

# Temperature carryover effect revealed for marine fishes using spatio-temporal distributed lag models

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17 Abstract:

18 Understanding the impact of changing temperature on population densities is necessary to predict  
19 the likely impact of climate anomalies (e.g., marine heatwaves) or forecast distribution shifts  
20 under future climate scenarios. Population densities are often analyzed using spatio-temporal  
21 models (STMs), which typically predict densities based on local habitat conditions while also  
22 estimating latent spatial and spatio-temporal variation. Recent research extends STMs by also  
23 estimating density responses to habitat conditions at nearby locations using a “spatially  
24 distributed lag” (SDL) that averages habitat conditions in the vicinity of samples. Here, we  
25 extend SDL by incorporating insights from diffusion-enhanced STMs to simultaneously estimate  
26 spatially distributed and time-lagged responses to nearby and past habitat conditions (a “spatio-  
27 temporal distributed lag” STDL). We then use summer bottom trawl survey data from the  
28 eastern Bering Sea (1982-2024) to measure whether spatial and/or temporal lags are  
29 parsimonious when predicting population density from temperature anomalies for six  
30 ecologically important fishes. Results show that time-lagged responses are parsimonious,  
31 positive, and substantial (correlation of 0.20-0.83 per year) for five species, and that density  
32 responses to temperature anomalies also diffuse outward over time for four species at 30-53  
33 kilometers per year. A self- and cross-test simulation experiment shows that model selection can  
34 identify the appropriate model and parameter estimates are approximately unbiased. We  
35 therefore conclude that temperature carry-over effects arise in marine fishes and recommend that  
36 future studies include nonlocal and time-lagged responses when measuring density responses to  
37 habitat.

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39 Keywords: Spatial distributed lag; spatio-temporal model; species distribution model; lagged  
40 response; nonlocal response

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42 **Data Availability Statement**

43 We use records of biomass and temperature samples from the eastern Bering Sea bottom trawl  
44 surveys, described by (Markowitz *et al.*, 2022) and downloaded using release 0.0.3 of the  
45 *surveyjoin* package (Ward *et al.*, 2025) with DOI <https://doi.org/10.5281/zenodo.14984411>. All  
46 code required to reproduce the analysis are available publicly online at <https://github.com/James->  
47 [Thorson-NOAA/spacetime-lag](https://github.com/James-Thorson-NOAA/spacetime-lag). We will add a DOI using Zenodo upon acceptance.

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50 **Introduction**

51 The association between animal densities and environmental variation is complicated due  
52 to nonlocal and time-lagged ecological responses. For example, migratory behaviors cause  
53 habitat conditions at one location to affect population densities at geographically distant sites, as  
54 shown by the association between local density and regional climate indices for both butterflies  
55 in California and fishes in the Bering Sea (Pardikes *et al.*, 2015; Thorson, 2019). Similarly,  
56 species interactions and age-structured dynamics result in time-lagged responses. For example,  
57 global variation in plant growth is better explained by climate indices when incorporating time-  
58 lagged responses (Wu *et al.*, 2015) due to delayed responses of the soil community in tallgrass  
59 prairie ecosystems (Arnone III *et al.*, 2008).

60 Species distribution models (SDMs) are widely used in ecology (Elith & Leathwick,  
61 2009) to estimate habitat associations, attribute density changes to habitat changes, and forecast  
62 future distribution under climate scenarios (Thorson & Kristensen, 2024). Missing covariates  
63 and ecological processes (e.g., animal movement) often cause model residuals for SDMs to be  
64 correlated in space or time, and this degrades predictive performance and statistical testing  
65 (Dormann *et al.*, 2007). Recent developments in spatio-temporal generalized linear mixed  
66 models (ST-GLMMs) allow analysts to control for (and condition predictions upon) spatial and  
67 spatio-temporal autocorrelation at high spatial resolution (Thorson & Kristensen, 2024).

68 SDMs generally predict local densities based upon measured habitat at the same place  
69 and time and will therefore neglect the potential role of nonlocal or time-lagged responses. In  
70 past instances when SDMs are designed to test the impact of past or nonlocal environmental  
71 conditions, nonlocal and lagged effects are often tested by comparing multiple covariates at  
72 different scales in a single model, by repeatedly fitting the model with different lagged

73 covariates, and using model selection to identify a single spatial scale or time-lag for covariates  
74 (Wu *et al.*, 2015; Núñez-Riboni *et al.*, 2021; Lindmark *et al.*, 2023). Another option is to use  
75 SDMs to compute time-series representing range shifts, and then apply “temporal distributed  
76 lags” (TDL) to estimate the lagged effect of time-series covariates on range-shift indices (e.g.,  
77 using the package *dlnm*; (Gasparrini *et al.*, 2010)). However, aggregating predictions from  
78 SDMs into an annual index reframes the analysis into a time-series framework, instead of  
79 estimating temporal lags directly within the spatially explicit SDM where spatially and  
80 temporally correlated residuals can be modelled (which *dlnm* is not designed to do).

81 Alternatively, spatio-temporal variation in habitat covariates can be compressed to construct  
82 time-series indices representing habitat variation (e.g., using empirical orthogonal function  
83 analysis), and these indices can be included as covariates using a spatially varying response to  
84 test for nonlocal habitat responses (Thorson, 2019; Thorson *et al.*, 2020). However, this  
85 technique ignores information about the spatial proximity of habitat variation at other sites  
86 affecting local density and therefore cannot estimate the spatial- or time-scale over which nearby  
87 habitat affects local densities.

88 To estimate the influence of nearby habitat on population density, recent ecological  
89 research has integrated “spatially distributed lags” (SDL) into species distribution models (Miller  
90 *et al.*, 2025; Lindmark *et al.*, 2026). SDLs estimate a spatially smoothed transformation of a  
91 given covariate, and then use that transformed covariate to predict the response of a regression  
92 model (e.g., Armstrong, 2006). Similarly, ecologists are developing “temporal distributed lags”  
93 (TDL) (Sollmann, 2024; Lalechère *et al.*, 2025), and discussing the importance of both spatial  
94 and temporal lags in species distribution models (Essl *et al.*, 2024). In parallel, recent statistical  
95 research has efficiently approximated a diffusive process across space and time and used this to

96 define the distribution for a spatio-temporal latent variable (Clarotto *et al.*, 2024; Lindgren *et al.*,  
97 2024). However, we are not aware of any extension re-purposing this diffusive process to define  
98 a spatio-temporal distributed lag for application within a species distribution model.

99 To address this gap, we introduce a computationally efficient model to identify nonlocal  
100 and/or lagged responses to habitat variables by using a “spatio-temporal distributed lag” (STDL)  
101 within an SDM. To ensure that results are applicable in a wide context, we also implement this  
102 while estimating spatial and spatio-temporal latent variables (e.g., using a ST-GLMM). To do so,  
103 we first review recent developments in SDLs and then extend this to incorporate time-lagged  
104 responses using a diffusion-enhanced process. We then demonstrate that time-lagged responses  
105 to temperature anomalies arise for five of six ecologically important fishes in the eastern Bering  
106 Sea, analyzed here from 1982–2024. We conclude by recommending that studies explore using  
107 STDL to incorporate nonlocal and time-lagged responses to thermal habitat when testing for (or  
108 forecasting) climate linkages in population distribution.

