-facing bars indicate that queens are larger than males, inward-facing bars that males  
 254 are larger. Branches are coloured by the degree of ancestral dimorphism (blue: queen > male, green:  
 255 male > queen).

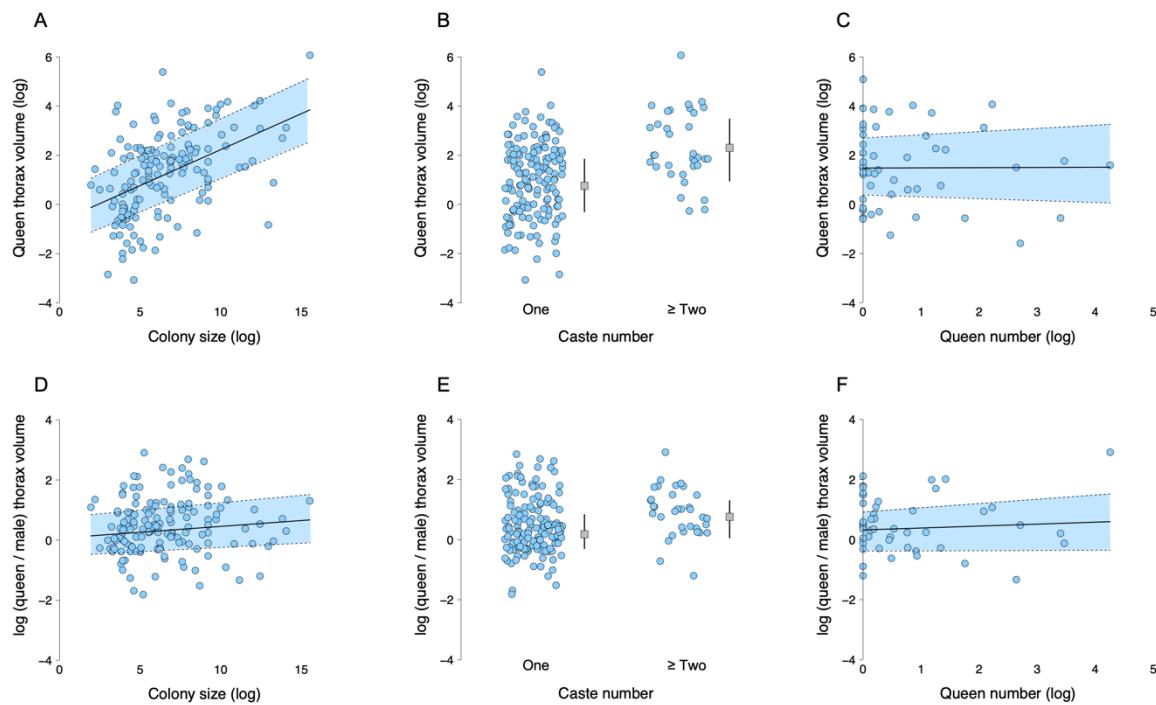
256 The evolutionary allometry between log transformed queen and male thorax volumes was  
 257 negative (major axis slope = 0.75, CI = 0.62 to 0.93, N = 732 species; Fig 3), indicating that  
 258 increases in male thorax volumes have been proportionally larger than increases in queen  
 259 thorax volume through evolutionary time.

260 Across species, queen thorax volume (log) increased significantly as colony (log) size  
 261 increased (slope = 0.29, CI = 0.21 to 0.38, N = 154 species; Figure 4a; Table 2). Queens from  
 262 species with two or more worker castes were significantly larger than those with one worker  
 263 caste (difference = 1.27, CI = 0.77 to 1.96, N = 187 species, Figure 4b; Table 2). Queen  
 264 thorax volume (log) was not associated with queen number (slope = -0.03, CI = -0.27 to 0.33,  
 265 N = 51 species; Figure 3c; Table 2). The relationship between queen thorax volume (log) and  
 266 colony size (log) was not moderated by queen number (interaction = 0.00, CI = -0.09 to 0.11,  
 267 N = 46 species; Table 2) and neither was the relationship between queen thorax volume (log)  
 268 and worker caste number (interaction = 0.31, CI = -0.36 to 0.84, N = 46 species; Table 2).