## 109 **Methods**

### 110 **Spatially distributed lags**

111 We start by defining a  $J \times T$  covariate matrix  $\mathbf{X}$  where  $x_{jt}$  is the covariate measurement at time  
112  $t \in \{1, \dots, T\}$  and location  $\mathbf{s}_j$  for  $j \in \{1, \dots, J\}$  locations in two-dimensional space within domain  
113  $D$ . We seek a spatio-temporal distributed lag operator  $h$  that transforms covariate matrix  $\mathbf{X}$  to  
114 calculate a transformed  $J \times T$  matrix  $\mathbf{Z} = h(\mathbf{X})$ . We can then interpolate the covariate to  
115 calculate  $x_t^*(\mathbf{s}^*)$  at a new location  $\mathbf{s}^*$  using a  $J$  length interpolation vector  $\mathbf{a}(\mathbf{s}^*)$  where  $x_t^*(\mathbf{s}^*) =$   
116  $\mathbf{a}(\mathbf{s}^*)^T \mathbf{x}_t$ . This operator should have the following properties:

117 1. *Interpretable parameters*: We seek to estimate a parameter  $\kappa_S$  representing the spatial  
 118 distance over which a covariate is smoothed in space (e.g., units of meters) and a separate  
 119 parameter  $\kappa_T$  representing the time-lag over which the covariate is smoothed in time (e.g.,  
 120 units per-year), where the model collapses to no lag in either space or time (i.e.,  $\mathbf{X} = \mathbf{Z}$ ) given  
 121 some value of those parameters. We also discuss a parameter  $\kappa_{ST}$  that controls how a  
 122 location  $x_{j_1 t_1}$  affects a different location  $x_{j_2 t_2}$  at a later time  $t_2 > t_1$  relative to the combined  
 123 effects of  $\kappa_S$  and  $\kappa_T$  (although we do not test its behavior here to simplify the presentation);  
 124 2. *Conservation of mass*: A covariate value  $x_{jt}$  at location  $\mathbf{s}_j$  and time  $t$  is distributed across  
 125 space and time by the STDL operator while leaving its total value (approximately)  
 126 unchanged. If we define the  $K \times J$  interpolation matrix  $\mathbf{A}$  for  $K$  evenly distributed spatial  
 127 locations  $\{\mathbf{s}_1, \mathbf{s}_2, \dots, \mathbf{s}_k\}$  within domain  $D$ , and further define  $\mathbf{X}^* = \mathbf{AX}$  and  $\mathbf{Z}^* = \mathbf{AZ}$ , then  
 128  $\sum_{t=1}^T \sum_{k=1}^K x_{kt}^* \approx \sum_{t=1}^T \sum_{k=1}^K z_{kt}^*$ ;  
 129 3. *Linear computation*: Using the STDL for a set of measurements  $\mathbf{Z} = h(\mathbf{X})$ , we seek to  
 130 compute  $\text{vec}(\mathbf{Z}) = \mathbf{D}^{-1} \text{vec}(\mathbf{X})$  where  $\text{vec}(\mathbf{X})$  stacks the columns of  $\mathbf{X}$  into a long vector with  
 131 length  $JT$ , and  $\mathbf{D}$  is a sparse  $JT \times JT$  matrix representing the STDL which then depends upon  
 132  $\kappa_S$  and  $\kappa_T$ , such that the computation time to compute  $\mathbf{D}^{-1} \text{vec}(\mathbf{X})$  increases linearly with the  
 133 size of  $JT$ .

134 Lindmark et al. (2026) constructed a spatially distributed lag,  $\mathbf{z}_t = (\mathbf{I} - \mathbf{P})^{-1} \mathbf{x}_t$  using a  $J \times J$   
 135 spatial path matrix  $\mathbf{P}$  given measurements  $\mathbf{x}_t$  at the vertices of triangles that cover the spatial  
 136 domain (a “finite element mesh” FEM). Using this FEM,  $\mathbf{P} = -\kappa_s \mathbf{C}^{-1} \mathbf{G}$  where  $\mathbf{C}$  is a diagonal  
 137  $J \times J$  matrix measuring the volume associated with each vertex, and  $\mathbf{G}$  is a sparse  $J \times J$  matrix  
 138 representing the “overlap” between each vertex (which is zero for vertices that do not share any  
 139 triangle). However, this spatially distributed lag did not account for time-lags and therefore

140 could not assess the relative importance of temporal versus spatial lags. We therefore seek to  
141 extend this recent research to also include time-lags.

142 **Extending to include time-lags**

143 We next incorporate time-lagged dynamics, where covariate measurements  $\mathbf{x}_t$  affect the STDL  
144 covariate  $\mathbf{z}_t$  in that same time but also in future times  $\mathbf{z}_{t+1}$ ,  $\mathbf{z}_{t+2}$ , etc. To do so, we construct a  
145  $JT \times JT$  dimensional path matrix  $\mathbf{P}_{\text{joint}}$  from spatial, temporal, and spatio-temporal lags:

$$\mathbf{P}_{\text{joint}} = \underbrace{\kappa_S^{-2}(\mathbf{P} \otimes \mathbf{I}_T)}_{\text{Space lag}} + \underbrace{\kappa_T(\mathbf{I}_S \otimes \mathbf{L})}_{\text{Time lag}} + \underbrace{\kappa_{ST}\kappa_S^{-2}(\mathbf{P} \otimes \mathbf{L})}_{\text{Space-time lag}}, \quad (1)$$

146 where  $\mathbf{L}$  is a  $T \times T$  first-difference matrix (with a band of 1s immediately below the diagonal and  
147 a band of -1s along the diagonal),  $\mathbf{I}_T$  is a  $T \times T$  identity matrix,  $\mathbf{I}_S$  is a  $J \times J$  identity matrix, and  
148  $-1 < \kappa_{ST} < 0$  controls the rate at which  $x_{jt}$  diffuses outward over time (with no diffusion when  
149  $\kappa_{ST} = -1$ ). To simplify presentation in the following, however, we drop the space-time lag (i.e.,  
150 fix  $\kappa_{ST} = 0$ ) and only estimate  $\kappa_S$  and  $\kappa_T$ . The STDL operator then calculates  $\text{vec}(\mathbf{z}) =$   
151  $(\mathbf{I} - \mathbf{P}_{\text{joint}})^{-1} \text{vec}(\mathbf{x})$  and  $\text{vec}(\mathbf{z})$  can be computed from  $\mathbf{I} - \mathbf{P}_{\text{joint}}$  using a sparse LU  
152 decomposition (Rue & Held, 2005) without directly constructing  $(\mathbf{I} - \mathbf{P}_{\text{joint}})^{-1}$ .

153 This expression results in a linear increase in mean-squared displacement (MSD) over  
154 time (i.e., the effect of a covariate  $x_{jt}$  propagates outwards spatially over time), and an  
155 exponential decay in the covariate effect over time. Specifically, it results in a first-order  
156 autocorrelation time  $\phi$ :

$$\phi = \frac{\kappa_T}{1 + \kappa_T}, \quad (2)$$

157 and a mean-squared displacement (MSD) for the covariate:

$$MSD = 4\kappa_S^{-2}(1 - \phi) = \frac{4\kappa_S^{-2}}{1 + \kappa_T}, \quad (3)$$

158 which we will visualize in detail later.

159 **Carry-over effects for temperature anomalies in the eastern Bering Sea**

160 To demonstrate nonlocal and/or lagged responses to habitat variables, we fit a species  
 161 distribution model to bottom trawl samples of fish biomass in the eastern Bering Sea. The trawl  
 162 survey was conducted following a fixed-station design with 291 to 376 stations over a  
 163 493,894.5 km<sup>2</sup> spatial domain from 1982 to 2019 and 2021 to 2024 (Markowitz *et al.*, 2022)  
 164 and downloaded using the *surveyjoin* package (Ward *et al.*, 2025). We specifically fit a separate  
 165 spatio-temporal generalized linear mixed model (ST-GLMM) to biomass  $y_i$  using area swept  $w_i$   
 166 as an offset for each of six ecologically important species: Pacific cod (*Gadus macrocephalus*),  
 167 Alaska pollock (*Gadus chalcogrammus*), capelin (*Mallotus villosus*), herring (*Clupea pallasii*),  
 168 arrowtooth flounder (*Atheresthes stomias*), and Pacific halibut (*Hippoglossus stenolepis*)  
 169 (Thorson & Kristensen, 2024). We specify a Tweedie distribution:

$$y_i \sim \text{Tweedie}(\mu_i, \phi, \psi) \quad (4)$$

170 which involves estimating two dispersion parameters that control the mean-variance relationship  
 171  $\text{Var}(y_i) = \phi\mu_i^\psi$ . The mean is then predicted from a log-linked linear predictor:

$$\log(\mu_i) = \underbrace{\beta}_{\text{Intercept}} + \underbrace{\omega_{j[i]}}_{\text{Spatial term}} + \underbrace{\epsilon_{j[i],t[i]}}_{\text{Spatio-temporal Term}} + \underbrace{\gamma_1 z_{j[i],t[i]} + \gamma_1 z_{j[i],t[i]}^2}_{\substack{\text{Quadratic effect of} \\ \text{spatio-temporal distributed lag} \\ \text{for temperature}}} + \underbrace{\log(w_i)}_{\text{Area offset}} \quad (5)$$

172 We specify a Gaussian Markov random field (GMRF) for the spatial term:

$$\boldsymbol{\omega} \sim \text{GMRF}(\mathbf{0}, \tau_\omega^2 \mathbf{Q}), \quad (6)$$

173 where  $\mathbf{Q}$  is the sparse precision matrix constructed using the SPDE method (Lindgren *et al.*,  
174 2011), and also specify a GMRF that follows a first-order autoregressive process for the spatio-  
175 temporal term:

$$\boldsymbol{\epsilon}_t \sim \begin{cases} \text{GMRF}(\mathbf{0}, (1 - \rho_\epsilon^2)\tau_\epsilon^2 \mathbf{Q}) & \text{if } t = 1 \\ \text{GMRF}(\rho_\epsilon \boldsymbol{\epsilon}_t, \tau_\epsilon^2 \mathbf{Q}) & \text{if } t > 1 \end{cases}. \quad (7)$$

176 This involves estimating the decorrelation rate  $\kappa$  that is shared between spatial and spatio-  
177 temporal terms, the time-correlation  $\rho_\epsilon$  for spatio-temporal residuals, and a separate pointwise  
178 variance for each term controlled by  $\tau_\omega^2$  and  $\tau_\epsilon^2$ , respectively. The SPDE method requires  
179 constructing a finite-element mesh (FEM) over the spatial domain, which we do using the  
180 *fmesher* package (Lindgren, 2023). We use a FEM cutoff of 30 km, resulting in  $J = 402$   
181 vertices over  $T = 45$  years, such that  $\boldsymbol{\omega}$  and  $\boldsymbol{\epsilon}_t$  contain 18,492 random effects.

182 Finally, we also estimate  $\kappa_S$  and  $\kappa_T$  for the STDL that converts seafloor temperature  
183 anomalies  $x_{jt}$  to effective covariate  $z_{jt}$ , while then estimating a dome-shaped (quadratic)  
184 response to  $z_{jt}$ . We use *in situ* measurements of water temperature obtained from the bottom  
185 trawl survey to define the seafloor temperature  $x_{jt}$  for each vertex  $j$  of the SPDE mesh at  
186 location  $\mathbf{s}_j$  in year  $t$ , using the nearest bottom trawl sample to  $\mathbf{s}_j$  in a given year. Because the  
187 survey was not conducted in 2020, we estimated bottom temperature for that year by averaging  
188 observations from the two adjacent survey years, 2019 and 2021. To allow a time-lagged effect  
189 of past temperatures for the first year of sampling, we imputed the 1981 values using the mean of  
190 1982-1983. We then convert the bottom temperature for a given location  $j$  and year  $t$  to a  
191 temperature anomaly by subtracting the mean value for that location across years. This  
192 temperature anomaly shows a well-documented oscillation (Stabeno *et al.*, 2019) between a

193 warm stanza (2002 to 2005), a cold stanza (2006 to 2013), another warm stanza (2014 to 2021),  
194 with close-to-average conditions subsequently (Fig. 1).

195 For each species, we fit four models formed from the  $2 \times 2$  factorial design of including  
196 the space-lag by estimating  $\kappa_S$  (or instead fixing  $\kappa_S = 0$ ) and/or including the time-lag by  
197 estimating  $\kappa_T$  (or instead fixing  $\kappa_T = 0$ ). For each model, we identify the maximum likelihood  
198 estimate of all fixed effects by applying the Laplace approximation to the joint likelihood of  
199 fixed and random effects (Skaug & Fournier, 2006), as implemented using the R (R Core Team,  
200 2023) package *TMB* (Kristensen *et al.*, 2016). *TMB* then calculates the gradient of the Laplace  
201 approximation with respect to fixed effects using automatic differentiation (Fournier *et al.*,  
202 2012), which we then optimize in the R statistical environment. *TMB* uses the Eigen package  
203 (Guennebaud *et al.*, 2010) to efficiently apply the sparse LU decomposition when calculating the  
204 STDL, and we use the delta method to compute standard errors for  $\phi$  (Eq. 2), MSD (Eq. 3), and  
205 RMSD =  $\sqrt{\text{MSD}}$ .

206 We explore model results in several ways:

- 207 1. *Parsimony and parameter estimates*: For each species, we calculate the Akaike Information  
208 Criterion (AIC) (Akaike, 1974) and use it to identify the most parsimonious of the four  
209 models. For all four models, we also extract the estimated spatial distributed lag ( $\kappa_S$ ) and the  
210 temporal distributed lag ( $\kappa_T$ ), and convert them to the equivalent mean-squared displacement  
211 MSD and the first-order autocorrelation  $\phi$ , respectively. We then compare the  $\phi$  and MSD  
212 across species and models.
- 213 2. *Visualized effect of temperature anomalies*: For the selected model for each species, we also  
214 visualize the predicted effect of a hypothetical anomaly in local temperature as it propagates

215 through space and time, based on the estimated values of  $\kappa_S$  and  $\kappa_T$ . This plot provides  
216 intuition about the spatial and temporal scale over which a temperature anomaly affects  
217 population density for that species.

218 3. *Effective seafloor temperature*: Finally, for the selected model for each species, we also  
219 visualize the effective seafloor temperature  $\mathbf{Z}^*$  after applying the STDL to the *in situ*  
220 measurements  $\mathbf{X}$  and then interpolating  $\mathbf{Z}$  to the  $25 \text{ km} \times 25 \text{ km}$  grid. This effective  
221 temperature then represents the net effective of animal movement and carryover effects that  
222 contribute to the estimated STDL.

223 Both (2) and (3) involve predicting raw covariate  $\mathbf{X}$  and the STDL covariate  $\mathbf{Z}$  at higher  
224 resolution. To do so we construct a set of  $K = 886$  square  $25 \text{ km} \times 25 \text{ km}$  grid cells that cover  
225 the spatial domain of the bottom trawl survey, and then interpolate covariates  $\mathbf{X}^* = \mathbf{AX}$  and  $\mathbf{Z}^* =$   
226  $\mathbf{AZ}$  using the  $K \times J$  interpolation matrix  $\mathbf{A}$ .

## 227 **Simulation experiment**

228 To explore model performance, we conduct a self- and cross-test simulation experiment  
229 assessing parameter recovery and whether AIC correctly identifies the true model across  
230 different estimation scenarios. To do so, we choose three species where model selection for real  
231 data selects either no STDL (Pacific cod), a temporal lag (Pacific halibut), or both spatial and  
232 temporal lags (capelin). For each species, we simulate 100 replicated data sets from the AIC-  
233 selected model (used as operating model), each of which condition upon the maximum  
234 likelihood estimates for fixed effects, simulating new realizations of the random effects, and then  
235 simulating new samples conditional upon both at the same location as real-world data. For each  
236 of 100 data sets, we then fit the original four estimation models: no lags, spatial lag, time-lag,

237 and both space and time lags (1200 model fits) and record the AIC and parameter estimates. We  
238 then explore (1) how often AIC identifies the correct data-generating process, and (2) how the  
239 estimated parameters compare with the original values used in the simulation.

240 **Results**

241 The most parsimonious model (lowest marginal AIC) includes a carry-over effect of temperature  
242 for five of the six species (Table 1). For these five species, the AIC-selected model has a  
243 temporal correlation  $\phi$  from ranging from 0.20 (arrowtooth flounder) to 0.83 (Pacific herring).  
244 Similarly, the spatial lag is parsimonious for four of the six species and has a root-mean-squared  
245 displacement (RMSD) ranging from 30 km (arrowtooth flounder) to 53 km (capelin), relative to  
246 the  $\sqrt{493,894.5} = 703$  km distance across the spatial domain. Models without the STDL run in  
247 3.2 to 11.2 minutes and adding the STDL increases runtime by 5-fold to 15-fold. As expected,  
248 the selected model has a 95% confidence interval for  $\phi$  and RMSD that does not overlap with  
249 zero when AIC favors a model with STDL, and the interval generally does overlap zero when the  
250 component is not selected by AIC (Fig. 2); for example Pacific cod where  $\phi = 0.04$  and is not  
251 selected as parsimonious.