269

270 **Figure 3.** The evolutionary allometry between queen thorax volume (log)  
 271 and male thorax volume (log) was negative. The solid line is the estimated major axis slope  
 272 (0.75), the dashed line is the isometric slope (1). Each point is a different species (N = 732).



273

274 **Figure 4.** Queen thorax volume (log) was significantly larger in species that *a*) formed larger colonies  
 275 (N = 154 species) and *b*) had more than one worker caste (N = 187 species), but *c*) was not associated  
 276 with log queen number (N = 51 species). Queen-male dimorphism in thorax volume increased *d*) non-  
 277 significantly with increasing log colony size (N = 154 species), *e*) significantly with worker caste  
 278 number (N = 187 species), and *f*) was not associated with log queen number (N = 51 species). Each  
 279 point is a different species. Regression lines and 95% CIs are plotted in A, C, D and F. The mean and  
 280 95% CI are shown in B and E.

281  
282**Table 2.** Parameter estimates from the five BPMMs examining queen thorax volume (log) in relation to colony size (log), worker caste number, queen number (log), and their interactions.

Fixed terms	Parameter	Estimate	Lwr CI	Upr CI	Phylogenetic $H^2$
<i>log colony size (N = 154 species)</i>	intercept	-0.76	-2.00	0.34	0.87
	slope	0.29	0.21	0.38	
<i>caste number (N = 187 species)</i>	intercept	0.76	-0.30	1.84	0.85
	slope	1.27	0.77	1.96	
<i>log queen number (N = 51 species)</i>	intercept	1.58	0.38	2.70	0.90
	slope	-0.03	-0.27	0.33	
<i>log colony size x log queen number (N = 46 species)</i>	intercept	-0.09	-1.77	1.35	0.87
	colony size slope	0.25	0.06	0.46	
	queen number slope	0.16	-0.77	0.80	
<i>caste number x log queen number (N = 46 species)</i>	intercept	1.36	0.40	2.28	0.85
	caste number slope	0.68	-0.06	2.15	
	queen number slope	-0.19	-0.51	0.27	
	interaction	0.31	-0.36	0.84	

283

Queens were increasingly larger than males as colony size increased (slope = 0.04, CI = -0.02 to 0.09, N = 154 species; Figure 4d; Table 3), although this relationship was not statistically significant. Dimorphism was significantly higher in species with two or more worker castes than those with one worker caste (difference = 0.33, CI = 0.04 to 0.75, N = 187 species; Figure 4e; Table 3). Queen-male dimorphism was not associated with queen number (slope = 0.07, CI = -0.14 to 0.26, N = 51 species; Figure 4f; Table 3) and the relationship between queen-male dimorphism and log colony size was not moderated by queen number (interaction = -0.03, CI = -0.11 to 0.04, N = 46 species; Table 3). The relationship between queen-male dimorphism and worker caste number was moderated by queen number: dimorphism tended to decrease with queen number in species with one worker caste, whereas dimorphism increased with queen number in species with more than one worker caste (interaction = 0.54, CI = 0.20 to 1.09, N = 46 species; Table 3).

**Table 3.** Parameter estimates from the five BPMMs examining queen-male dimorphism in thorax volume in relation to colony size (log), worker caste number, queen number (log), and their interactions.