252 To illustrate the predicted effect of the estimated spatial and time-lags, we illustrate how a  
253 hypothetical localized temperature anomaly propagates across space and over time (Fig. 3).  
254 Pacific cod (Fig. 3 top row) is the only species where AIC selects neither the time- or nor space-  
255 lags. For this species, the local temperature anomaly  $\mathbf{X}_t^*$  has a mean-squared displacement of  
256  $MSD = 911 \text{ km}^2$ , i.e.,  $RMSD = \sqrt{911} = 30 \text{ km}$ . This matches the scale used when discretizing  
257 the continuous covariate (i.e., 40 km cutoff in the finite-element mesh), such that the resolution  
258 of the finite element mesh provides a “lower bound” on the spatial resolution of the simulated

259 local temperature anomaly  $\mathbf{X}_t^*$ . The diffused covariate  $\mathbf{Z}_t^*$  then has the same total value and MSD  
260 in that year, and  $\mathbf{Z}_{t+1}^* = 0$  in subsequent years (shown as dark blue in lag-1 and lag-2 columns)  
261 because there is no time-lagged dynamics ( $\kappa_T = 0$ ). By contrast, Pacific halibut selects a time-  
262 lag but no spatial lag (Fig. 3, bottom row), with  $\phi = 0.31$ . As a result, the covariate is smoothed  
263 across years, where the total effect in the first three years is 0.69, 0.22, and 0.07 (i.e.,  $\frac{0.22}{0.69} =$   
264 0.31), and the sum across all subsequent years is approximately 1 (i.e., the total effect of a  
265 temperature anomaly is preserved but smoothed across subsequent years). However, the spatial  
266 lag is not selected, such that the spatial effect does not propagate outward over time (MSD =  
267  $978 \text{ km}^2$  in all years). As a third example, walleye pollock (Fig. 3, 2<sup>nd</sup> row) selects both a time  
268 and space lag, with estimated  $\text{MSD} = 1747 \text{ km}^2$  and  $\phi = 0.31$ . In this case, the effect of a  
269 temperature anomaly propagates outwards over time, i.e.,  $\text{MSD} = 2621 \text{ km}^2$  in the initial year  
270 and  $\text{MSD} = 4294 \text{ km}^2$  in the following year.

271 The STDL estimates substantial differences in the effective temperature anomaly  $\mathbf{Z}^*$   
272 among species, and we use the transition from cold (2013) to warm (2017) conditions as an  
273 illustrative example (Fig. 4). For Pacific cod, AIC selects the model without any space or time-  
274 lag, and therefore effective temperature (Fig. 4 top row) is identical to the raw measurements  
275 (Fig. 1). As an extreme contrast, the selected model for Pacific herring has strong spatial and  
276 time-lags ( $\text{RMSD} = 46 \text{ km}$  and  $\phi = 0.84$ ), so effective temperature shows both less variation  
277 across space within a year and also a slower transition from below- (blue) to above-average (red)  
278 conditions starting in 2016 (Fig. 4, 4<sup>th</sup> row). Using Pacific halibut as an example that includes  
279 time-lags but no spatial lag ( $\phi = 0.31$ ), we see the same high-resolution spatial variation in  
280 effective temperature as for measurements (Fig. 1) and for Pacific cod (Fig. 1 top row), but the  
281 persistence of below-average effective temperature across the northern portion of the survey area

282 even as temperature measurements are increasing in 2014. We therefore see that STDL estimates  
283 the effective thermal environment, which can differ from raw measurements and among species.

284 Finally, the simulation experiment confirms that AIC can identify the combination of  
285 spatial and temporal distributed lags that are used to simulate data (Fig. 5). In particular, the  
286 correct model is identified in >75% of simulation replicates for all three species. Similarly, the  
287 estimates of spatio-temporal lags are approximately unbiased for those cases where they are  
288 simulated (Fig. 6). We therefore conclude that these parameters are estimable given the sample  
289 sizes explored here.

## 290 **Discussion**

291 In this paper, we provide the first demonstration that both temporal and high-resolution spatial  
292 lags arise when using habitat variables (e.g., temperature anomalies) to predict population  
293 density. The method involves estimating two additional, interpretable parameters (i.e., with units  
294 of distance and time), and the spatio-temporal distributed lag can revert to the conventional  
295 species distribution model (i.e., using measured covariates directly) as a nested submodel.  
296 Similarly, a simulation experiment suggests that model selection can identify the appropriate  
297 combination of spatial and temporal lags, and that estimates are approximately unbiased using  
298 the sample sizes explored here. The estimated temporal lags are strongest for the two pelagic  
299 species (Pacific herring and capelin have  $\phi = \{0.83, 0.70\}$ ), and either weak or absent for two  
300 seafloor-associated species (Pacific halibut and Pacific cod have  $\phi = \{0.31, 0.04\}$ ). The method  
301 also allows us to visualize the effective temperature anomaly for each fish population, which  
302 differs substantially among species.

303        The link between spatio-temporal distributed lags (Eq. 1) and animal movement suggests  
304    many avenues for future extensions to this approach. We did not explore estimating the spatio-  
305    temporal interaction  $\kappa_{ST}$  so that we could focus on two interpretable parameters. However,  
306    estimating  $\kappa_{ST}$  allows the STDL to estimate a separate RMSD in the first year relative to how  
307    much RMSD increases in subsequent years;  $\kappa_{ST} = 0$  (as assumed here) results in MSD increasing  
308    linearly with time, whereas  $\kappa_{ST} = -1$  results in MSD being equal for all years. This parameter  
309    therefore allows a model to estimate the rate of spatio-temporal diffusion, at the cost of slower  
310    model fitting. Similarly, the spatial diffusion rate  $\kappa_S$  might itself depend upon covariates  
311    (Lindgren *et al.*, 2011), where temperature anomalies might have a more localized impact on  
312    nearshore than deep-water habitats. Future studies could incorporate this novel type of covariate  
313    interaction during the construction of stiffness matrix **G**. Finally, including advection would  
314    allow covariates at one location to affect population responses some distance away (e.g., 100 km  
315    eastward). For an animal with predictable seasonal movement, this would allow winter  
316    covariates to affect summer densities at a geographically distant site.

317        Oceans are experiencing extremely warm conditions (Hobday *et al.*, 2016), and there are  
318    well-documented examples of marine heatwaves impacting ocean animals (Fossheim *et al.*,  
319    2015; Szwalski *et al.*, 2023). However, a global synthesis (Fredston *et al.*, 2023) found no  
320    consistent change in region-wide seafloor-community biomass occurring synchronous with  
321    marine heatwaves. We hypothesize that this mismatch arises because spatial and temporal lags  
322    can complicate studies seeking to attribute ecological responses to climate drivers. In cases such  
323    as this, we hypothesize that the STDL allows analysts to attribute localized density responses to  
324    temperature anomalies, while automatically testing for lagged responses and identifying the  
325    appropriate scale linking temperature to population responses. We therefore recommend greater

326 use of STDL in studies attributing ecological dynamics to climate drivers, and the growing  
327 availability of global databases of biological monitoring (Maureaud *et al.*, 2024) will facilitate  
328 these studies.

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332 **References**

333 Akaike H (1974) New look at statistical-model identification. *IEEE Transactions on Automatic  
334 Control*, **AC19**, 716–723.

335 Armstrong B (2006) Models for the Relationship between Ambient Temperature and Daily  
336 Mortality. *Epidemiology*, **17**, 624–631.

337 Arnone III JA, Verburg PSJ, Johnson DW et al. (2008) Prolonged suppression of ecosystem  
338 carbon dioxide uptake after an anomalously warm year. *Nature*, **455**, 383–386.

339 Clarotto L, Allard D, Romary T, Desassis N (2024) The SPDE approach for spatio-temporal  
340 datasets with advection and diffusion. *Spatial Statistics*, **62**, 100847.

341 Dormann C, McPherson J, Araújo M et al. (2007) Methods to account for spatial autocorrelation  
342 in the analysis of species distributional data: a review. *Ecography*, **30**, 609–628.

343 Elith J, Leathwick JR (2009) Species distribution models: ecological explanation and prediction  
344 across space and time. *Annual review of ecology, evolution, and systematics*, **40**, 677–  
345 697.

346 Essl F, García-Rodríguez A, Lenzner B et al. (2024) Potential sources of time lags in calibrating  
347 species distribution models. *Journal of Biogeography*, **51**, 89–102.

348 Fossheim M, Primicerio R, Johannessen E, Ingvaldsen RB, Aschan MM, Dolgov AV (2015)

349           Recent warming leads to a rapid borealization of fish communities in the Arctic. *Nature*

350           *Climate Change*, **5**, 673–677.

351 Fournier DA, Skaug HJ, Ancheta J et al. (2012) AD Model Builder: using automatic

352           differentiation for statistical inference of highly parameterized complex nonlinear

353           models. *Optimization Methods and Software*, **27**, 1–17.

354 Fredston AL, Cheung WW, Frölicher TL et al. (2023) Marine heatwaves are not a dominant

355           driver of change in demersal fishes. *Nature*, **621**, 324–329.

356 Gasparrini A, Armstrong B, Kenward MG (2010) Distributed lag non-linear models. *Statistics in*

357           *Medicine*, **29**, 2224–2234.

358 Guennebaud G, Jacob B, others (2010) Eigen v3.

359 Hobday AJ, Alexander LV, Perkins SE et al. (2016) A hierarchical approach to defining marine

360           heatwaves. *Progress in Oceanography*, **141**, 227–238.

361 Kristensen K, Nielsen A, Berg CW, Skaug H, Bell BM (2016) TMB: Automatic differentiation

362           and Laplace approximation. *Journal of Statistical Software*, **70**, 1–21.

363 Lalechère E, Marrec R, Lenoir J (2025) A Non-Equilibrium Species Distribution Model Reveals

364           Unprecedented Depth of Time Lag Responses to Past Environmental Change

365           Trajectories. *Ecology Letters*, **28**, e70040.

366 Lindgren F (2023) fmesher: Triangle Meshes and Related Geometry Tools.

367 Lindgren F, Rue H, Lindström J (2011) An explicit link between Gaussian fields and Gaussian

368           Markov random fields: the stochastic partial differential equation approach. *Journal of*

369           *the Royal Statistical Society: Series B (Statistical Methodology)*, **73**, 423–498.

370 Lindgren F, Bakka H, Bolin D, Krainski E, Rue H (2024) A diffusion-based spatio-temporal  
371 extension of Gaussian Matérn fields. *Statistics and Operations Research Transactions*  
372 (*SORT*), **48**, 3–66.

373 Lindmark M, Anderson SC, Gogina M, Casini M (2023) Evaluating drivers of spatiotemporal  
374 variability in individual condition of a bottom-associated marine fish, Atlantic cod  
375 (*Gadus morhua*). *ICES Journal of Marine Science*, **80**, 1539–1550.

376 Lindmark M, Anderson SC, Thorson JT (2026) Estimating scale-dependent covariate responses  
377 using two-dimensional diffusion derived from the stochastic partial differential equation  
378 method. *Methods in Ecology and Evolution*, **17**, 207–218.

379 Markowitz EH, Dawson EJ, Charriere NE, Prohaska BK, Rohan SK, Stevenson DE, Britt LL  
380 (2022) Results of the 2021 eastern and northern Bering Sea continental shelf bottom  
381 trawl survey of groundfish and invertebrate fauna.

382 Maureaud AA, Palacios-Abrantes J, Kitchel Z et al. (2024) FISHGLOB\_data: an integrated  
383 dataset of fish biodiversity sampled with scientific bottom-trawl surveys. *Scientific Data*,  
384 **11**, 24.

385 Miller DL, Newman K, Cornulier T (2025) Adding structure to generalized additive models, with  
386 applications in ecology.

387 Núñez-Riboni I, Akimova A, Sell AF (2021) Effect of data spatial scale on the performance of  
388 fish habitat models. *Fish and Fisheries*, **22**, 955–973.

389 Pardikes NA, Shapiro AM, Dyer LA, Forister ML (2015) Global weather and local butterflies:  
390 variable responses to a large-scale climate pattern along an elevational gradient. *Ecology*,  
391 **96**, 2891–2901.

392 R Core Team (2023) *R: A Language and Environment for Statistical Computing*. R Foundation  
393 for Statistical Computing, Vienna, Austria.

394 Rue H, Held L (2005) *Gaussian Markov random fields: theory and applications*, 1st edition edn.  
395 CRC Press, 280 pp.

396 Skaug H, Fournier D (2006) Automatic approximation of the marginal likelihood in non-  
397 Gaussian hierarchical models. *Computational Statistics & Data Analysis*, **51**, 699–709.

398 Sollmann R (2024) Estimating the temporal scale of lagged responses in species abundance and  
399 occurrence. *Ecosphere*, **15**, e4704.

400 Stabeno PJ, Bell SW, Bond NA, Kimmel DG, Mordy CW, Sullivan ME (2019) Distributed  
401 Biological Observatory Region 1: Physics, chemistry and plankton in the northern Bering  
402 Sea. *Deep Sea Research Part II: Topical Studies in Oceanography*, **162**, 8–21.

403 Szuwalski CS, Aydin K, Fedewa EJ, Garber-Yonts B, Litzow MA (2023) The collapse of eastern  
404 Bering Sea snow crab. *Science*, **382**, 306–310.

405 Thorson JT (2019) Measuring the impact of oceanographic indices on species distribution shifts:  
406 The spatially varying effect of cold-pool extent in the eastern Bering Sea. *Limnology and*  
407 *Oceanography*, **64**, 2632–2645.

408 Thorson J, Kristensen K (2024) *Spatio-Temporal Models for Ecologists*, 1st edition edn.  
409 Chapman and Hall/CRC, Boca Raton, FL, 276 pp.

410 Thorson JT, Ciannelli L, Litzow MA (2020) Defining indices of ecosystem variability using  
411 biological samples of fish communities: A generalization of empirical orthogonal  
412 functions. *Progress in Oceanography*, **181**, 102244.

413 Ward EJ, English PA, Rooper CN et al. (2025) 'surveyjoin': A Standardized Database of  
414 Fisheries Bottom Trawl Surveys in the Northeast Pacific Ocean. 2025.03.14.643022.

415 Wu D, Zhao X, Liang S, Zhou T, Huang K, Tang B, Zhao W (2015) Time-lag effects of global  
416 vegetation responses to climate change. *Global Change Biology*, **21**, 3520–3531.