Fixed terms	Parameter	Estimate	Lwr CI	Upr CI	Phylogenetic $h^2$
<i>log colony size (N = 154 species)</i>	intercept	0.13	-0.68	0.73	0.76
	slope	0.04	-0.02	0.09	
<i>caste number (N = 187 species)</i>	intercept	0.18	-0.29	0.83	0.75
	slope	0.33	0.04	0.75	
<i>log queen number (N = 51 species)</i>	intercept	0.29	-0.38	0.92	0.74
	slope	0.07	-0.14	0.26	
<i>log colony size x log queen number (N = 46 species)</i>	intercept	0.33	-0.67	1.28	0.70
	colony size slope	-0.03	-0.15	0.13	
	queen number slope	0.35	-0.14	0.94	
<i>caste number x log queen number (N = 46 species)</i>	intercept	-0.03	-0.11	0.04	0.67
	caste number slope	0.38	-0.05	1.09	
	queen number slope	-0.20	-0.48	0.11	
	interaction	0.54	0.20	1.09	

299

300 **DISCUSSION**

301 The superorganismal anisogamy model predicts that ant queens should be largest in species  
302 with large colony sizes, multiple worker castes, and one queen per colony. In contrast, male  
303 size is predicted to be unaffected by colony size and queen number, leading to sexual size  
304 dimorphism which should covary with these parameters. Consistently, we found that queens  
305 are typically larger than males (in 72% of species), and large queens tend to occur in large  
306 colonies (Figure 4a) and in colonies with multiple worker castes (Figure 4b) and that queens  
307 were increasingly larger than males in species with more than one worker caste (Figure 4e).  
308 However, neither queen size (Figure 4c) or queen-male dimorphism (Figure 4f) was  
309 associated with queen number. Queen size and male size were strongly phylogenetically  
310 correlated (Figure 3).

311 According to our theoretical model, large queens should occur most often in species with a  
312 high probability of independent colony founding. We did not find a relationship between  
313 queen number and queen size, however. There are several explanations for this theory-data  
314 mismatch. First, queen number might not capture the probability of independent colony  
315 founding accurately enough. We assumed that queen number is negatively associated with  
316 the probability of independent colony founding, which is likely to be correct, but we lack an  
317 empirical understanding of how steeply this relationship changes. Even in species where a  
318 large proportion of queens disperse, queen number may be high. We also note our dataset  
319 lacks species with extreme queen numbers. In *Formica aquilonia* and *F. polycetena*, for  
320 example, several hundred queens per colony is typical (Rosengren et al. 1993). Second, some  
321 monogynous and polygynous species might found their colonies through temporary social  
322 parasitism (Buschinger 2009; Borowiec et al. 2021). If queens invade heterospecific nests and  
323 parasitize the resident workers, they are less dependent on their own resources for colony  
324 founding, and under weaker selection for increased size. Third, within-species variation in  
325 queen number could mask mean differences in queen size. Many ant species are socially  
326 polymorphic (Boomsma et al. 2014; Boulay et al. 2014; Bell-Roberts et al. 2024) and there is  
327 evidence that queens from multi-queen colonies are smaller than those from single-queen  
328 colonies e.g. in *F. truncorum* (Sundström 1995) and *F. selysi* (Meunier and Chapuisat 2009)  
329 but not in *Myrmica ruginodis* (Wolf et al. 2018). Fourth, queen number is a labile trait in  
330 evolutionary time (Boomsma et al. 2014; Boulay et al. 2014) whereas morphological  
331 evolution is more constrained. Changes in size may lag behind changes in queen number.  
332 Finally, our theory might need revising.

333 Our proxy for queen size might also make it difficult to detect an association between queen  
334 size and number. Thorax volume is thought to be a good approximation of the energetic  
335 resources available to an ant queen during colony founding, due to the histolysis of flight  
336 muscles (Peeters 2012). However, independent colony founding also uses energy from fat  
337 reserves in the abdomen (40-60 % of a queen's mass), and it is possible that queen-male  
338 differences in total body size including abdomen would be more pronounced, even if large  
339 flight muscles evolved to carry this abdominal weight (Helms & Kaspari 2015). Either way,  
340 measures of abdomen volume during colony founding are not available for many species  
341 (Helms & Kaspari 2015) and museum images are not appropriate for approximating this  
342 since collected queens may or may not be from established colonies. That said, our finding  
343 that queen size is associated with both colony size and worker caste number suggests that our  
344 proxy is capturing the necessary variation.