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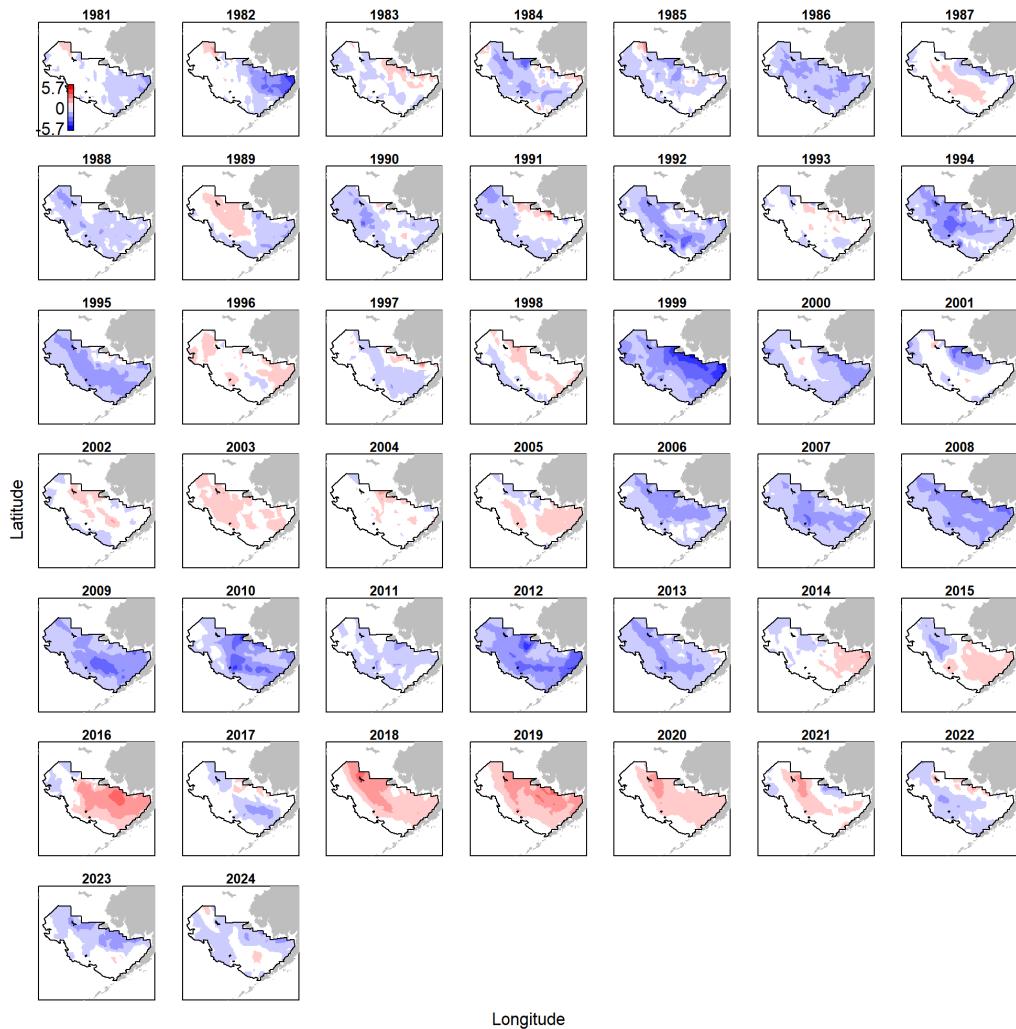
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421 Table 1 – Summary of model results for the six species and four models formed from the  $2 \times 2$   
 422 cross of including a space lag (X in space column) or time lag (X in time-lag). We specifically  
 423 show the runtime in minutes (including optimization from uniformed starting values and  
 424 standard-error calculations), the marginal AIC relative to the most parsimonious model (in bold  
 425 for selected model), the first-order autocorrelation  $\phi$  calculated from estimated time-lag  $\kappa_T$  (Eq.  
 426 2), the mean-squared displacement MSD calculated from the space-lag  $\kappa_S$  (Eq. 3), and the  
 427 square-root of MSD (with units of km)

Species (common name)	space	time	Runtime (min)	$\Delta\text{AIC}$	$\phi$	MSD (km <sup>2</sup> )	RMSD (km)
pacific cod			<b>3.24</b>	<b>0</b>	NA	NA	NA
pacific cod	X		3.85	2	NA	0	0
pacific cod		X	4.87	1.5	0.04	NA	NA
pacific cod	X	X	17.35	3.5	0.04	0	0
walleye pollock			3.42	2.55	NA	NA	NA
walleye pollock	X		4.28	3.28	NA	664	26
walleye pollock		X	3.71	2.21	0.16	NA	NA
walleye pollock	X	X	<b>15.37</b>	<b>0</b>	<b>0.31</b>	<b>1747</b>	<b>42</b>
capelin			3.31	21.88	NA	NA	NA
capelin	X		5.1	11.1	NA	5072	71
capelin		X	3.56	10.3	0.52	NA	NA
capelin	X	X	<b>29.73</b>	<b>0</b>	<b>0.7</b>	<b>2804</b>	<b>53</b>
pacific herring			8.19	10.26	NA	NA	NA
pacific herring	X		10.32	12.26	NA	0	0
pacific herring		X	8.79	3.51	0.73	NA	NA
pacific herring	X	X	<b>29.26</b>	<b>0</b>	<b>0.83</b>	<b>2135</b>	<b>46</b>
arrowtooth flounder			6.77	6.12	NA	NA	NA
arrowtooth flounder	X		8.63	2.87	NA	912	30
arrowtooth flounder		X	9.84	3.14	0.18	NA	NA
arrowtooth flounder	X	X	<b>32.26</b>	<b>0</b>	<b>0.2</b>	<b>911</b>	<b>30</b>
pacific halibut			11.15	9.58	NA	NA	NA
pacific halibut	X		4.62	11.58	NA	0	0
pacific halibut		X	<b>2.89</b>	<b>0</b>	<b>0.31</b>	NA	NA
pacific halibut	X	X	11.87	2	0.31	0	0

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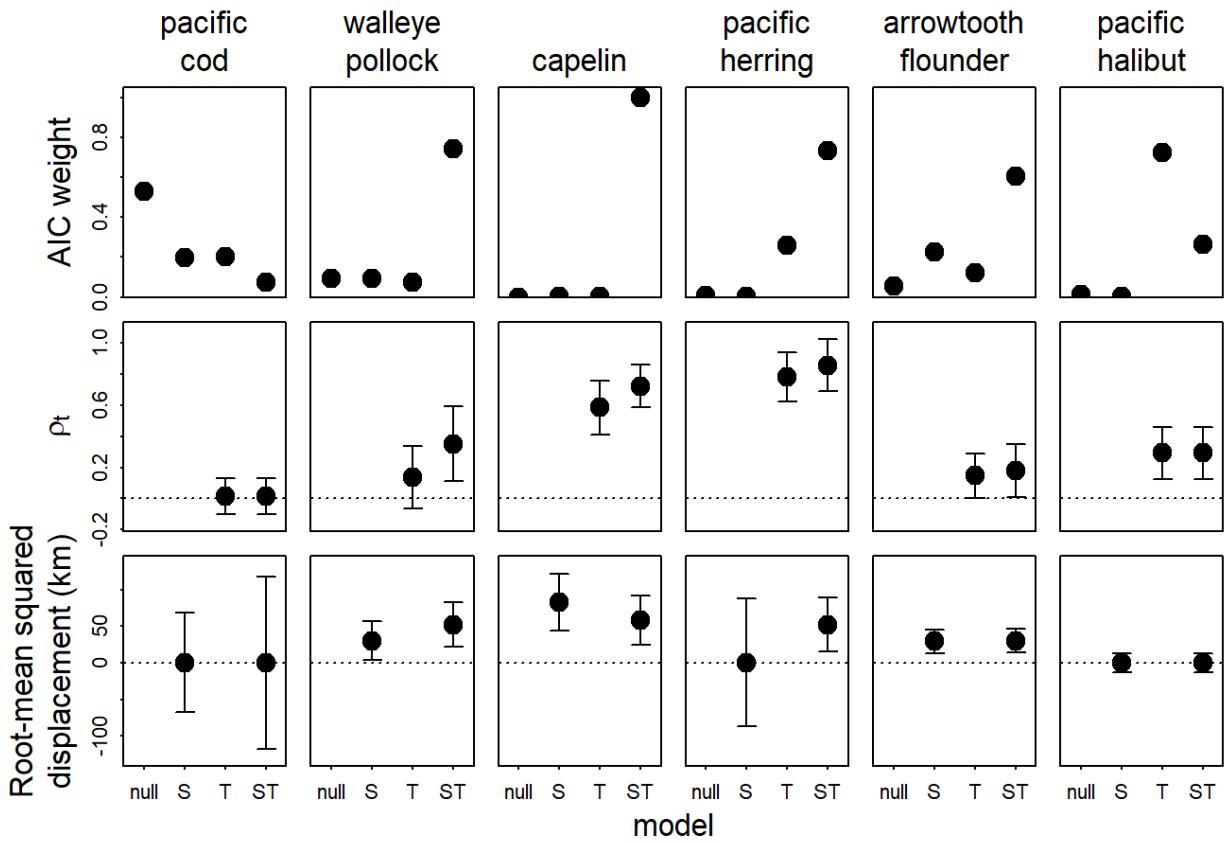
429 Fig. 1 – Visualizing temperature anomalies  $X^*$  (see panel 1981 for color legend) interpolated to  
430 the  $40 \times 40$  km grid cells distributed across the eastern Bering Sea survey area (black outline)  
431 relative to land in Alaska (grey areas) from 1981 to 2024 (panels).



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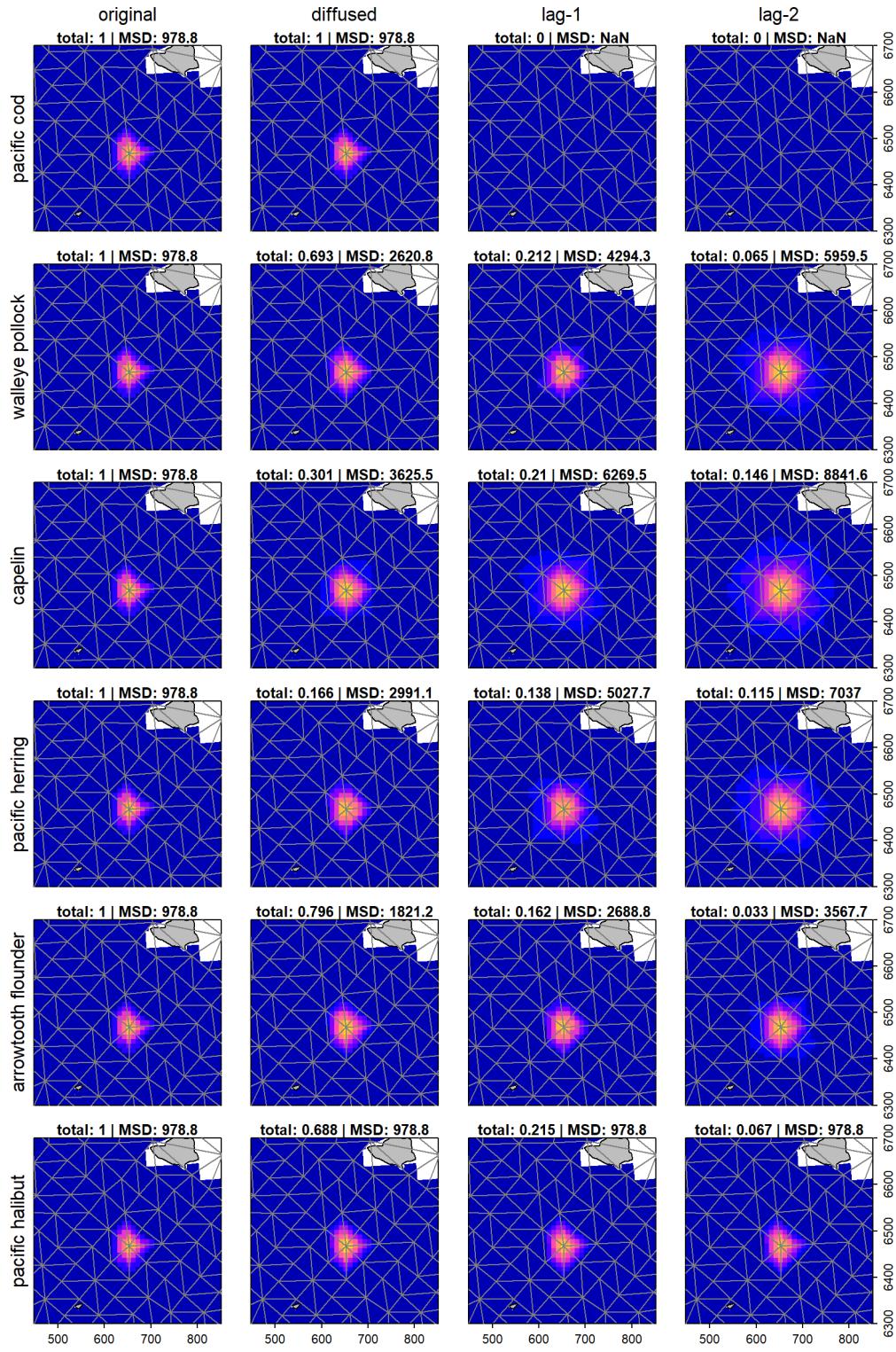
435 Fig. 2 – Visualizing estimated AIC weight (top row), the correlation among years (2<sup>nd</sup> row), and  
436 the root-mean-squared displacement (3<sup>rd</sup> row) for the spatio-temporal distributed lag for each of  
437 four models (x-axis; null: no lags; S: just spatial lag; T: just time-lag; ST: both space and time  
438 lags) for each of six species (columns)



439

440

441 Fig. 3 – Using the selected model for each species (row), visualizing the effect of a hypothetical,  
442 localized temperature anomaly measurement  $\mathbf{x}_t^*$  interpolated to the  $40 \text{ km} \times 40 \text{ km}$  grid cells  
443 (left column), and how it translates to the effective temperature in the same year  $\mathbf{z}_t^*$  (2<sup>nd</sup> column),  
444 one year later  $\mathbf{z}_{t+1}^*$  (3<sup>rd</sup> column), or two years later  $\mathbf{z}_{t+2}^*$  (4<sup>th</sup> column). We specifically fix  $x_{jt} = c$   
445 for the location  $\mathbf{s}_j$  in the middle of the spatial domain, with value  $c$  fixed to ensure that  
446  $\sum_{k=1}^K x_{kt}^* = 1$ , where  $k$  is the number of grid cells. For each year, we calculate the total  $\sum_{k=1}^K x_{kt}^*$   
447 or  $\sum_{k=1}^K z_{kt}^*$  and the root-mean-squared displacement (listed above each panel). We also show  
448 the edges of the set of triangles (grey lines) used to represent the finite-element mesh (using a  
449 cutoff of 40 km).