345 An unexpected result was the significant interaction between worker caste number and queen  
346 number (Table 3). Queen-male dimorphism tended to decrease with queen number in species  
347 with one worker caste but increase with queen number in species with more than one worker  
348 caste. This result is in the opposite direction to that predicted. In more complex colonies,  
349 those with more than one worker caste, large queens were only expected when the probability

350 of independent colony founding is high. An outlier in our dataset appears to be driving this  
351 relationship: *Crematogaster pygmaea*. This ant species has twice as many queens per colony  
352 (> 70) as the species with the second most queens. Excluding it from the analysis renders the  
353 interaction non-significant.

354 Our finding that queen and male sizes are phylogenetically correlated is consistent with our  
355 model if  $\alpha$ , which affects male and queen fitness alike, is a more important driver of size  
356 variation than  $\beta$ , which only affects queen fitness. However, we expect  $\beta$  to be influenced by  
357 ecological factors to a much greater extent than  $\alpha$ , and thus our baseline expectation in  
358 relation to the model is that  $\beta$  should be the major driver of variation. There are both adaptive  
359 (correlated selection) and non-adaptive (genetic constraints) explanations for the  
360 phylogenetic correlation of male and queen sizes.

361 First, large size may be favoured in both queens and males, but via different mechanisms.  
362 There is evidence that larger males achieve more matings in mating swarms and males in  
363 species with female calling can survive for several weeks, which could influence their body  
364 size evolution (Boomsma et al. 2005; Shik et al. 2013). As dispersal tends to be male biased  
365 in ants, especially in species with multiple queens (Hakala et al. 2019), larger size may also  
366 be favoured to facilitate active directed flight. It is also possible that large male sizes are  
367 favoured in species with large colonies, if such colonies place demands on large testes or  
368 accessory glands to facilitate colony founding and egg laying. Our finding that males have  
369 larger thorax volumes than queens in 28% of the species we sampled suggests that male size  
370 can be under positive selection.

371 Second, the queen-male phylogenetic correlation could be due to a genetic correlation  
372 between queen and male sizes that constrains dimorphism. However, worker and queen sizes  
373 can be vastly different, and workers themselves can vary considerably from caste to caste  
374 (Hölldobler and Wilson 1990; Bell-Roberts et al. 2024), suggesting that genetic constraints  
375 can be overcome if optimal sizes are divergent enough. The fact that workers, who rear the  
376 brood, control the size of developing individuals also suggests a lack of genetic constraints.  
377 We need more data on the determinants of colony success and variation in male behaviour to  
378 better understand the interplay between divergent selection, genetic correlations and  
379 correlated evolution.

380 Applying the same theory, with appropriate modifications, to different major evolutionary  
381 transitions is a rare undertaking. While broad correlations between queen size and colony size  
382 and complexity in social insects have been discussed in light of social evolution theory (e.g.  
383 Bourke 1999; Matte & LeBoeuf 2025; Bell-Roberts et al 2024), we provide a case study  
384 where we directly apply similar models across levels, in order to uncover similarities and  
385 differences in social evolution across life's hierarchical levels.

386

## 387 **DATA AVAILABILITY**

388 Data, code, and supplementary information currently available here:

389 [https://github.com/pipdowning/SuperOrganismal\\_Anisogamy/tree/main](https://github.com/pipdowning/SuperOrganismal_Anisogamy/tree/main)

390

## 391 **AUTHOR CONTRIBUTIONS**

392 PAD: methodology, formal analysis, investigation, data curation, visualisation, writing –  
393 original draft, writing – review and editing; JL: conceptualization, methodology, formal  
394 analysis, investigation, visualisation, writing – original draft, writing – review and editing;  
395 LB-R: data curation, writing – original draft, writing – review and editing; HH:

396 conceptualization, project administration, data curation,, writing – original draft, writing –  
397 review and editing

398

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402

403 **CONFLICT OF INTEREST**

404 We declare no conflict of interest.

405

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