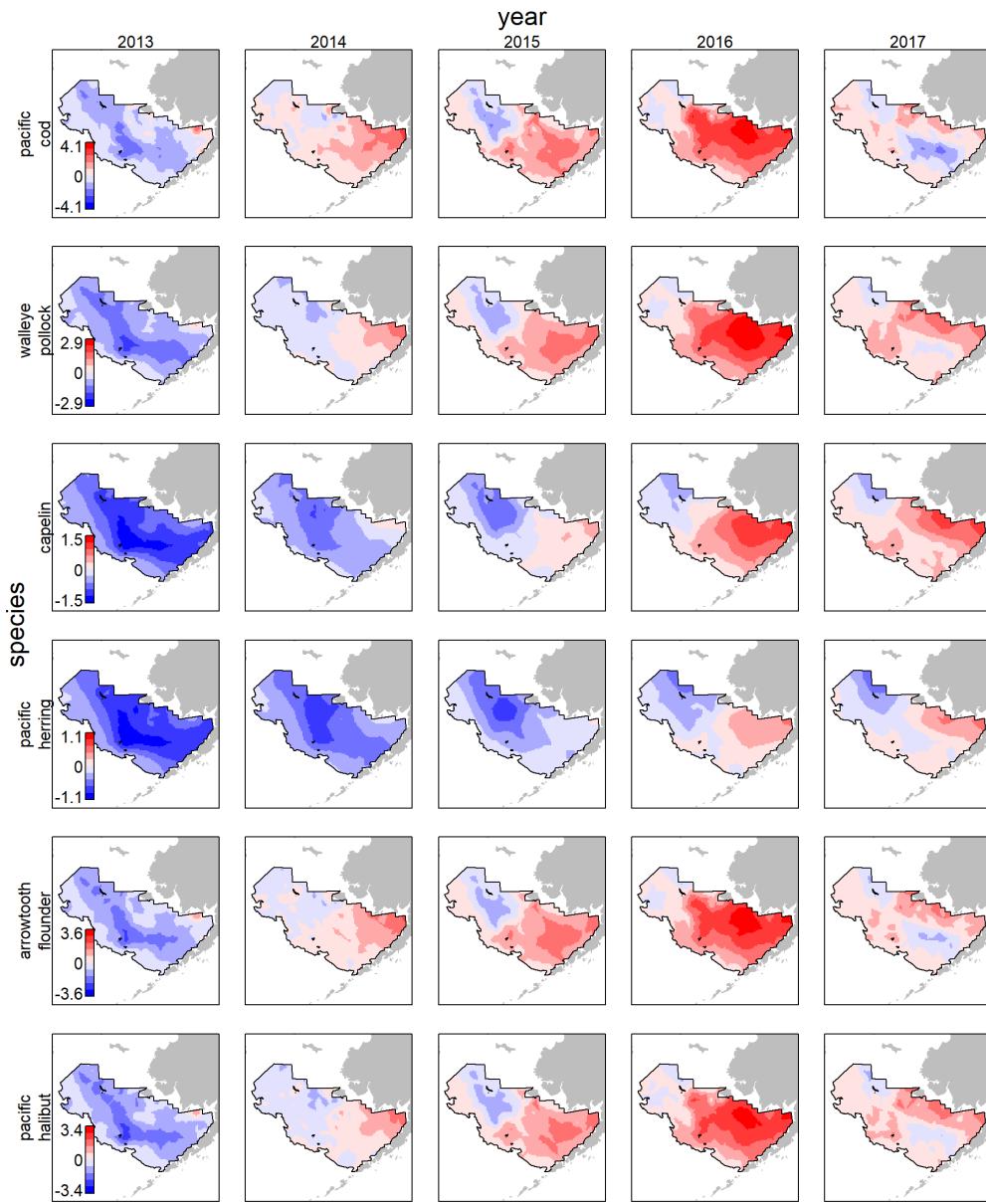


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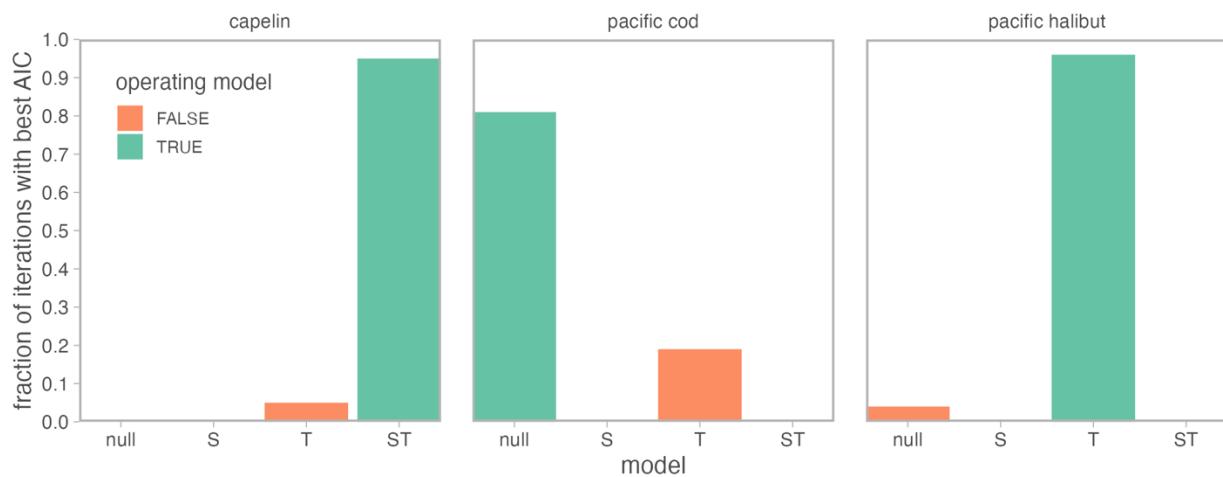
453 Fig. 4 – Visualizing the effective seafloor temperature anomaly  $\mathbf{z}_t^*$  (in units  $^{\circ}\text{C}$  relative to the  
454 average for 1982-2014) for each species (rows) in the five years that rapidly transition from cool  
455 (2013, left column) to warm conditions (2017, right column), and using a separate color legend  
456 for each species (within the left panel for each row); compare with Fig. 1 to see the effect of the  
457 spatio-temporal distributed lag.



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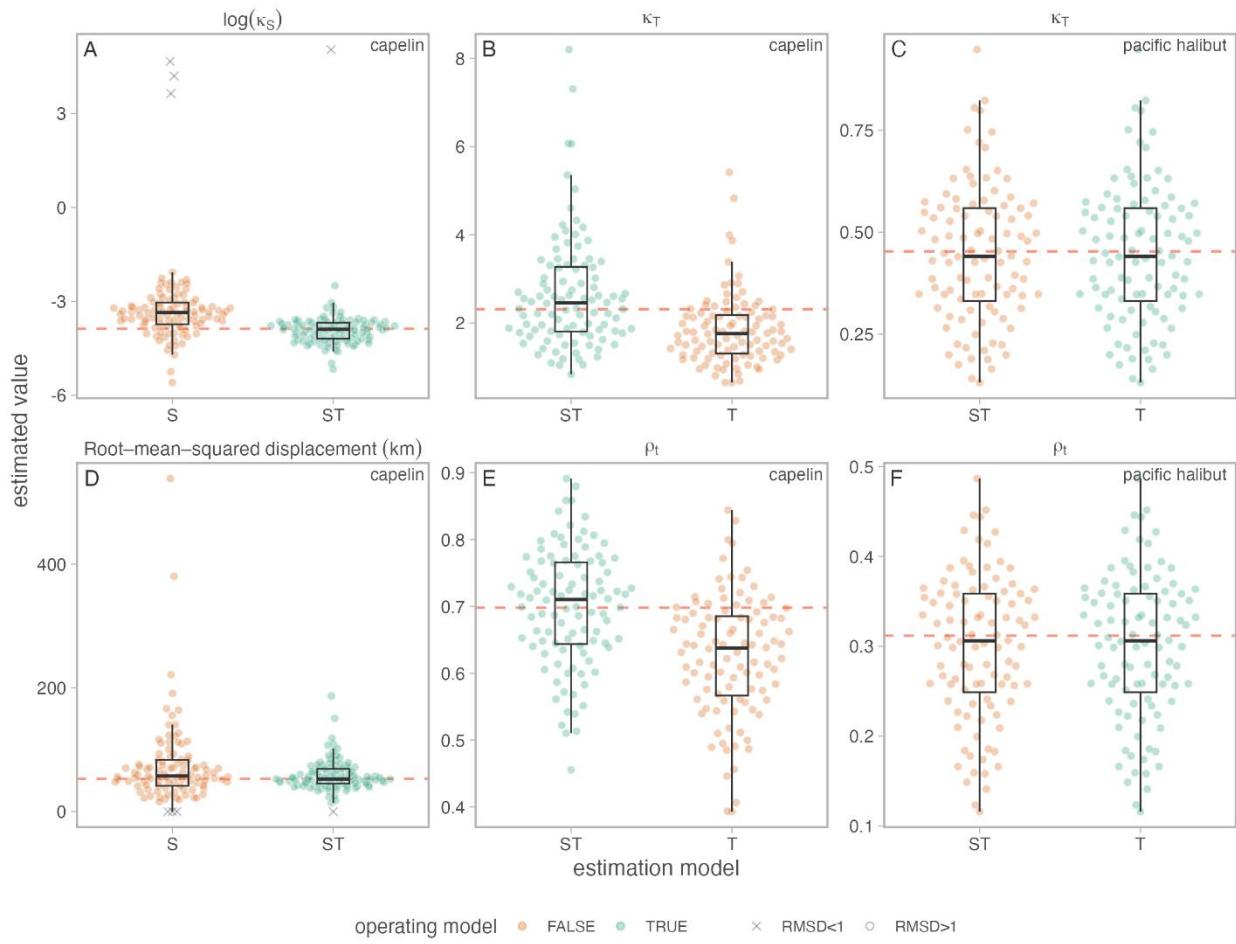
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460 Fig. 5 – Performance for marginal AIC to identify the correct model within a simulation  
461 experiment for three species. For each species (columns), we show the four estimation models  
462 (x-axis; null: no lags; S: just spatial lag; T: just time-lag; ST: both space and time lags), and the  
463 proportion of 100 simulation replicates where each model was selected (y-axis). Color  
464 corresponds to whether the operating model matches the estimation model, where green matches  
465 (correct model is chosen) and orange is a mismatch (incorrect model chosen).



466

467 Fig. 6 – Performance of parameter estimation in the simulation experiment, showing the two  
 468 parameters in the spatio-temporal distributed lag for capelin (panel A and B) and the temporal lag  
 469 for Pacific halibut (panel C), as well as the derived calculation for root-mean-squared-  
 470 displacement in km (RMSD) (panel D) and correlation among years (autocorrelation) (panel E  
 471 and F). For each quantity, we show 100 estimates (dots) and the true value (red line; y-axis) for  
 472 the two estimation models, where green indicates the operating model and orange indicates the  
 473 alternative model that also estimates the same parameter (x-axis; S: just spatial lag; T: just time-  
 474 lag; ST: both space and time lags). Estimates where  $\text{RMSD} < 1$  are shown as crosses.



475

476